# **Prospects for GPDs extraction with Double DVCS**

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- → Starting point: GPD
- Double deeply virtual Compton scattering (DDVCS)
  - Goal & motivation
  - > Formulation à la Kleiss & Stirling
  - > Tests of our KS-based formulation
- → Summary

# Starting point: GPD

 GPD = Generalized Parton Distribution ≈ "3D version of a PDF (Parton Distribution Function)." With x the fraction of the hadron's longitudinal momentum carried by a quark:

$$GPD_f(x,\xi,t) = \frac{1}{2} \int \frac{dz^-}{2\pi} e^{ix\bar{p}^+z^-} \langle N' | \bar{\mathfrak{q}}_f(-z/2) \gamma^+ \mathcal{W}[-z/2,z/2] \mathfrak{q}_f(z/2) | N \rangle \Big|_{z_\perp = z^+ = 0}$$
  
$$t = \Delta^2 = (p'-p)^2, \quad \xi = -\frac{\bar{q}\Delta}{2\bar{p}\bar{q}}, \quad \rho = \frac{-\bar{q}^2}{2\bar{p}\bar{q}}, \quad \bar{q} = \frac{q+q'}{2}, \quad \bar{p} = \frac{p+p'}{2}$$

- Importance:
  - Connected to QCD energy-momentum tensor, and so to spin. GPDs are a way to address the hadron's spin puzzle
  - Tomography: distribution of longitudinal momentum on the transverse (to hadron's motion) plane

$$q(x, \mathbf{b}_{\perp}) = \int \frac{\mathrm{d}^{2} \boldsymbol{\Delta}}{4\pi^{2}} e^{-i\mathbf{b}_{\perp} \cdot \boldsymbol{\Delta}} \frac{H^{q}(x, 0, t = -\boldsymbol{\Delta}^{2})}{\mathbf{A} \operatorname{particular GPD}}$$

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# Our goal

- **Goal:** assessment of feasibility of double deeply virtual Compton scattering (DDVCS) at JLab12, EIC and JLab20+. Phenomenology: xsec, asymmetries, etc
- What is DDVCS? Electroproduction of a lepton pair



$$-t = -(p'-p)^2 \qquad \xi = -\frac{\Delta \bar{q}}{2\bar{p}\bar{q}}$$

$$\Delta = p' - p = q - q', \quad \bar{q} = \frac{q + q'}{2}, \quad \bar{p} = \frac{p + p'}{2}$$

GPD = Generalized Parton Distribution. Factorized amplitude into GPD and hard contribution (perturbative term)

## Why DDVCS?

- **Goal:** assessment of feasibility of double deeply virtual Compton scattering (DDVCS) at JLab12, EIC and JLab20+. Phenomenology: xsec, asymmetries, etc
- **Problem:** currently, GPDs are accessible experimentally via deeply virtual Compton scattering (DVCS), timelike Compton scattering (TCS) and deeply virtual meson production (DVMP) only



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## Why DDVCS?

- Goal: assessment of feasibility of double deeply virtual Compton scattering (DDVCS) at JLab12, EIC and JLab20+
- **Problem:** DVCS amplitude allows for measurement of the GPD with restriction to  $x = \xi$ . Similar situation happens with TCS for  $x = -\xi$



Sketch of DVCS amplitude (LO)

$$\mathcal{A}_{\text{DVCS}} \sim \int_{-1}^{1} dx \, \frac{1}{x - \xi + i0} \text{GPD}(x, \xi, t) + \cdots$$
$$= \text{PV}\left(\int_{-1}^{1} dx \frac{1}{x - \xi} \text{GPD}(x, \xi, t)\right) - \int_{-1}^{1} dx \, i\pi \delta(x - \xi) \text{GPD}(x, \xi, t) + \cdots$$

So we can measure GPDs at  $x = \xi$  only, i.e., we can access  $\text{GPD}(\xi, \xi, t)$ 

Real part may be expressed by the imaginary part by means of dispersion relations

## Why DDVCS?

- **Problem:** DVCS amplitude allows for measurement of the GPD with restriction to  $x = \xi$ . Similar situation happens with TCS for  $x = -\xi$
- Solution by DDVCS: the extra virtuality allows for the introduction of a new (generalized) Bjorken variable  $\xi$  so that we can access GPDs for  $x = \rho \neq \xi$



Sketch of DDVCS amplitude (LO)

$$\begin{aligned} \mathcal{A}_{\text{DDVCS}} &\sim \int_{-1}^{1} dx \, \frac{1}{x - \rho + i0} \text{GPD}(x, \xi, t) + \cdots \\ &= PV \left( \int_{-1}^{1} dx \frac{1}{x - \rho} \text{GPD}(x, \xi, t) \right) - \int_{-1}^{1} dx \, i\pi \delta(x - \rho) \text{GPD}(x, \xi, t) + \cdots \\ &\xi = -\frac{\bar{q}\Delta}{2\bar{p}\bar{q}}, \quad \rho = \frac{-\bar{q}^2}{2\bar{p}\bar{q}} \end{aligned}$$

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### Formulation à la Kleiss & Stirling

- 1<sup>st</sup> proposed by Belitsky, Mueller, Guidal and Vanderhaeghen in:
  - Exclusive Electroproduction of Lepton Pairs as a Probe of Nucleon Structure, PRL 90, 022001 (2003)
  - > Double Deeply Virtual Compton Scattering off the Nucleon, PRL 90, 012001 (2003)
- Xsec by Belitsky and Mueller in *Probing generalized parton distributions with electroproduction of lepton pairs off the nucleon*, Phys. Rev. D 68, 116005 (2003)
- That work seems to include some typos or mismatches because we cannot reproduce appropriate limits with it: taking a virtuality of DDVCS to be a reality you get either DVCS or TCS
- Consequently, we have performed a rederivation of DDVCS' formulae via Kleiss & Stirling's methods

### Kleiss & Stirling's technique (KS): the basics

- The idea of KS: reduce amplitudes to complex numbers before addressing xsec
- Transform spinor products into new scalars s and t (prevents the use of traces of Dirac gamma matrices):

$$s(p_1, p_2) := \bar{u}_+(p_1)u_-(p_2) = -s(p_2, p_1)$$
  
$$t(p_1, p_2) := \bar{u}_-(p_1)u_+(p_2) = [s(p_2, p_1)]^*$$
  
$$s(p_1, p_2) = (p_1^y + ip_1^z)\sqrt{\frac{p_2^0 - p_2^x}{p_1^0 - p_1^x}} - (p_2 \leftrightarrow p_1)$$

KS' paper: Spinor Techniques for Calculating p anti  $p \rightarrow W+-/Z0 + Jets$ . Nuclear Physics B262 (1985) 235-262

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#### Electroproduction of lepton pair = DDVCS + **BH (pure QED)**



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#### Example: BH1 à la KS

• KS application to BH1 diagram of DDVCS:  $i\widetilde{\mathcal{M}}_{BH1} = \left(\frac{ie^4}{(q_2^2 + i0)(\Delta^2 + i0)((k - \Delta)^2 + i0)}\right)^{-1} i\mathcal{M}_{BH1}$ amplitude

$$\begin{split} i\widetilde{\mathcal{M}}_{\rm BH1} = & (F_1 + F_2) \sum_L \left( Y_{s_2s_1} f(s_\ell, \ell_-, \ell_+; s, k', L) f(s, L, k; +, r'_{s_2}, r_{s_1}) + Z_{s_2s_1} f(s_\ell, \ell_-, \ell_+; s, k', L) f(s, L, k; -, r'_{-s_2}, r_{-s_1}) \right) - \frac{F_2}{2M} J_{s_2, s_1}^{(2)} \sum_{L, R} f(s_\ell, \ell_-, \ell_+; s, k', L) g(s, L, R, k) \end{split}$$

• For example, *f* = contraction of 2 currents

$$f(s, k_0, k_1; s', k_2, k_3) = \bar{u}_s(k_0)\gamma^{\mu}u_s(k_1)\bar{u}_{s'}(k_2)\gamma_{\mu}u_{s'}(k_3)$$

that can be expressed by means of *s* and *t* KS scalars

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#### **Dedicated softwares**

#### → PARTONS platform: open-source C++ program

- Contains several GPD models
- Leading twist... but higher twist corrections will be included in near future
- Useful for theorists and experimentalists
- Provides xsecs, Compton Form Factors, etc
- DVCS, TCS and DVMP are already included

To download and for tutorials: http://partons.cea.fr

Description of architecture: Eur. Phys. J. C78 (2018), 478

Software



#### **Dedicated softwares**

#### → EpIC Monte Carlo event generator in C++

- Uses PARTONS framework
- Includes radiative corrections
- Generates the kinematic configurations following the probability distributions given by PARTONS
- DVCS, TCS and DVMP are already included



Access EpIC via GitHub:

https://github.com/pawelsznajder/epic

Detail description and architecture: arXiv:2205.01762 [hep-ph]

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#### Testing of CFFs: $Q^2 = 1.5 \text{ GeV}^2$ , t = -0.15 GeV<sup>2</sup>



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#### Testing of CFFs: $t = -0.15 \text{ GeV}^2$



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DDVCS to DVCS



DDVCS to TCS

Evaluate energy of incoming virtual photon to be used as energy of TCS photon beam

$$\nu = \frac{Q^2}{2Mx_B}$$

Divide by flux  $\Gamma$  and get rid of  $x_B$  and  $Q^2$  differentiation

$$\Gamma = \frac{\alpha_{em}}{2\pi Q^2} \left( 1 + \frac{(1-y)^2}{y} - \frac{2(1-y)Q_{\min}^2}{yQ^2} \right) \frac{\nu}{Ex_B}, \qquad Q_{\min}^2 = \frac{(ym_e)^2}{1-y}$$

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DDVCS to DVCS



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#### DVCS limit (BH1 + crossed)



 $x_B = 0.04$ , t = -0.1 GeV<sup>2</sup>, Q<sup>2</sup> = 10 GeV<sup>2</sup>, Q<sup>2</sup>  $\approx$  0.001 GeV<sup>2</sup>, E<sub>beam</sub> = 160 GeV

#### DVCS formulae:

Belitsky et al., *Theory of deeply virtual Compton scattering on the nucleon*, Nuclear Physics B629 (2002)

Belitsky et al., *Compton scattering: from deeply virtual to quasi-real*, Nuclear Physics B878 (2014)

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TCS limit (BH2 + crossed)



 $x_B = 2 \cdot 10^{-4}$ , t = -0.5 GeV<sup>2</sup>, Q<sup>2</sup> = 2 \cdot 10^{-3} GeV<sup>2</sup>, Q<sup>3</sup> = 1 GeV<sup>2</sup>, E<sub>beam</sub> = 12 GeV

#### TCS formulae:

Berger et al., *Timelike Compton scattering: exclusive photoproduction of lepton pairs*, The European Physics Journal C 23 (2002)

#### **DVCS** limit (VCS)



 $x_B = 0.04$ , t = -0.01 GeV<sup>2</sup>, Q<sup>2</sup> = 10 GeV<sup>2</sup>, E<sub>beam</sub> = 160 GeV,  $\phi = 0$ 

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### Summary

- New analytical formulae have been derived including polarized target
- DDVCS is already implemented in PARTINE (LO and LT)
- We are interested in observables such as the beam spin asymmetry proportional to Im(BH x VCS\*)
- Code will be included in ODVCS
- We are in contact with experimentalists that will use these codes and we invite everybody to contribute!