

# Evidence for intrinsic charm quarks in the proton

Tommaso Giani

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*Richard D. Ball , Alessandro Candido , Juna Cruz Martininez, Stefano Forte,  
Tommaso Giani , Felix Hekhorn, Kirill Kudashkin, Giacomo Magni and Juan Rojo*



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**THE INTRINSIC CHARM OF THE PROTON**

S.J. BRODSKY<sup>1</sup>

*Stanford Linear Accelerator Center,  
Stanford, California 94305, USA*

and

P. HOYER, C. PETERSON and N. SAKAI<sup>2</sup>

*NORDITA, Copenhagen, Denmark*

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Recent data give unexpectedly large cross-sections for charmed particle production at high  $x_F$  in hadron collisions. This may imply that the proton has a non-negligible  $uudc\bar{c}$  Fock component. The interesting consequences of such a hypothesis are explored.

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## Evidence for intrinsic charm quarks in the proton

[The NNPDF Collaboration](#)

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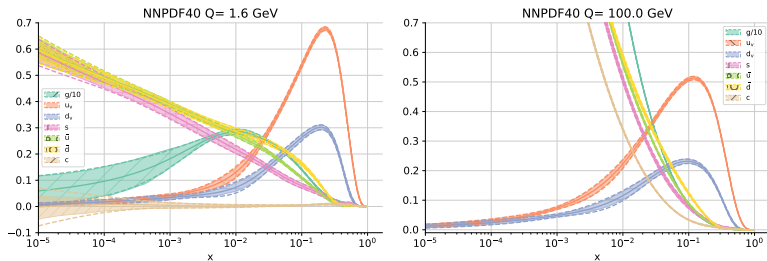
1 Introduction: the treatment of the charm PDF

2 The NNPDF4.0 determination of PDFs

3 Extraction of intrinsic  $c$

4 Phenomenology:  $Z+c$  @ LHCb

## Introduction: the treatment of the charm PDF



$$F(x, Q^2) = \sum_i f_i(\mu^2) \otimes \hat{F}_i\left(\frac{Q^2}{\mu^2}, \alpha_s\right) + \mathcal{O}\left(\frac{\Lambda_{QCD}^2}{Q^2}\right)$$

→  $f_i(x, \mu^2)$  are universal: can be extracted from a set of data for some processes and used to make predictions for others

# Heavy quarks PDFs

## $N_f = 4$ scheme (massless scheme)

- $Q \gg m_c$
- computation of  $\hat{F}$  does not retain mass effects
- collinear  $\log \frac{Q^2}{m_c^2}$  are factored in charm PDF  $\rightarrow f_c^{n_f+1}(x, \mu)$
- 4 active flavors in  $\beta$  function and DGLAP

## $N_f = 3$ scheme (massive scheme)

- $Q \sim m_c$
- computation of  $\hat{F}$  retains mass effects, and explicit not resummed  $\log \frac{Q^2}{m_c^2}$
- charm decouples: renormalization-group independent charm PDF  $\rightarrow f_c^{n_f}(x)$   
[Collins, Wilczek and Zee, Phys.Rev. D18,242, 1978]
- 3 active flavors in  $\beta$  function and DGLAP

$$4\text{FS} : f_q^{n_f+1}(x, Q^2), \quad q = \{u, d, s, c, \bar{u}, \bar{d}, \bar{s}, \bar{c}\}$$

$$3\text{FS} : f_q^{n_f}(x, Q^2), f_h^{n_f}(x) \quad q = \{u, d, s, \bar{u}, \bar{d}, \bar{s}\} \quad h = \{c, \bar{c}\}$$

Relation between the PDFs and  $\alpha_s$  in the two schemes is given by

$$\begin{pmatrix} f_q \\ f_c \end{pmatrix}^{n_f+1}(\mu_h^2) = \begin{pmatrix} A_{qq} & A_{qc} \\ A_{cq} & A_{cc} \end{pmatrix} \begin{pmatrix} f_q \\ f_c \end{pmatrix}^{n_f}(\mu_h^2)$$

- Operator Matrix Elements (OME)  $A_{ij}$  known up to  $N^3LO$
- OME depend on  $\alpha_s(\mu_h)$  and  $\log \frac{\mu_h}{m_c}$



## Perturbative charm

Charm in  $N_f = 4$  generated purely by perturbative matching

$$f_c^{n_f}(x) = 0 \quad \rightarrow \quad f_c^{n_f+1}(x, m_c^2) = \sum_{i=q,g} A_{ci} f_i^{n_f}(x, m_c^2) = \mathcal{O}(\alpha_s^2)$$

$$f_c^{n_f+1}(x, Q^2) \propto \alpha_s \log \frac{Q^2}{m_c^2} \left( P_{qg} \otimes f_g^{(n_f+1)} \right) + \mathcal{O}(\alpha_s^2)$$

- once the light flavors are determined, charm is fixed by matching and evolution

## Fitted charm

Non vanishing  $N_f = 3$  charm PDF is allowed

$$f_c^{n_f}(x) \neq 0 \rightarrow f_c^{n_f+1}(x, m_c^2) = \sum_{i=q,g} A_{ci} f_i^{n_f}(x, m_c^2) + A_{cc} f_c^{n_f}(x)$$

- 4FS charm is not fixed by the light flavors PDF
- we can fit charm PDF from data as any other quark

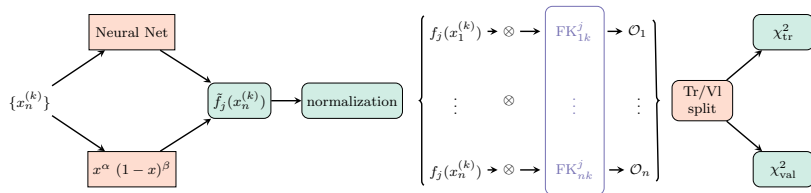
**Can we provide a determination of  $f_c^{n_f}(x)$  ?**

**intrinsic charm  $\iff f_c^{n_f}(x) \neq 0$**

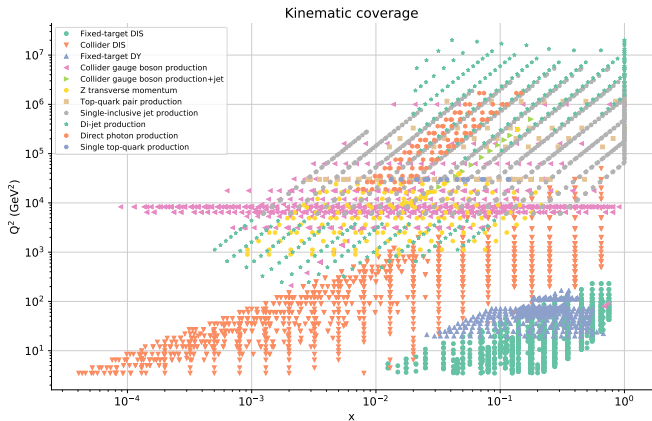
## The NNPDF4.0 determination of PDFs

# Methodology

- PDFs are parameterized in  $N_f = 4$ , at  $Q_0 = 1.65$  GeV
- PDFs parameterized using a neural network and a preprocessing polynomial factor



- split of data in training validation sets  $\rightarrow \chi_{tr}^2, \chi_{val}^2$
- minimization performed on  $\chi_{tr}^2$ , stopping controlled by  $\chi_{val}^2$



- new processes included for the first time: single top,  $W$ +jet, isolated photon, di-jets
- extensive use of 13 TeV dataset
- total of  $\mathcal{O}(4000)$  datapoints

Data set	NNPDF4.0	NNPDF3.1	ABMP16	CT18	MSHT20
ATLAS $W, Z$ 7 TeV (2010)	✓	✓	✓	✓	✓
ATLAS $W, Z$ 7 TeV (2011)	✓	✓	✗	✓	✓
ATLAS low-mass DY 7 TeV	✓	✓	✗	✗	✗
ATLAS high-mass DY 7 TeV	✓	✓	✗	✗	✓
ATLAS $W$ 8 TeV	✓	✗	✗	✗	✓
ATLAS DY 2D 8 TeV	✓	✗	✗	✗	✓
ATLAS high-mass DY 2D 8 TeV	✓	✗	✗	✗	✓
ATLAS $\sigma_{W, Z}$ 13 TeV	✓	✗	✓	✗	✗
ATLAS $W^+$ +jet 8 TeV	✓	✗	✗	✗	✓
ATLAS $Z$ $p_T$ 8 TeV	✓	✓	✗	✓	✓
ATLAS $\sigma_{H^{\pm}}$ 7, 8 TeV	✓	✓	✓	✗	✗
ATLAS $\sigma_{H^0}$ 13 TeV	✓	✓	✓	✗	✗
ATLAS $t\bar{t}$ lepton+jets 8 TeV	✓	✓	✗	✓	✓
ATLAS $t\bar{t}$ dilepton 8 TeV	✓	✗	✗	✗	✓
ATLAS single-inclusive jets 7 TeV, R=0.6	✗	✓	✗	✓	✓
ATLAS single-inclusive jets 8 TeV, R=0.6	✓	✗	✗	✗	✗
ATLAS dijets 7 TeV, R=0.6	✓	✗	✗	✗	✗
ATLAS direct photon production 13 TeV	✓	✗	✗	✗	✗
ATLAS single top $R_t$ 7, 8, 13 TeV	✓	✗	✓	✗	✗
ATLAS single top diff. 7, 8 TeV	✓	✗	✗	✗	✗
ATLAS single top diff. 8 TeV	✓	✗	✗	✗	✗

Data set	NNPDF4.0	NNPDF3.1	ABMP16	CT18	MSHT20
LHCb $Z$ 940 pb	✓	✓	✗	✗	✓
LHCb $Z \rightarrow ee$ 2 fb	✓	✓	✓	✓	✓
LHCb $W, Z \rightarrow \mu$ 7 TeV	✓	✓	✓	✓	✓
LHCb $W, Z \rightarrow \mu$ 8 TeV	✓	✓	✓	✓	✓
LHCb $Z \rightarrow \mu\mu, ee$ 13 TeV	✓	✗	✗	✗	✗

Data set	NNPDF4.0	NNPDF3.1	ABMP16	CT18	MSHT20
CMS $W$ electron asymmetry 7 TeV	✓	✓	✗	✓	✓
CMS $W$ muon asymmetry 7 TeV	✓	✓	✓	✓	✗
CMS Drell-Yan 2D 7 TeV	✓	✓	✗	✗	✓
CMS $W$ rapidity 8 TeV	✓	✓	✓	✓	✓
CMS $Z$ $p_T$ 8 TeV	✓	✓	✗	✓	✗
CMS $W + c$ 7 TeV	✓	✓	✗	✗	✓
CMS $W + c$ 13 TeV	✓	✗	✗	✗	✗
CMS single-inclusive jets 2.76 TeV	✗	✓	✗	✗	✓
CMS single-inclusive jets 7 TeV	✗	✓	✗	✓	✓
CMS dijets 7 TeV	✓	✗	✗	✗	✗
CMS single-inclusive jets 8 TeV	✗	✗	✗	✓	✓
CMS 3D dijets 8 TeV	✓	✗	✗	✗	✗
CMS $\sigma_{H^{\pm}}^{\text{tot}}$ 5 TeV	✓	✗	✓	✗	✗
CMS $\sigma_{H^{\pm}}^{\text{tot}}$ 7, 8 TeV	✓	✓	✓	✗	✓
CMS $\sigma_{H^{\pm}}^{\text{tot}}$ 13 TeV	✓	✓	✓	✗	✗
CMS $t\bar{t}$ lepton+jets 8 TeV	✓	✓	✗	✗	✓
CMS $t\bar{t}$ dilepton 8 TeV	✓	✗	✗	✓	✓
CMS $t\bar{t}$ dilepton+jet 13 TeV	✓	✗	✗	✗	✗
CMS $t\bar{t}$ dilepton 13 TeV	✓	✗	✗	✗	✗
CMS single top $\sigma_{\ell} + \sigma_{\bar{\ell}}$ 7 TeV	✓	✗	✓	✗	✗
CMS single top $R_t$ 8, 13 TeV	✓	✗	✓	✗	✗

- Python object oriented codebase
- Freedom to use external libraries (default: TensorFlow)
- Documentation and tutorials provided
- Results for a replica available in less than an hour ( $\sim 40$ mins on 1 CPU)
- **Code fully public**



Tests passing DOI [10.5281/zenodo.5362229](https://doi.org/10.5281/zenodo.5362229)

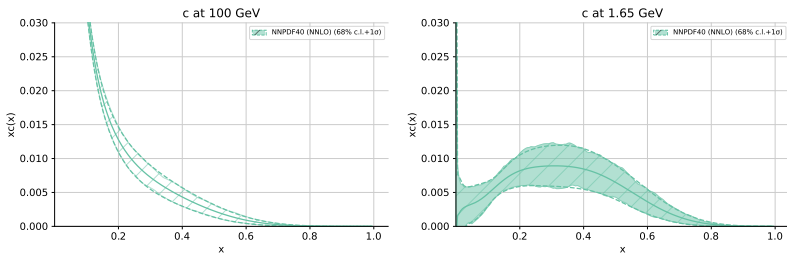
## NNPDF: An open-source machine learning framework for global analyses of parton distributions

The [NNPDF collaboration](#) determines the structure of the proton using Machine Learning methods. This is the main repository of the fitting and analysis frameworks. In particular it contains all the necessary tools to [reproduce](#) the NNPDF4.0 PDF determinations.

Extraction of intrinsic c



NNPDF4.0 charm PDF: parameterized and determined from experimental data in  $N_f = 4$ .



$$\tilde{f}^{n_f+1}(Q_1^2) = \tilde{E}^{(n_f+1)}(Q_1^2 \leftarrow \mu_h) \tilde{A}^{n_f}(\mu_h^2) \tilde{E}^{(n_f)}(\mu_h \leftarrow Q_0^2) \tilde{f}^{n_f}(Q_0^2)$$

# EKO

Evolution Kernel Operators



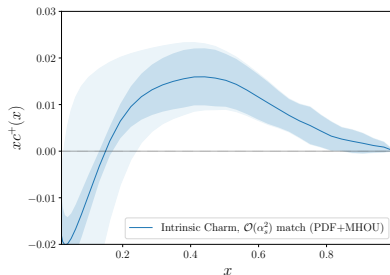
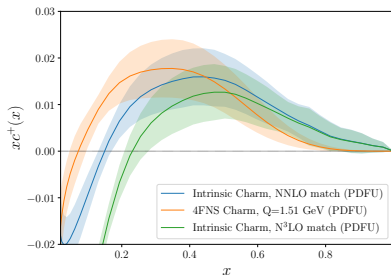
EKO is a Python module to solve the DGLAP equations in N-space in terms of Evolution Kernel Operators in x-space.

[Candido, Hekhorn and Magni, Eur.Phys.J.C 82 (2022)]

- implementation of DGLAP solutions at LO, NLO, NNLO
- various solution methods implemented
- implementation of matching in Mellin space
- inverse Matching implemented both exactly and expanding and  $\alpha_s$

## Intrinsic charm

$$f_i^{n_f+1}(x, \mu = 1.65 \text{ GeV}) \rightarrow f_i^{n_f+1}(x, \mu = 1.51 \text{ GeV}) \rightarrow f_c^{n_f}(x)$$

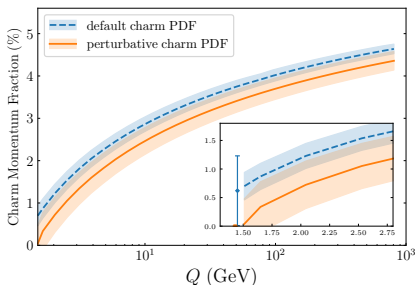


- valence like peak in the region  $0.3 < x < 0.6$
- in the region  $0.3 < x < 0.6$  PDF uncertainty is the dominant one
- large perturbative uncertainties for  $x < 0.2$

# Momentum fraction

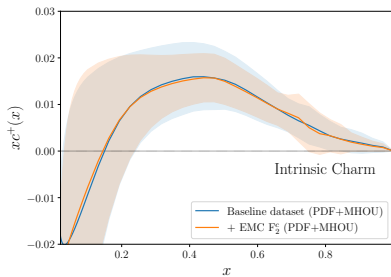
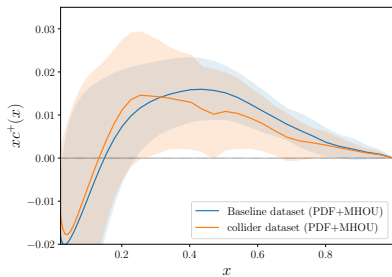
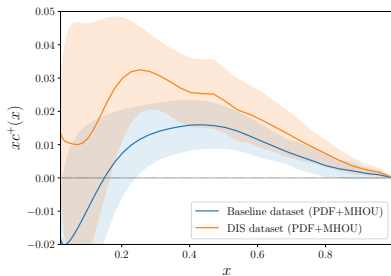
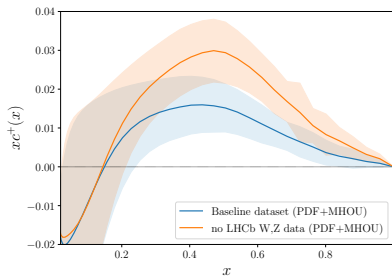
$$[c] = \int_0^1 dx x c^+(x, Q)$$

Scheme	$Q$	Charm PDF	$m_c$	$[c]$ (%)
3FNS	–	default	1.51 GeV	$0.62 \pm 0.28_{\text{pdf}} \pm 0.54_{\text{mhou}}$
4FNS	1.65 GeV	default	1.51 GeV	$0.87 \pm 0.23_{\text{pdf}}$
4FNS	1.65 GeV	perturbative	1.51 GeV	$0.346 \pm 0.005_{\text{pdf}} \pm 0.44_{\text{mhou}}$



- momentum fraction of 4FNS PDF different from 0 at  $3\sigma$  level (PDF uncertainty only)
- big MHO uncertainty on IC momentum fraction (due to region  $x < 0.2$ )
- not possible to tell whether 4FS momentum fraction is of perturbative or intrinsic origin

# Dataset dependence



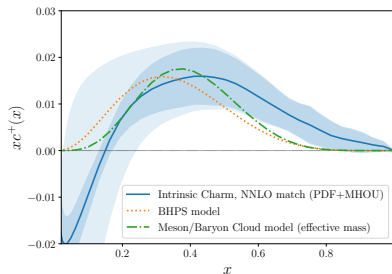
# Comparison with models

- BHPS model: [Phy. Letter B (1980) 451-455]

$$x c^+ = \frac{1}{2} N x^3 \left[ \frac{1}{3} (1-x) (1+10x+x^2) + 2x (1+x^2) \ln x \right]$$

- Meson Baryon model: [arxiv:1311.1578]

$$x c^+ = \frac{N}{B (\alpha + 2, \beta + 1)} x^{1+\alpha} (1-x)^\beta$$

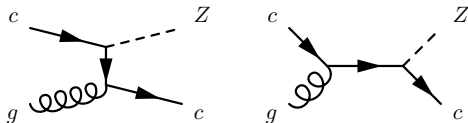


Phenomenology:  $Z+c$  @ LHCb

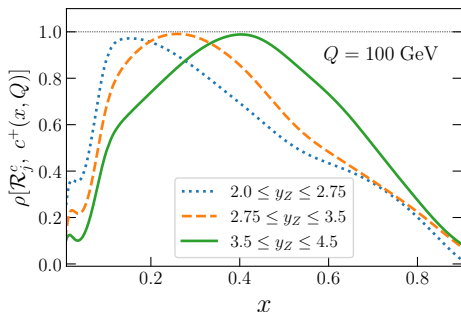
# Z+c measurements from LHCb

Measurement of Z bosons produced in association with charm in the forward region  
[Phys.Rev.Lett. 128 (2022)]

$$\mathcal{R}_j^c = \frac{\sigma(pp \rightarrow Z + \text{charm jet})}{\sigma(pp \rightarrow Z + \text{jet})}$$



$y(Z)$	$\mathcal{R}_j^c$ (%)
2.00–2.75	$6.84 \pm 0.54 \pm 0.51$
2.75–3.50	$4.05 \pm 0.32 \pm 0.31$
3.50–4.50	$4.80 \pm 0.50 \pm 0.39$
2.00–4.50	$4.98 \pm 0.25 \pm 0.35$

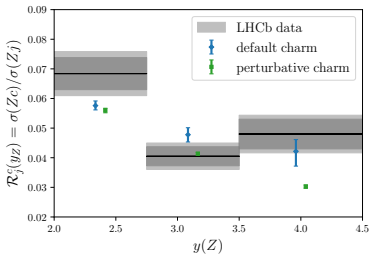
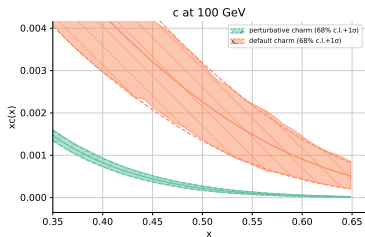


→ The most forward rapidity bin is sensitive to charm PDF in the region of the valence peak

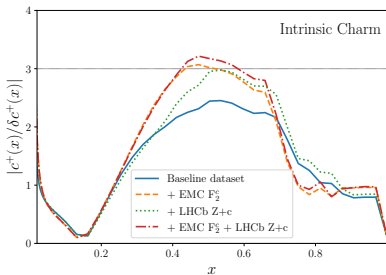
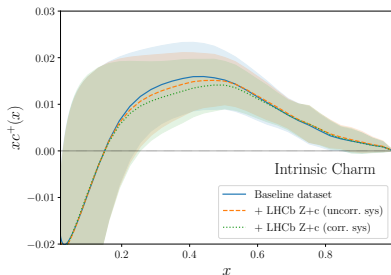
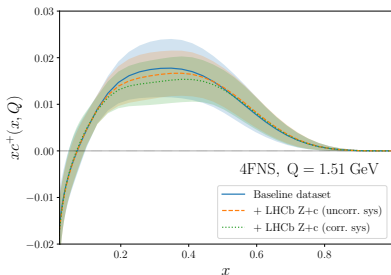


Theory prediction for  $R_j^c$  computed using POWHEG @ NLO + PS, using both perturbative and default (fitted) charm

Z bosons	$p_T(\mu) > 20 \text{ GeV}, 2.0 < \eta(\mu) < 4.5, 60 < m(\mu^+\mu^-) < 120 \text{ GeV}$
Jets	$20 < p_T(j) < 100 \text{ GeV}, 2.2 < \eta(j) < 4.2$
Charm jets	$p_T(c \text{ hadron}) > 5 \text{ GeV}, \Delta R(j, c \text{ hadron}) < 0.5$
Events	$\Delta R(\mu, j) > 0.5$



- theory prediction based on perturbative charm in disagreement with LHCb data
- better agreement found using NNPDF4.0 baseline (fitted charm)



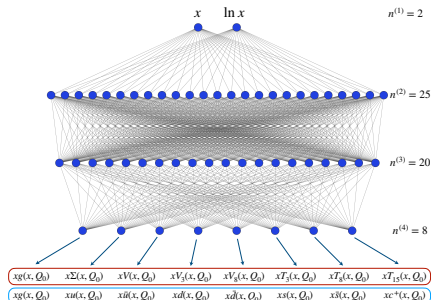
- inclusion of LHCb (by bayesian RW) and EMC data gives compatible results with moderate reduction of PDF error
- local significance for IC at  $2.5\sigma$  in  $0.3 < x < 0.6$ , getting to  $3\sigma$  when including LHCb and EMC data

# Summary

- starting point: NNPDF4.0 charm PDF, fitted in the 4FS
- determination of charm PDF in the 3FNS
  - local evidence for non-vanishing valence peak
  - large uncertainties at small  $x$
- future data
  - HL-LHC data
  - EIC data for  $F_c^2$
- to do:
  - $c - \bar{c}$  asymmetry

# Hyperoptimization

Parameter	NNPDF4.0
Architecture	2-25-20-8
Activation function	hyperbolic tangent
Initializer	glorot_normal
Optimizer	Nadam
Clipnorm	$6.0 \times 10^{-6}$
Learning rate	$2.6 \times 10^{-3}$
Maximum # epochs	$17 \times 10^3$
Stopping patience	10% of max epochs
Initial positivity $\Lambda^{(POS)}$	185
Initial integrability $\Lambda^{(int)}$	10



✗ Selecting manually the best set of parameters is a slow process and systematic success is not guaranteed

✓ Hyperparameter scan: let the computer decide automatically

- Define a methodology (a specific hyperparameter combination)
- Define a reward function to grade the methodology
- Scan over thousands of hyperparameter combinations and select the best one

Evolution equations

$$\mu_F^2 \frac{d\mathbf{f}}{d\mu_F^2} (x, \mu_F^2) = \mathbf{P}(\alpha_s(\mu_R^2), \mu_F^2) \otimes \mathbf{f}(\mu_F^2),$$

can be written in Mellin space as

$$\frac{d\tilde{\mathbf{f}}}{d\alpha_s}(N, \alpha_s) = -\frac{\gamma(N, \alpha_s)}{\beta(\alpha_s)} \tilde{\mathbf{f}}(N, \alpha_s),$$

and solved as

$$\tilde{\mathbf{f}}(N, \alpha_s) = \tilde{\mathbf{E}}(\alpha_s \leftarrow \alpha_s^0) \tilde{\mathbf{f}}(N, \alpha_s^0), \quad \tilde{\mathbf{E}}(\alpha_s \leftarrow \alpha_s^0) = \mathcal{P} \exp \left[ - \int_{\alpha_s^0}^{\alpha_s} \frac{\gamma(\alpha'_s)}{\beta(\alpha'_s)} d\alpha'_s \right].$$

In x-space

$$\mathbf{f}(x, \mu) = \mathbf{E}(\mu \leftarrow \mu_0) \otimes \mathbf{f}(x, \mu_0).$$

## Matching

When we cross the threshold for heavy quark production we have to apply the matching

$$\tilde{\mathbf{f}}^{n_f+1}(Q_1^2) = \tilde{\mathbf{E}}^{(n_f+1)}(Q_1^2 \leftarrow \mu_h) \tilde{\mathbf{A}}^{n_f}(\mu_h^2) \tilde{\mathbf{E}}^{(n_f)}(\mu_h \leftarrow Q_0^2) \tilde{\mathbf{f}}^{n_f}(Q_0^2)$$

$$\begin{aligned} \left( \begin{array}{c} \tilde{V} \\ \tilde{h}_- \end{array} \right)^{n_f+1}(\mu_h^2) &= \tilde{\mathbf{A}}_{NS,h_-}^{n_f}(\mu_h^2) \left( \begin{array}{c} \tilde{V} \\ \tilde{h}_- \end{array} \right)^{n_f}(\mu_h^2) \\ \left( \begin{array}{c} \tilde{g} \\ \tilde{\Sigma} \\ \tilde{h}_+ \end{array} \right)^{n_f+1}(\mu_h^2) &= \tilde{\mathbf{A}}_{S,h_+}^{n_f}(\mu_h^2) \left( \begin{array}{c} \tilde{g} \\ \tilde{\Sigma} \\ \tilde{h}_+ \end{array} \right)^{n_f}(\mu_h^2) \end{aligned}$$

OME depend on  $\alpha_s^{n_f+1}(\mu_h^2)$  and  $\log(\mu_h^2/m_h^2)$

## Matching: more in details

OME are available up to N3LO with only NLO for heavy quark entries

$$\bar{\mathbf{A}}^{nf}(\mu_h^2) = \mathbf{I} + \alpha_s(\mu_h^2) \bar{\mathbf{A}}^{nf,(1)} + \alpha_s^2(\mu_h^2) \bar{\mathbf{A}}^{nf,(2)} + \alpha_s^3(\mu_h^2) \bar{\mathbf{A}}^{nf,(3)} + \dots$$

$$\bar{\mathbf{A}}_{S,h_+}^{nf,(1)} = \begin{pmatrix} A_{gg}^{S,(1)} & 0 & A_{gH}^{S,(1)} \\ 0 & 0 & 0 \\ A_{Hg}^{S,(1)} & 0 & A_{HH}^{S,(1)} \end{pmatrix}, \quad \bar{\mathbf{A}}_{S,h_+}^{nf,(2)} = \begin{pmatrix} A_{gg}^{S,(2)} & A_{gq}^{S,(2)} & 0 \\ 0 & A_{qq}^{S,(2)} & 0 \\ A_{Hg}^{S,(2)} & A_{Hq}^{S,(2)} & 0 \end{pmatrix}, \quad \bar{\mathbf{A}}_{S,h_+}^{nf,(3)} = \begin{pmatrix} A_{gg}^{S,(3)} & A_{gq}^{S,(3)} & 0 \\ 0 & A_{qq}^{S,(3)} & 0 \\ A_{Hg}^{S,(3)} & A_{Hq}^{S,(3)} & 0 \end{pmatrix}$$

$$\bar{\mathbf{A}}_{NS,h_-}^{nf,(1)} = \begin{pmatrix} 0 & 0 \\ 0 & A_{HH}^{NS,(1)} \end{pmatrix}, \quad \bar{\mathbf{A}}_{NS,h_-}^{nf,(2)} = \begin{pmatrix} A_{qq}^{NS,(2)} & 0 \\ 0 & 0 \end{pmatrix}, \quad \bar{\mathbf{A}}_{NS,h_-}^{nf,(3)} = \begin{pmatrix} A_{qq}^{NS,(3)} & 0 \\ 0 & 0 \end{pmatrix}$$

NNLO [[Eur.Phys.J.C 1 \(1998\) 301-320](#)],

NLO massive [[Phys.Lett.B 754 \(2016\) 49-58](#)],

N<sup>3</sup>LO [[Ablinger, Blumlein et al, 2009-2017](#)]

The inversion can be done either perturbatively or exactly

$$\left(\bar{\mathbf{A}}^{nf}\right)^{-1}(\mu_h^2) = \mathbf{I} - \alpha_s(\mu_h^2) \bar{\mathbf{A}}^{nf,(1)} + \alpha_s^2(\mu_h^2) \left(\bar{\mathbf{A}}^{nf,(2)} - \left(\bar{\mathbf{A}}^{nf,(1)}\right)^2\right) + \mathcal{O}(\alpha_s^3)$$

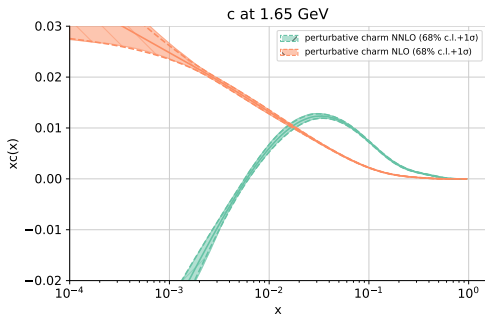
# Fitted vs perturbative charm

## Fitted charm

- agnostic about  $f_c^{n_f}$
- independent of matching conditions: no dependence on perturbative order,  $\mu_h$ ,  $m_c$
- more realistic PDF error given by the data

## Perturbative charm

- ✗ fix  $f_c^{n_f} = 0$
- ✗ c PDF built using matching + evolution: perturbative unstable, strong dependence on  $\mu_h$ ,  $m_c$
- ✗ big MHO uncertainty, unrealistic PDF error





# Mass dependence

