Heavy flavour physics

Lecture 2

Marcin Kucharczyk

IFJ PAN, Kraków 01 December 2022

Contents

Lecture 2

- Experimental facilities
- CKM matrix and types of CP violation
- \bullet Measurements of CKM angles β and α

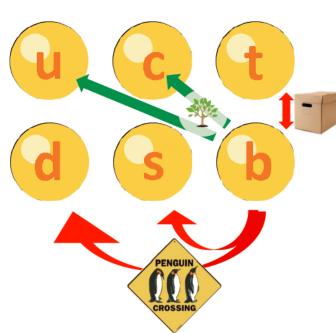
Experimental facilities

Heavy flavour physics

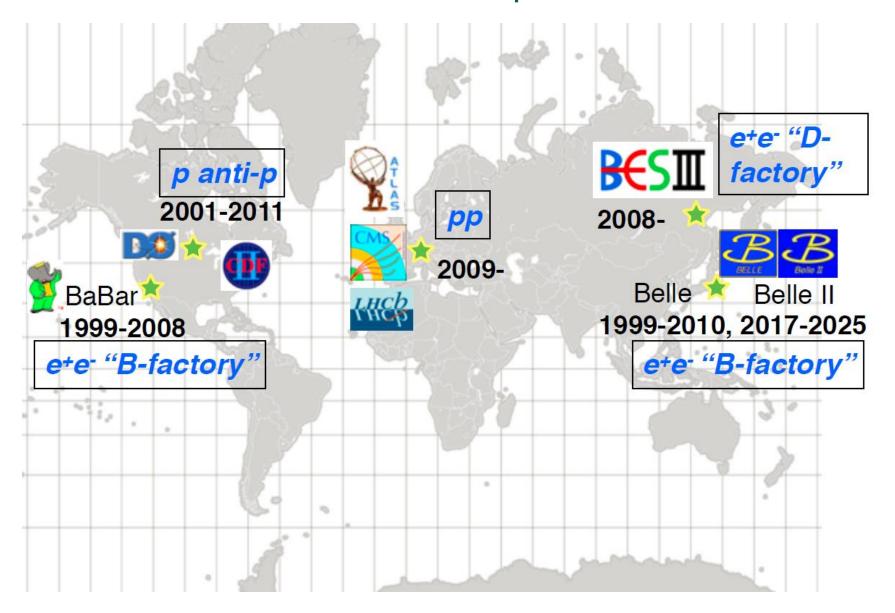
- Focus in these lecture will be on
 - flavour changing interactions of charm and beauty quarks
- But quarks feel the strong interaction and hadronize
 - various different beauty hadrons
 - many possible decays to different final states
 - → hadronization introduces great complications, BUT also increases the observability of CP violation effects
- Many aspects of flavour physics left out in this lecture
 - neutrino physics: have own phenomenology
 - light quark flavour physics
 - charged lepton physics
 - top-flavour physics: different, as the top does not hadronize

Rich phenomenology with beauty quarks

- The beauty quark ...
 - is the heaviest quark that forms hadronic bound states
 - → high mass: many accessible final states
 - must decay outside the 3rd family
 - → all decays are CKM suppressed
 - \rightarrow long lifetime of B meson (~1.6ps)
- Beauty-decays:
 - dominant decay process: "tree"
 b → c transition
 - very suppressed "tree" $b \rightarrow u$ transition
 - FCNC "penguin" $b \rightarrow s$ and $b \rightarrow d$ transitions
 - flavour oscillations ($b \rightarrow t$ "box" diagrams)
 - CP violation expect large CP asymmetries in some B decays



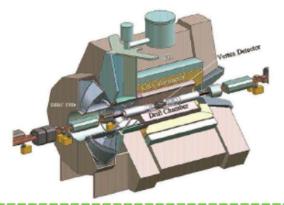
Where are B and D mesons produced



Flavour physics experiments

B-factories (BaBar & Belle)

- e⁺e⁻ experiment at SLAC / KEK
- Dedicated B-physics experiment

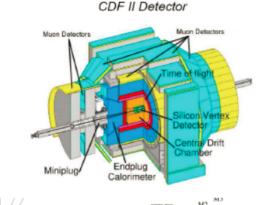


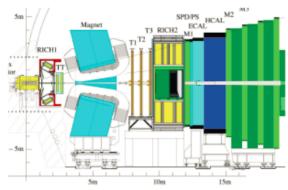
General purpose detectors (ATLAS, CMS, CDF, D0)

- Proton colliders @ CERN / Tevatron
- 4π multi purpose detectors

LHCb

- Proton colliders @ CERN
- Dedicated B-physics experiment

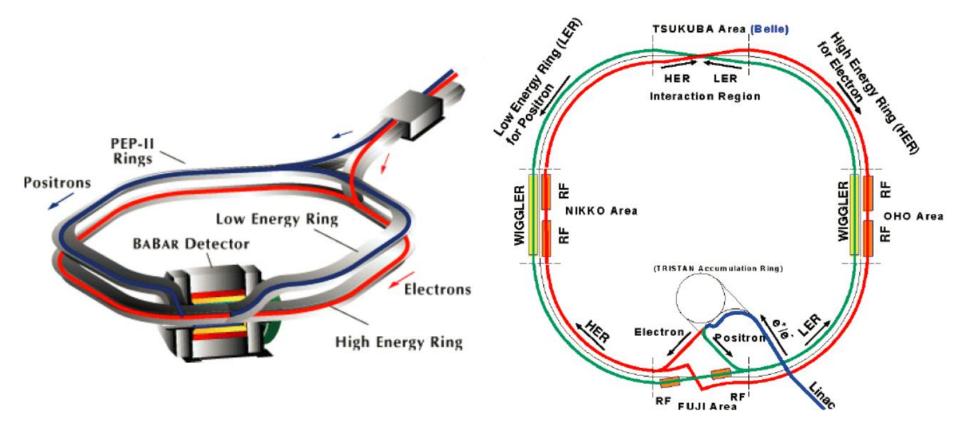




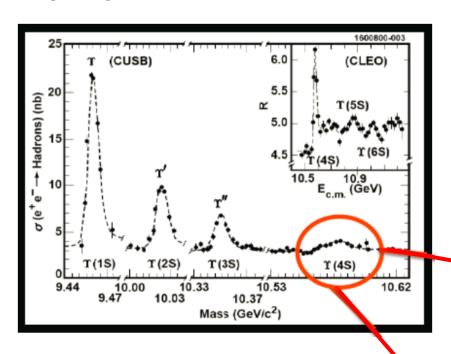
e⁺e⁻: Asymmetric B factories

PEPII at SLAC

KEKB at KEK 9.0 GeV e⁻ on 3.1 GeV e⁺ 8.0 GeV e⁻ on 3.5 GeV e⁺



Y(4S) resonance



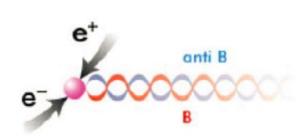
Cleanest way to produce B mesons in e⁺e⁻ collisions: at centre-of-mass energy = mass of Y(4S)

$$\sqrt{s} = 10.58 \text{ GeV}$$

Y(4S) is bound bb-state that decays to $\sim 100\%$ to B+B- or B0B(bar) pairs

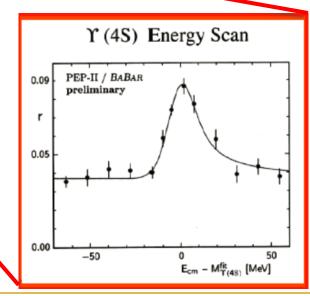
~1.1M BB(bar) pairs per fb⁻¹

$$\sigma_{\rm bb}$$
 / $\sigma_{\rm continuum}$ ~ 1/3



BB pair is produced in a coherent state

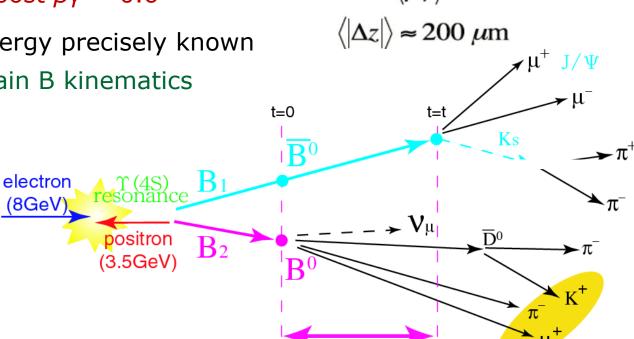
→ two B mesons evolve until one decays



Kinematics at e⁺e⁻ colliders

- Symmetric collider: B-mesons produced almost at rest
 - → short lifetime make flight distance unmeasurably small
- Asymmetric collider (KEKB, PEPII)
 - \rightarrow with boost $\beta \gamma \sim 0.6$
- Beam energy precisely known

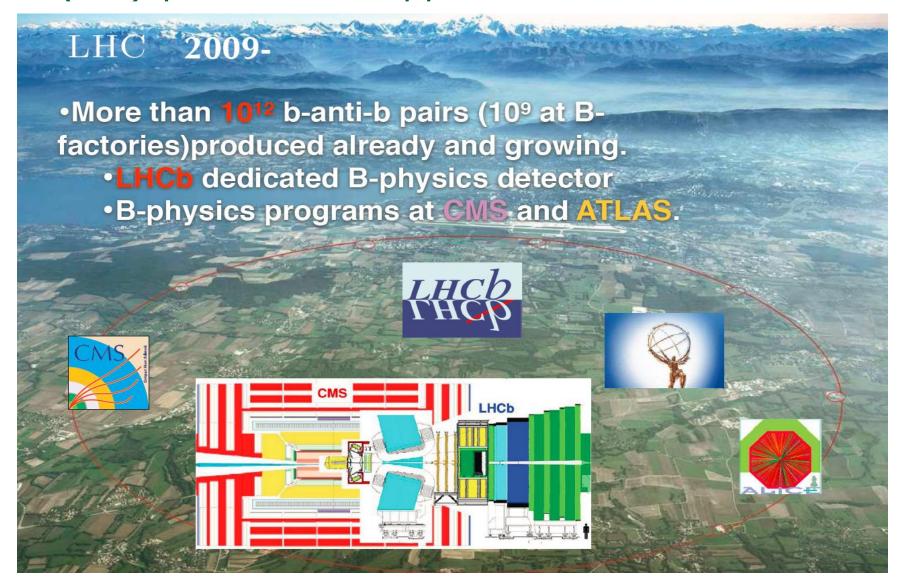
→ constrain B kinematics



ΔZ~200μm

- To measure t require B meson to be moving
 - \rightarrow e⁺e⁻ at threshold with asymmetric collisions

bb(bar) production at pp collider

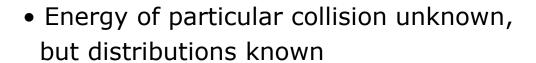


Proton collisions

- Protons are complicated objects
 - valence & sea quarks, gluons
- Available energy of "proton" collision depends on partons

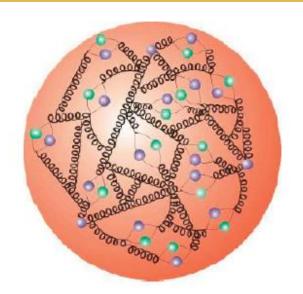
$$s' = x_1 \cdot x_2 \cdot s$$

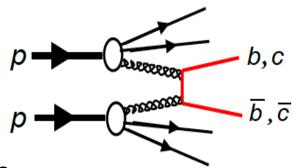
 x_i = Bjorken x (fractional momentum) of parton





- average s' ~ 0.1 s
- dominant process @ LHC: gluon fusion

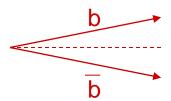




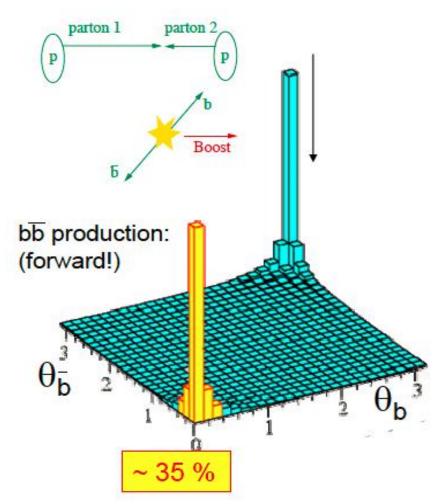
10

Event kinematics

In high energy collisions, bb(bar) pairs produced predominantly in forward or backward directions

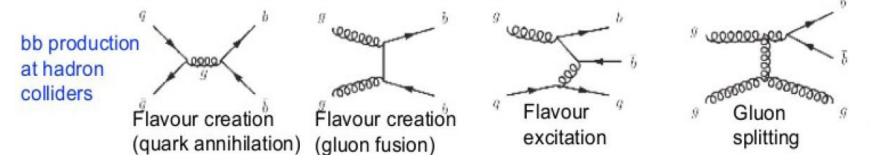


- B hadron mass ~ 5 GeV
 - asymmetric x-values
 - strongly boosted ($\beta\gamma \sim 100$)
 - average flight length ~ 7mm
- Boost allows time dependent analyses of fast B_s mixing
- B hadron admixture:
 - 40% B⁰
 - 40% B[±]
 - $-10\% B_{s}$
 - $-10\% \Lambda_h$
 - <1% others (B_c, B*, B**, ...)

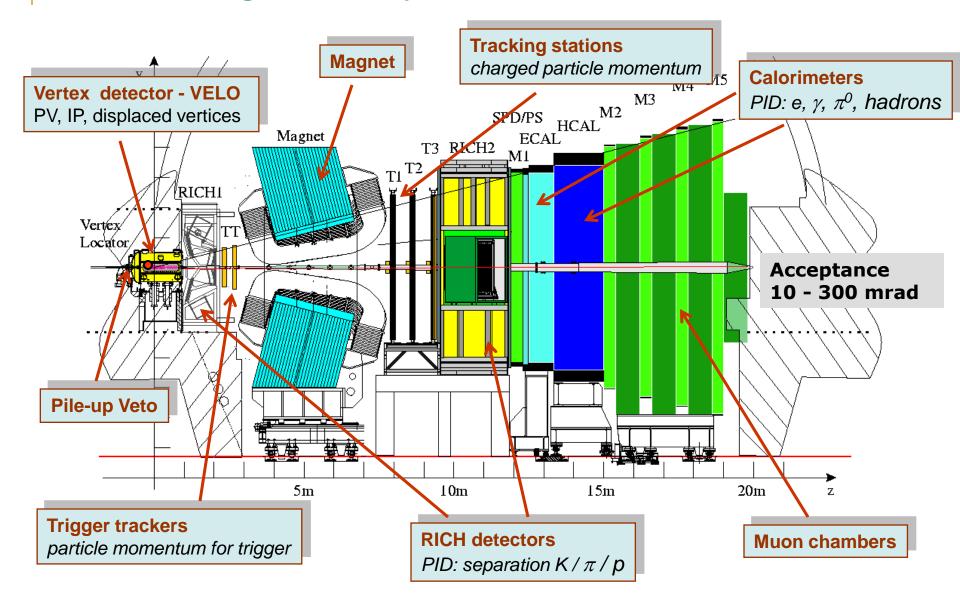


b production at hadron colliders

| | $e^+e^- \rightarrow \Upsilon(4s) \rightarrow B\overline{B}$ PEP-II, KEK-B | $p\overline{p} \rightarrow b\overline{b}X (\sqrt{s} = 2 \text{ TeV})$ TeVatron | $pp \rightarrow b\bar{b}X (\sqrt{s} = 14 \text{ TeV})$ | |
|----------------------------|--|---|---|--|
| prod | 1 nb | ~100 µb | ~500 µb | |
| typ. $b ar{b}$ rate | 10 Hz | ~100 kHz | ~500 kHz | |
| purity | ~1/4 | $\sigma_{b\bar{b}}/\sigma_{inel} \approx 0.2\%$ | $\sigma_{b\bar{b}}/\sigma_{inel} \approx 0.6\%$ | |
| pile-up | 0 | 1.7 | 0.5-20 | |
| B content | $B^{+}B^{-}(50\%), B^{0}\overline{B}^{0}(50\%)$ | $B^+(40\%), B^0(40\%), B_s(10\%), B_c(<1\%), b-baryons(10\%)$ | | |
| B boost | small, βγ~0.56 | large, decay vertices are displaced | | |
| event structure | BB pair alone | many particles non-associated to $bar{b}$ | | |
| prod. vertex | Not reconstructed | reconstructed with many tracks | | |
| $B^0\overline{B}^0$ mixing | coherent | incoherent→ flavour tagging dilution | | |



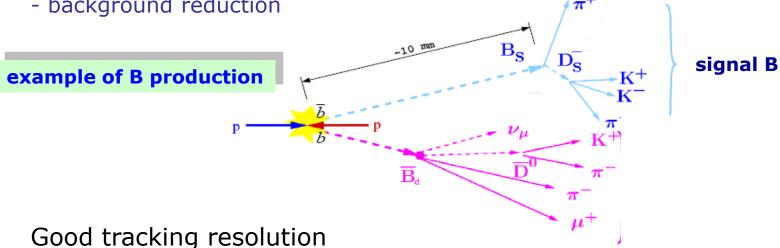
LHCb - single arm spectrometer



Detector requirements

Good decay vertex resolution

proper time resolutionbackground reduction



- proper tracking and good momentum resolution

Particle identification in the wide momentum range (2 - 100 GeV/c)

- background reduction if kinematic separation not sufficient

Fast and efficient trigger system

- selection of interesting events from large background

Fast data aquisition system

LHC flavour physics programme

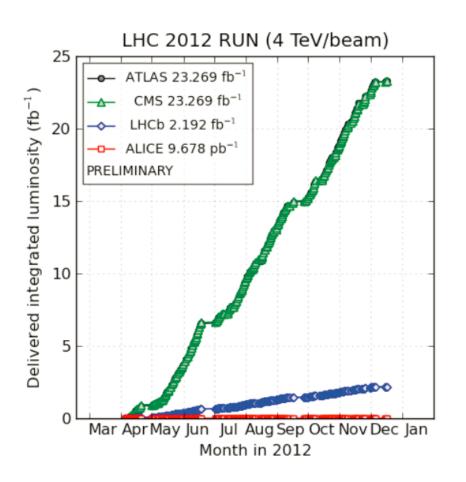
ATLAS / CMS

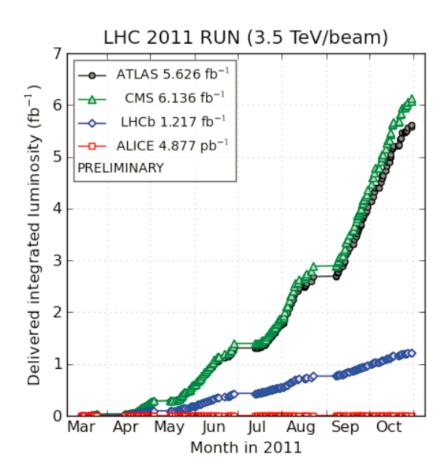
- Central detectors, |η|<2.5
- High Luminosity (>10³⁴cm⁻²s⁻¹)
 → high pileup ~20
- Trigger
 - Relatively low rate (~200-400Hz)
 - High PT muon triggers
- Analysis
 - Mostly modes with dimuons
 - Limited flavour tagging
- Particle identification
 - Excellent muon ID
 - Limited K / π separation

LHCb

- Forward spectrometer, 1.9< η < 5
- Lower Luminosity (4x10³²cm⁻²s⁻¹)
 → pileup ~1.5
- Trigger
 - High trigger rate (~2kHz)
 - Muon & hadron triggers, softer thresholds
 - Large bandwidth for charm
- Analysis
 - Hadronic and low M modes accessible
 - Excellent flavour tagging & σ_t
- Particle identification
 - Excellent muon ID
 - Dedicated RICH PID (K / π)

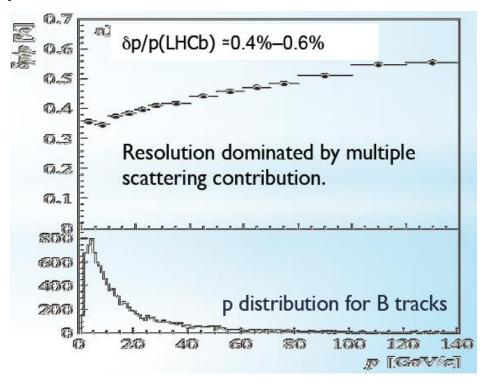
Key issues for B physics: data statistics





Full dataset (Run I): ATLAS = CMS = 10 * LHCb

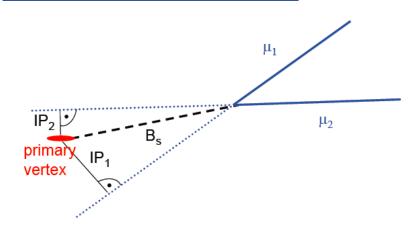
Key issues for B physics: momentum and mass resolution



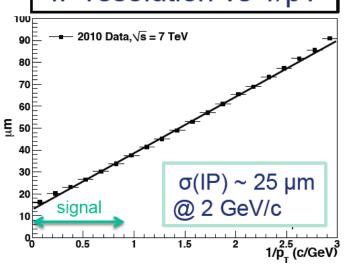
| | momentum resolution | mass resolution J/ψ→μμ | |
|-------|------------------------|---------------------------|--|
| LHCb | δp/p = 0.4-0.6 % | 13 MeV | |
| CMS | δpt/pt = 1-3 % | 40 MeV | |
| ATLAS | δpt/pt = 5-6 % | 71 MeV | |

Key issues for B physics: IP and PV resolution

Impact parameter (IP):



IP resolution vs 1/pT

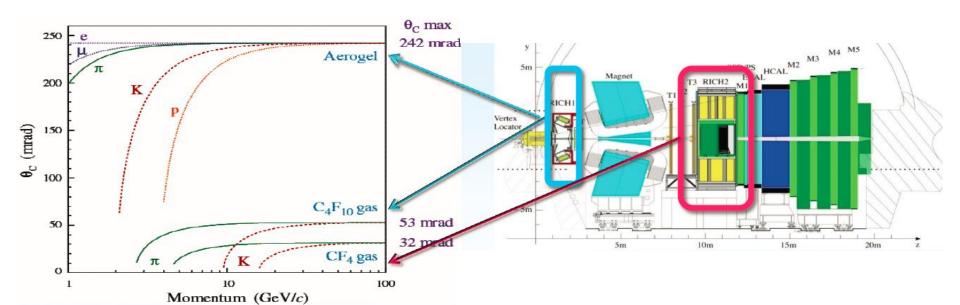


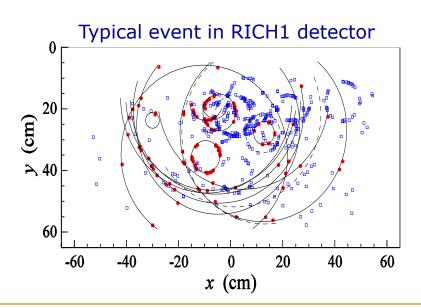
Primary vertex resolutions (25 tracks):

| | LHCb [µm] | ATLAS [µm] | CMS [µm] |
|--------------|-----------|------------|----------|
| σ(x) | 15.8 | 60 | 20-40 |
| σ (y) | 15.2 | 60 | 20-40 |
| σ(z) | 76 | 100 | 40-60 |

| | ATLAS | CMS | CDF | LHCb |
|-------------------------------|---------|--------|-------|-------|
| Decay time resolution (B_s) | ~100 fs | ~70 fs | 87 fs | 45 fs |

Key issues for B physics: particle identification





RICH1

aerogel (silicate foam) + C₄F₁₀

$$n(aerogel) = 1.03$$

 \rightarrow 2 - 10 GeV - slowest particles

$$n(C_4F_{10}) = 1.0014$$

 \rightarrow 10 - 60 GeV

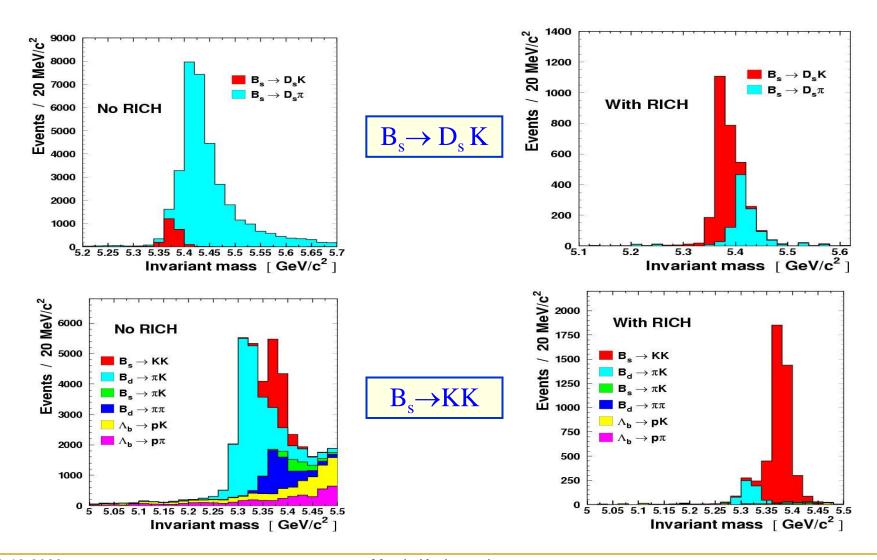
RICH2

carbon tetrafluoride CF₄

$$n(CF_4) = 1.0005 \rightarrow 16 - 100 \text{ GeV}$$

Key issues for B physics: particle identification

• Results of the simulation of B decays showing the necessity of particle ID



Key issues for B physics: trigger system

Challenge is

- to efficiently select most interesting B decays
- while maintaining manageable data rates

LHCb trigger scheme 40 MHz L0 e, γ L0 had μ 1 MHz ECAL Alley Had. Alley Muon Alley

L0 – high p_T signals in calorimeters & muon chambers

HLT1 – associate L0

signals with tracks &

HLT2 – inclusive sig-

natures + exclusive

selections using full

detector information

displaced vertices

Main backgrounds

- "minimum bias" inelastic pp scattering
- other charm and beauty decays

30 kHz Global reconstruction

Inclusive selections: topological, μ, μ+track, μμ, D→X, Φ

Exclusive selections

2 kHz

Write to tape

Handles

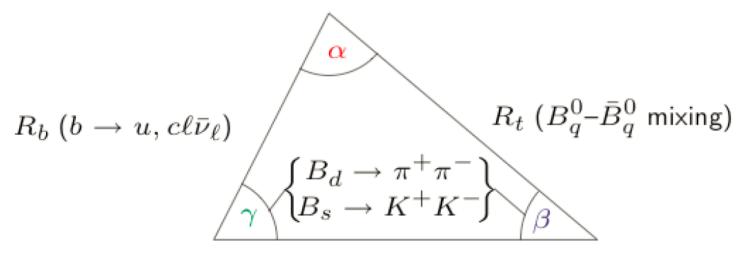
- high p_T signals (muons)
- displaced vertices

01-12-2022 Marcin Kucharczyk 21

CKM matrix and types of CP violation

Over-constraining the Unitarity Triangle

$$B \to \pi\pi$$
 (isospin), $B \to \rho\pi$, $B \to \rho\rho$



$$B \to \pi K$$
 (penguins)

$$\left.\begin{array}{l}
B_u^{\pm} \to K^{\pm}D \\
B_d \to K^{*0}D \\
B_c^{\pm} \to D_s^{\pm}D
\end{array}\right\} \text{ only trees}$$

$$B_d \to \psi K_S \ (B_s \to \psi \phi : \phi_s \approx 0)$$

$$B_d o \phi K_{\rm S}$$
 (pure penguin)

$$B_d \to D^{(*)\pm}\pi^{\mp}: \ \gamma + 2\beta \\ B_s \to D_s^{\pm}K^{\mp}: \ \gamma + \phi_s$$
 only trees

Phases and CP-Violation

CP violation:
$$|\mathcal{A}(B \to f)|^2 \neq |\mathcal{A}(\bar{B} \to \bar{f})|^2$$

Within weak interaction, moving from particle to antiparticle, system amplitudes are complex conjugated

No CP violation if:

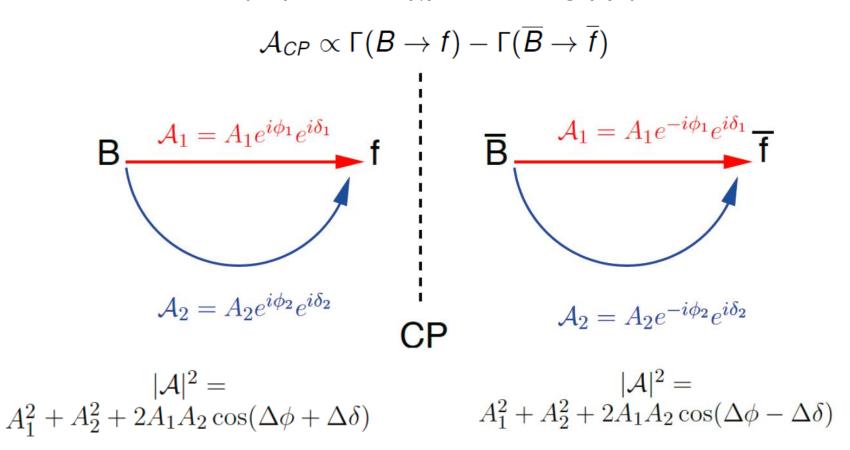
- There is only one amplitude contributing to the decay: $|\mathcal{A}|^2 = |\mathcal{A}^*|^2$
- The sum of two amplitudes, where both are complex conjugated, by moving from particle to antiparticle system:

$$|\mathcal{A}_1 + \mathcal{A}_2|^2 = (\mathcal{A}_1 + \mathcal{A}_2)(\mathcal{A}_1^* + \mathcal{A}_2^*) = |\mathcal{A}_1^* + \mathcal{A}_2^*|^2$$

For CP violation one needs two complex amplitudes, where one of them is complex conjugated and one is not by moving from particle to antiparticle system

Phases and CP-Violation

CP violation: interplay of weak (ϕ) and strong (δ) phases



 A_1 i A_2 need to have different weak phases ϕ and different strong phases δ Strong phases are notoriously difficult to compute

Categories of CP violation

Consider decay of neutral particle to a CP eigenstate

$$\lambda_{CP} = \frac{q}{p} \frac{\overline{A}}{A}$$

1) Indirect CP violation, or CPV in mixing:

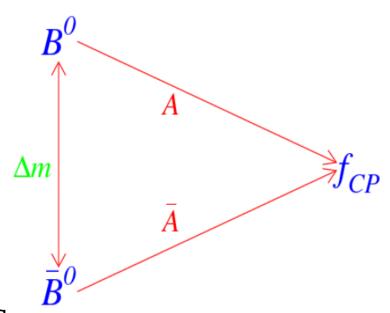
$$|\frac{q}{p}| \neq 1$$

2) Direct CP violation, or CPV in decays:

$$|\frac{\overline{A}}{A}| \neq 1$$

3) CP violation in interference between mixing and decay:

$$\Im\left(\frac{q}{p}\frac{\overline{A}}{A}\right)\neq 0$$



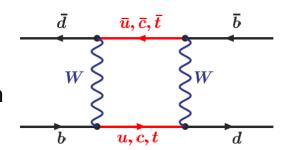
3 types of CP-Violation: In mixing

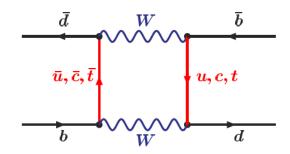
1) CP violation in mixing: CP eigenstates \neq mass eigenstates

Mixing occurs via box diagrams: $\Delta F = 2$ transitions

• SM predictions for

- neutral kaon system
- neutral D meson system
- B_d⁰ system
- B_s⁰ system





The 4 different neutral meson systems have very different mixing properties

- In case of a CP eigenstate: time evolution of the neutral mesons generates a "strong phase" $\sim \sin(\Delta mt)$
- CP asymmetries become time dependent:

$$\mathcal{A}_{CP}(t) = rac{C \cos(\Delta m t) - S \sin(\Delta m t)}{\cosh(\Delta \Gamma t/2) + D \sinh(\Delta \Gamma t/2)}$$

$$C^2 + S^2 + D^2 = 1$$

• Two eigenstates:

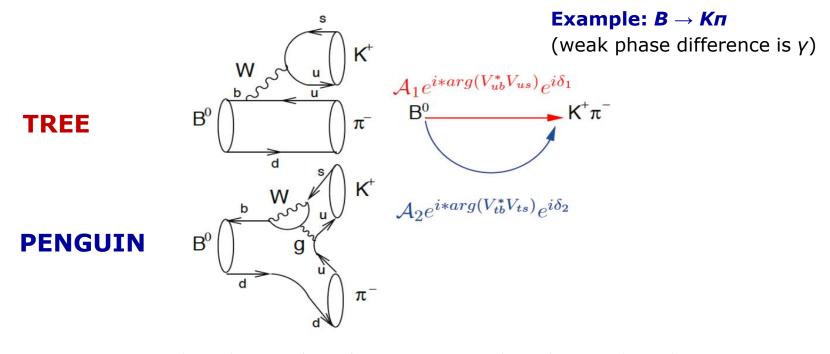
$$\Delta m = m_1 - m_2$$
 $\Delta \Gamma = \Gamma_1 - \Gamma_2$

 $\Delta\Gamma \sim 0$ for B_d $\Delta\Gamma$ not negligible for B_s

direct CP violation $\rightarrow C \neq 0$ CP violation in interference $S \neq 0$

3 types of CP-Violation: In decays

- 2) Direct CP violation condition: $|A(bar) / A| \neq 1$
 - need A and A(bar) to consist of (at least) two parts with different weak (ϕ) and strong (δ) phases
 - often realised by "tree" and "penguin" diagrams



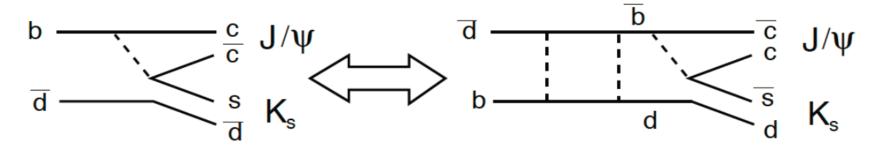
$$A = |T|e^{i(\delta_{T} - \Phi_{T})} + |P|e^{i(\delta_{P} - \Phi_{P})} \quad \overline{A} = |T|e^{i(\delta_{T} + \Phi_{T})} + |P|e^{i(\delta_{P} + \Phi_{P})}$$

$$A_{CP} = \frac{|\overline{A}|^{2} - |A|^{2}}{|\overline{A}|^{2} + |A|^{2}} = \frac{2|T||P|\sin(\delta_{T} - \delta_{P})\sin(\phi_{T} - \phi_{P})}{|T|^{2} + |P|^{2} + 2|T||P|\cos(\delta_{T} - \delta_{P})\cos(\phi_{T} - \phi_{P})}$$

3 types of CP-Violation: In interference

3) CP violation in interference between mixing and decay

Same final state through decay & mixing + decay



$$\mathcal{A}_{1} = \mathcal{A}_{mix}(B^{0} \to B^{0}) * \mathcal{A}_{decay}(B^{0} \to J/\Psi K_{s})$$

$$= \cos(\frac{\Delta mt}{2}) * A * e^{i\omega}$$

$$\mathcal{A}_{2} = \mathcal{A}_{mix}(B^{0} \to \bar{B}^{0}) * \mathcal{A}_{decay}(\bar{B}^{0} \to J/\Psi K_{s})$$

$$= i\sin(\frac{\Delta mt}{2}) * e^{+i\phi} * A * e^{-i\omega}$$

 $\Delta \phi = \phi - 2\omega$ (assume no CP violation in mixing and in decay)

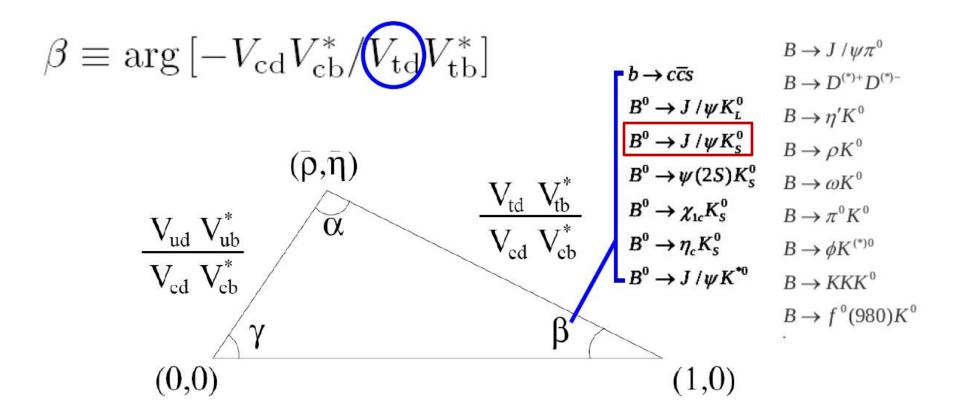
 $\Delta \delta = \pi/2 \Leftarrow$ mixing introduce second phase difference

01-12-2022 Marcin Kucharczyk 28

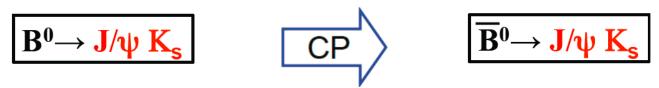
Measurements of CKM angles

1st CKM measurement: $sin(2\beta)$

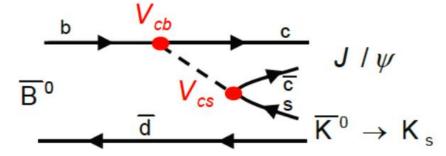
- Theoretically cleaner (SM uncertainties $\sim 10^{-2}$ to 10^{-3})
 - → tree dominated decays to charmonium + K⁰ final states



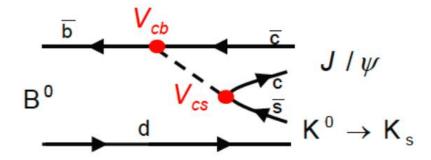
$sin(2\beta)$: Golden decay $B^0 \rightarrow J/\psi K_s$



Leading-order tree decays to cc(bar)s final states

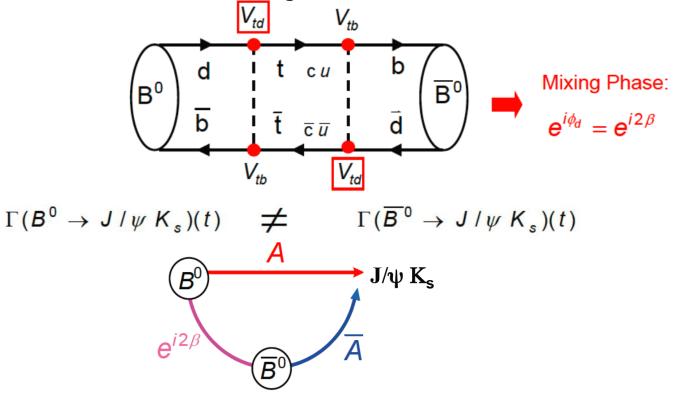


- \rightarrow here the CKM elements contributing are $V_{cb}V^*_{cs}$ that in Wolfenstein CKM parametrisation have no phase
- The CP conjugated case is also leading to (about) the same final state:



$sin(2\beta)$: Golden decay $B^0 \rightarrow J/\psi K_s$

• Because both *B* and *B(bar)* can decay to this common final state, this can interfere with the oscillation diagram:



$$\mathcal{A}_{CP} = \frac{\Gamma(\overline{B^0} \to J/\psi K_S) - \Gamma(B^0 \to J/\psi K_S)}{\Gamma(\overline{B^0} \to J/\psi K_S) + \Gamma(B^0 \to J/\psi K_S)} = \sin(2\beta)\sin(\Delta mt)$$

 \rightarrow requires knowledge of production flavour of the B

$sin(2\beta)$: Golden decay $B^0 \rightarrow J/\psi K_s$

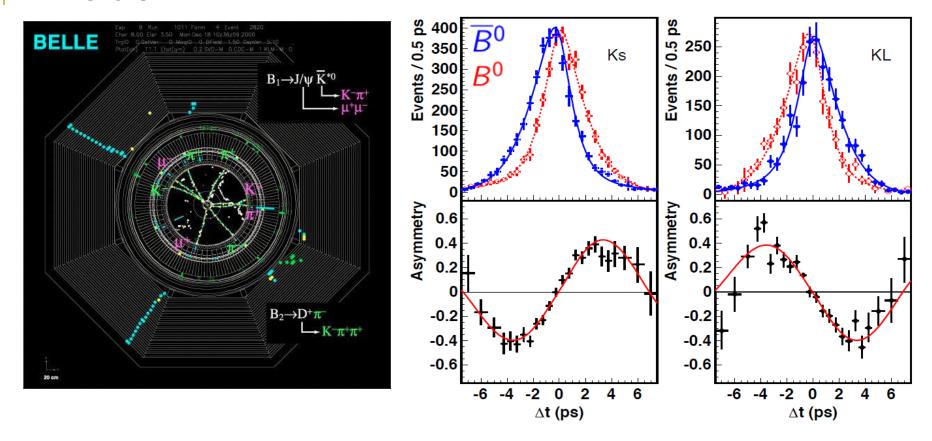
The colour-suppressed tree dominates

- \rightarrow subleading $b\rightarrow sc(bar)c$ penguin has (predominantly) the same weak phase
- → CKM-suppressed pollution by penguins golden channel
- $|A(bar)| = |A| \Rightarrow$ no direct CP violation
- C = 0 & S = $-\eta_{CP} \sin(2\beta)$
 - → sine term has a non-zero coefficient → there is CP violation in the interference between mixing and decay amplitudes in cc(bar)s decays
- reasonable branching fraction & experimentally clean signature

How can we measure decay time in $e^+e^- \rightarrow Y(4S) \rightarrow B^0B^0(bar)$?

- the answer: asymmetric-energy B factory (e.g. Belle)
- key points
 - $\rightarrow Y(4S) \rightarrow B^0B^0(bar)$ produces coherent pairs
 - \rightarrow B mesons are moving in LAB frame

$sin(2\beta)$: Belle measurement

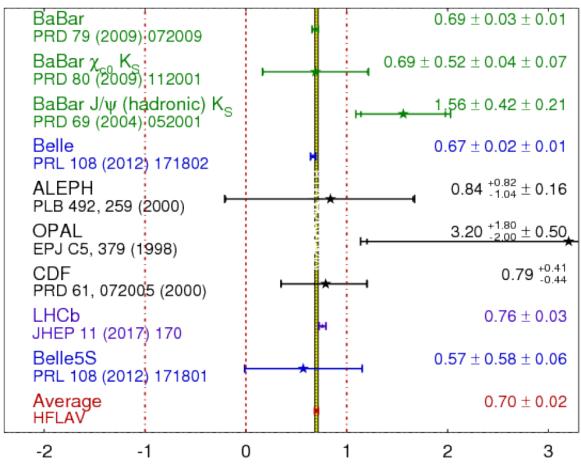


What do we have to do to measure $A_{CP}(t)$?

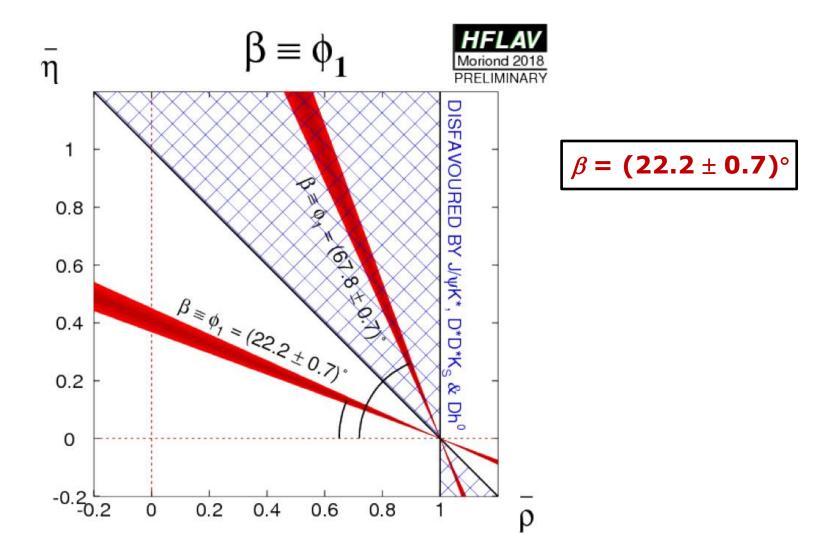
- \bullet step 1: produce and detect $B^0 \to f_{CP}$ events
- step 2: separate B⁰ from B⁰(bar)
- step 3: measure the decay time t

$sin(2\beta)$: Compilation of results

$$sin(2\beta) \equiv sin(2\phi_1) \frac{\textit{HFLAV}}{\textit{Moriond 2018}}$$



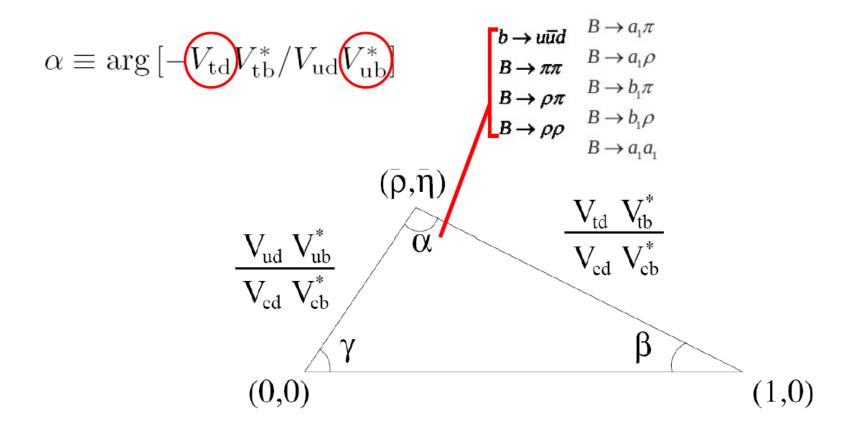
$sin(2\beta)$: Compilation of results



2nd CKM measurement: α angle

 $b \rightarrow uu(bar)d$ transitions with possible loop contributions. Extract α using:

- SU(2) isospin relations
- SU(3) flavour related processes

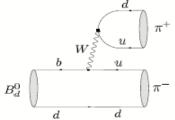


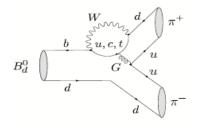
Measurement of α

• Time-dependent CP violation in modes dominated by $b \to uu(bar)d$ tree diagrams probes α (or π – $(\beta+\gamma)$)

$$\rightarrow$$
 C = 0 & S = $+\eta_{CP} \sin(2\alpha)$

- $b \rightarrow du(bar)u$ penguin transitions contribute to same final states
 - → "penguin pollution"
 - \rightarrow C \neq 0 \Leftrightarrow direct CP violation can occur
 - \rightarrow S \neq + η_{CP} sin(2 α)





In this case the penguin diagram is not CKM suppressed so it spoils the clean measurement of the CP violation effect

- Two approaches (optimal approach combines both)
 - → try to use modes with small penguin contribution
 - → correct for penguin effect (isospin analysis)

$$C_{hh} \propto \sin(\delta)$$

$$S_{hh} = \sqrt{1 - C_{hh}^2} \sin(2\alpha_{\text{eff}})$$

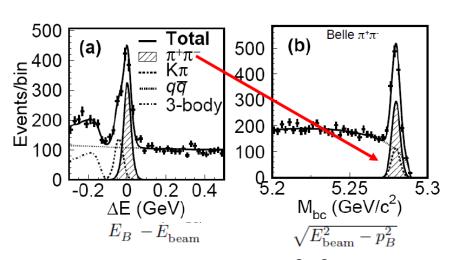
$$\delta = \delta_P - \delta_T$$

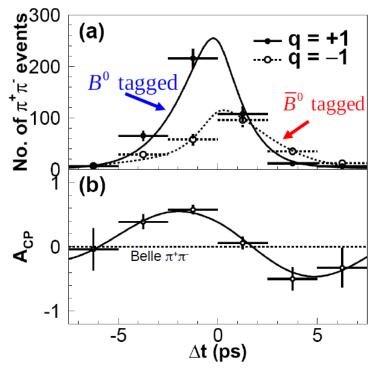
Measurement of $\alpha: B^0 \to \pi\pi$

$B^0 \rightarrow \Pi\Pi$

• easy to isolate signal for $\mathbf{n}^+\mathbf{n}^-$ and $\mathbf{n}^+\mathbf{n}^0$ as these modes are relatively clean

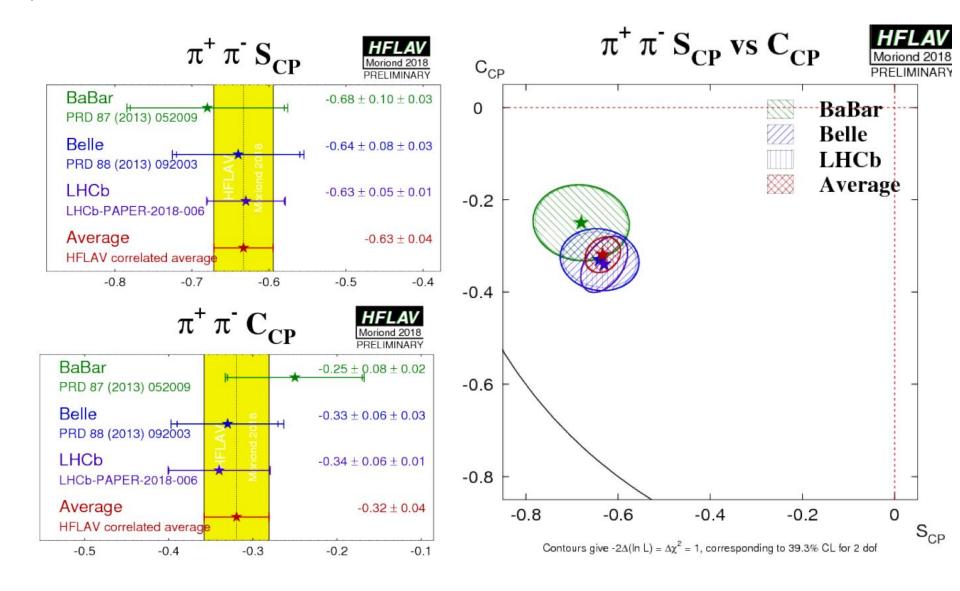
and have relatively large BR $\sim O(5 \times 10^{-6})$





- much harder to isolate π⁰π⁰
 - \rightarrow BR $\sim 1.5 \times 10^{-6}$
 - → no tracks in the fnal state to provide vertex info
 - $\rightarrow B^0 \rightarrow \pi^0 \pi^0 \rightarrow \gamma \gamma \gamma \gamma$ has a large ΔE resolution
 - possible to separate flavour tags to measure C
 - this completes set of information required for an isospin analysis

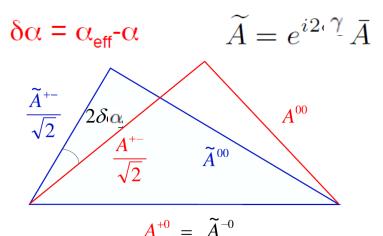
Measurement of $\alpha: B^0 \to \pi^+\pi^-$



Measurement of α : *Isospin analysis*

Use triangle construction to find difference ($\delta \alpha$) between " $\alpha_{\rm eff}$ " and α

• requires measurement of rates and asymmetries of $B^+ \rightarrow \pi^+ \pi^0 \& B^0 \rightarrow \pi^0 \pi^0$



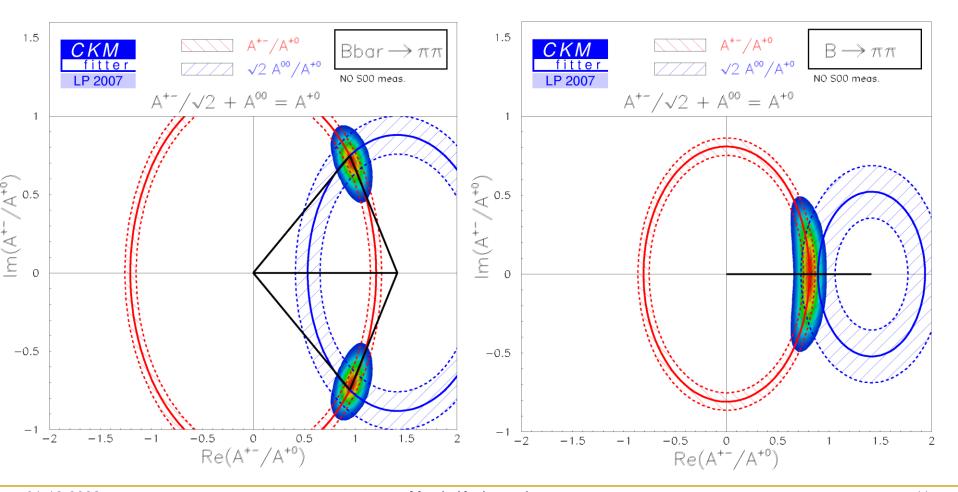
- $B \to \pi + \pi^-$, $\pi^+ \pi^0$, $\pi^0 \pi^0$ decays are connected by isospin relations
- $\pi\pi$ states can have I = 2 or I = 0

- $\frac{1}{\sqrt{2}}A^{+-} + A^{00} = A^{+0}$ $\frac{1}{\sqrt{2}}A^{+-} + \frac{1}{\sqrt{2}}A^{00} = \frac{1}{\sqrt{2}}A^{+0}$
- $\frac{1}{\sqrt{2}} \overline{A}^{+-} + \overline{A}^{00} = \overline{A}^{+0}$
- \rightarrow the gluonic penguins contribute only to the I = 0 state ($\Delta I = 1/2$)
- $\rightarrow \pi^+\pi^0$ is a pure I = 2 state ($\Delta I = 3/2$) and it gets contribution only from the tree diagram
- ightarrow triangular relations allow for the determination of the phase diference induced on lpha

Both BR(B⁰) and BR(B⁰(bar)) have to be measured in all the $\pi\pi$ channels

Measurement of α : *Isospin analysis*

There are SU(2) violating corrections to consider, for example electroweak penguins (\sim 5%), but these are much smaller than current experimental accuracy and eventually they can be incorporated into the isospin analysis



Measurement of $\alpha: B^0 \to \rho \rho$

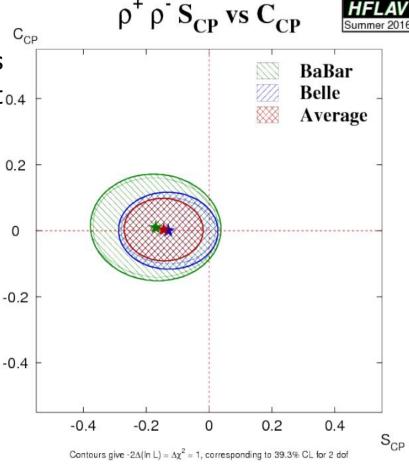
 vector-vector modes: angular analysis reaquired to determine the CP content_{0.4}

L=0,1,2 partial waves:

- → longitudinal: CP-even state
- → transverse: mixed CP states
- isospin analysis:
 - \rightarrow possible contribution from $\rho^0 \rho^0$
- wide p resonance

But

- BR 5 times larger with respect to ππ
- penguin pollution smaller than in ππ
- ρ are almost 100% polarized:
 - → almost a pure CP-even state



from nn, pp, np combined

$$\alpha = (93.3 \pm 5.6)^{\circ}$$