



# The Gluon Exchange Model: solving the puzzle of nuclear stopping power

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- 1. Motivation ;**
- 2. The Gluon Exchange Model ;**
- 3. Summary ;**
- 4. Outlook.**

Based on:

APPB 51 (2020) 1207

PLB 816 (2021) 136200

EPJPlus 136 (2021) 971

APPB 52 (2021) 981

ArXiv: 2111.03401

↳ submitted to PLB

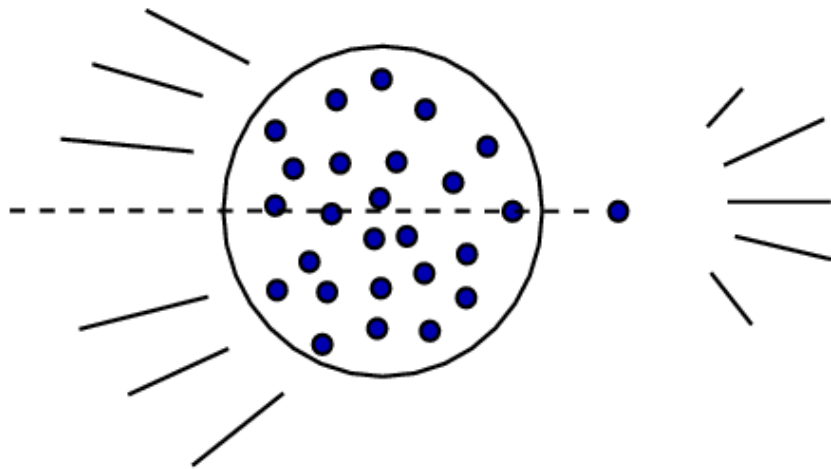
# 1) Motivation

This talk will be concerned with **proton-proton** and **proton-nucleus** collisions at  $\sqrt{s_{NN}} \sim 20 \text{ GeV}$ .

The implications touch **all the high energy scale** (LHC, cosmic), and also **nucleus-nucleus** (heavy ion) physics.

We are interested in the emission of secondary **baryons (protons, neutrons)** in these collisions.

Despite  $\sim 50$  years of study these “**soft**” processes ( $p_T < 1 \text{ GeV}/c$ ) are relatively **poorly understood**, and phenomenological research remains **data-driven**. This is because perturbative Quantum Chromodynamics **does not apply here**.



At the beginning of the last decade **new experimental data** appeared.

The exploitation of these data allows for a more precise, **better understanding** of soft baryon emission processes.

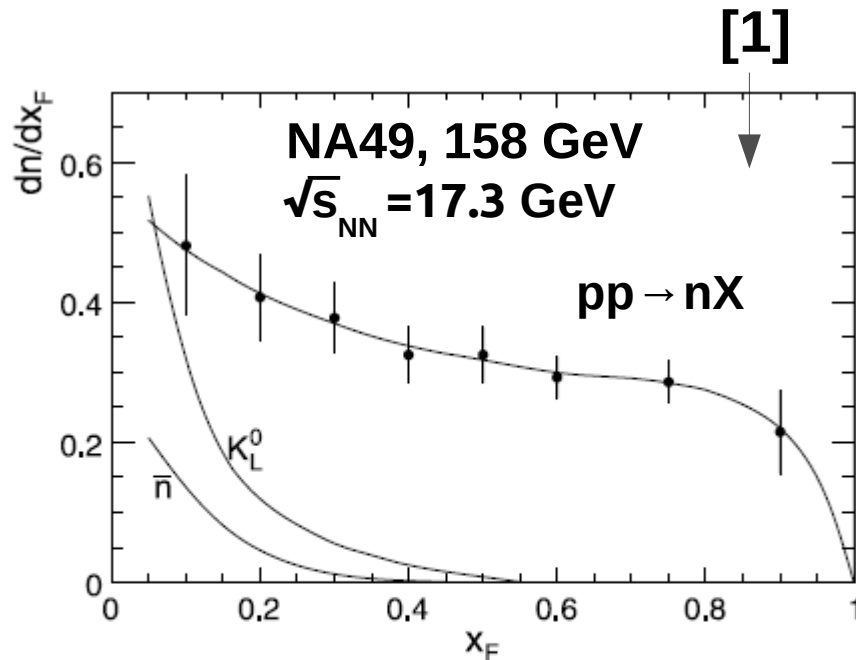
( **Note!** All kinematical variables are in the **nucleon-nucleon c.m.s.** )

# New experimental data

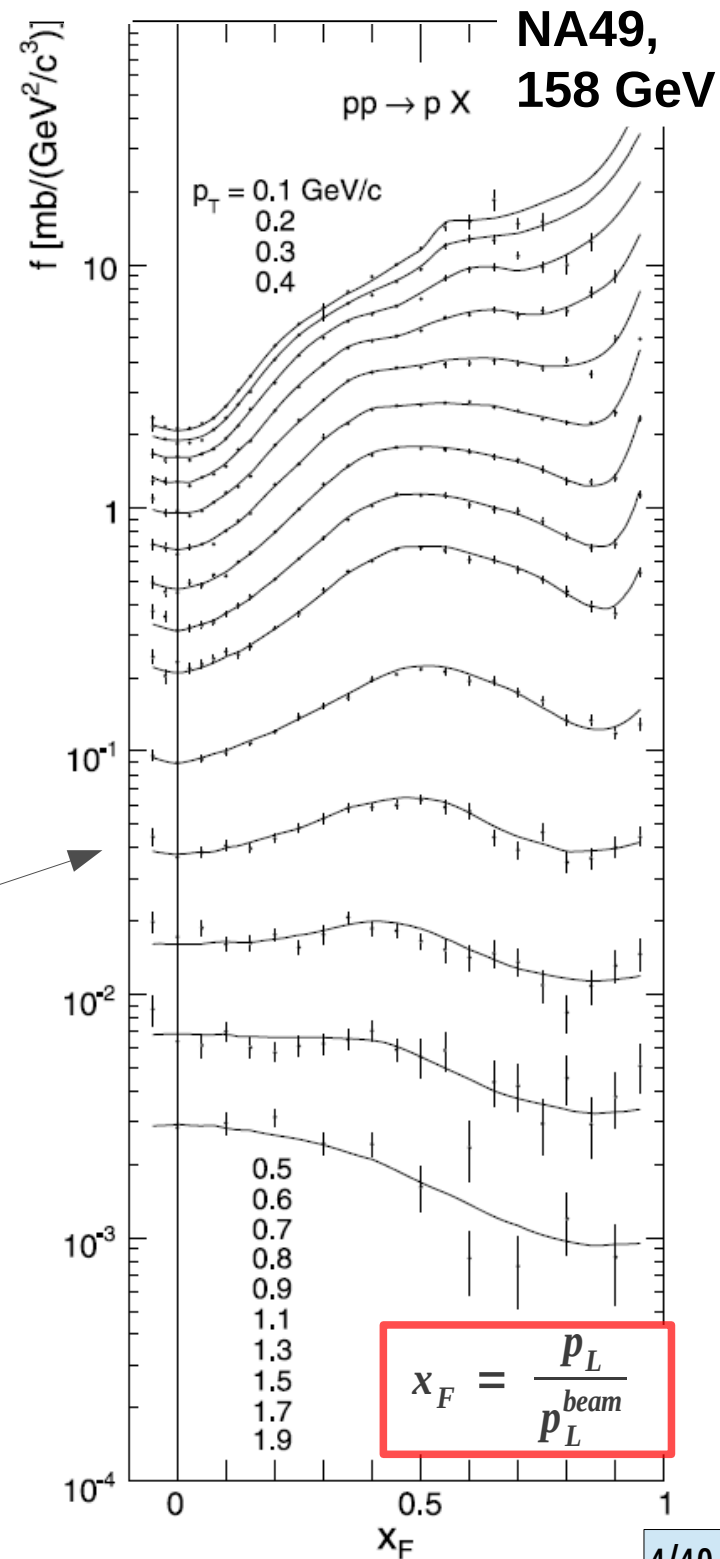
- [1] T. Anticic *et al.* [NA49 Collab.], Eur. Phys. J. **C65**, 9 (2010),
- [2] B. Baatar *et al.* [NA49 Collab.], Eur. Phys. J. **C73**, 2364 (2013).

IFJ PAN participated in the NA49 experiment at CERN (presently NA61/SHINE).

1. No need to use protons as a **(wrong!) proxy** for **all the baryons** ;
2. Hermeticity (full projectile hemisphere, no  $p_T$ -cutoff) ;
3. Both **pp** and **pC** data sets were provided by the same experiment.



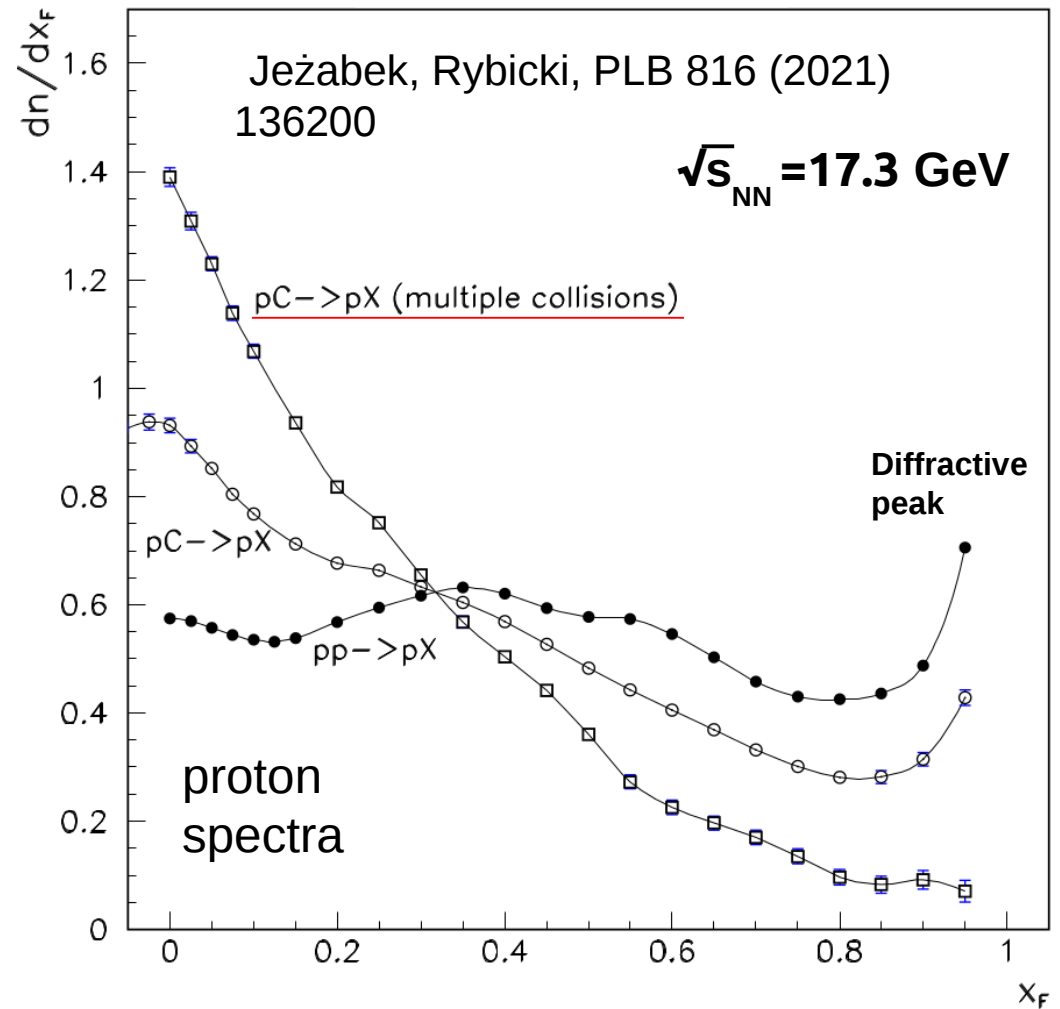
Our personal  
baryon  
number test:  
0.96 (96/100)  
[ excellent!!! ]



# Proton-proton vs proton-nucleus collisions

$$\frac{dn}{dx_F} (pC_{\text{multiple collisions}} \rightarrow pX) = \frac{1}{1 - P(1)} \left( \frac{dn}{dx_F} (pC \rightarrow pX) - P(1) \cdot \frac{dn}{dx_F} (pp \rightarrow pX) \right)$$

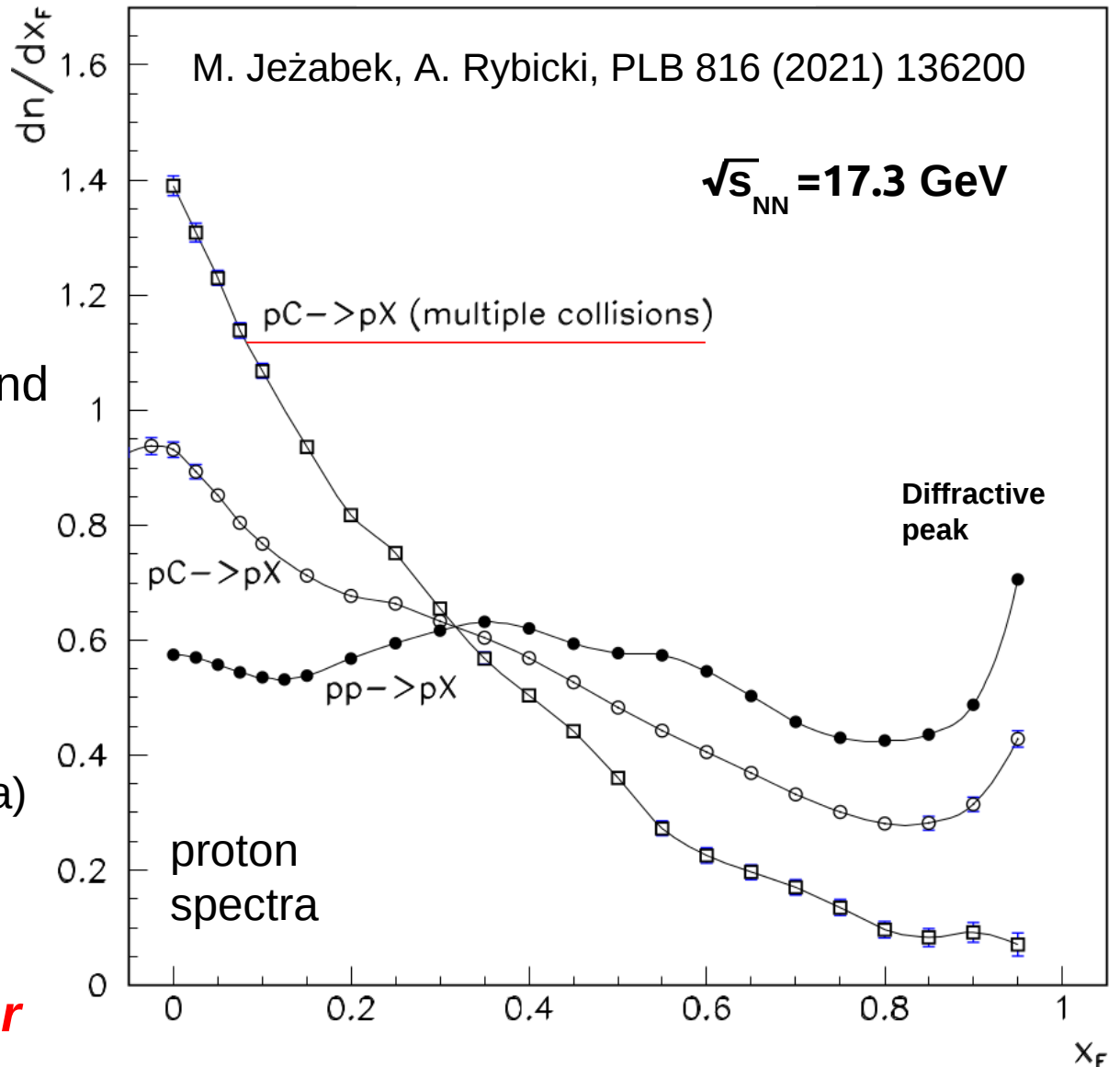
1. pp and pC data from the same NA49 experiment.
2. **P(1)** - probability of proton collision with one wounded nucleon.
3. **Advantage:** we can extract pC collisions in which the proton collides with **multiple** (more than one) nucleons.



# Qualitative difference between single and multiple proton-nucleon collisions!

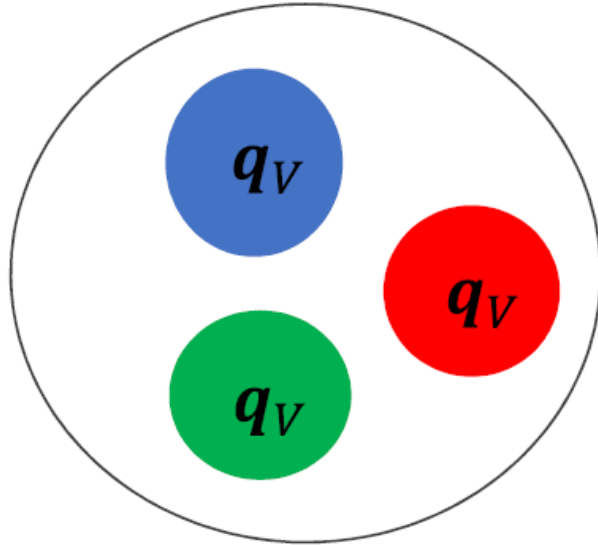
- multiple collisions: **vanishing of diffractive peak** ;
- multiple collisions: **very strong nuclear stopping power** !
- it seems **hopeless** to understand this process w/o involving the **internal structure** of the proton...
- ... but even models which did (Capella and Tran Thanh Van, Jeżabek, Karczmarczuk, Różańska) **failed** to describe the **strength** of this effect.

***“The puzzle of nuclear stopping power”***

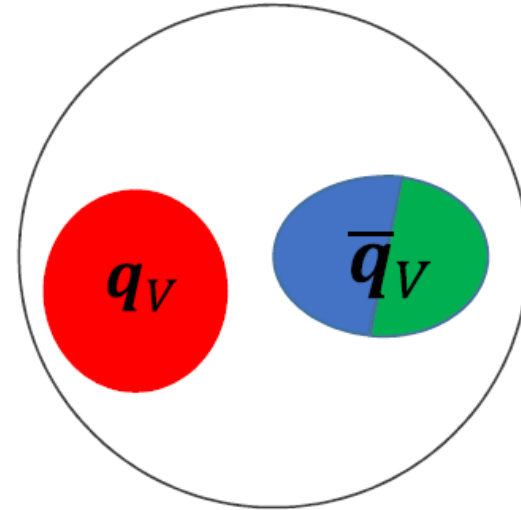


# 2) the Gluon Exchange Model (GEM)

# How do we imagine a proton in “soft” processes ?



Baryon

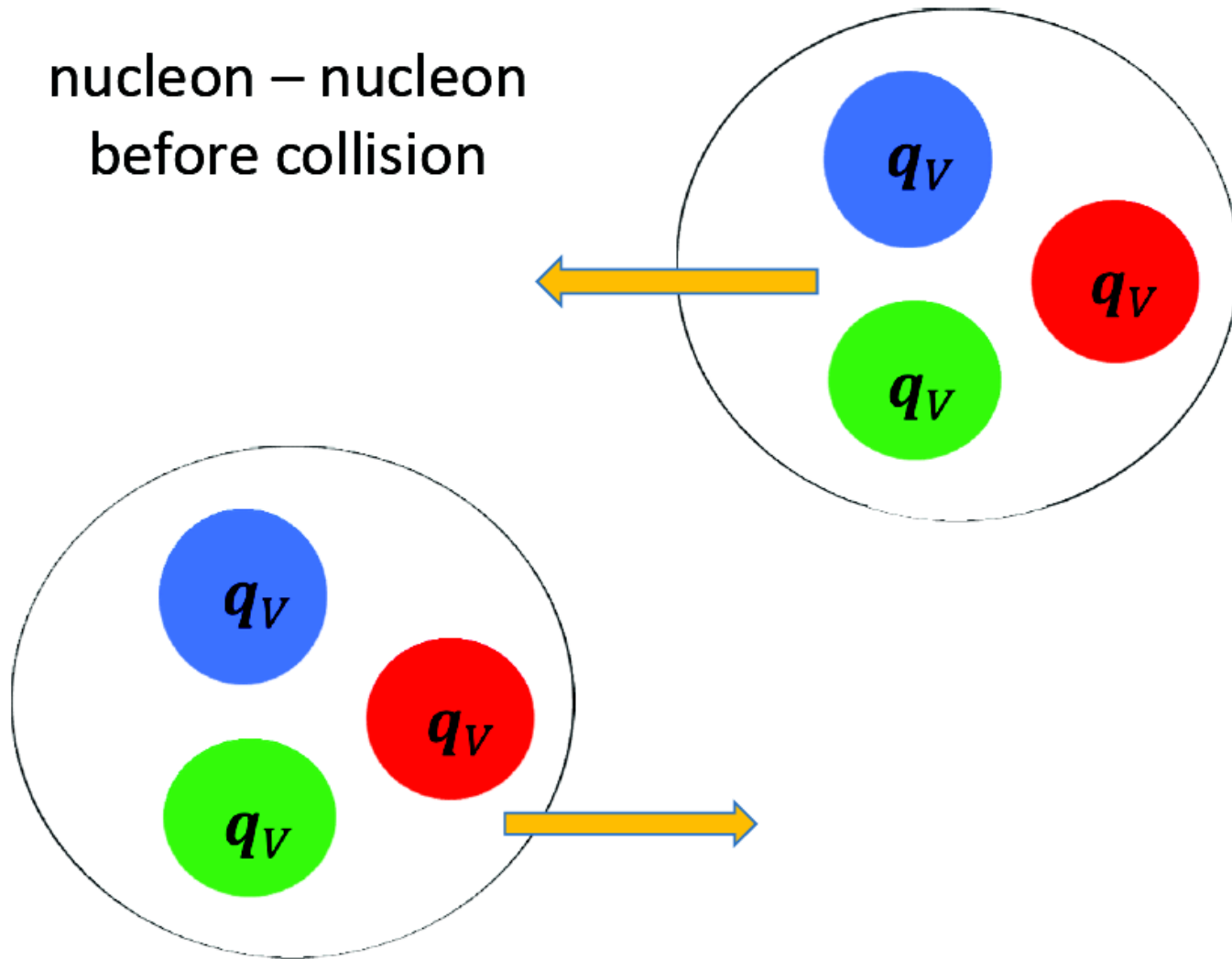


Meson

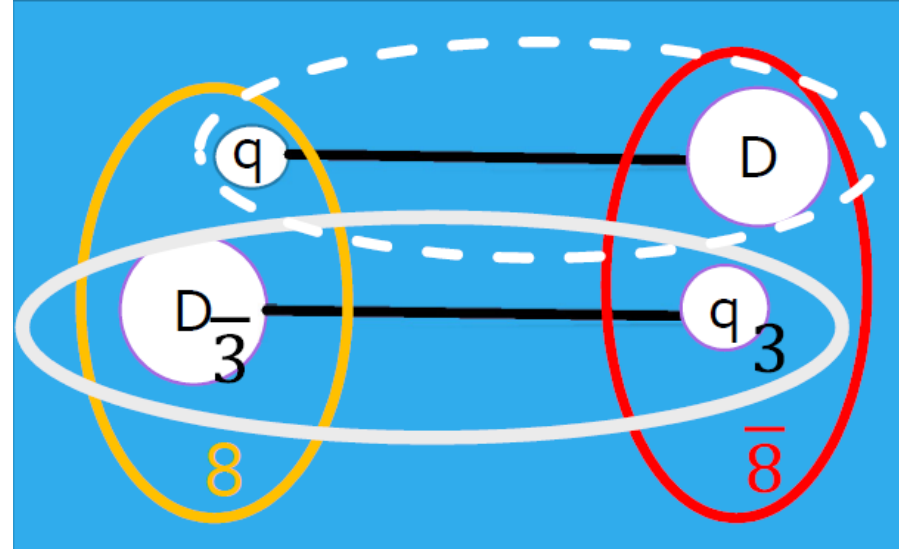
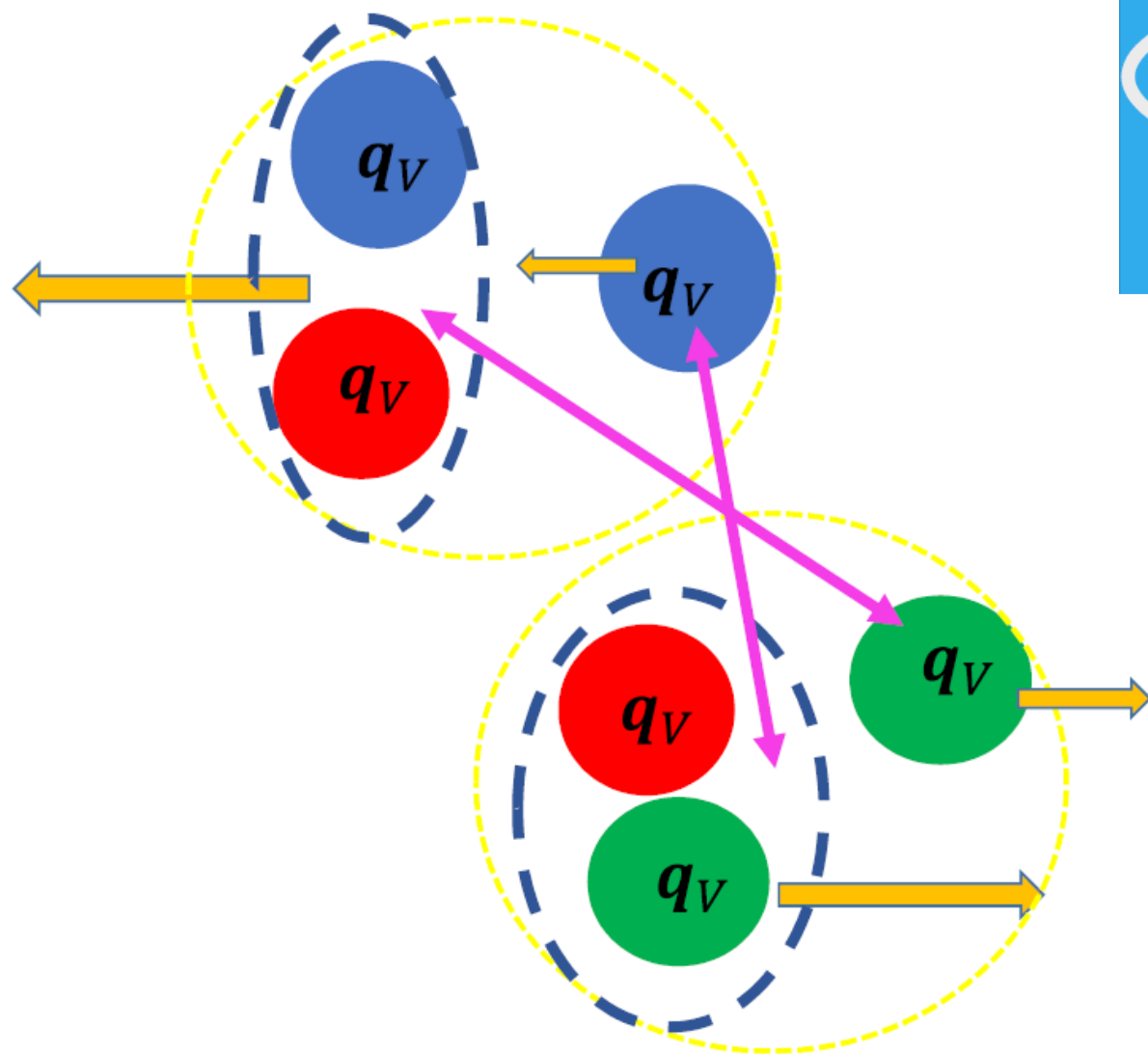
- Quarks and gluons carry a special quantum number: **color** ;
- quarks are **color triplets** ;
- gluons are **color octets** ;
- antiquarks carry anti-color ;
- gluon exchange = **exchange of color** !
- **all hadrons** (protons, neutrons, mesons etc.) are **color-neutral** .



nucleon – nucleon  
before collision



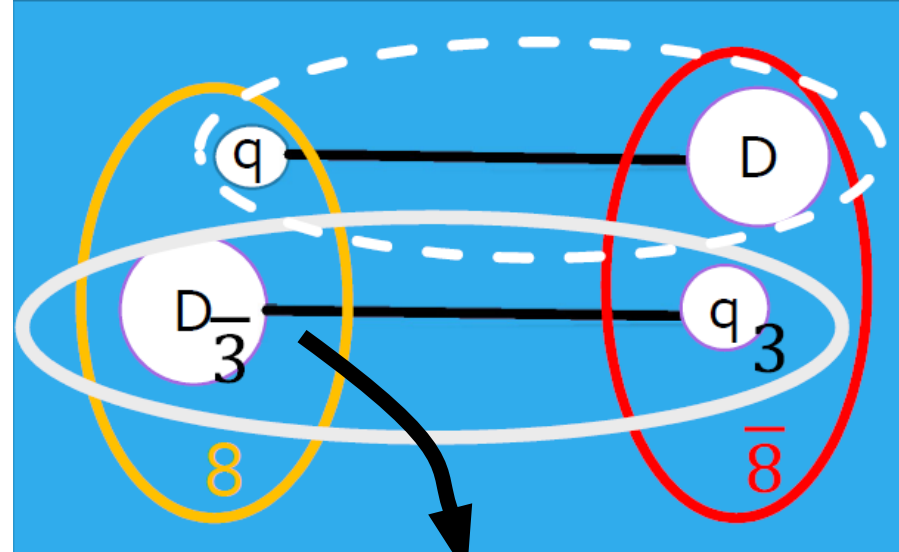
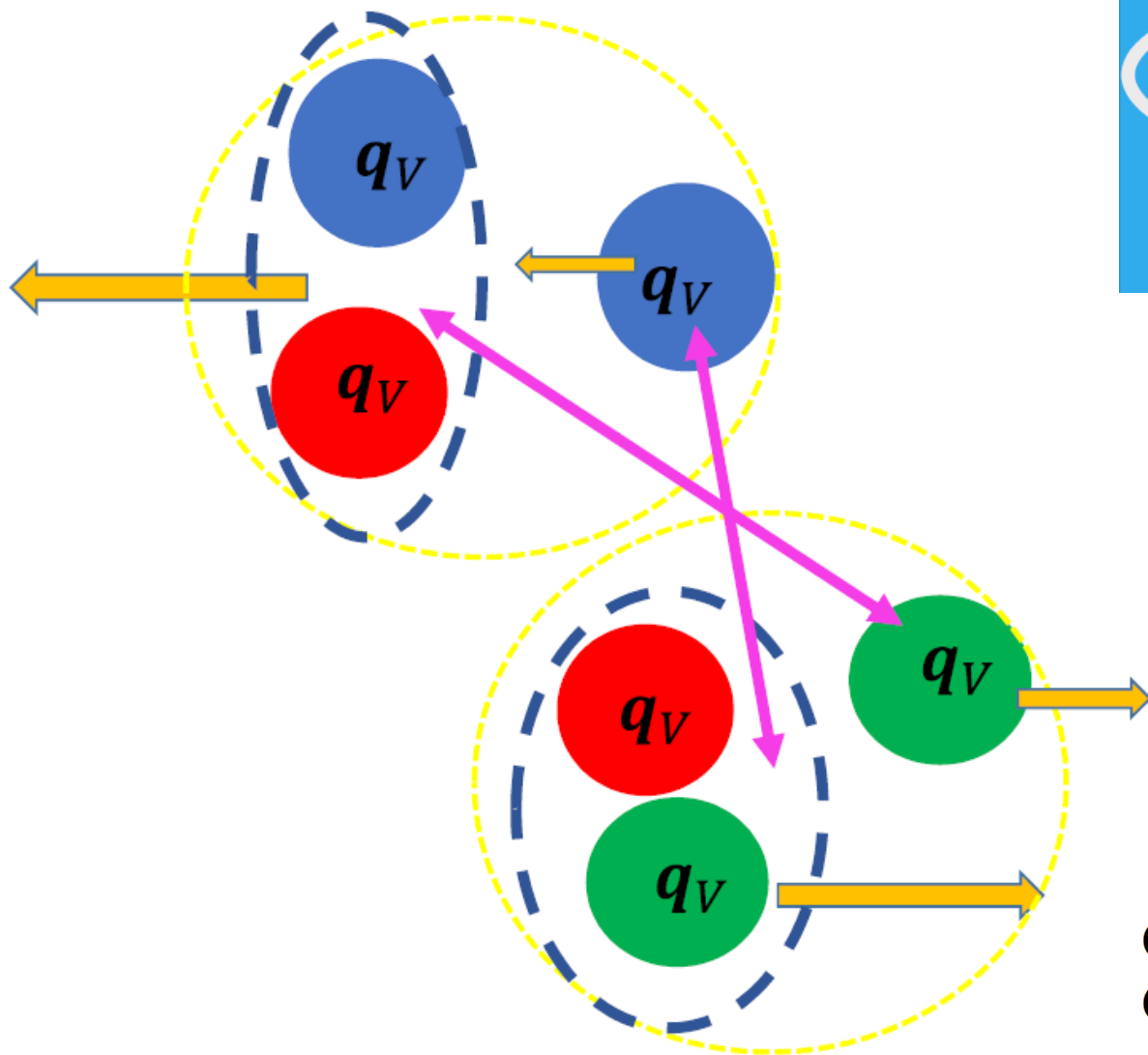
nucleon – nucleon  
after collision



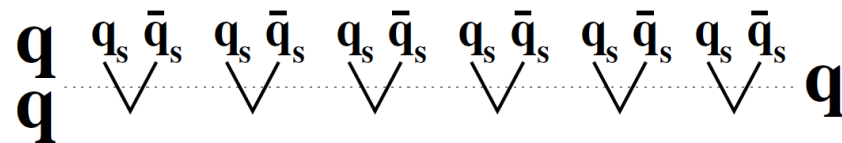
(\*) **Diquark** = two quarks  
in **color antitriplet state ( $\bar{3}$ )**.

Note: this is like in the  
Dual Parton Model (DPM).  
A. Capella and J. Tran Thanh Van,  
PLB **93**, 1980,  
MJ, J. Karczmarczuk,  
M. Rózańska, ZPC **29**, 1985.

nucleon – nucleon  
after collision



**String fragmentation**  
proceeds through  $q\bar{q}$  pairs  
thus it starts from the  
Diquark.



**Note: Diquarks are essential for the emission of baryons !**

- **Question:**

**will three valence quarks in the proton be sufficient to describe the emission of secondary baryons?**

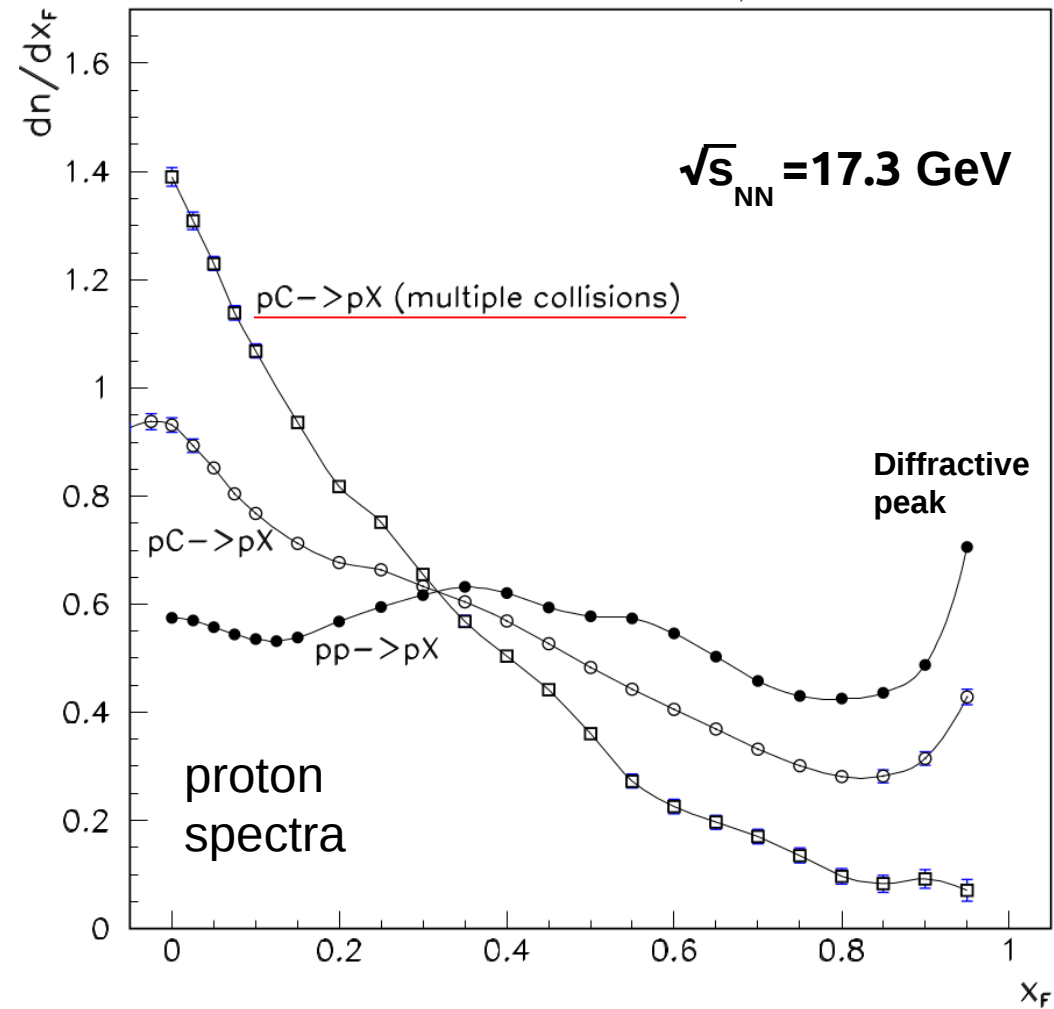
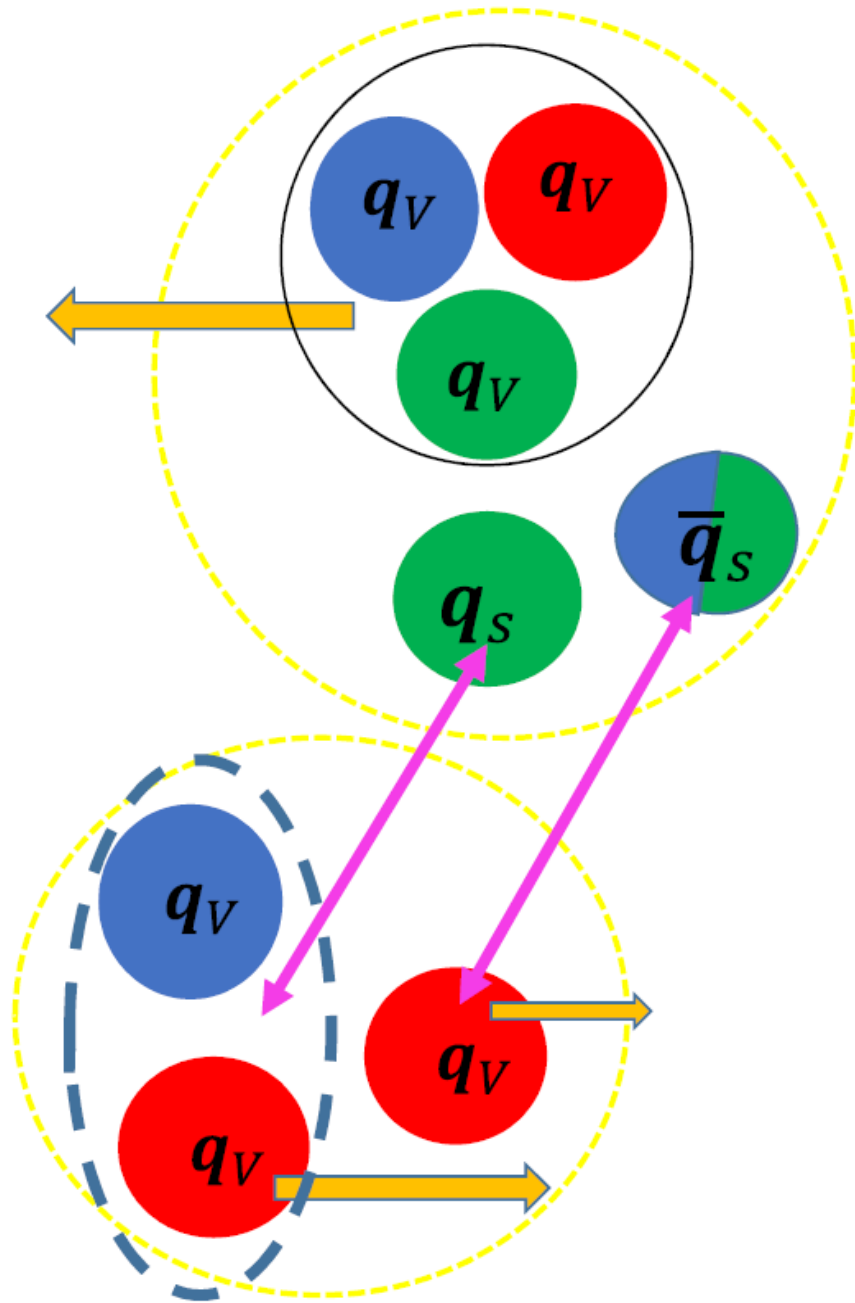
- **in proton-proton collisions → M.J., A.R., PLB 816 (2021) 136200 ;**
- **in proton-nucleus collisions → M.J., A.R., EPJPlus 136 (2021) 971 .**

# Gluon Exchange Model

## DPM + new contributions

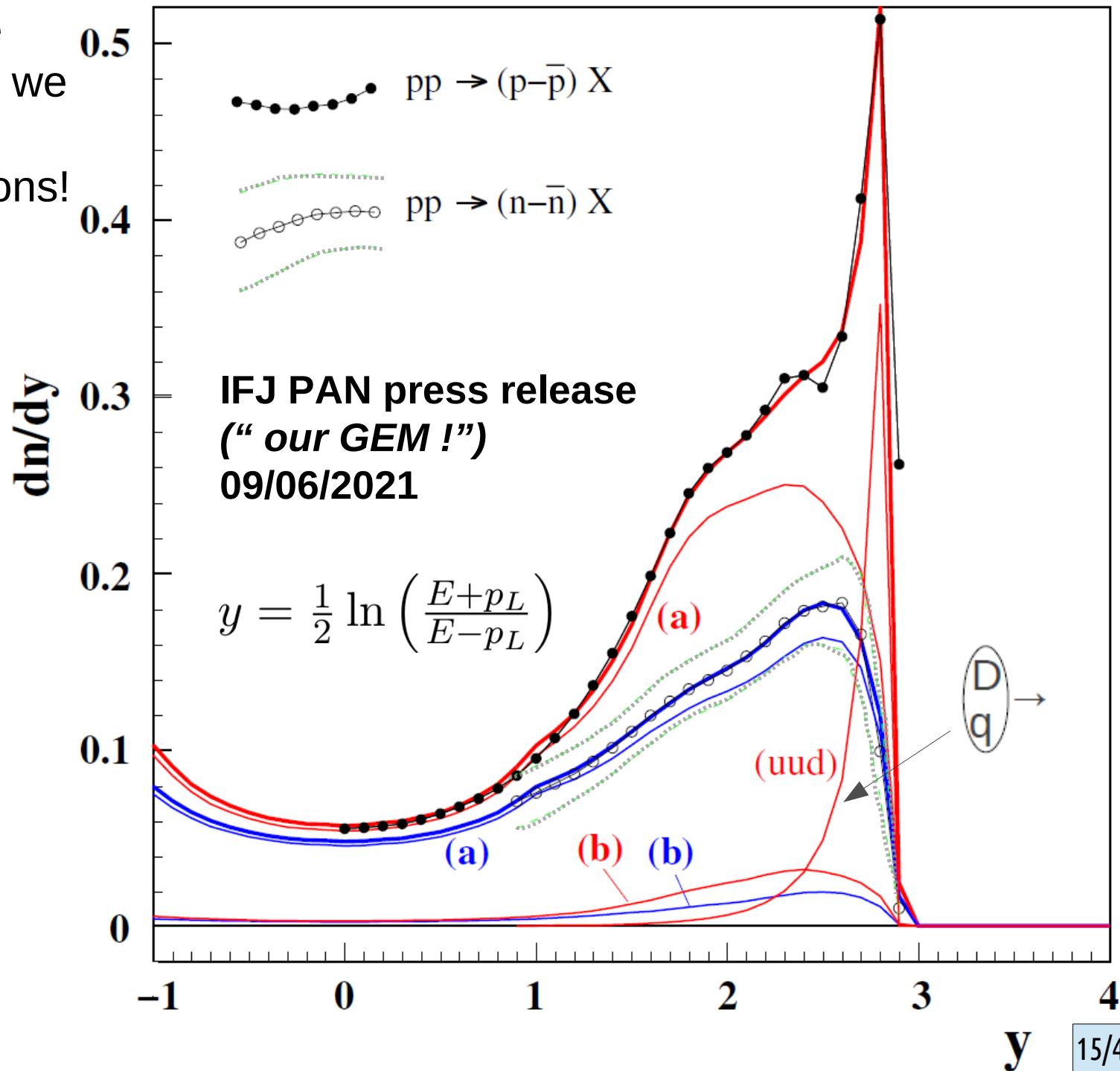
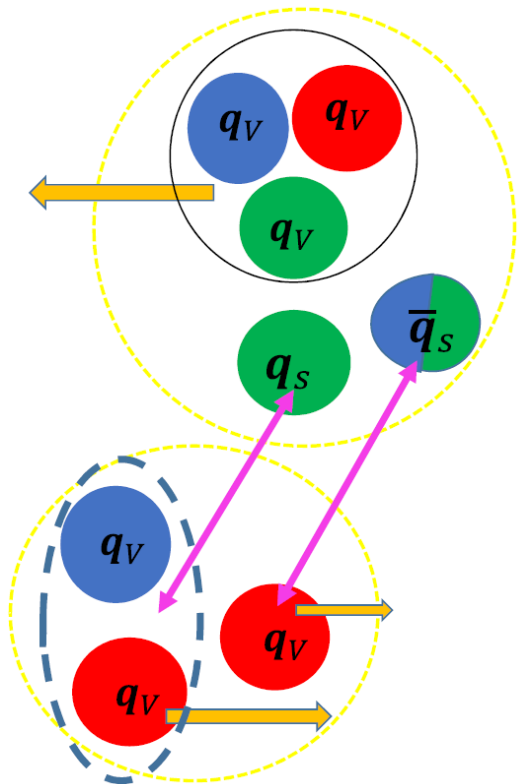
**nucleon – nucleon:**  
inelastic diffraction

Jeżabek, Rybicki,  
PLB 816 (2021) 136200



- **Note!**
- **Below we will discuss NET baryon spectra as a function of rapidity :**
$$y = \frac{1}{2} \ln \left( \frac{E+p_L}{E-p_L} \right)$$
- **Baryon-antibaryon pair production has been subtracted from all the distributions !**
- **Unlike at the LHC, at the SPS the  $\bar{p}/p$  ratio is  $\sim 0.25$  at  $y_{(c.m.s.)} = 0$  .**

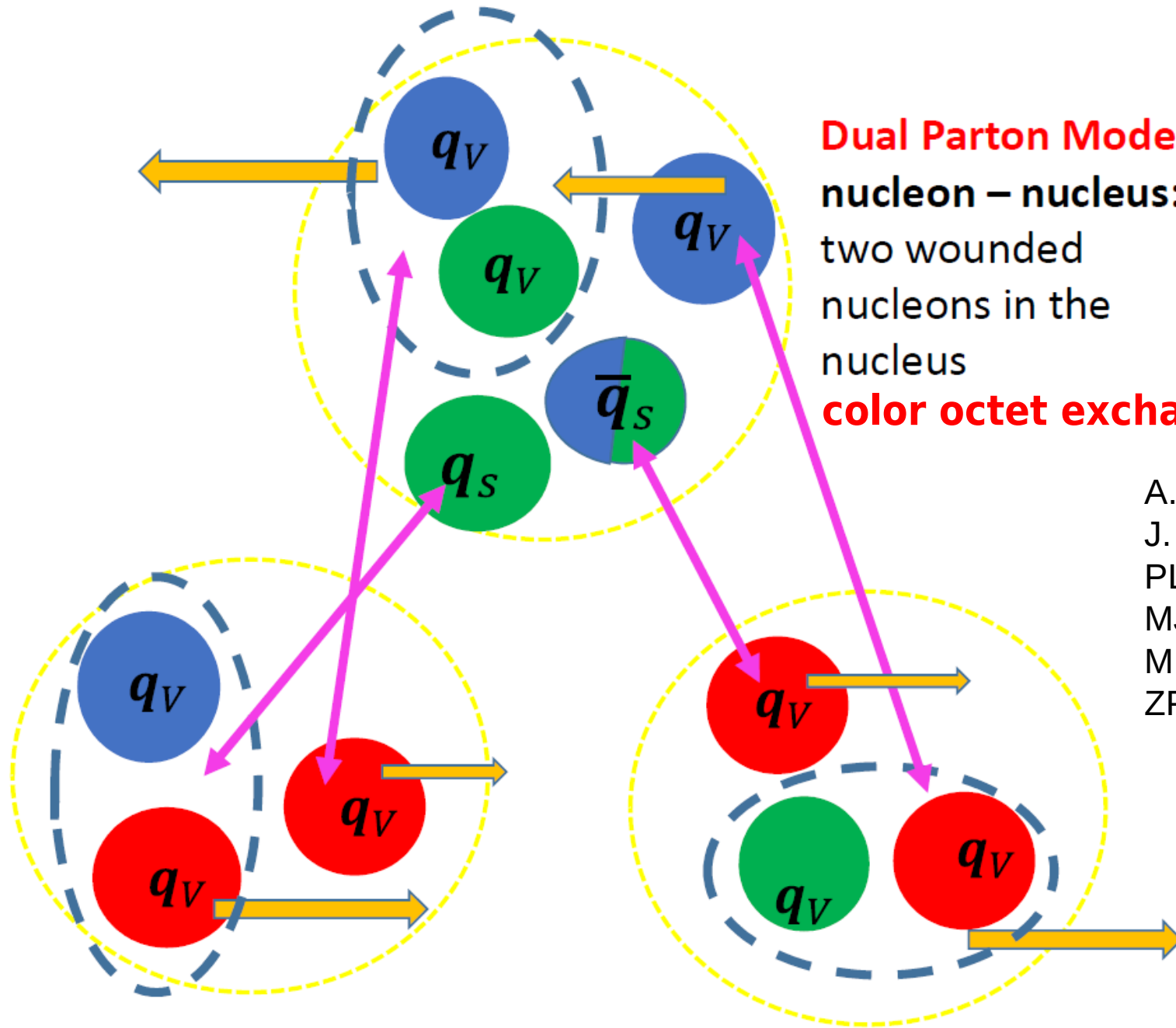
Note:  
**this is the structure**  
**of the proton** which we  
 need to understand  
 proton-proton collisions!



# Baryon stopping in proton-nucleus collisions

Proton-carbon (pC) data from the NA49 experiment,  
Eur. Phys. J. **C73**, 2364 (2013) .





## Dual Parton Model (1980)

nucleon – nucleus:

two wounded  
nucleons in the  
nucleus

**color octet exchange**

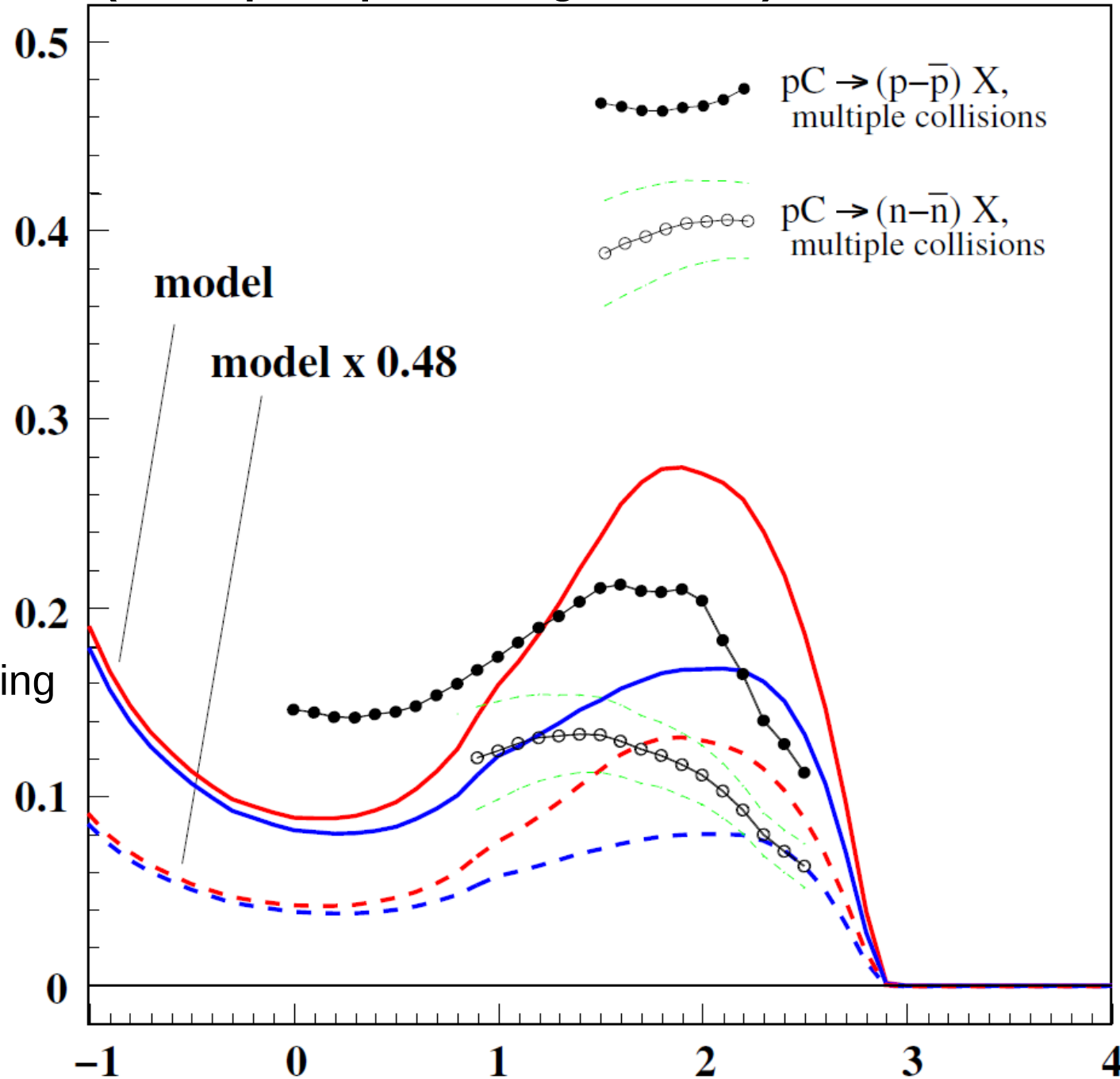
A. Capella and  
J. Tran Thanh Van,  
PLB **93**, 1980,  
MJ, J. Karczmarczuk,  
M. Rózańska,  
ZPC **29**, 1985.

**Sea quark/antiquark degrees of freedom** for multiple collision processes: **DPM**.  
**Still, secondary baryons are created from valence diquarks.**

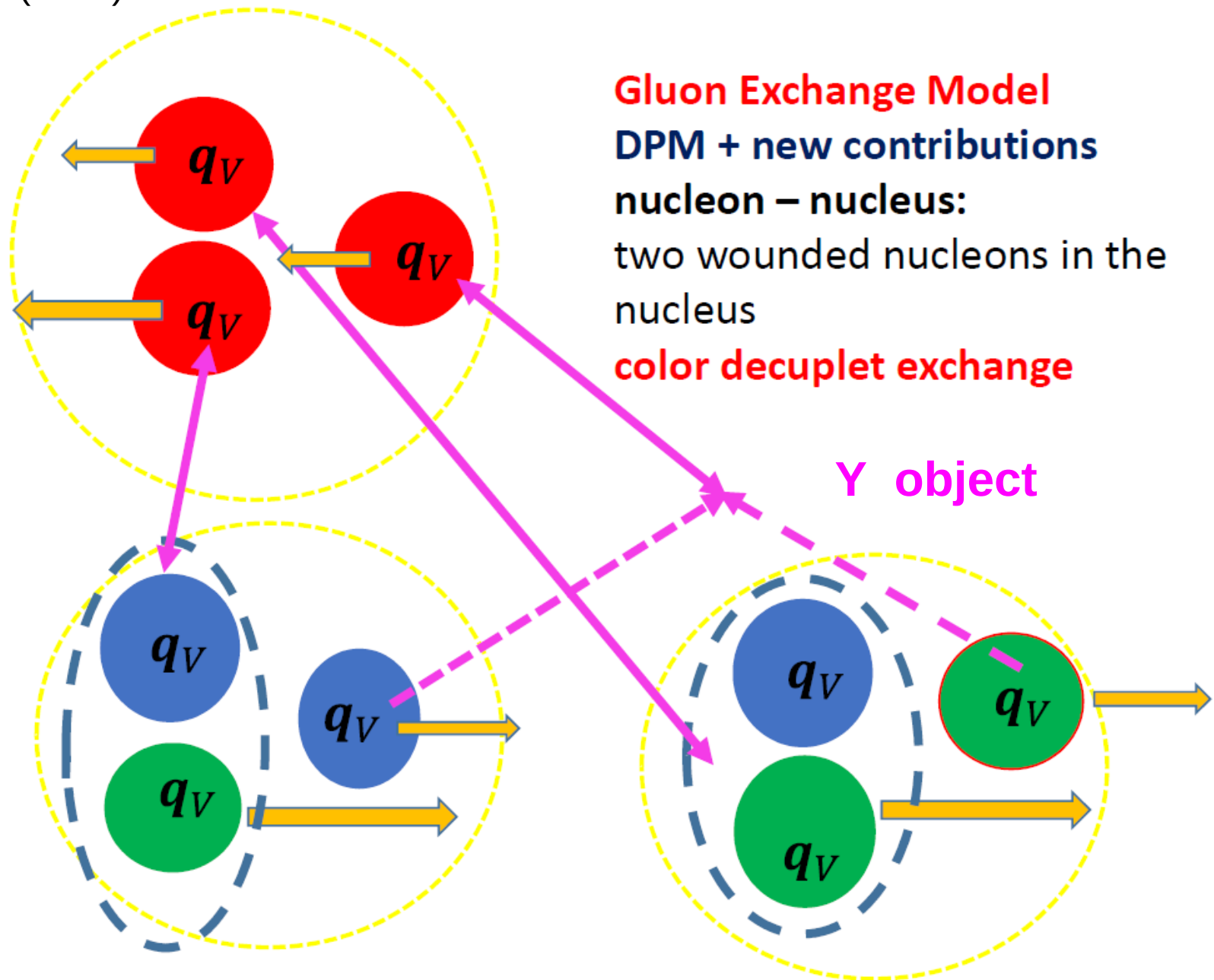
# GEM in pA collisions (the diquark-preserving scenario)

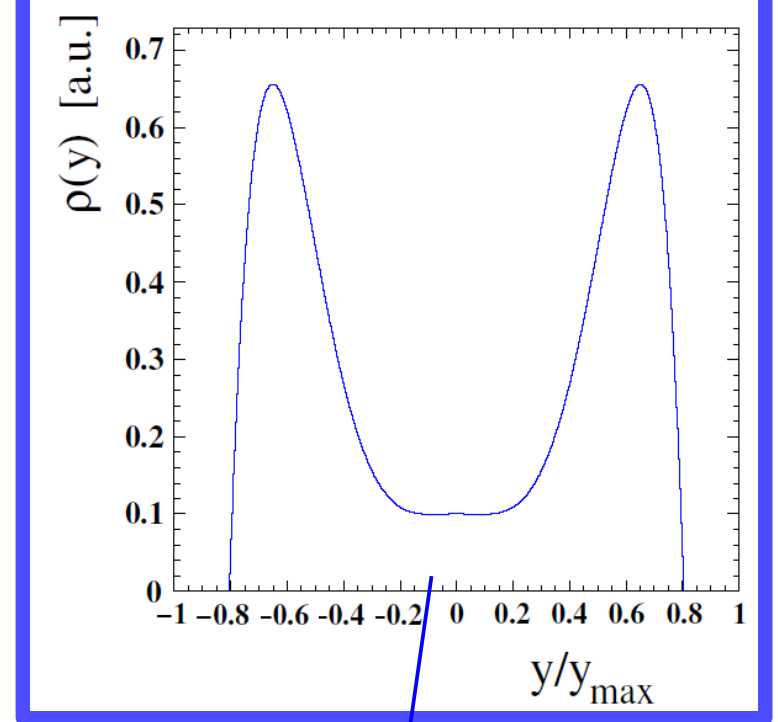
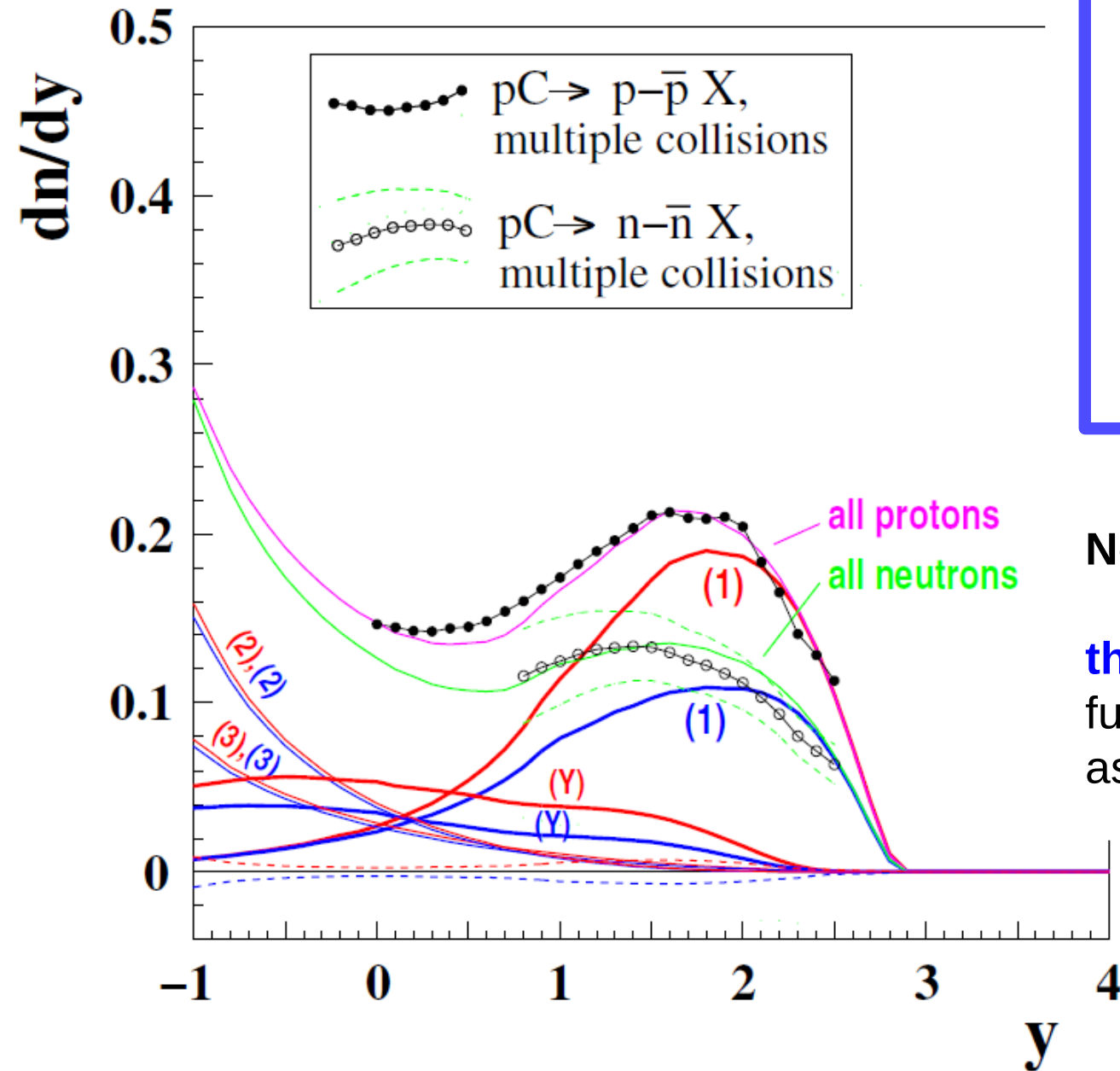
Note:  
this is (again) the  
**puzzle of nuclear stopping power.**

(\*) see also  
M.J., M. Rózańska,  
PLB 175 (1986) 206.



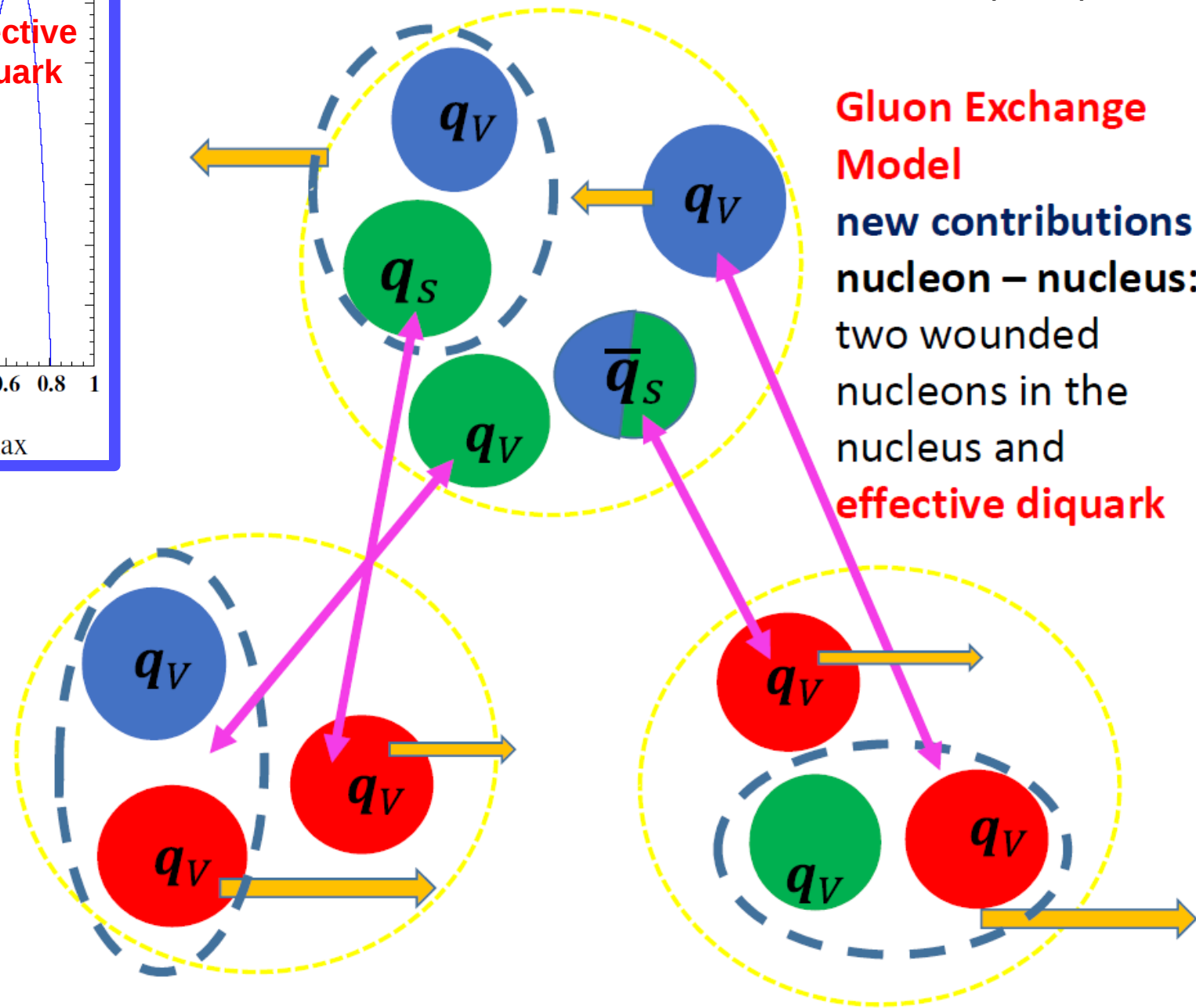
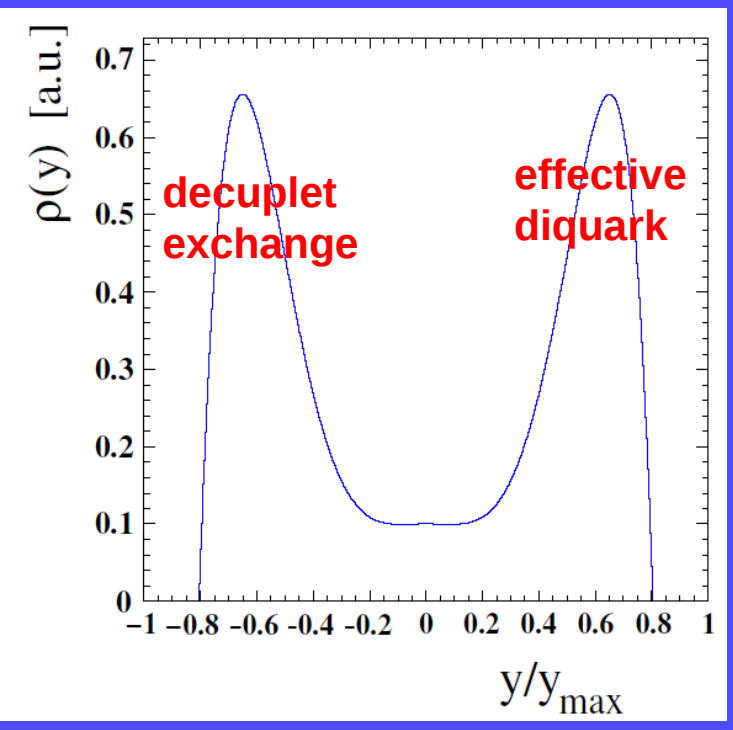
- Exp. data: diquark-preserving diagrams **cannot** be responsible for 100% of baryon “stopping” ;
- Upper limit for this contribution : **48%** .





Note!

**this** is the fragmentation function which we had to assume for the “Y object”.



we need to go beyond valence diquarks

# Summary (1)

1. For pp collisions, we found that it is necessary to go beyond the **valence quark degrees of freedom (inelastic diffraction)** ;
2. The importance of **sea quarks and antiquarks** in the multiple collision process was known already in the Dual Parton Model. Still, **secondary baryons** were produced only from **valence diquarks** ;
3. Relying uniquely on **valence quarks** in the proton brought us to two configurations: **color octet** and **color decuplet** ;
4. This brought us to a **non-intuitive** fragmentation function for the “Y” object ;
5. In order to preserve an intuitive fragmentation scheme, the exp. data **forced us** to introduce **effective diquarks (valence + sea quark)**.

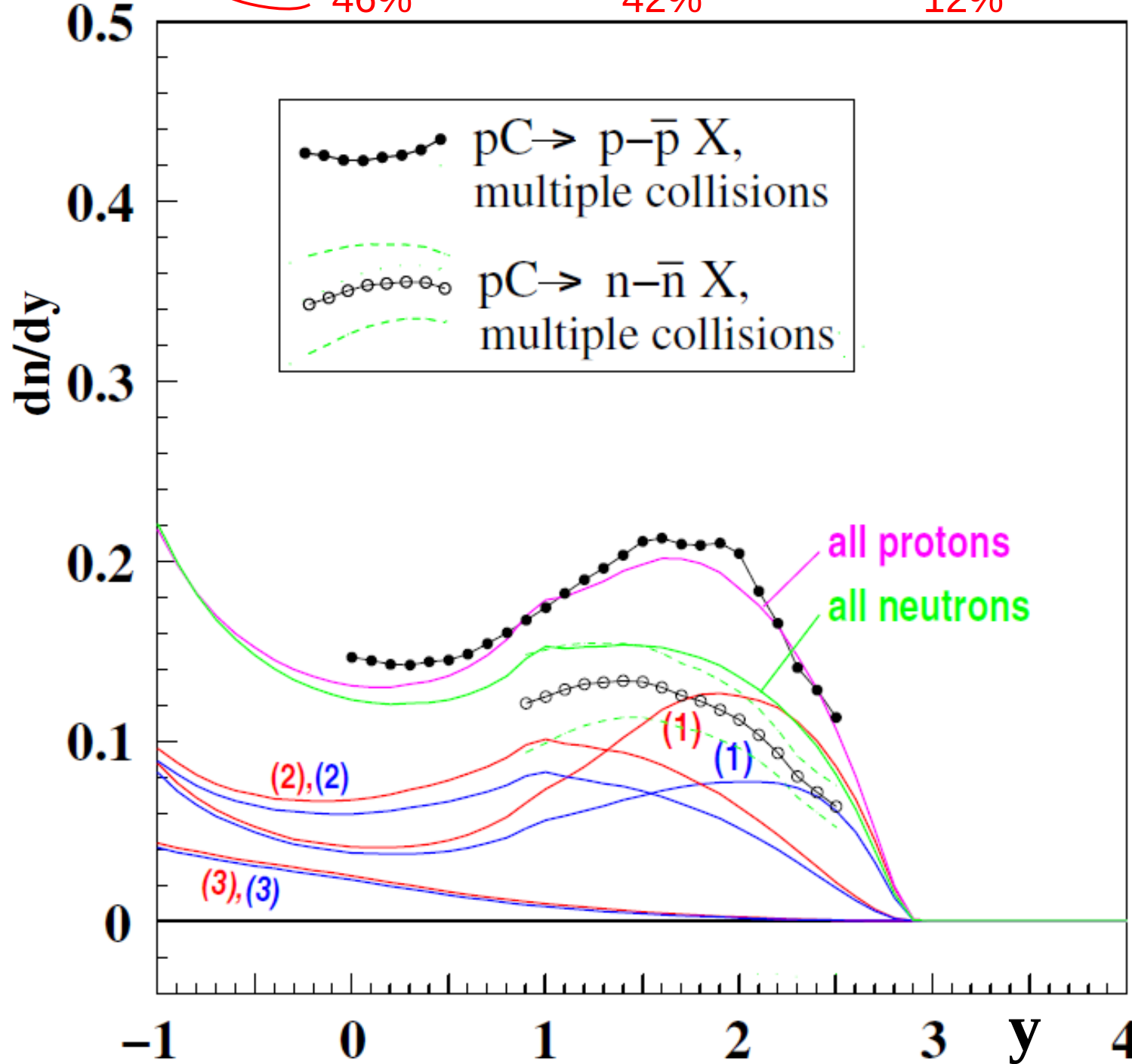
In order to understand these numbers, we will now introduce a **statistical postulate**.

### GEM in pA collisions (1) octet, (2) effective diquark, (3) decuplet.

46%

42%

12%



M.J., A.R.,  
EPJPlus 136 (2021) 971

# Statistical scheme for color exchange in p-nucleus collisions:

M.J., A.R.,  
ArXiv: 2111.03401,  
submitted to PLB.

1.  $N$  gluons are exchanged.

2. We consider two options:

(a) one gluon brings the valence quarks of the projectile proton into the **color octet** state. The remaining  $N-1$  gluons couple to sea quark-antiquark pairs ;

Valence and sea quarks are in the **color representation**  $R_8^{N-1} = \underset{\sim}{8} \otimes \underset{\sim}{3}^{N-1}$ ,

**Effective diquarks** can be of type: **valence-valence, valence-sea, sea-sea** .

(b) two gluons bring the valence quarks of the projectile into the **symmetric color decuplet** state. The remaining  $N-2$  gluons couple to sea quark-antiquark pairs ;

Valence and sea quarks are in the **color representation**  $R_{10}^{N-2} = \underset{\sim}{10} \otimes \underset{\sim}{3}^{N-2}$ ,

Effective diquarks can be of type: **no-diquark, valence-sea, sea-sea** .



3. The **probability** of obtaining an **effective diquark of a given type** can be obtained by decomposition into **irreducible representations**, and assuming that probabilities to form a diquark are **equal** for all the allowed pairs of quarks.

For  $N=1$  : **octet** :

$$R_8^0 = \underline{8} = (2,1,0)$$

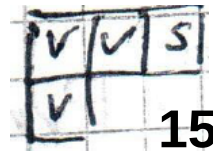
Dimension = 8



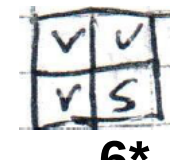
$$P_{VV} = 1$$

For  $N=2$  : **octet** :

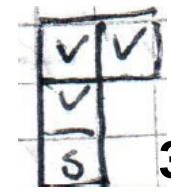
$$R_8^1 = \underline{8} \otimes \underline{3} = (3,1,0) \oplus (2,2,0) \oplus (2,1,1)$$



15



6\*



3

**decuplet** :

$$R_{10}^0 = \underline{10} = (3,0,0)$$

$$P_0 = 1$$

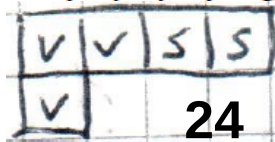


10

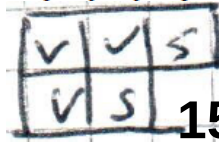
The experimental qualitative difference between  $N=1$  and  $N \geq 2$  (slide 6) becomes evident here.

For  $N=3$  : **octet** :

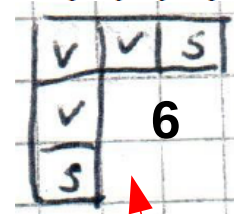
$$R_8^2 = \underline{8} \otimes \underline{3}^2 = (4,1,0) \oplus 2 \cdot (3,2,0) \oplus 2 \cdot (3,1,1) \oplus 2 \cdot (2,2,1)$$



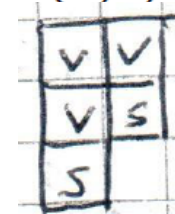
24



15\*



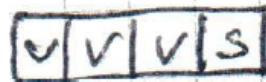
6



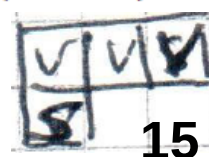
3\*

**decuplet** :

$$R_{10}^1 = \underline{10} \otimes \underline{3} = (4,0,0) \oplus (3,1,0)$$



15



15

ss diquark!

M.J., A.R.,  
ArXiv: 2111.03401,  
submitted to PLB.

$$R_8^0 = \underline{8} = (2,1,0)$$

$$R_8^1 = \underline{8} \otimes \underline{3} = (3,1,0) \oplus (2,2,0) \oplus (2,1,1)$$

$$R_8^2 = \underline{8} \otimes \underline{3}^2 = (4,1,0) \oplus 2 \cdot (3,2,0) \oplus 2 \cdot (3,1,1) \oplus 2 \cdot (2,2,1)$$

$$R_8^3 = (5,1,0) \oplus 3 \cdot (4,2,0) \oplus 3 \cdot (4,1,1) \oplus 2 \cdot (3,3,0) \oplus 6 \cdot (3,2,1) \oplus 2 \cdot (2,2,2)$$

$$R_8^4 = (6,1,0) \oplus 4 \cdot (5,2,0) \oplus 4 \cdot (5,1,1) \oplus 5 \cdot (4,3,0) \oplus 12 \cdot (4,2,1) \oplus 8 \cdot (3,3,1) \oplus 8 \cdot (3,2,2)$$

$$R_8^5 = (7,1,0) \oplus 5 \cdot (6,2,0) \oplus 5 \cdot (6,1,1) \oplus 9 \cdot (5,3,0) \oplus 20 \cdot (5,2,1) \oplus 5 \cdot (4,4,0) \oplus 25 \cdot (4,3,1) \oplus 20 \cdot (4,2,2) \oplus 16 \cdot (3,3,2)$$

$$R_8^6 = (8,1,0) \oplus 6 \cdot (7,2,0) \oplus 6 \cdot (7,1,1) \oplus 14 \cdot (6,3,0) \oplus 30 \cdot (6,2,1) \oplus 14 \cdot (5,4,0) \oplus 54 \cdot (5,3,1) \oplus 40 \cdot (5,2,2) \oplus 30 \cdot (4,4,1) \oplus 61 \cdot (4,3,2) \oplus 16 \cdot (3,3,3)$$

$$R_8^7 = (9,1,0) \oplus 7 \cdot (8,2,0) \oplus 7 \cdot (8,1,1) \oplus 20 \cdot (7,3,0) \oplus 42 \cdot (7,2,1) \oplus 28 \cdot (6,4,0) \oplus 98 \cdot (6,3,1) \oplus 70 \cdot (6,2,2) \oplus 14 \cdot (5,5,0) \oplus 98 \cdot (5,4,1) \oplus 155 \cdot (5,3,2) \oplus 91 \cdot (4,4,2) \oplus 77 \cdot (4,3,3)$$

$$R_8^8 = (10,1,0) \oplus 8 \cdot (9,2,0) \oplus 8 \cdot (9,1,1) \oplus 27 \cdot (8,3,0) \oplus 56 \cdot (8,2,1) \oplus 48 \cdot (7,4,0) \oplus 160 \cdot (7,3,1) \oplus 112 \cdot (7,2,2) \oplus 42 \cdot (6,5,0) \oplus 224 \cdot (6,4,1) \oplus 323 \cdot (6,3,2) \oplus 112 \cdot (5,5,1) \oplus 344 \cdot (5,4,2) \oplus 232 \cdot (5,3,3) \oplus 168 \cdot (4,4,3)$$

**color octet  
representations  
up to 9 gluons**

M.J., A.R.,  
ArXiv: 2111.03401,  
submitted to PLB.

**color decuplet  
representations  
up to 9 gluons**

$$R_{10}^0 = \overset{10}{\sim} = (3,0,0)$$

$$R_{10}^1 = \overset{10}{\sim} \otimes \overset{3}{\sim} = (4,0,0) \oplus (3,1,0)$$

$$R_{10}^2 = \overset{10}{\sim} \otimes \overset{3^2}{\sim} = (5,0,0) \oplus 2 \cdot (4,1,0) \oplus (3,2,0) \oplus (3,1,1)$$

$$R_{10}^3 = (6,0,0) \oplus 3 \cdot (5,1,0) \oplus 3 \cdot (4,2,0) \oplus 3 \cdot (4,1,1) \oplus (3,3,0) \oplus 2 \cdot (3,2,1)$$

$$R_{10}^4 = (7,0,0) \oplus 4 \cdot (6,1,0) \oplus 6 \cdot (5,2,0) \oplus 6 \cdot (5,1,1) \oplus 4 \cdot (4,3,0) \oplus 8 \cdot (4,2,1) \oplus 3 \cdot (3,3,1) \oplus 2 \cdot (3,2,2)$$

$$R_{10}^5 = (8,0,0) \oplus 5 \cdot (7,1,0) \oplus 10 \cdot (6,2,0) \oplus 10 \cdot (6,1,1) \oplus 10 \cdot (5,3,0) \oplus 20 \cdot (5,2,1) \oplus 4 \cdot (4,4,0) \oplus 15 \cdot (4,3,1) \oplus 10 \cdot (4,2,2) \oplus 5 \cdot (3,3,2)$$

$$R_{10}^6 = (9,0,0) \oplus 6 \cdot (8,1,0) \oplus 15 \cdot (7,2,0) \oplus 15 \cdot (7,1,1) \oplus 20 \cdot (6,3,0) \oplus 40 \cdot (6,2,1) \oplus 14 \cdot (5,4,0) \oplus 45 \cdot (5,3,1) \oplus 30 \cdot (5,2,2) \oplus 19 \cdot (4,4,1) \oplus 30 \cdot (4,3,2) \oplus 5 \cdot (3,3,3)$$

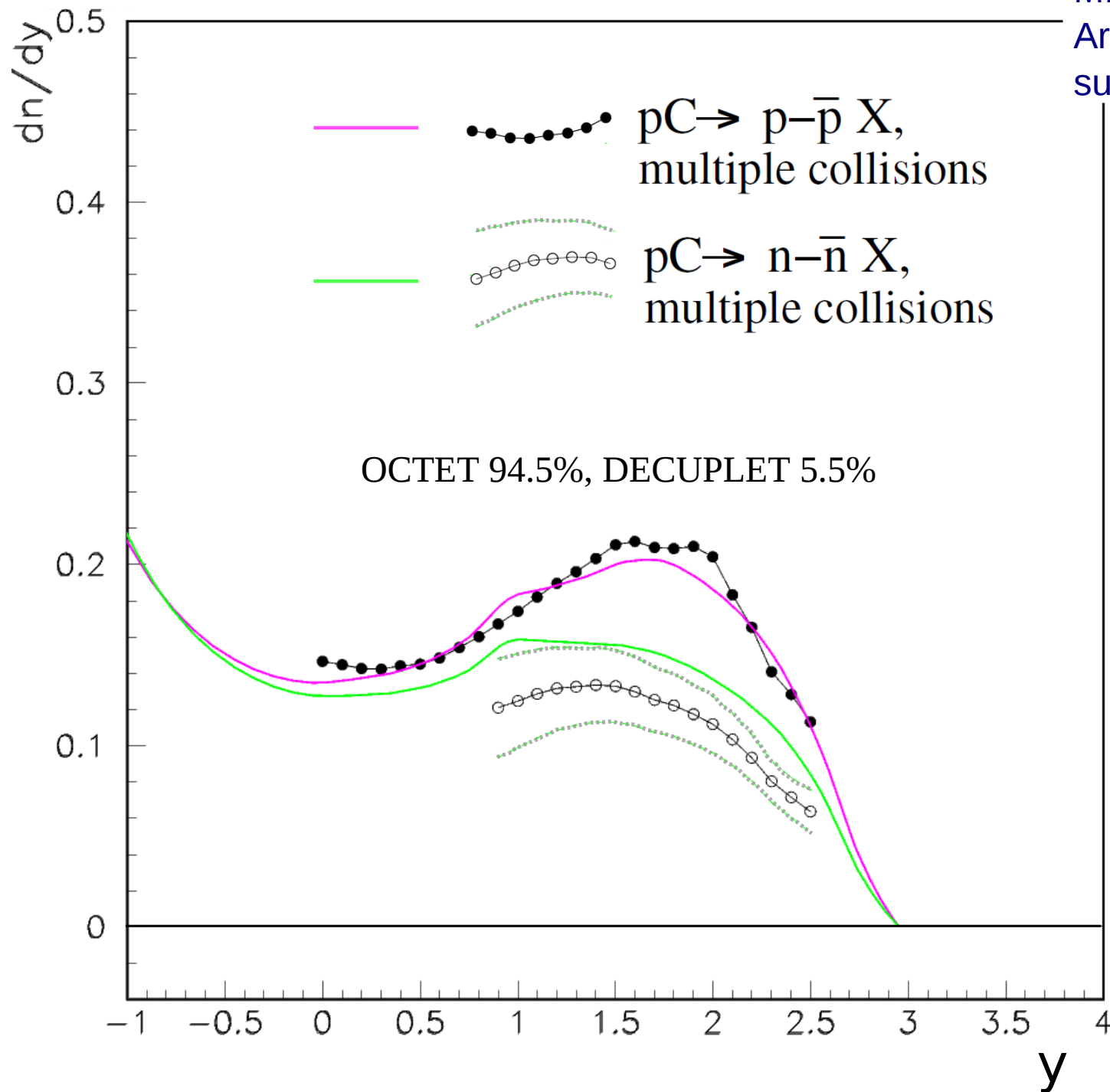
$$R_{10}^7 = (10,0,0) \oplus 7 \cdot (9,1,0) \oplus 21 \cdot (8,2,0) \oplus 21 \cdot (8,1,1) \oplus 35 \cdot (7,3,0) \oplus 70 \cdot (7,2,1) \oplus 34 \cdot (6,4,0) \oplus 105 \cdot (6,3,1) \oplus 70 \cdot (6,2,2) \oplus 14 \cdot (5,5,0) \oplus 78 \cdot (5,4,1) \oplus 105 \cdot (5,3,2) \oplus 49 \cdot (4,4,2) \oplus 35 \cdot (4,3,3)$$

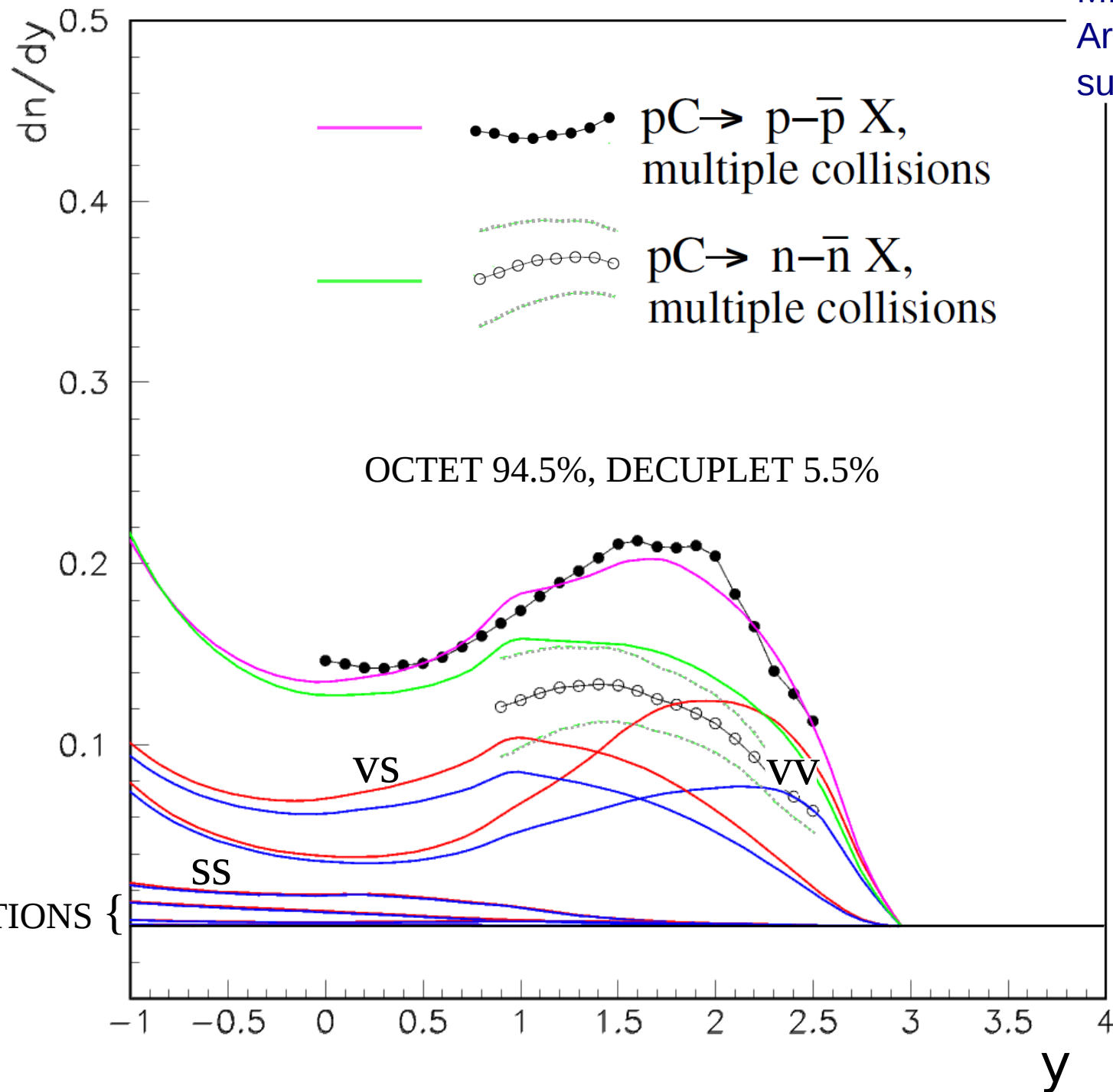
M.J., A.R.,  
ArXiv: 2111.03401,  
submitted to PLB.

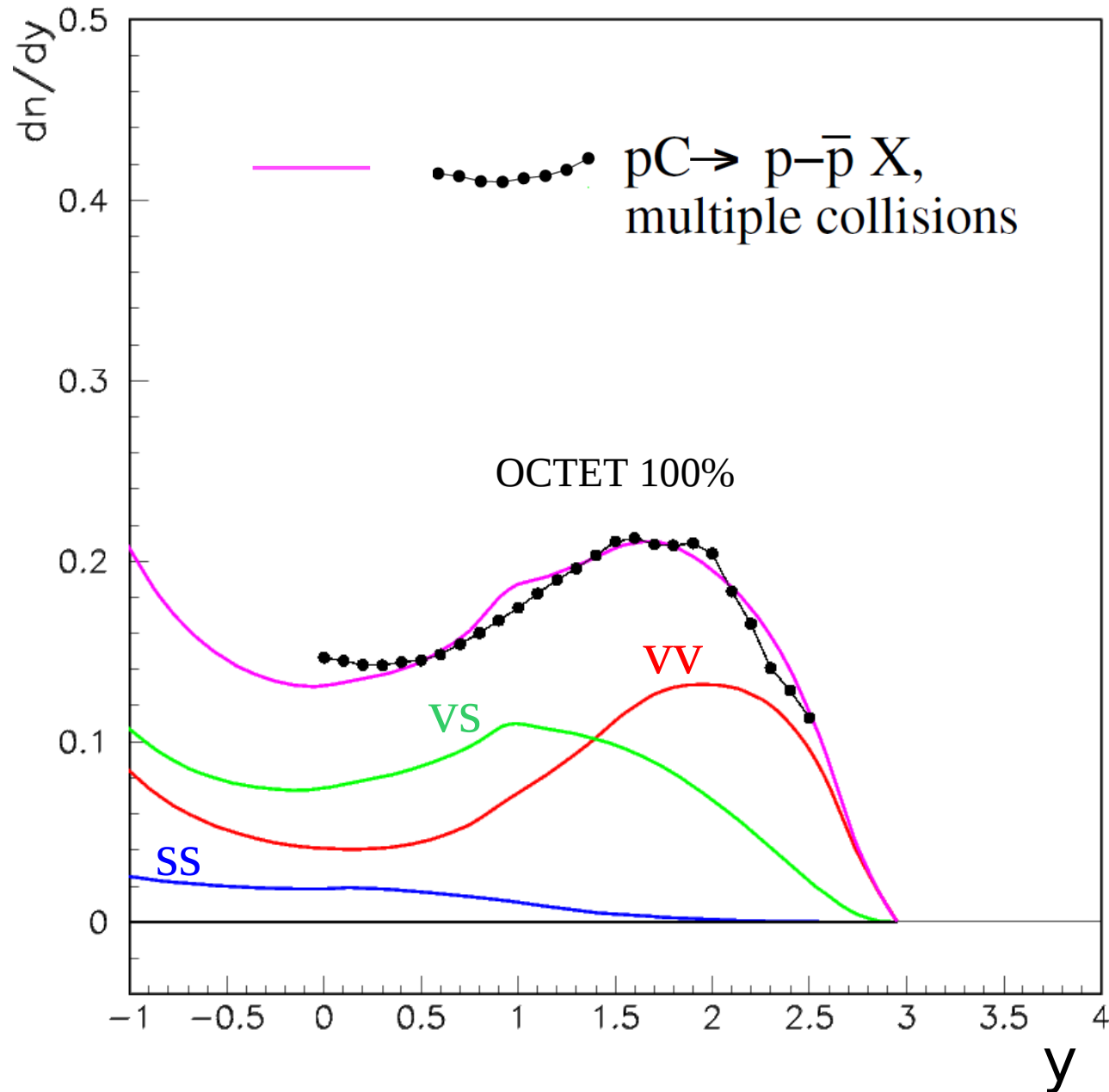
## Octet

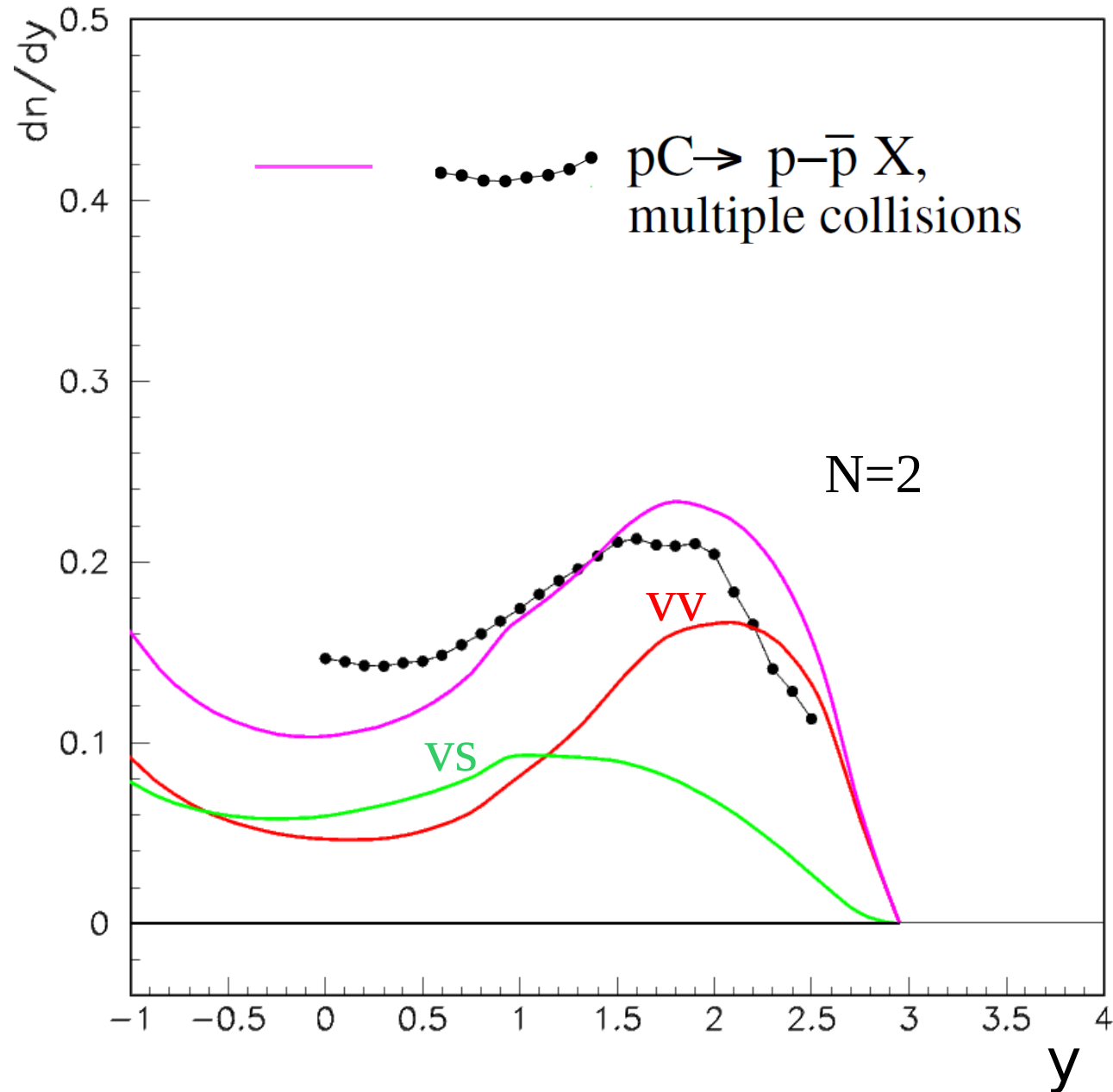
## Decuplet

	$\underline{8} \otimes \underline{3}^{N-1}$			$\underline{10} \otimes \underline{3}^{N-2}$		
<b>N</b>	<b>V V</b>	<b>V S</b>	<b>S S</b>	<b>0</b>	<b>V S</b>	<b>S S</b>
1	1	-	-	-	-	-
2	0.5917	0.4083	-	1	-	-
3	0.3740	0.5223	0.1037	0.5	0.5	-
4	0.2520	0.5407	0.2073	0.2333	0.6238	0.1429
5	0.1784	0.5213	0.3002	0.1037	0.6179	0.2784
6	0.1319	0.4908	0.3773	0.0444	0.5733	0.3823
7	0.1010	0.4582	0.4408	0.0185	0.5234	0.4581
8	0.0797	0.4272	0.4931	0.0075	0.4770	0.5155
9	0.0644	0.3989	0.5367	0.0030	0.4366	0.5604

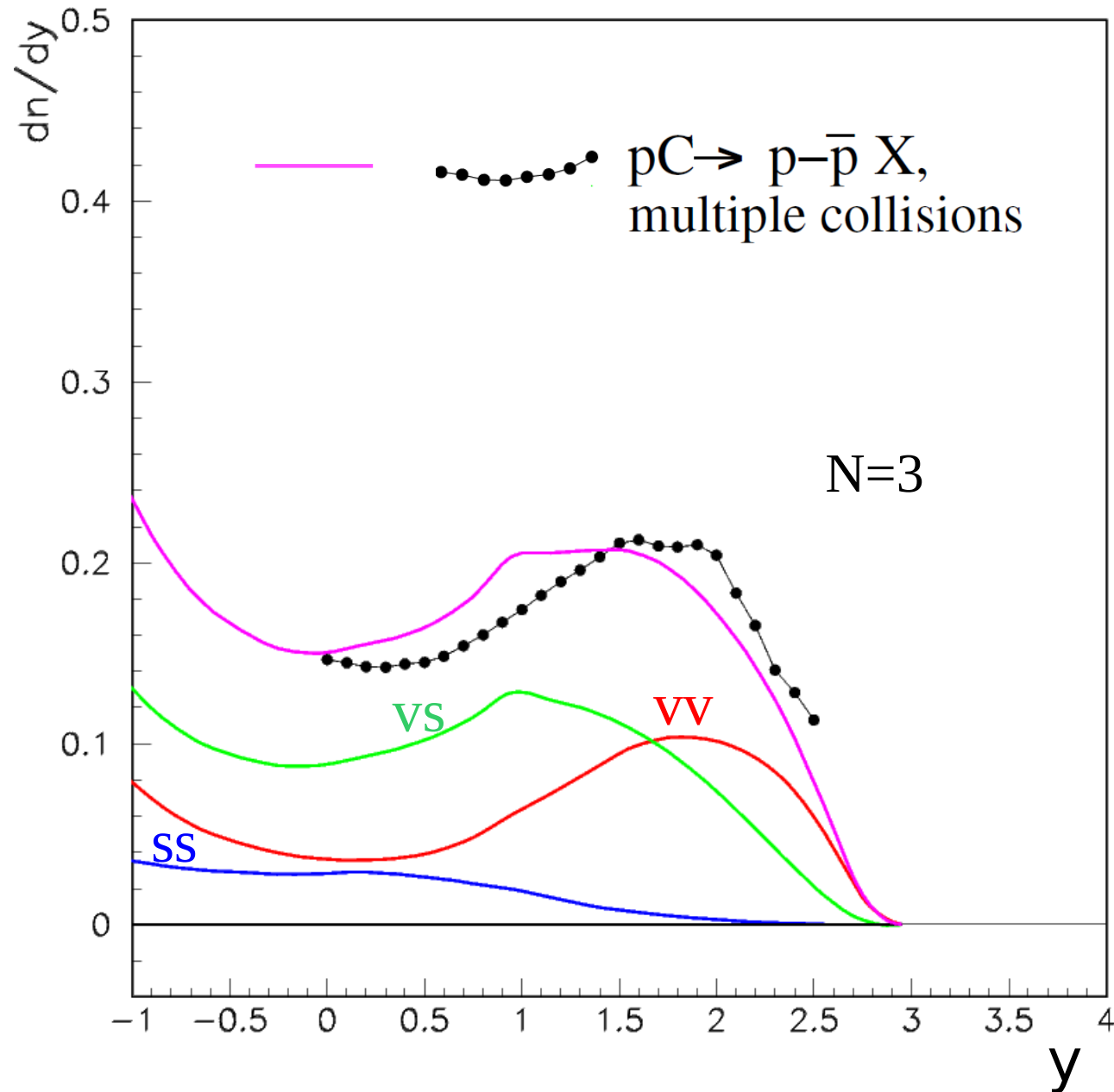


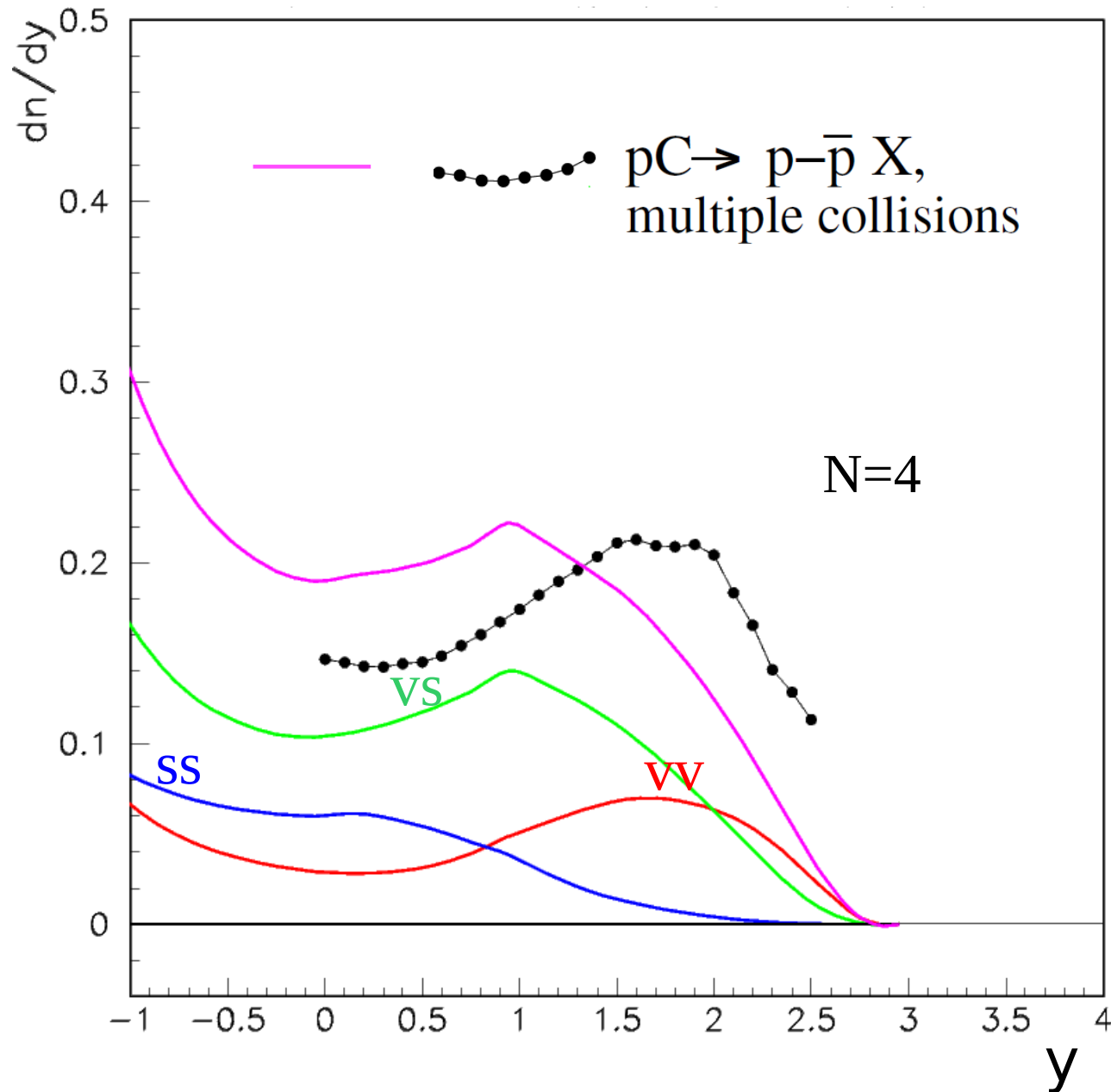


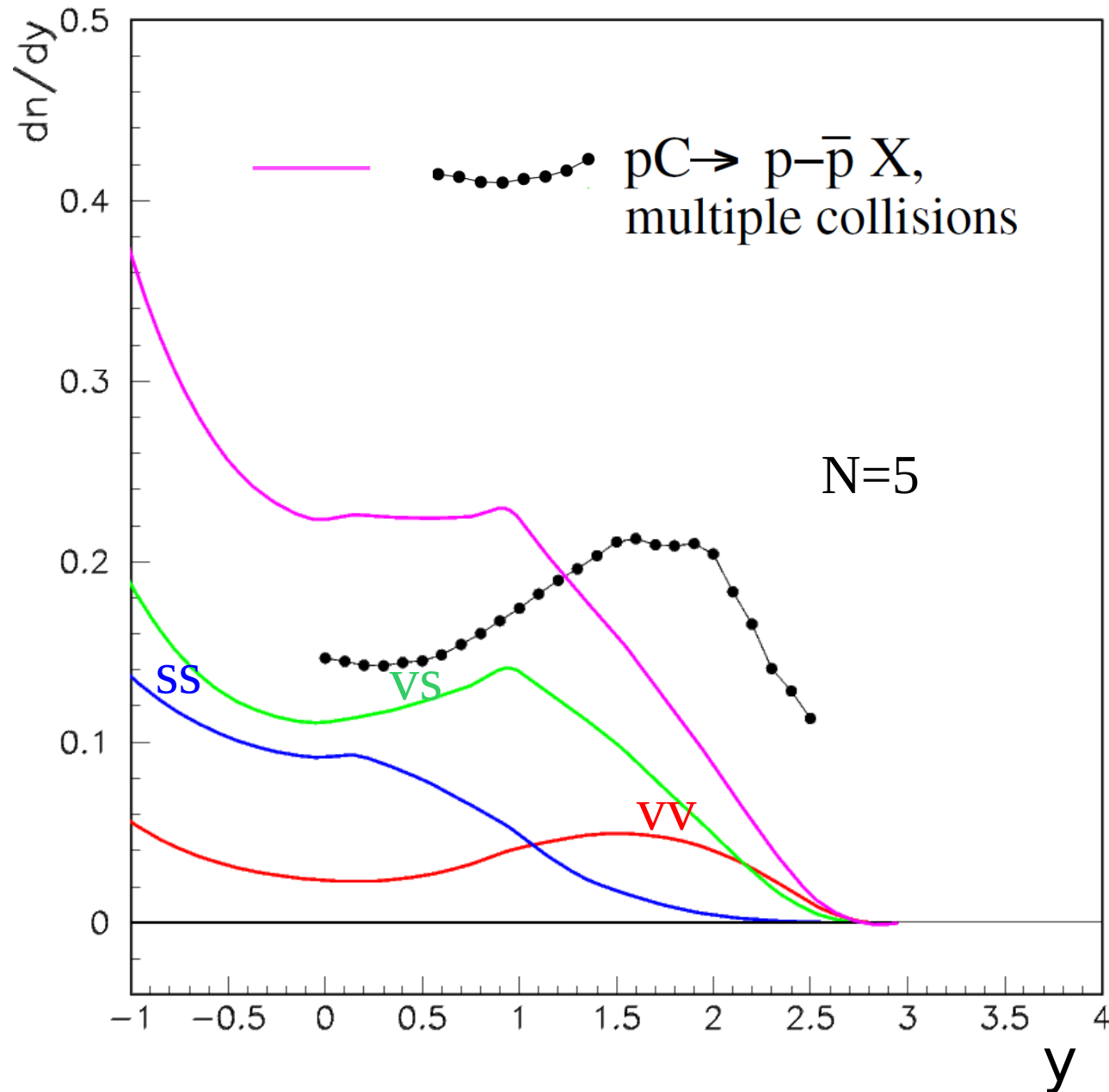


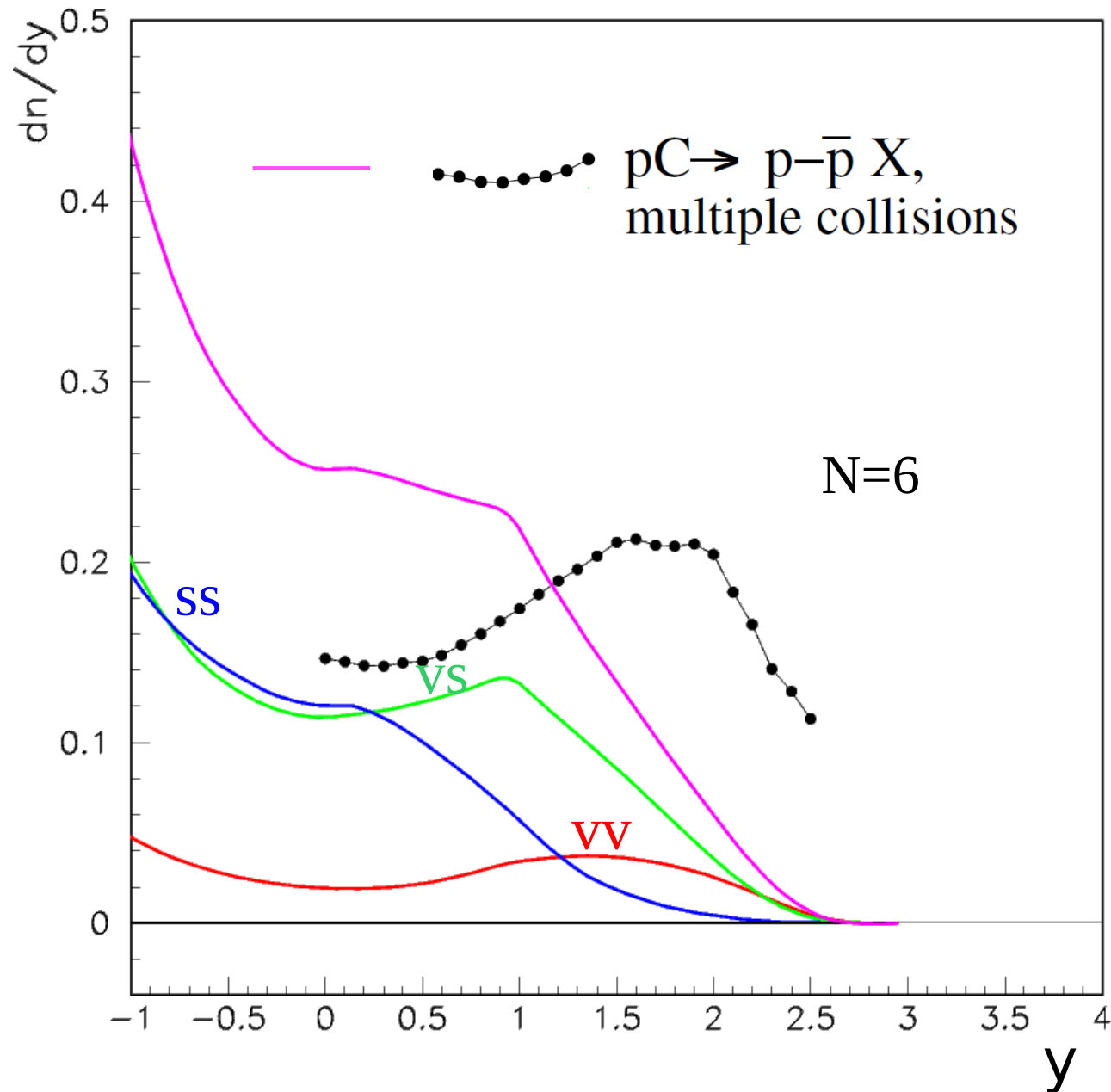


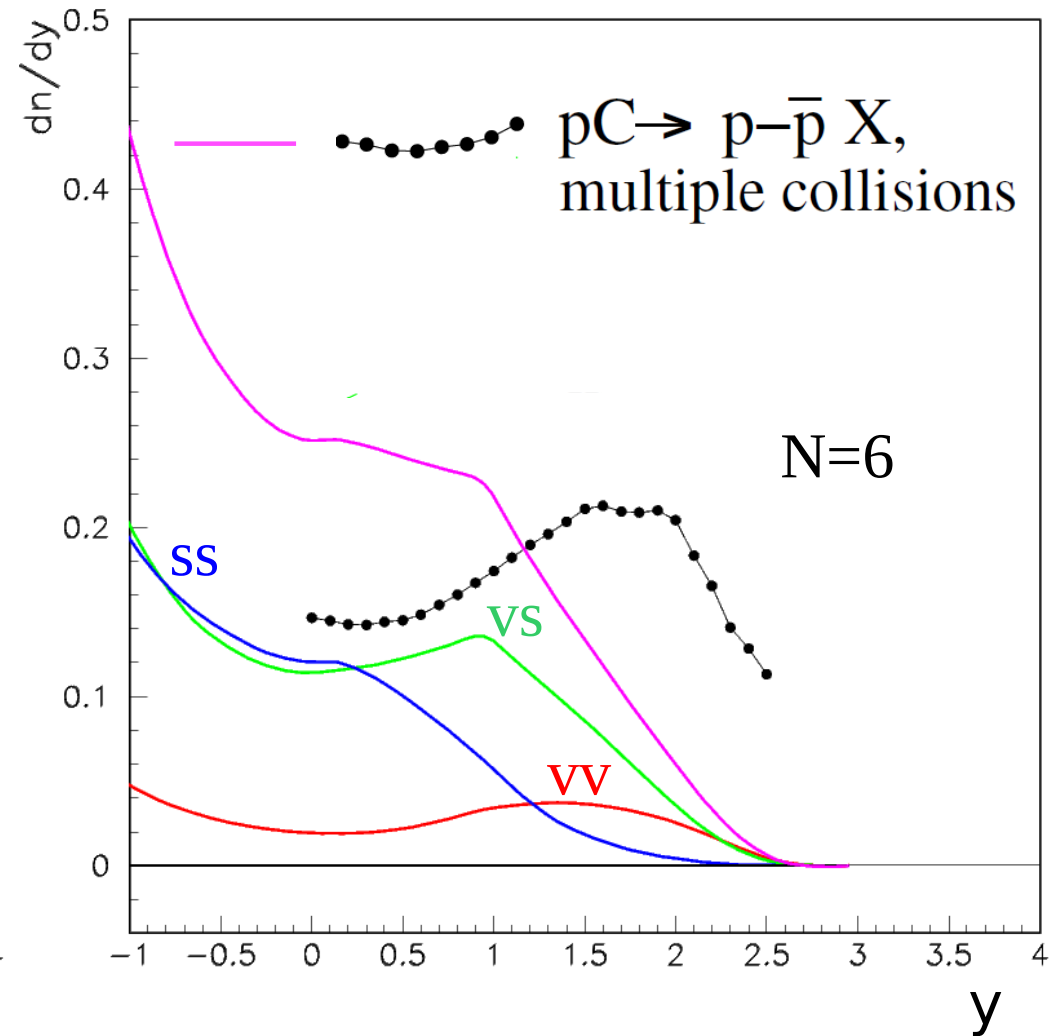
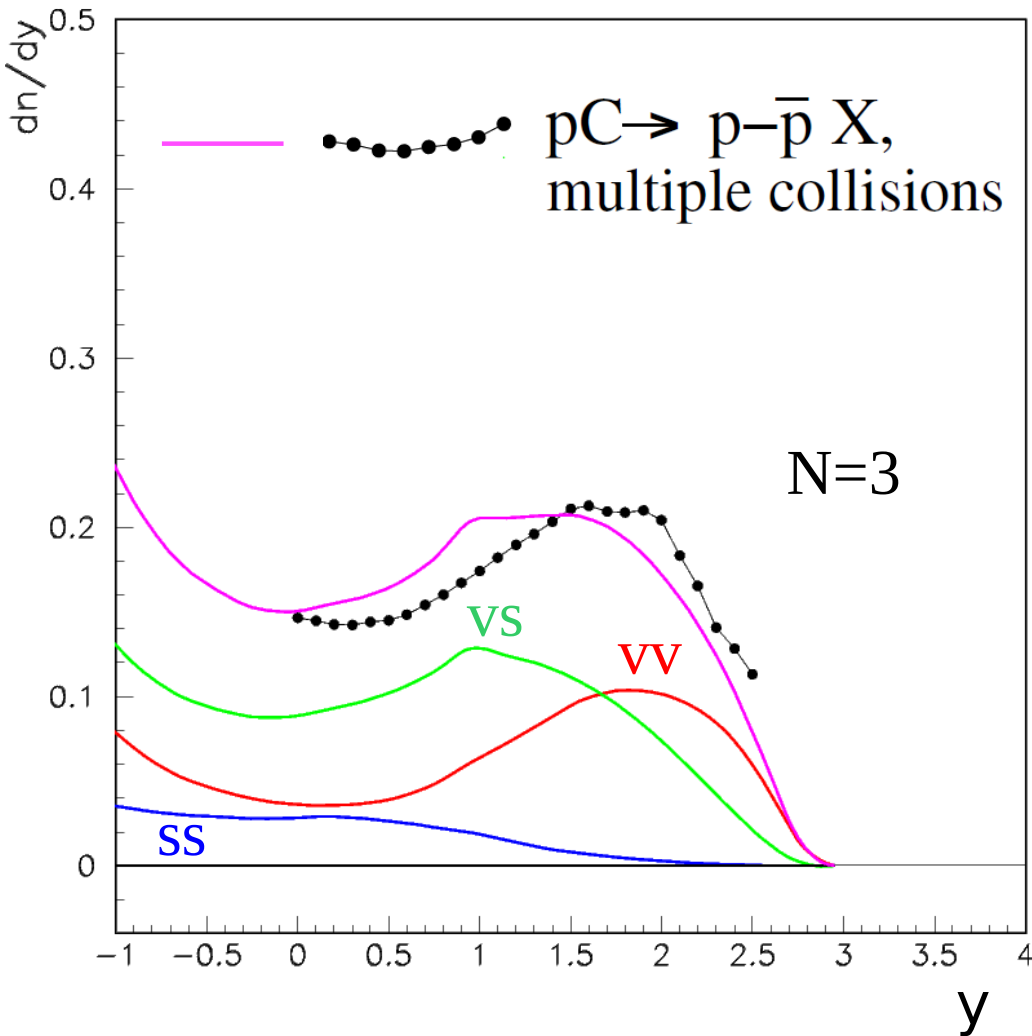












The process of baryon stopping is governed by the different **color configurations** of constituents of the proton (**valence-valence**, **valence-sea**, **sea-sea**), which **emerge** as a function of the **number of collisions**.

→ should be verified with experimental data on **p-Pb reactions**.

# 3) Summary

1. The process of emission of **secondary baryons** plays an important role in understanding of high energy proton-proton, proton-nucleus and heavy ion collisions (including **particle production**, **quark-gluon plasma** formation).
2. We attempted to describe new, precise **experimental data** on **pp** and **pC collisions** by proposing a **new model**, starting from the picture of the proton composed of **three valence quarks**.
3. An essential role is played by the **color configurations** of **constituents of the proton** in multiple scattering processes.
4. The inclusion of **valence degrees of freedom** alone is **not sufficient** to describe the experimental data.
5. Our work indicates that there are **four classes of contributions** to the spectra of secondary baryons, corresponding to **three types of diquarks** (**valence-valence**, **valence-sea**, **sea-sea**), and to **no diquark** in the forward hemisphere.

# 4) Outlook

1. Scattering of **antiprotons** on **protons** and **nuclei** is even more interesting, and may reveal **new phenomena** which will provide a deeper understanding of the **nature of annihilation** ;
2. **Work in progress** ;
3. **Ideal task for NA61/SHINE.**

# Acknowledgments

M.J. gratefully acknowledges the many years long collaboration with Maria Róžańska; this collaboration contributed in an essential way to the phenomenology and ideas presented in this paper.

Also A.R. warmly thanks M. Róžańska for very instructive discussions on the physics of soft baryon emission.

**... thank you !**



# ***Extra slides***

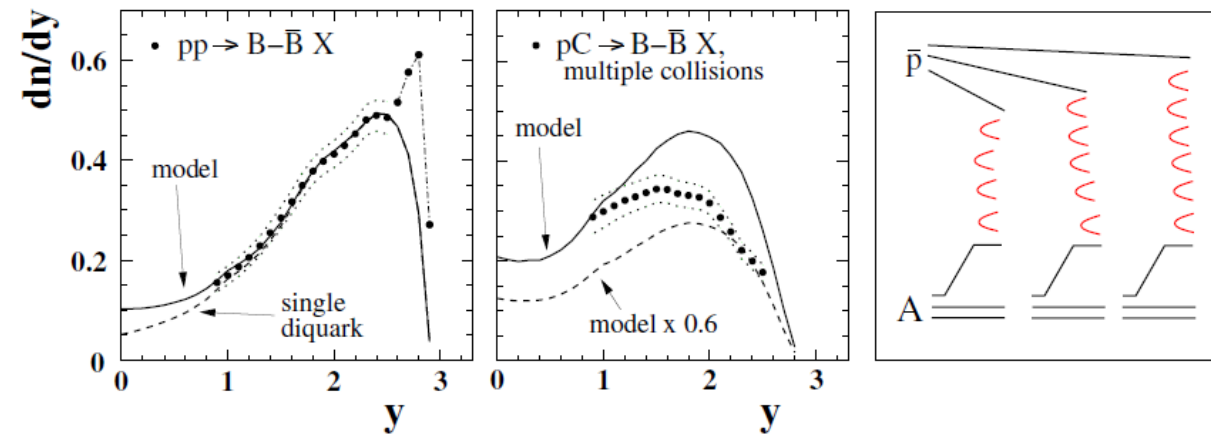
## Report from the NA61/SHINE experiment at the CERN SPS

The NA61/SHINE Collaboration

This document reports on the status and plans of the NA61/SHINE experiment at the CERN SPS as of October 2020. The document refers to the proposal SPSC-P-330.

### 7.2 New measurements with anti-proton beams for physics of strong interactions

A new idea of measurements of collisions of anti-protons with elementary and nuclear targets has been proposed in Ref. [93]. The authors argue that the relatively slow progress in the understanding of baryon stopping processes over the last three-four decades was due to the limitations inherent to the older experimental data sets [94]. These limitations, which



**Figure 29:** *Left:* distribution of net non-strange baryons measured in proton-proton collisions at  $\sqrt{s_{NN}}=17.3$  GeV (data points), put together with the result of the DPM model calculation drawn as a solid line. *Central:* same distribution obtained for proton-carbon reactions in which the projectile proton undergoes multiple collisions with carbon target nucleons (data points), put together with the DPM model result drawn as a solid line; the same model result scaled by 0.6 is also shown. *Right:* diagram of annihilation of the negative baryon number from the anti-proton on multiple nucleons from the nuclear target. The left and central panels come from Ref. [93].

a considerable improvement of the baryon stopping process, at the price of a manpower/financial effort which is close to negligible with respect to the overall working effort of the heavy ion field.