

# Heavy flavour physics

## Lecture 3

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# Contents

## **Lecture 3**

- Measurement of CKM angle  $\gamma$
- QCD penguins
- $B_s$  mixing
- Electroweak penguins
- Higgs penguins

# Measurements of CKM angles

# 3rd CKM measurement: $\gamma$

Extract  $\gamma$  with  $B \rightarrow D^{(*)}K^{(*)}$  final states using:

- GLW: Use CP eigenstates of  $D^0$
- ADS: Interference between favoured and doubly suppressed decays
- GGSZ: Use the Dalitz structure of  $D \rightarrow K_s h^+ h^-$  decays

$b \rightarrow c$  interfering with  $b \rightarrow u$

$B \rightarrow D^{(*)}K^{(*)}$

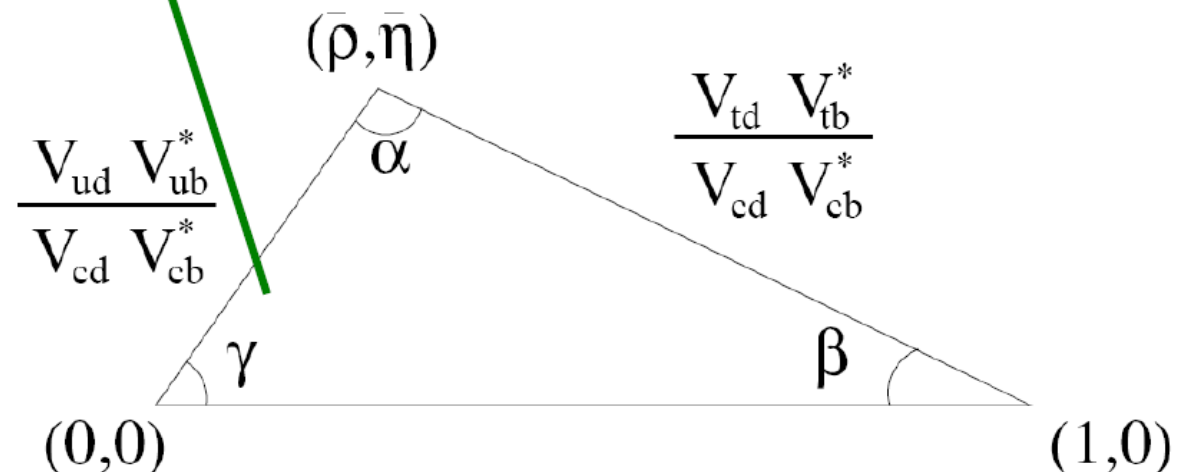
$B^0 \rightarrow D^- K^0 \pi^+$

$B^0 \rightarrow D^{(*)} \pi$

$B^0 \rightarrow D^{(*)} \rho$

+ charmless

$$\gamma \equiv \arg \left[ -V_{ud} V_{ub}^* / V_{cd} V_{cb}^* \right]$$



# Measurement of $\gamma$

- Charmless B decays, eg.  $B^0 \rightarrow K^+\pi^-$

- contributions from

- P :  $b \rightarrow s u(\bar{u})$  penguin

- T :  $b \rightarrow u s(\bar{u})$  tree

- relative weak (CP violating) phase is  $\gamma$

- relative strong (CP conserving) phase  $\delta$

$$A_{CP} = 2|P||T|\sin(\gamma)\sin(\delta)/\{|P|^2+|T|^2+2|P||T|\cos(\gamma)\cos(\delta)\}$$

- Hadronic uncertainties:

- even if we observe  $A_{CP} \neq 0$ , cannot easily extract  $\gamma$

- other processes also contribute

- A theoretically clean measurement of  $\gamma$  can be made using  $B \rightarrow DK$  decays

- Reconstruct D mesons in states accessible to both  $D^0$  and  $D^0(\bar{u})$

- interference between  $b \rightarrow c u(\bar{u})s$  and  $b \rightarrow u c(\bar{u})s$

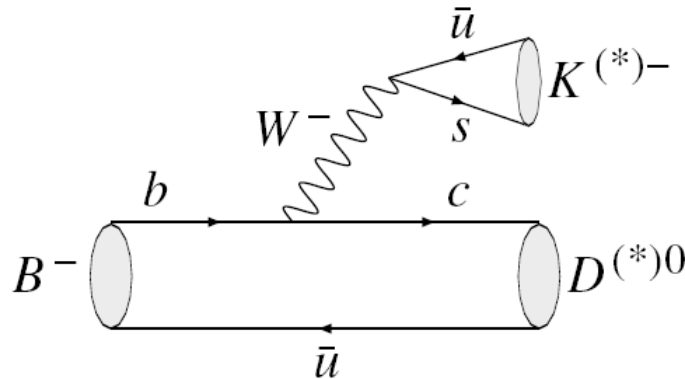
- relative weak phase is  $\gamma$

- various different D decays utilized

- large statistical errors at present

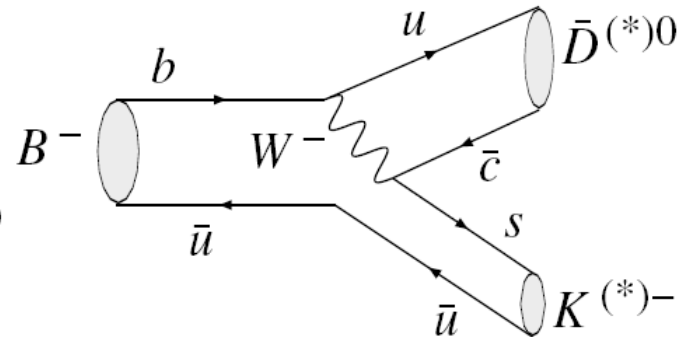
# The idea of measurement

- Two possible diagrams for  $B^- \rightarrow DK^-$



$$\propto V_{cb} V_{us}^*$$

- colour allowed
- final state contains  $D^0$



$$\propto V_{ub} V_{cs}^*$$

- colour suppressed
- final state contains  $D^0(bar)$

- Relative magnitude of suppressed amplitude is  $r_B$
- Relative weak phase is  $-\gamma$ , relative strong phase is  $\delta_B$
- Need  $D^0$  and  $D^0(bar)$  to decay to common final state

# Three ways to make DK interfere

GLW(*Gronau, London, Wyler*) method:

more sensitive to  $r_B$

uses the CP eigenstates  $D^{(*)0}_{CP}$  with final states:

$K^+K^-$ ,  $\pi^+\pi^-$  (CP-even),  $K_S\pi^0$  ( $\omega, \phi$ ) (CP-odd)

$$R_{CP\pm} = 1 + r_B^2 \pm 2r_B \cos \gamma \cos \delta_B \quad A_{CP\pm} = \frac{\pm 2r_B \sin \gamma \sin \delta_B}{1 + r_B^2 \pm 2r_B \cos \gamma \cos \delta_B}$$

ADS(*Atwood, Dunietz, Soni*) method:  $B^0$  and  $\bar{B}^0$  in the same final state with  $D^0 \rightarrow K^+\pi^-$  (suppr.) and  $\bar{D}^0 \rightarrow K^+\pi^-$  (fav.)

$$R_{ADS} = r_B^2 + r_{DCS}^2 + 2r_B r_{DCS} \cos \gamma \cos(\delta_B + \delta_D)$$

the most sensitive way to  $\gamma$

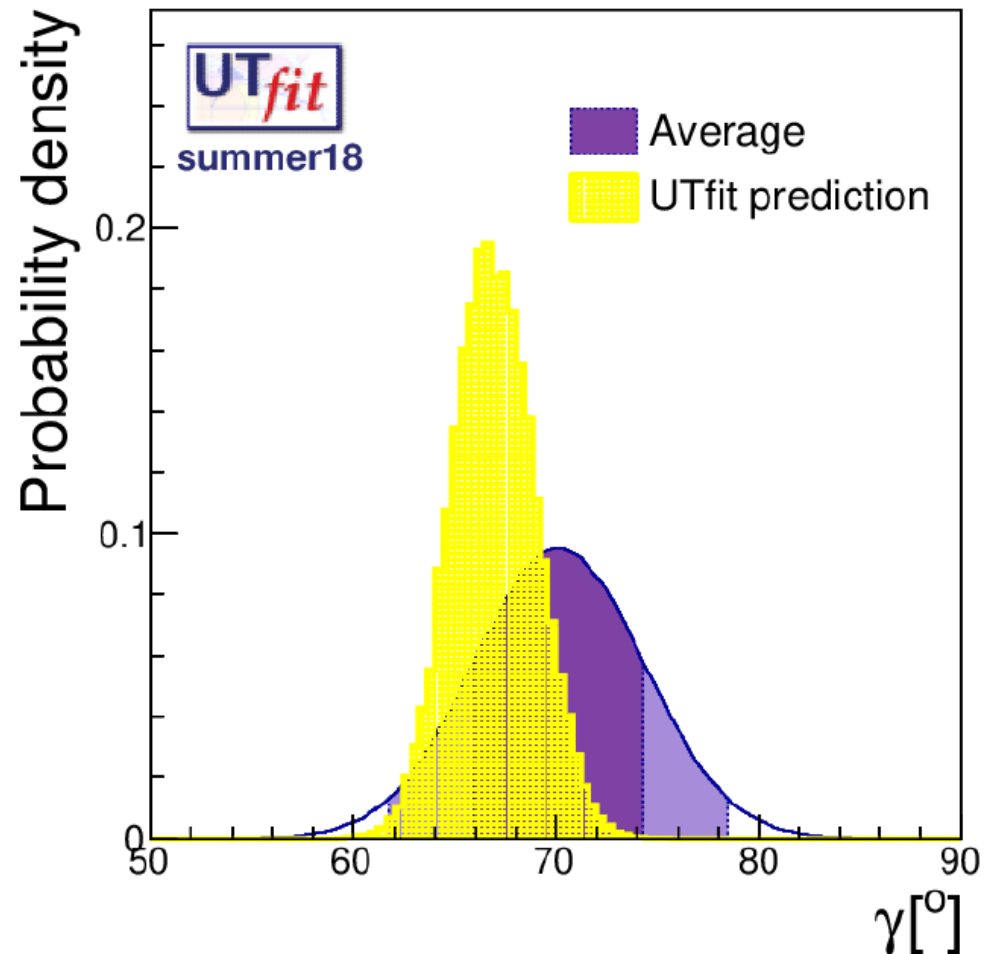
$D^0$  Dalitz plot with the decays  $B^- \rightarrow D^{(*)0}[K_S\pi^+\pi^-] K^-$

**3 free parameters to extract:  $\gamma$ ,  $r_B$  and  $\delta_B$**

# Constraint from $\gamma$

Best constraint from combining all available results

- $B \rightarrow DK$ ,  $B \rightarrow D^{(*)}K$ ,  $B \rightarrow DK^{(*)}$
- Different D decays
  - D → CP eigenstates
  - D → suppressed states
    - (eg.  $K\pi$ )
  - D → multibody states
    - (eg.  $K_S \pi^+ \pi^-$ )



$\gamma$  from B into DK decays:

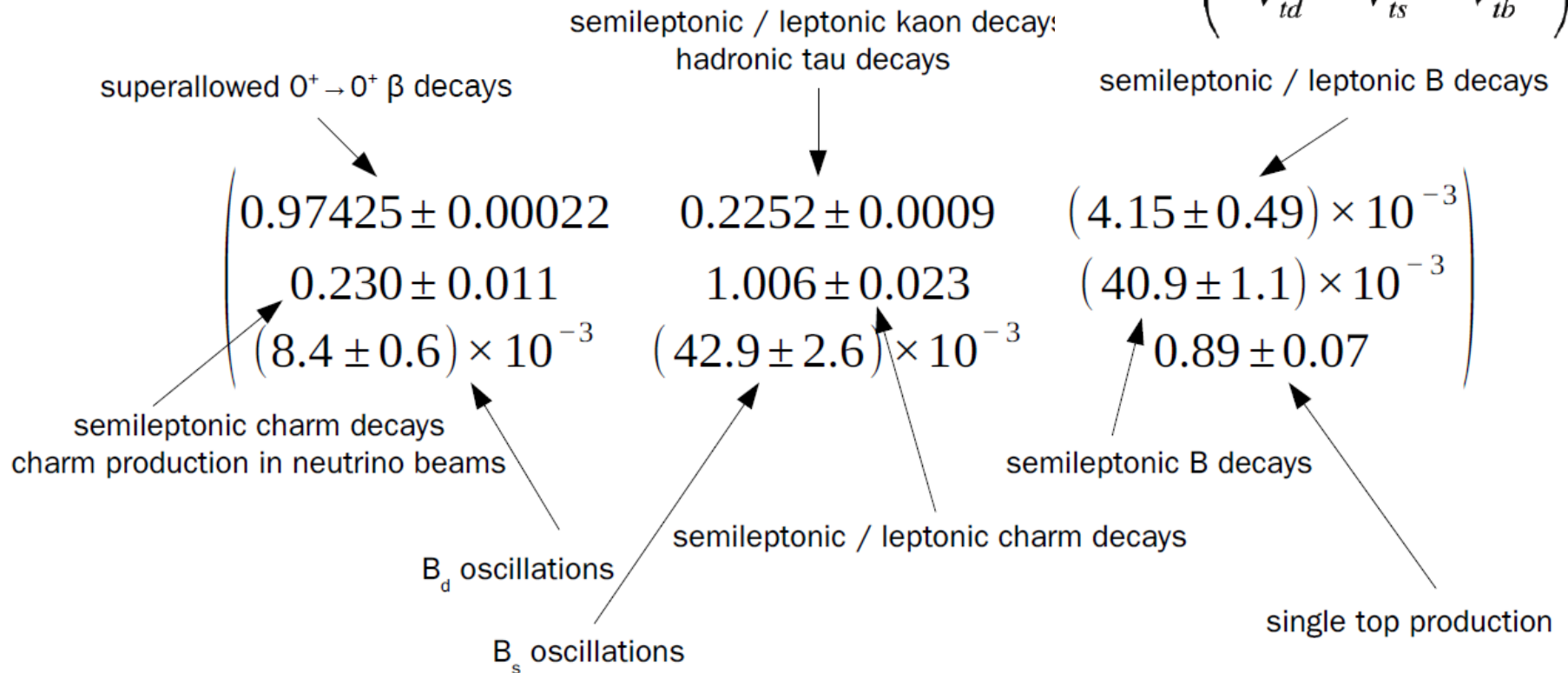
combined:  $(73.4 \pm 4.4)^\circ$

UTfit prediction:  $(65.8 \pm 2.2)^\circ$



# CKM matrix - magnitudes

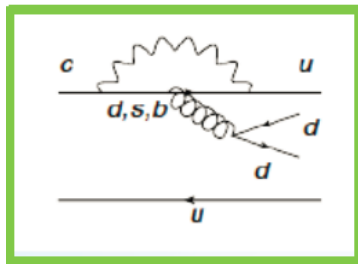
$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



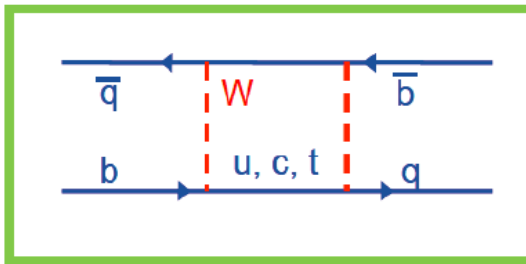
significant progress in many of these over the last few years  
(including some new results not yet in the PDG compilation)

# FCNC loops in the SM

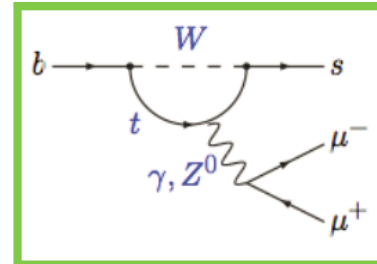
Map of flavour transitions and types of loop processes



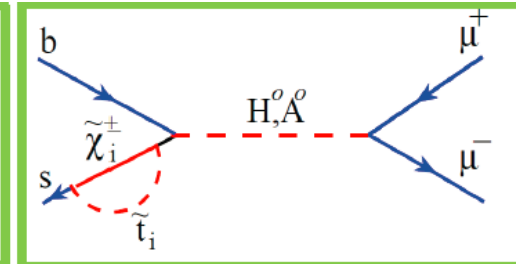
QCD penguin



$\Delta F=2$  box



EW penguin



Higgs penguin

	$b \rightarrow s$	$b \rightarrow d$	$c \rightarrow u$	$s \rightarrow d$
QCD penguin	$A_{CP}(B_s \rightarrow hhh)$	$A_{CP}(B^0 \rightarrow hhh)$	$\Delta a_{CP}(D \rightarrow hh)$	$K \rightarrow \pi^0 ll$ $\varepsilon' / \varepsilon$
$\Delta F=2$ box	$\Delta M_{Bs}$ $A_{CP}(B_s \rightarrow J/\psi \phi)$	$\Delta M_{Bd}$ $A_{CP}(B^0 \rightarrow J/\psi K_s)$	$x, y, q/p$	$\Delta M_K$ $\varepsilon_K$
EW penguin	$B \rightarrow K^{(*)} \mu \mu$ $B \rightarrow X_s \gamma$	$B \rightarrow \pi \mu \mu$ $B \rightarrow X \gamma$	$D \rightarrow X_u ll$	$K \rightarrow \pi^0 ll$ $K \rightarrow \pi^\pm \nu \nu$
Higgs penguin	$B_s \rightarrow \mu \mu$	$B^0 \rightarrow \mu \mu$	$D \rightarrow \mu \mu$	$K^0 \rightarrow \mu \mu$

QCD penguins

# Search for CP violation in charm decays

## Charm physics

- Neutral D meson offers the only chance to study  $\Delta F = 2$  (mixing) phenomena among up-type quarks
- FCNC in decays can also be studied
- CP violation in the D system is tiny in the SM, and hence its study probes New Physics
  - precise measurements needed to test realistic NP models

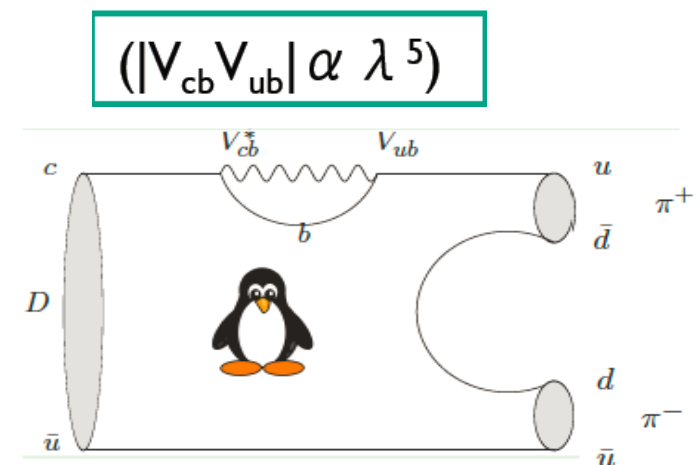
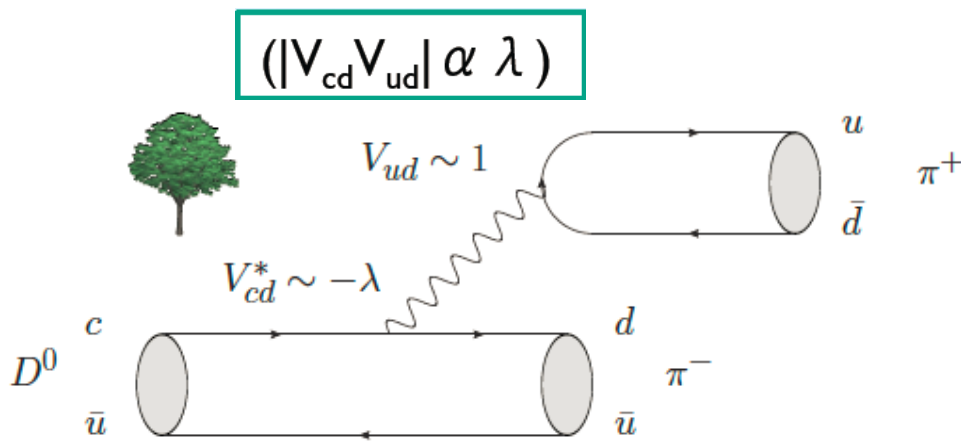
# CP violation in charm

- Charm:

- direct CP violation (in decay) in SM is small

- could there be large **direct CP violation** in charm **penguin decays**?

- CP violation  $O(1\%)$  would be „clear sign for NP“



Time integrated  $A_{CP}$  has both direct and indirect components

## CP violation in charm: $\Delta A_{CP}$

$$A_{\text{raw}}(f) = A_{CP}(f) + A_D(f) + A_P(D^{*+})$$

- Physical CP asymmetry (very small)
  - Detection asymmetry, cancels for  $D^0 \rightarrow \pi\pi, KK$
  - Production asymmetry
- } large  $O(1\%)$



$$\Delta A_{CP} = A_{\text{raw}}(K^-K^+) - A_{\text{raw}}(\pi^-\pi^+) = A_{CP}(K^-K^+) - A_{CP}(\pi^-\pi^+)$$

w/ U-spin symmetry:  $A_{CP}(K^-K^+) = -A_{CP}(\pi^-\pi^+)$

# CP violation in charm: $\Delta A_{CP}$

- $\Delta A_{CP}$  cancels detector and production asymmetries to first order
- The SM, and most NP models, predict opposite sign for KK and  $\pi\pi$
- Use of U-spin and QCD factorization leads to:

$$\Delta A_{CP} \sim 4 \text{ penguin/tree} \sim 0.04\%$$

## Analysis:

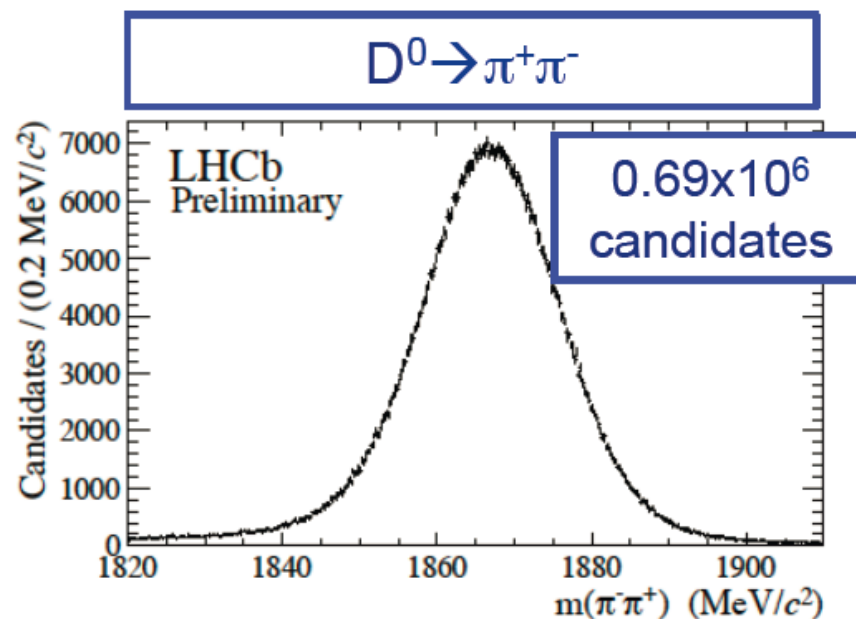
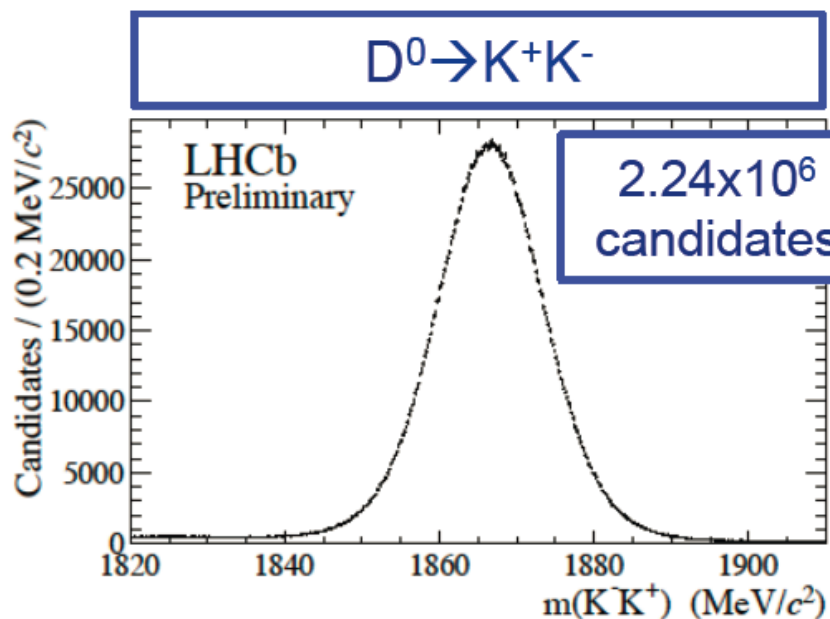
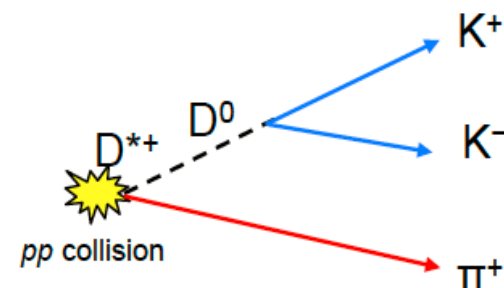
- LHCb performed two (experimentally orthogonal) measurements
- $D^{*\pm} \rightarrow D^0 [h^+h^-] \pi^\pm$  pion's charge determines the flavour of  $D^0$
- Alternatively, using  $B \rightarrow D \mu \nu$  decays the muon's charge determines the flavour.
- Most of the systematics cancel in the subtraction, and are controlled by swapping the magnetic field

# Measure CP violation: $D^{*+} \rightarrow D^0 \pi^+$

- LHCb performed two independent measurements

→ „D\* tagged”:  $D^{*\pm} \rightarrow D^0 (\rightarrow K^+ K^- \text{ or } \pi^+ \pi^-) \pi^\pm$

- pion charge determines  $D^0$  production flavour



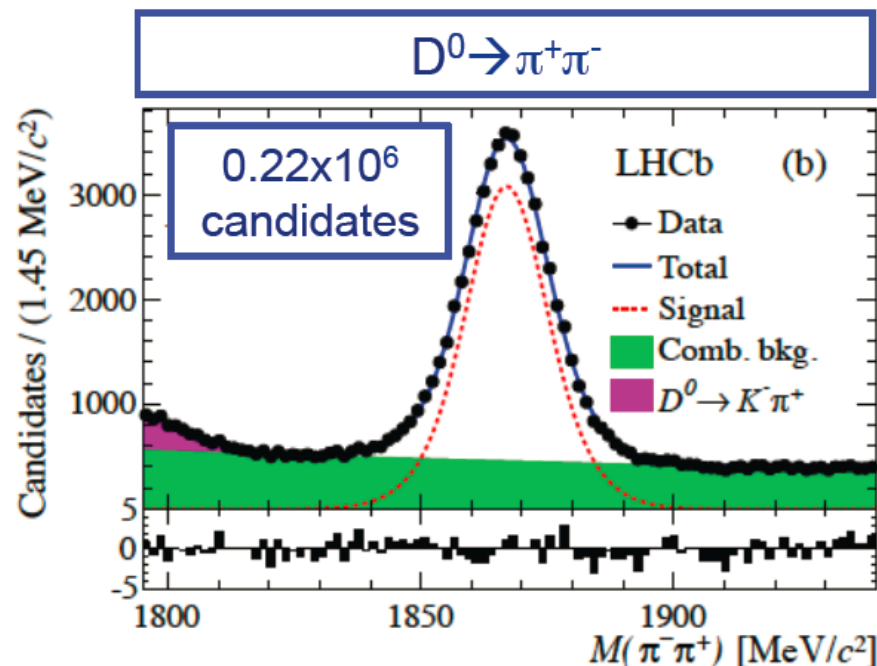
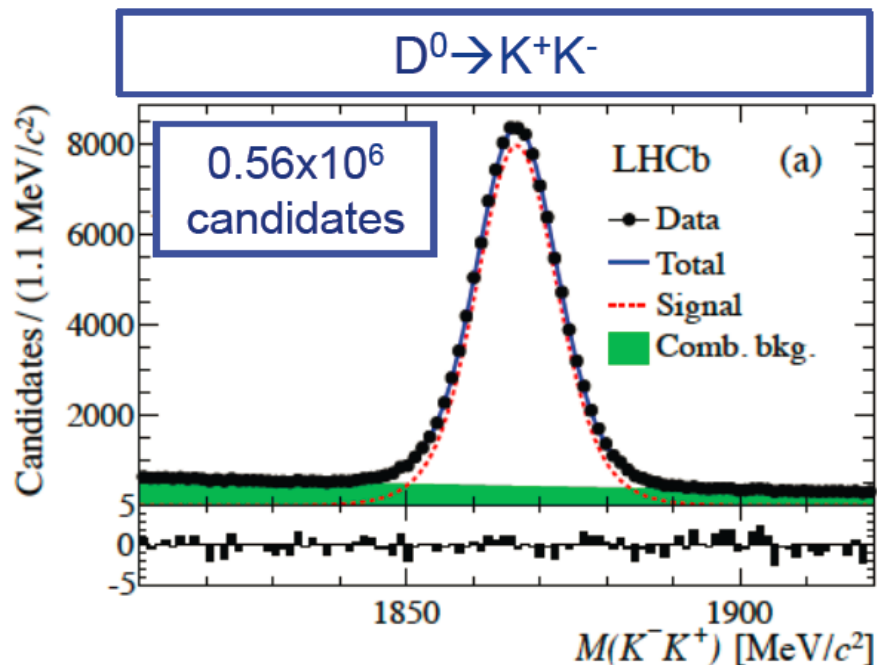
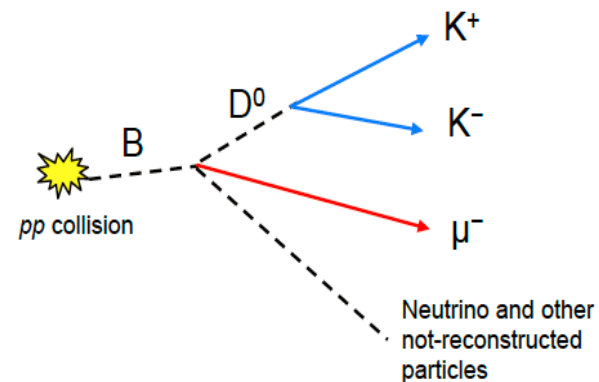


# Measure CP violation: $D^{*+} \rightarrow D^0 \pi^+$

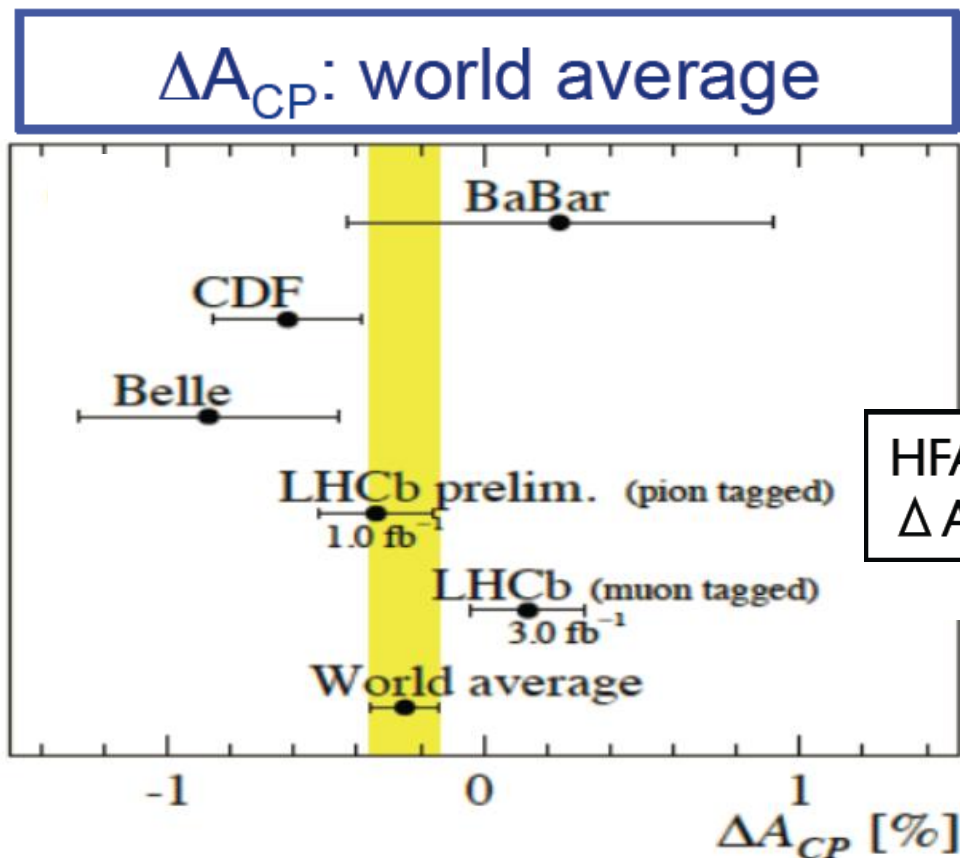
- LHCb performed two (experimentally orthogonal) measurements

→ “Muon tagged”:  $B^\pm \rightarrow D^0 (\rightarrow K^+ K^- \text{ or } \pi^+ \pi^-) \mu^\pm \nu X$

- muon charge determines  $D^0$  production flavour



# Measure CP violation: $D^{*+} \rightarrow D^0 \pi^+$



HFAG:

$$\Delta A_{CP} = (-0.253 \pm 0.104)\%$$

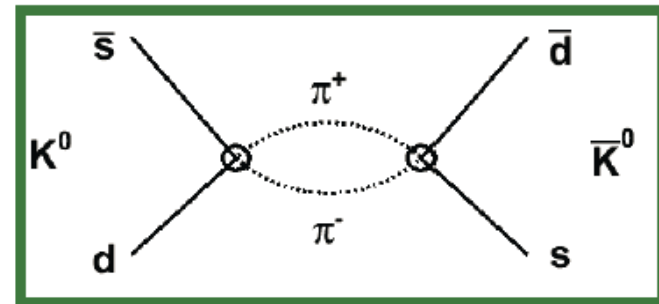
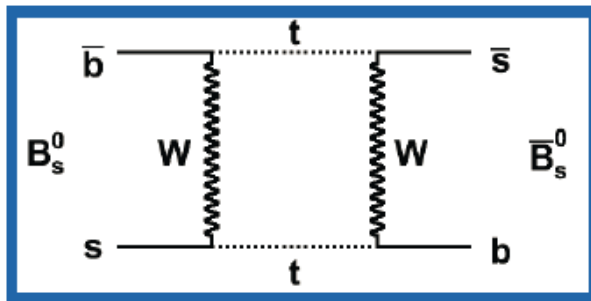
**No significant evidence for CP violation**  
**Effects O(%) are out of the game**

$\Delta F=2$  boxes:  
 $B_s$  mixing

# Neutral meson mixing

The eigenstates of flavour  $M^0$ , anti- $M^0$ , degenerated in pure QCD, mix under weak interactions:  
 $M^0$ :  $K^0$  (anti-s d),  $D^0$ (c anti-u),  $B^0$ (anti-b d),  $B_s^0$ (anti-b s)

Mixing can occur via **short distance** or **long distance** processes:



Time-dependent Schrödinger equation

$$i \frac{\partial}{\partial t} \begin{pmatrix} M^0 \\ \overline{M}^0 \end{pmatrix} = H \begin{pmatrix} M^0 \\ \overline{M}^0 \end{pmatrix} = \left( M - \frac{i}{2} \Gamma \right) \begin{pmatrix} M^0 \\ \overline{M}^0 \end{pmatrix}$$

$\mathbf{H}$  is Hamiltonian;  $\mathbf{M}$  and  $\mathbf{\Gamma}$  are 2x2 Hermitian matrices

**CPT theorem:**  $M_{11} = M_{22}$  &  $\Gamma_{11} = \Gamma_{22}$

→ particle and antiparticle have equal masses and lifetimes

# Mixing formalism

Time evolution of  $B^0$  or  $B^0(\text{bar})$  can be described by an *effective* Hamiltonian

Hamiltonian

$$\mathcal{H} = M - \frac{i}{2}\Gamma = \underbrace{\begin{pmatrix} M & M_{12} \\ M_{12}^* & M \end{pmatrix}}_{\substack{\text{hermitian} \\ \text{Mass term:} \\ \text{"dispersive"}}} - \frac{i}{2} \underbrace{\begin{pmatrix} \Gamma & \Gamma_{12} \\ \Gamma_{12}^* & \Gamma \end{pmatrix}}_{\substack{\text{hermitian} \\ \text{Decay term:} \\ \text{"absorptive"}}$$

Schrödinger equation

$$i \frac{d}{dt} \begin{pmatrix} |B^0(t)\rangle \\ |\bar{B}^0(t)\rangle \end{pmatrix} = \mathcal{H} \begin{pmatrix} |B^0(t)\rangle \\ |\bar{B}^0(t)\rangle \end{pmatrix}$$

Define the mass eigenstates (physical states):  $|B_{H,L}\rangle = p|B^0\rangle \mp q|\bar{B}^0\rangle$

$p$  &  $q$  complex coefficients that satisfy  $|p|^2 + |q|^2 = 1$

Heavy and light mass eigenstates have time dependence:  $|B_{H,L}(t)\rangle = e^{-(im_{H,L} + \Gamma_{H,L}/2)t} |B_{H,L}(0)\rangle$

Diagonalising → the mass and decay width difference

$\begin{aligned} \Delta m &= m_{B_H} - m_{B_L} = 2 M_{12}  \\ \Delta \Gamma &= \Gamma_L - \Gamma_H = 2 \Gamma_{12}  \cos \phi \end{aligned}$	$\phi = \arg(-M_{12}/\Gamma_{12})$
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$S, L$  (short-, long-) or  $L, H$  (light, heavy) depending on values of  $\Delta m$  &  $\Delta \Gamma$  (1,2 usually for CP eigenstates)

# Mixing formalism

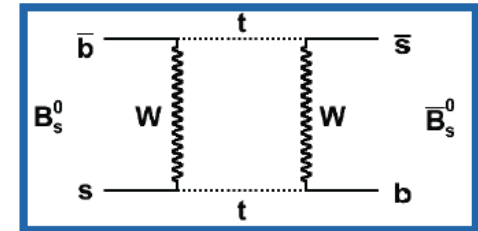
Solving the Schrödinger equation gives:

$$\frac{q}{p} = -\sqrt{\frac{M_{12}^* - i\Gamma_{12}^*/2}{M_{12} - i\Gamma_{12}/2}} \quad \Delta m = 2 \operatorname{Re} \sqrt{(M_{12} - i\Gamma_{12}/2)(M_{12}^* - i\Gamma_{12}^*/2)}$$

$$\Delta \Gamma = 2 \operatorname{Im} \sqrt{(M_{12} - i\Gamma_{12}/2)(M_{12}^* - i\Gamma_{12}^*/2)}$$

- $\Delta m$ : value depends on rate of mixing diagram

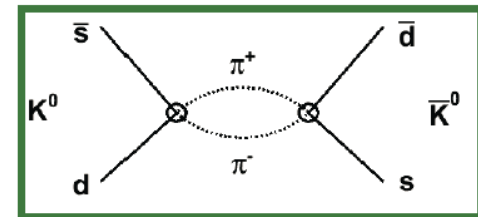
→ short distance, virtual (off shell)



- $\Delta \Gamma$ : value depends on widths of decays into common final states (CP-eigenstates)

→ long distance, on shell states

→ large for  $K^0$ , small for  $D^0$  &  $B^0$



- $q/p \approx 1$  if  $\arg(\Gamma_{12}/M_{12}) \approx 0$  ( $|q/p| \approx 1$  if  $M_{12} \ll \Gamma_{12}$  or  $M_{12} \gg \Gamma_{12}$ )

→ CP conserved if physical states = CP eigenstates ( $|q/p| = 1$ )

→ CP violation in mixing when mass eigenstates  $\neq$  CP eigenstates  $|q/p| \neq 1$

# Mixing of neutral mesons

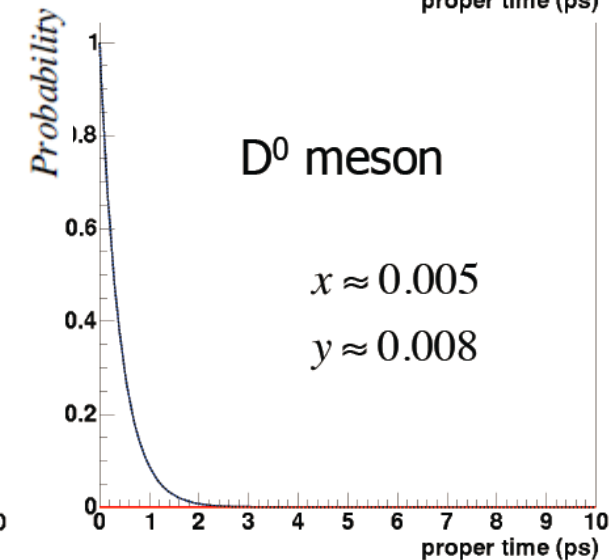
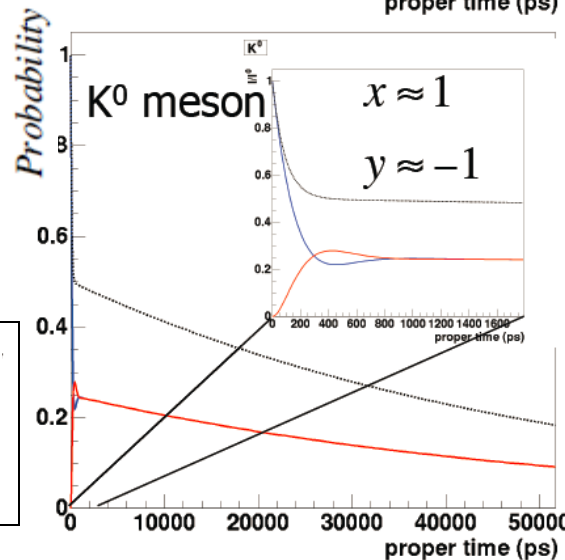
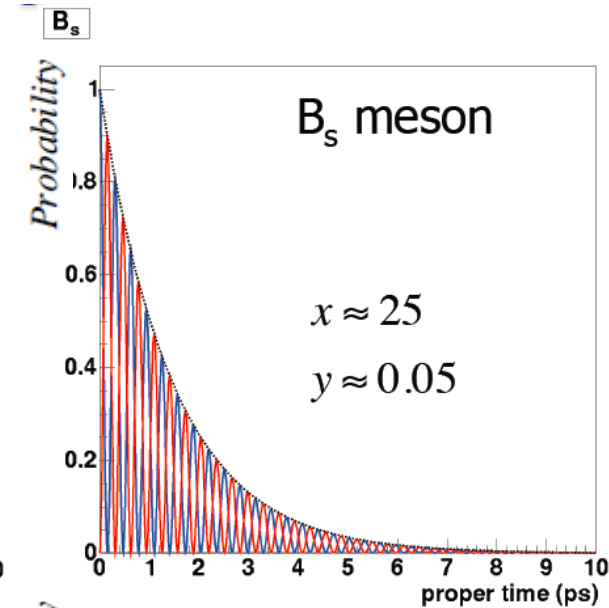
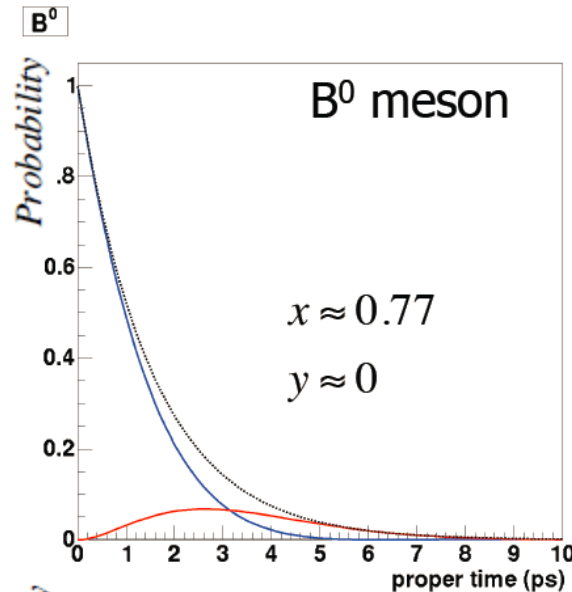
4 different neutral meson systems have very different mixing properties:

- **$B_s$  system**  
→ very fast mixing
- **Kaon system**  
→ large decay time difference
- **Charm system**  
→ very slow mixing

$x$ : the average number of oscillations before decay  
 $y$ : the relative decay width difference

$$x \equiv \frac{\Delta m}{\Gamma}$$

$$y \equiv \frac{\Delta \Gamma}{2\Gamma}$$



# Kaon and charm mixing

- **Kaon mixing**

→ CPLEAR experiment

- tag strangeness of initial kaon using charge of associated kaon from production  $p\bar{p} \rightarrow K+K^0(\bar{K})\pi^- / K^-K^0\pi^+$

- **Charm mixing**

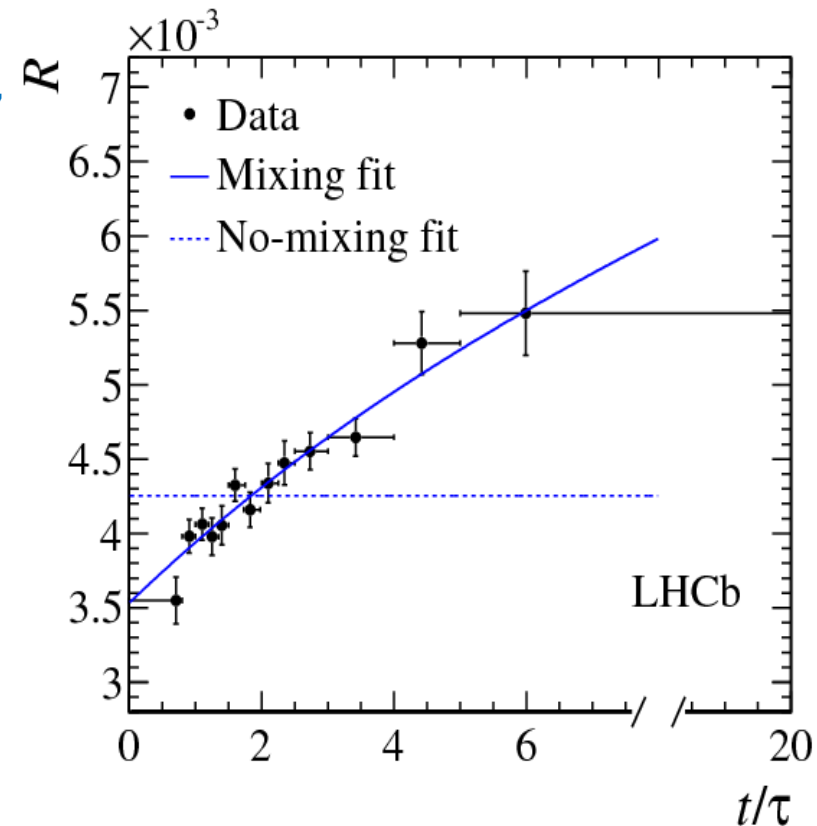
→ evidence ( $3\sigma$ ) for charm mixing in 2007 from BaBar & Belle

→ followed by further evidence from CDF

→ combined significance of mixing overwhelming, but no single  $5\sigma$  measurement until LHCb

→ time-dependence of ratio of wrong-sign (WS) to right-sign (RS)  $D^0 \rightarrow K\pi$  decays

- WS/RS known by  $D^{*+} \rightarrow D^0\pi$  tag





# $B^0$ - $B^0(\text{bar})$ oscillations

ARGUS experiment (1987)

## First evidence

- Same sign leptons  
→ same flavour B mesons
- Mixing probability is large  
→ top quark is heavy
- Mixing probability:  $r = 0.21 \pm 0.08$
- PDG 2006:  $r = 0.188 \pm 0.003$
- From 103/pb of data

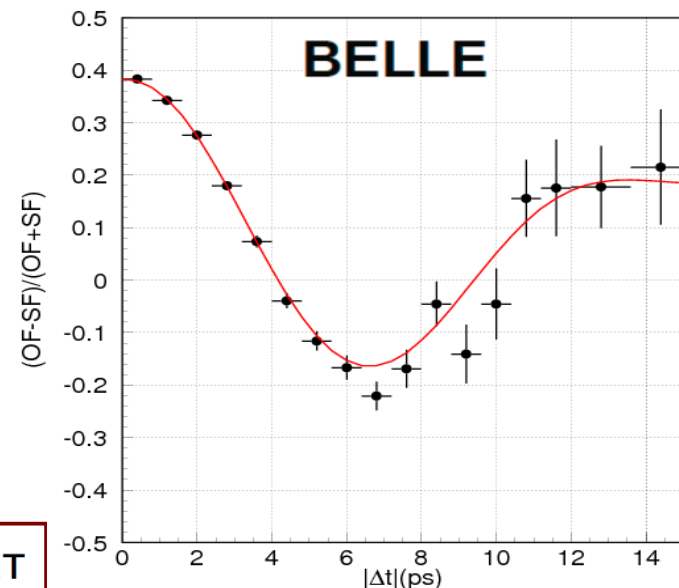
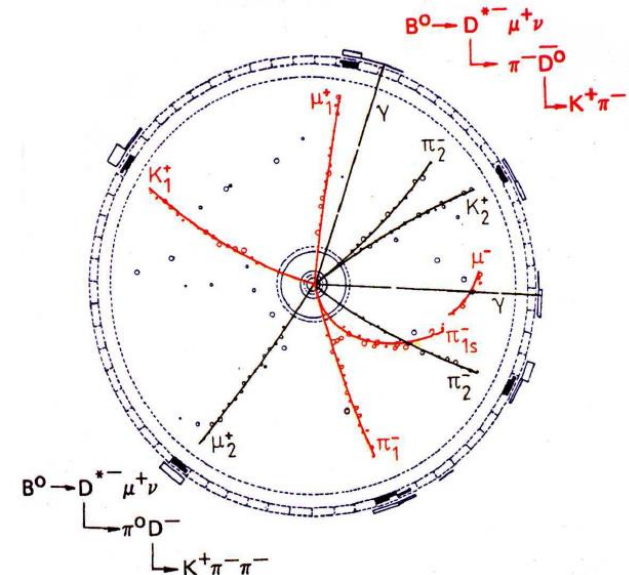
## B mixing with current data sets

- Belle experiment (2005)

$$\Delta m = (0.511 \pm 0.005 \pm 0.006) \text{ ps}^{-1}$$

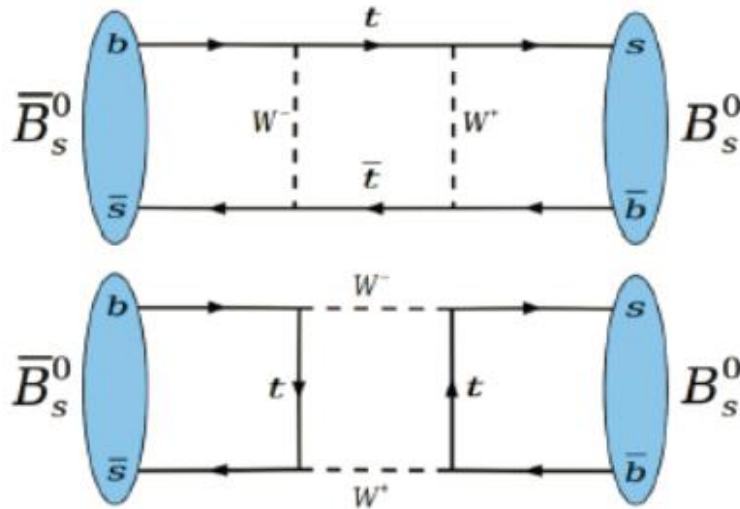
- From 140/fb of data

$$P(\Delta t) = (1 \pm \cos(\Delta m \Delta t)) e^{-|\Delta t|/2\tau}$$



# $B_s$ - $\bar{B}_s$ oscillations

Dominant Feynman diagrams (Standard Model)



$$\Delta m_s = m_H - m_L = 2|M_{12}|$$

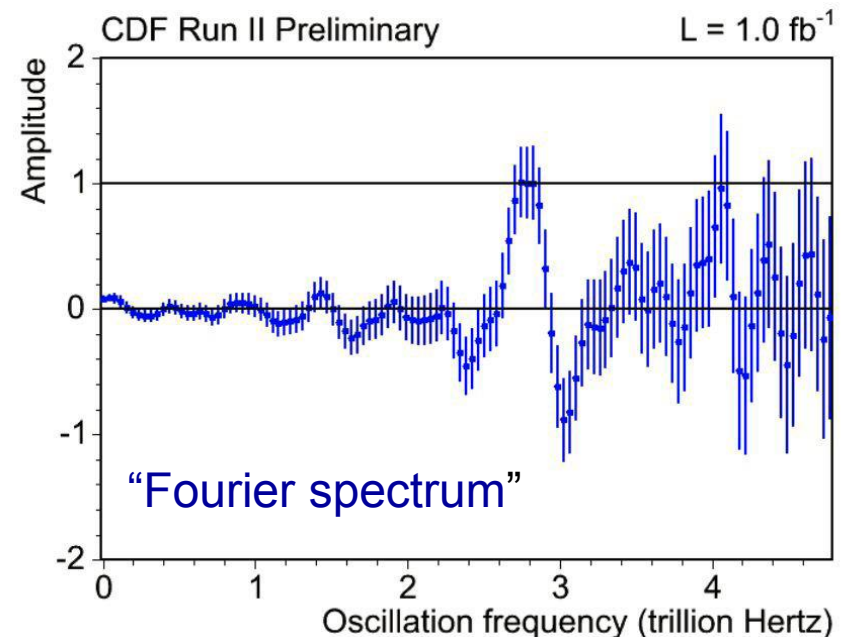
$$\Delta \Gamma_s = \Gamma_L - \Gamma_H$$

$$\phi_M = \arg(M_{12})$$

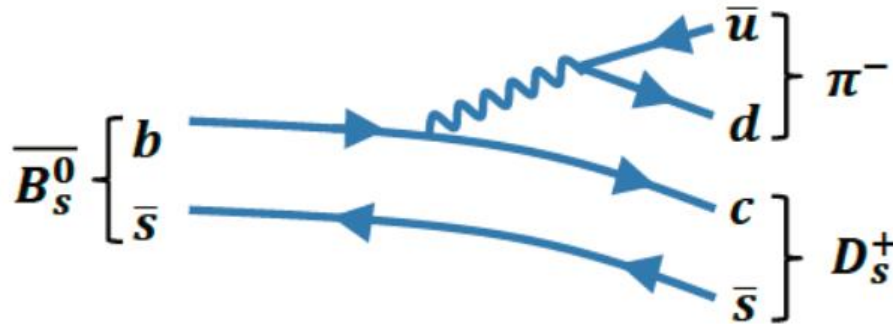
These oscillations were first observed at the Tevatron in 2006:

$$\Delta m_s = 17.77 \pm 0.10(\text{stat}) \pm 0.07(\text{sys}) \text{ ps}^{-1}$$

Now this measurement has been repeated with much better precision by LHCb

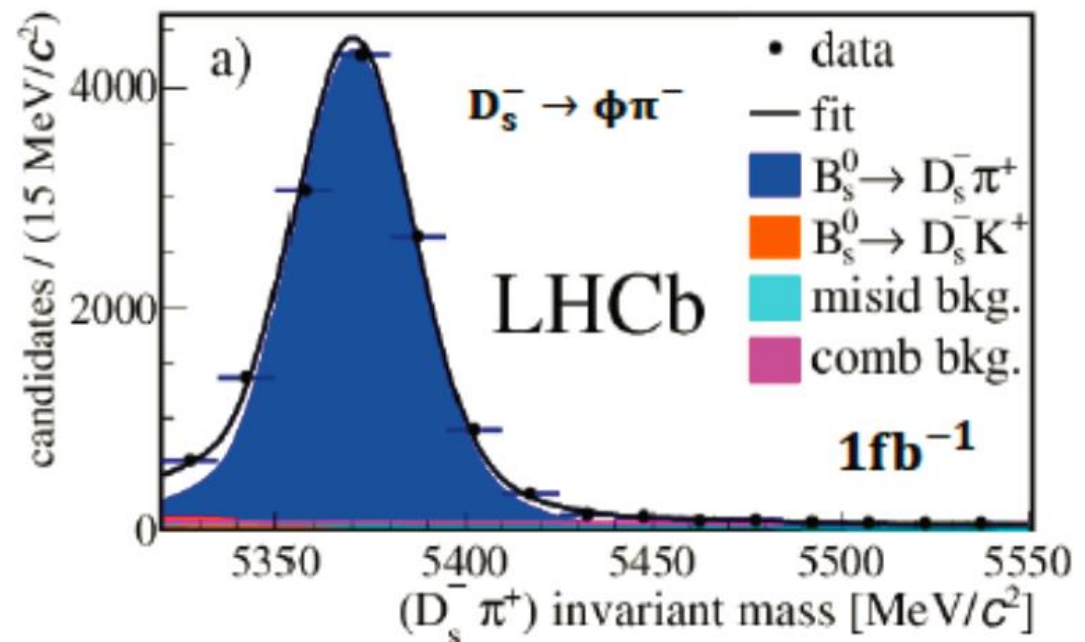


# LHCb: $\Delta m_s$ from $B_s \rightarrow D_s \pi$



- Very high statistics
- Low background level
- Can resolve  $B_s$  mixing frequency due to high boost

Use flavour tagging to determine flavour at production, pion charge for flavour at decay



# Flavour tagging at hadron colliders

Tagging efficiency

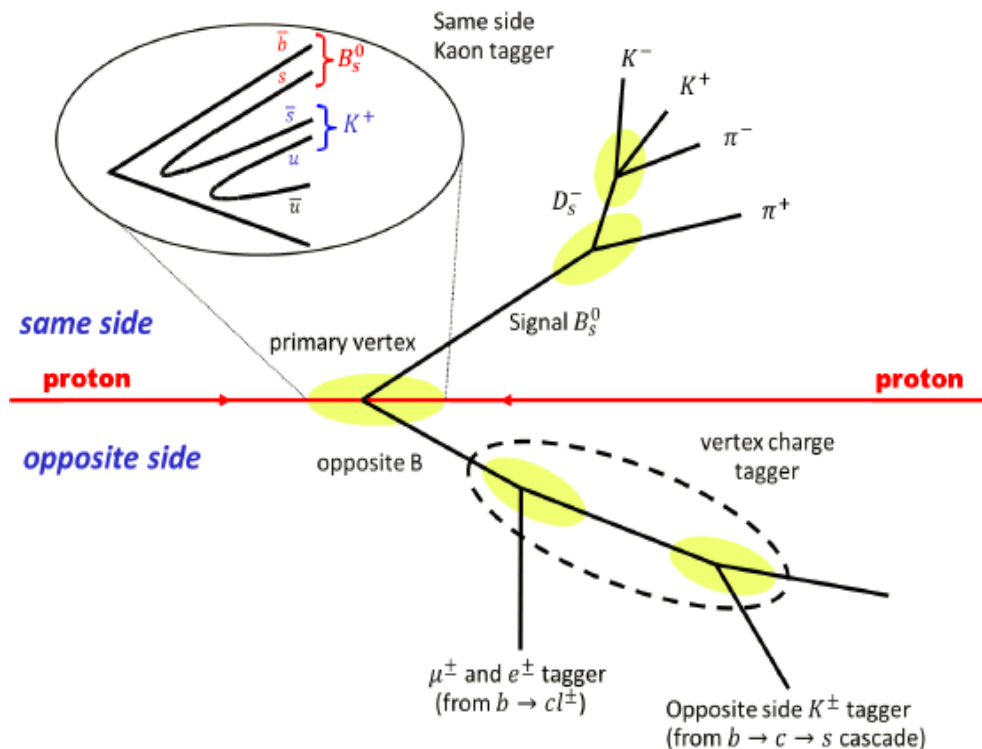
$$\varepsilon = \frac{\# \text{ tagged candidates}}{\# \text{ all candidates}}$$

Mistag probability

$$\omega = \frac{\# \text{ tagged wrong}}{\# \text{ tagged}}$$

Dilution

$$D = (1 - 2\omega)$$



- Opposite side taggers
  - exploits  $b\bar{b}$  pair production by partially reconstructing the second B-hadron in the event
- Same side kaon tagger
  - exploits hadronization of signal  $B_s$ -meson
- Combined tagging power (in  $B_s^0 \rightarrow D_s^- \pi^+$ )
  - $\varepsilon D^2 = 3.5 \pm 0.5\%$

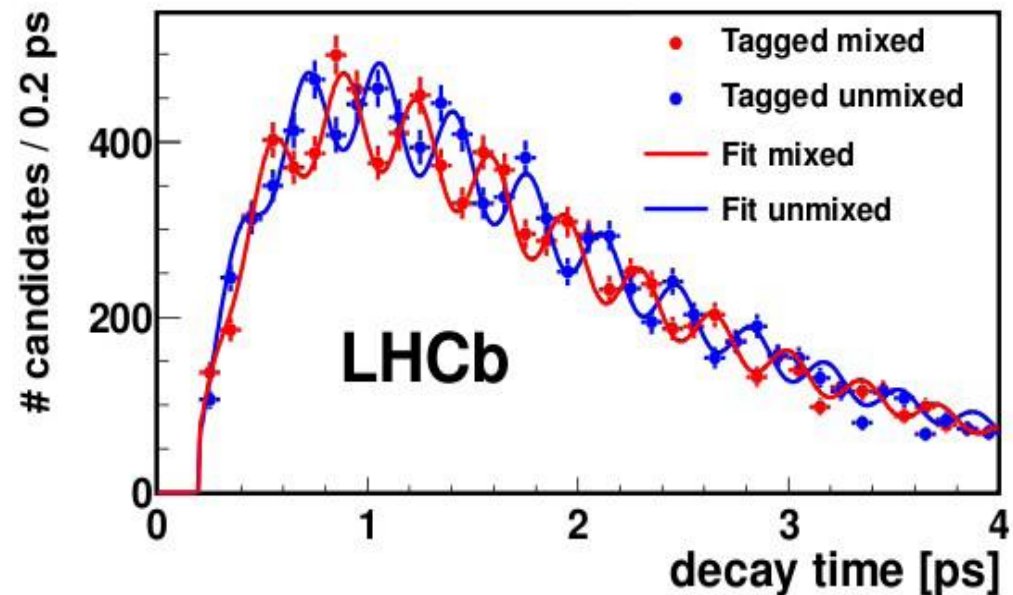
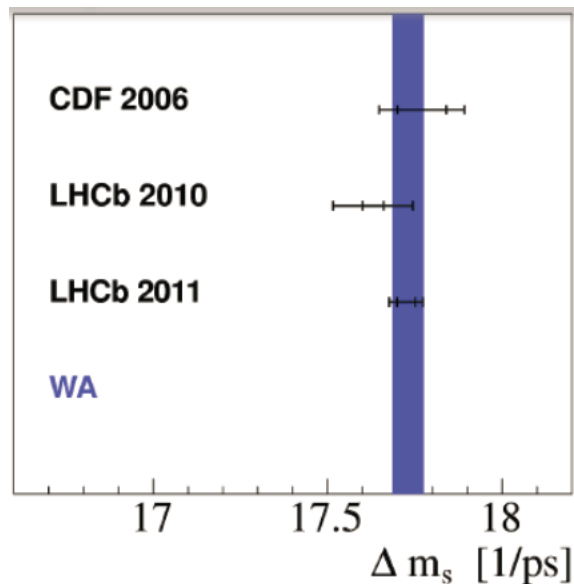
Compare this to  $e^+e^-$  colliders:  
 $\varepsilon D^2 \sim 30\%$

# LHCb: $\Delta m_s$ from $B_s \rightarrow D_s \pi$

What is needed to measure  $\Delta m_s$  ?

- Resolve the fast  $B_s$  oscillations ( $\rightarrow$  average decay time resolution  $\sim 45$  fs)
- Decays into flavour specific final state:  $B_s \rightarrow D_s \pi$  ( $\rightarrow$  high BR  $\sim 0.3\%$ )
- Tag the  $B_s$  flavour at production
  - $\rightarrow$  high efficiency and low mistag rate
  - $\rightarrow$  tagging power:  $\sim 4\%$

Most precise measurement of  $\Delta m_s$

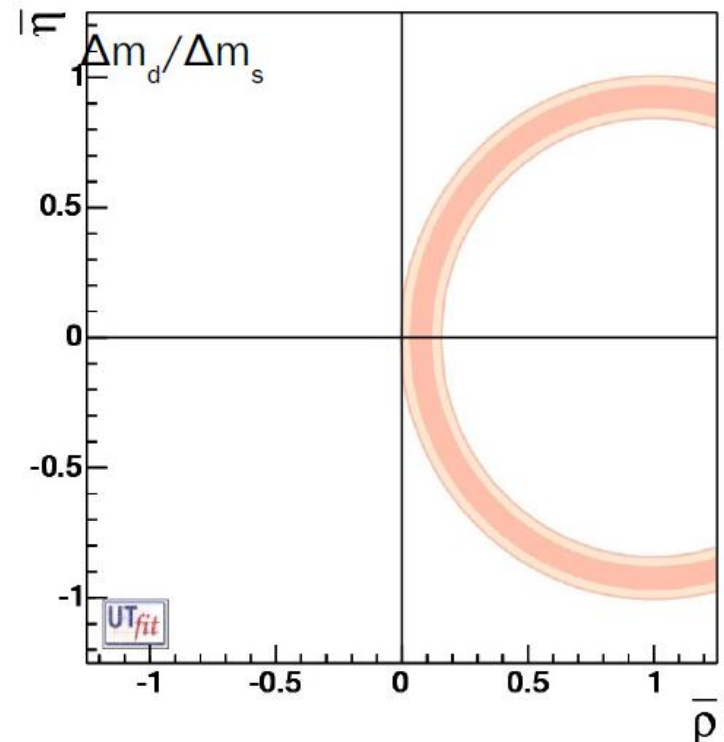
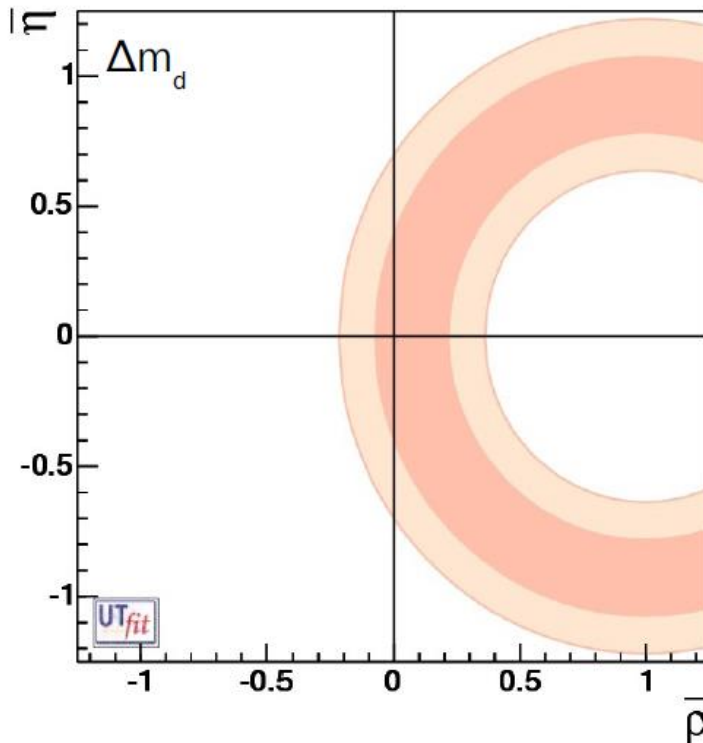


$$\Delta m_s = 17.768 \pm 0.023(stat) \pm 0.006(syst) ps^{-1}$$

# Constraints from mixing

- $\Delta m_d$  contains information on  $|V_{td}|$
- $\Delta m_d / \Delta m_s$  preferred since theoretically cleaner

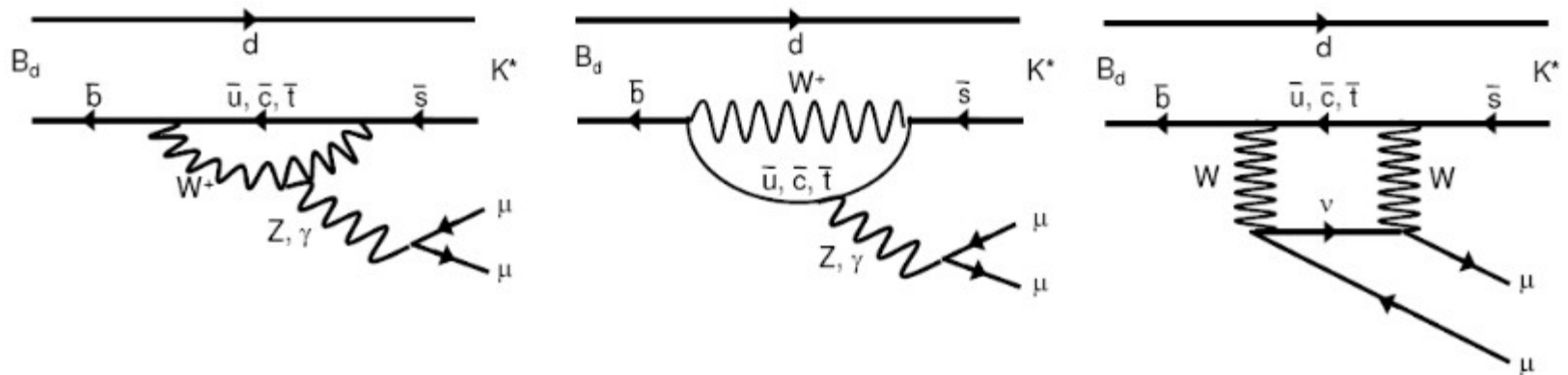
→ constraint on  $R_t = \left| \frac{V_{td} V_{tb}^*}{V_{cd} V_{cb}^*} \right|$



$\Delta F=1$ :  
Electroweak penguins

# $b \rightarrow s$ transitions

- $b \rightarrow s l^+ l^-$  processes also governed by FCNCs
  - rates and asymmetries of many exclusive processes sensitive to NP
- Golden  $\Delta F=1$  EW penguin decay:  $B_d \rightarrow K^{*0} \mu^+ \mu^-$ 
  - superb laboratory for NP tests
  - experimentally clean signature
  - many kinematic variables ...
  - with clean theoretical predictions (at least at low  $q^2$ )





# $b \rightarrow s$ transitions: theoretical framework

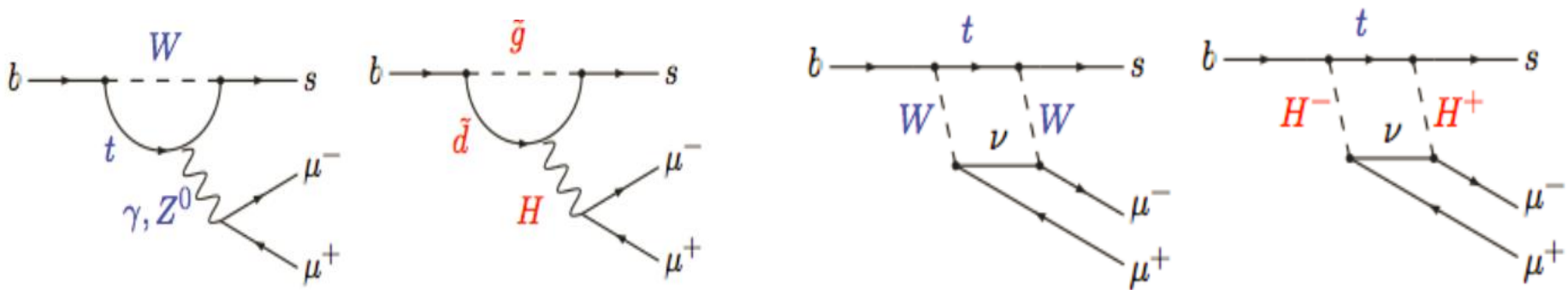
Describe  $b \rightarrow s$  transitions by an effective Hamiltonian

$$H_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i \left[ \underbrace{C_i(\mu) O_i(\mu)}_{\text{left-handed part}} + \underbrace{C'_i(\mu) O'_i(\mu)}_{\text{right-handed part suppressed in SM}} \right]$$

$i = 1, 2$	Tree
$i = 3 - 6, 8$	Gluon penguin
$i = 7$	Photon penguin
$i = 9, 10$	Electroweak penguin
$i = S$	Higgs (scalar) penguin
$i = P$	Pseudoscalar penguin

- long distance effects absorbed in the definition of the operators  $O_i$
- interesting short distance can be computed perturbatively in Wilson coefficients  $C_i$

$b \rightarrow s$  transitions are sensitive to:  $O_7(\prime)$ ,  $O_9(\prime)$ ,  $O_{10}(\prime)$

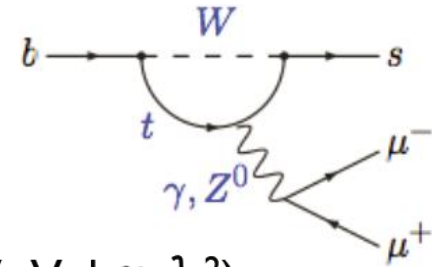


- $B^0 \rightarrow K^* \mu^+ \mu^-$  is the most prominent channel (large statistics & flavour specific)
- Studies with rarer  $B_s \rightarrow \phi \mu^+ \mu^-$ ,  $\Lambda_b^0 \rightarrow \Lambda \mu^+ \mu^-$ , ... have started

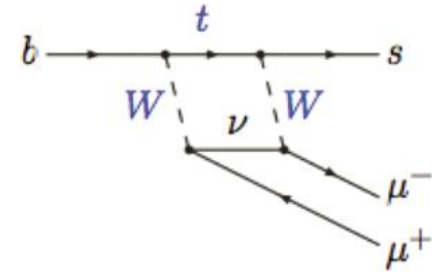
# $B^0 \rightarrow K^* \mu^+ \mu^-$ - angular analysis

- $B^0 \rightarrow K^* \mu^+ \mu^-$  is the golden mode to test new vector(-axial) couplings in  $b \rightarrow s$  transitions
- $K^* \rightarrow K \pi$  is self tagged, hence angular analysis ideal to test helicity structure
- Sensitivity to  $O_7$ ,  $O_9$  and  $O_{10}$  and their primed counterparts:

$$\begin{aligned}
 Q_7 &= \frac{e}{g^2} m_b \bar{s} \sigma^{\mu\nu} (1 + \gamma_5) F_{\mu\nu}^{-1} b \quad [\text{real or soft photon}] \\
 Q_9 &= \frac{e^2}{g^2} \bar{s} \gamma_\mu (1 - \gamma_5) b \bar{\ell} \gamma_\mu \ell \quad [b \rightarrow s \mu \mu \text{ via } Z/\text{hard } \gamma] \\
 Q_{10} &= \frac{e^2}{g^2} \bar{s} \gamma_\mu (1 - \gamma_5) b \bar{\ell} \gamma_\mu \gamma_5 \ell \quad [b \rightarrow s \mu \mu \text{ via } Z]
 \end{aligned}$$



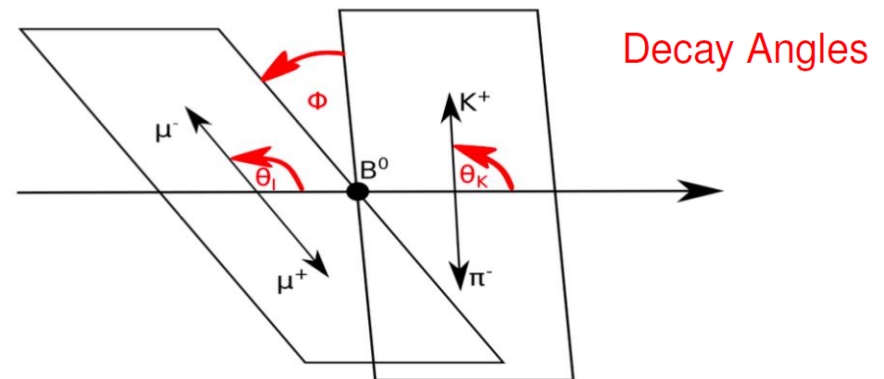
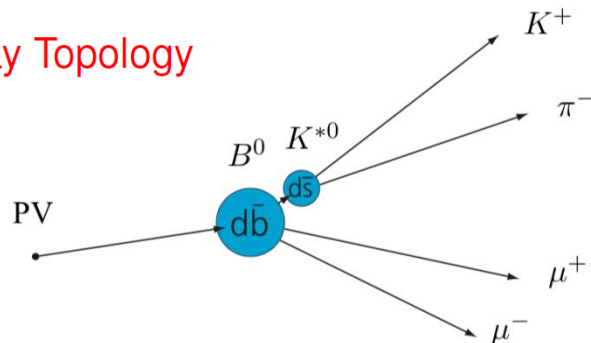
$b \rightarrow s$  ( $|V_{tb} V_{ts}| \propto \lambda^2$ )



Right-handed currents:  $1 - \gamma_5 \rightarrow 1 + \gamma_5$

## Decay topology

Decay Topology



# $B^0 \rightarrow K^* \mu^+ \mu^-$ - angular analysis

$B^0 \rightarrow K^* \mu^+ \mu^-$  full decay rate is given as differential decay distribution

$$\frac{1}{\Gamma} \frac{d^3(\Gamma + \bar{\Gamma})}{d \cos \theta_\ell d \cos \theta_K d\phi} = \frac{9}{32\pi} \left[ \frac{3}{4}(1 - F_L) \sin^2 \theta_K + F_L \cos^2 \theta_K + \frac{1}{4}(1 - F_L) \sin^2 \theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2 \theta_K \cos 2\theta_\ell + \right. \\ S_3 \sin^2 \theta_K \sin^2 \theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos \phi + \\ S_5 \sin 2\theta_K \sin \theta_\ell \cos \phi + S_6^s \sin^2 \theta_K \cos \theta_\ell + \\ S_7 \sin 2\theta_K \sin \theta_\ell \sin \phi + \\ \left. S_8 \sin 2\theta_K \sin 2\theta_\ell \sin \phi + S_9 \sin^2 \theta_K \sin^2 \theta_\ell \sin 2\phi \right]$$

- Experiments typically measure sub-set of these observables by integrating out some parts
- Classical observable measured for the FIRST time by LHCb
- Results from **B-factories** and **CDF** very much limited by the statistical uncertainty

# $B^0 \rightarrow K^* \mu^+ \mu^-$ - angular analysis

Folding technique ( $\phi \rightarrow \phi + \pi$ ) for  $\phi < 0$ , reduces the nr of parameters to fit to four

By exploiting symmetries:  
this form can be reduced to ...

$$\hat{\phi} = \begin{cases} \phi + \pi & \text{if } \phi < 0 \\ \phi & \text{otherwise} \end{cases}$$

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_K d\hat{\phi}} = \frac{9}{16\pi} \left[ \begin{aligned} & F_L \cos^2 \theta_K + \frac{3}{4}(1 - F_L)(1 - \cos^2 \theta_K) - \\ & F_L \cos^2 \theta_K (2 \cos^2 \theta_\ell - 1) + \\ & \frac{1}{4}(1 - F_L)(1 - \cos^2 \theta_K)(2 \cos^2 \theta_\ell - 1) + \\ & S_3(1 - \cos^2 \theta_K)(1 - \cos^2 \theta_\ell) \cos 2\hat{\phi} + \\ & \frac{4}{3} A_{FB}(1 - \cos^2 \theta_K) \cos \theta_\ell + \\ & A_9(1 - \cos^2 \theta_K)(1 - \cos^2 \theta_\ell) \sin 2\hat{\phi} \end{aligned} \right]$$

fraction of longitudinal polarisation of the  $K^*$

forward-backward asymmetry of the dilepton system

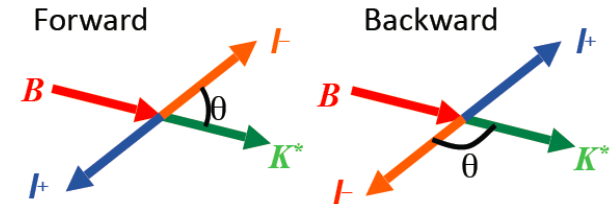
Simpler expression remains, sensitive to:  $F_L$ ,  $A_{FB}$ ,  $S_3$ ,  $A_9$

→ lost sensitivity to terms 4, 5, 7 and 8

# $B^0 \rightarrow K^* \mu^+ \mu^-$ - Forward-Backward asymmetry

Hadronic uncertainties under reasonable control for:

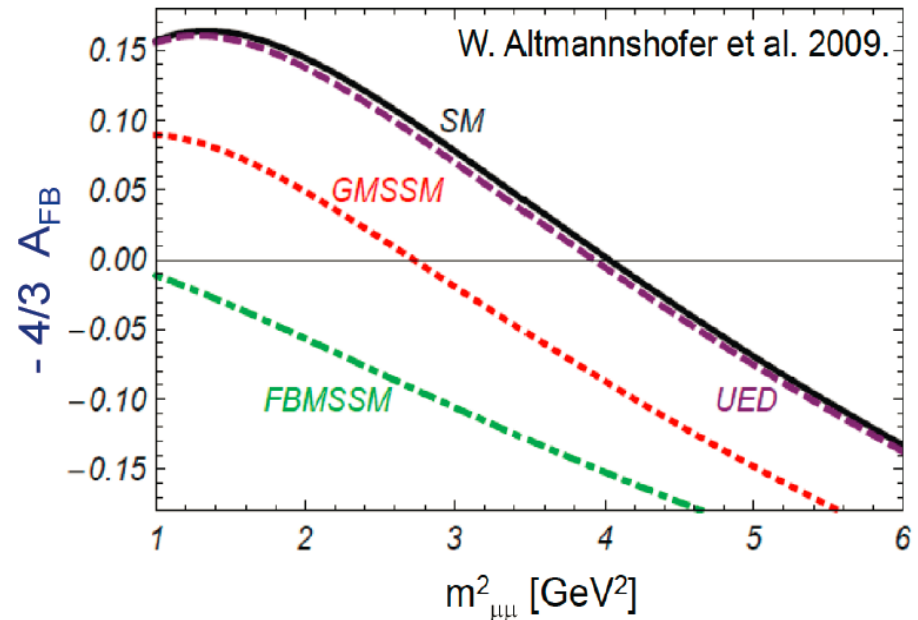
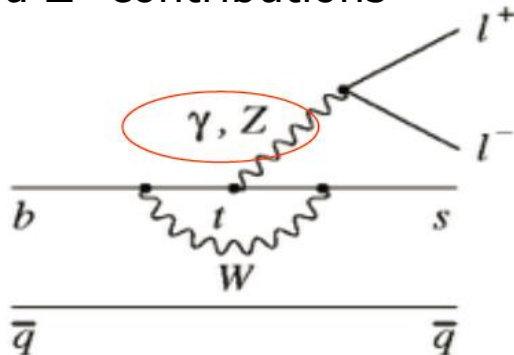
- $F_L$ : Fraction of  $K^*$  longitudinal polarization
- $A_{FB}$ : Forward-Backward asymmetry of lepton
- $S_3 \sim A_T^2 (1 - F_L)$ : Asymmetry in  $K^*$  transverse polarization



$A_{FB}$  zero crossing point particularly well predicted within the SM

$$A_{FB} \propto -\text{Re}[(2C_7^{eff} + \frac{q^2}{m_b^2} C_9^{eff}) C_{10}]$$

The SM forward-backward asymmetry in  $b \rightarrow s l^+ l^-$  arises from **interference** between  $\gamma$  and  $Z^0$  contributions



FBMSSM

Flavor Blind MSSM

GMSSM:

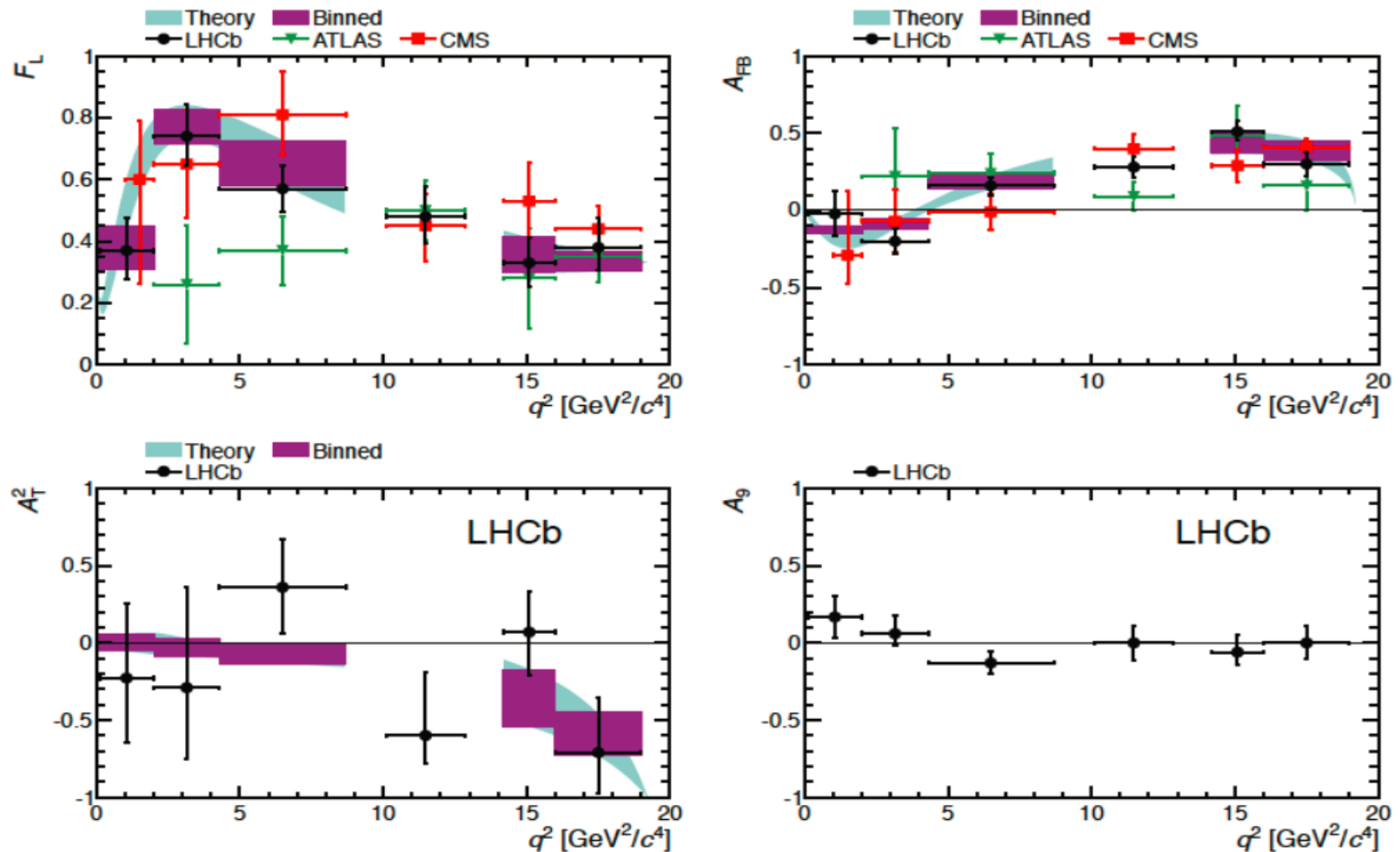
Non Minimal Flavor Violating MSSM

UED:

One universal extra dimension

# $B^0 \rightarrow K^* \mu^+ \mu^-$ - angular analysis results

Generally very good agreement with SM in the observables  $F_L$ ,  $A_{FB}$ ,  $S_3$ ,  $A_9$



LHCb 2012: First measurement of  $A_{FB}$  zero-crossing point:  $q_0 = 4.9 \pm 0.9 \text{ GeV}^2/c^4$

# $B^0 \rightarrow K^* \mu^+ \mu^-$ - angular analysis results

- Earlier we lost sensitivity to 4 terms to simplify the fit
- Now: extract the observables related to those terms!

Other folding techniques, applying different transforms, can give access to the rest of observables:

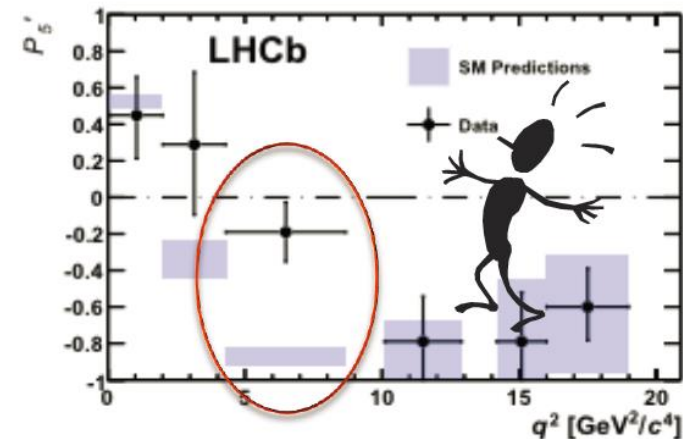
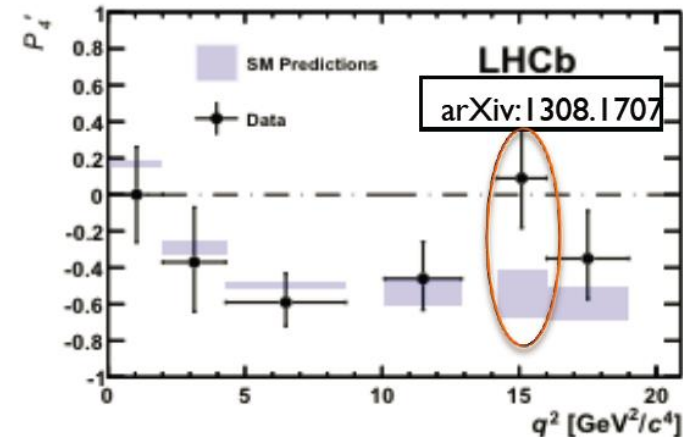
**S** - standard observables

**P** - theoretically cleaner observables

$$P'_{i=4,5,6,8} = \frac{S_{j=4,5,7,8}}{\sqrt{F_L(1 - F_L)}}$$

Local fluctuation in  $P'_5 > 3\sigma$  from the SM prediction has been observed

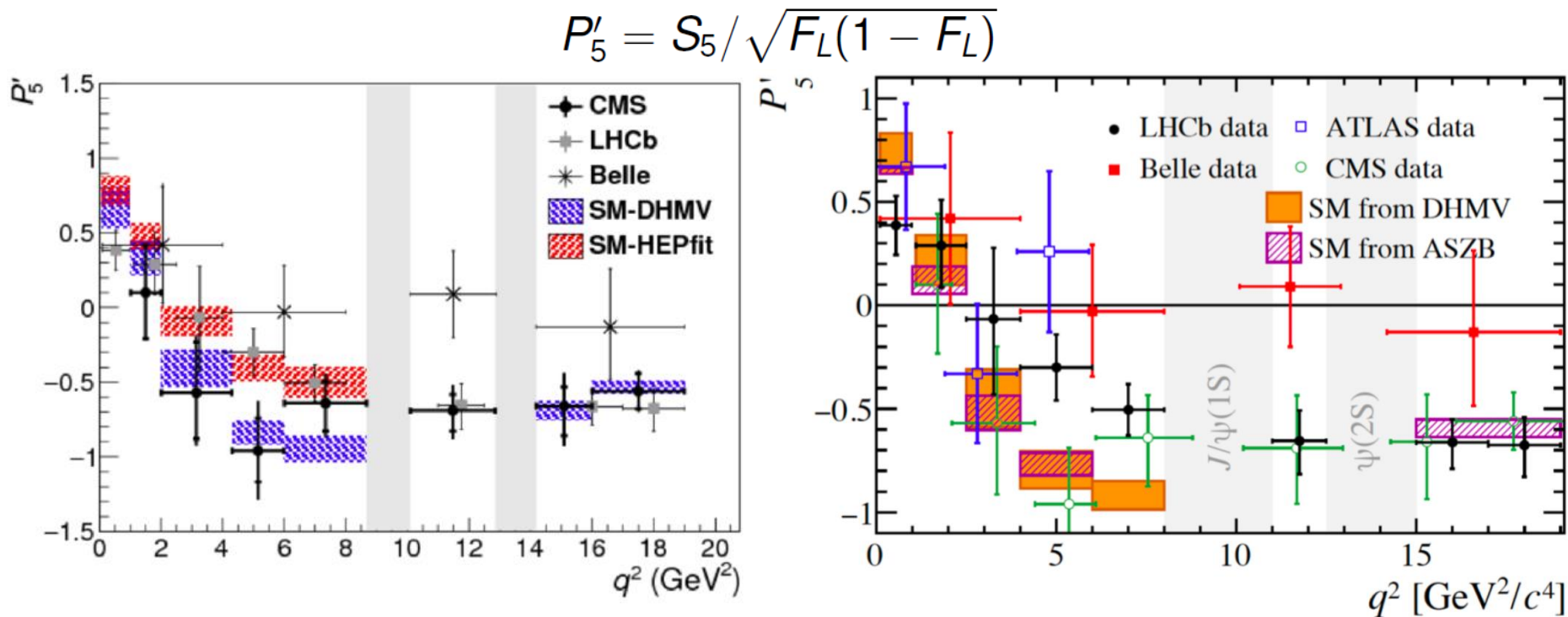
$P'_{4\phi}, S_{4\phi}$	$\begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \phi \rightarrow \pi - \phi & \text{for } \theta_\ell > \pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$
$P'_{5\phi}, S_{5\phi}$	$\begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$
$P'_{6\phi}, S_{7\phi}$	$\begin{cases} \phi \rightarrow \pi - \phi & \text{for } \phi > \pi/2 \\ \phi \rightarrow -\pi - \phi & \text{for } \phi < -\pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$
$P'_{8\phi}, S_{8\phi}$	$\begin{cases} \phi \rightarrow \pi - \phi & \text{for } \phi > \pi/2 \\ \phi \rightarrow -\pi - \phi & \text{for } \phi < -\pi/2 \\ \theta_K \rightarrow \pi - \theta_K & \text{for } \theta_\ell > \pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2. \end{cases}$





# $B^0 \rightarrow K^* \mu^+ \mu^-$ - angular analysis results

- LHCb performed first full angular analysis in 2016
  - extracted full set of CP-averaged angular terms and correlations
  - determined full set of CP-asymmetries

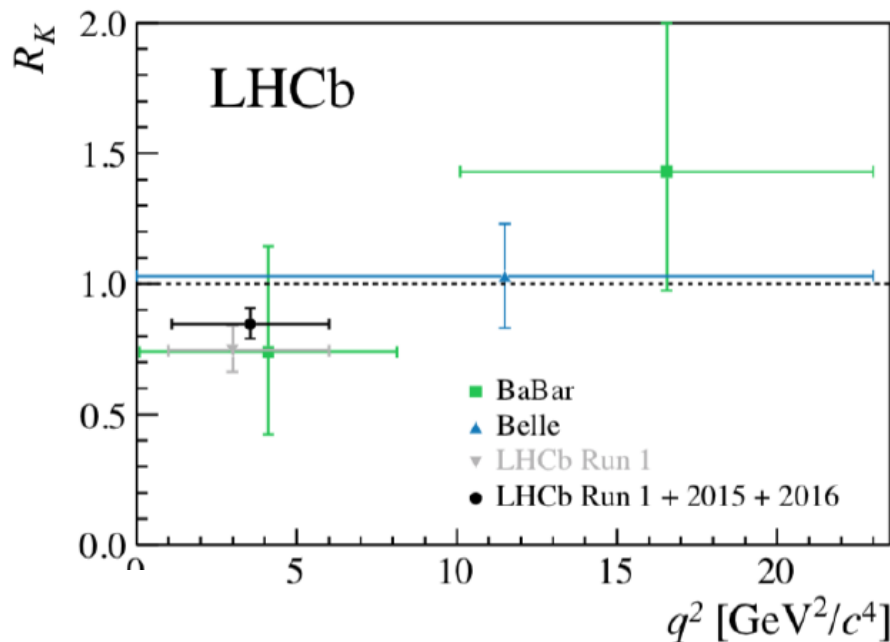


Differences with predictions based on the Standard Model at the level of 3.4 standard deviations



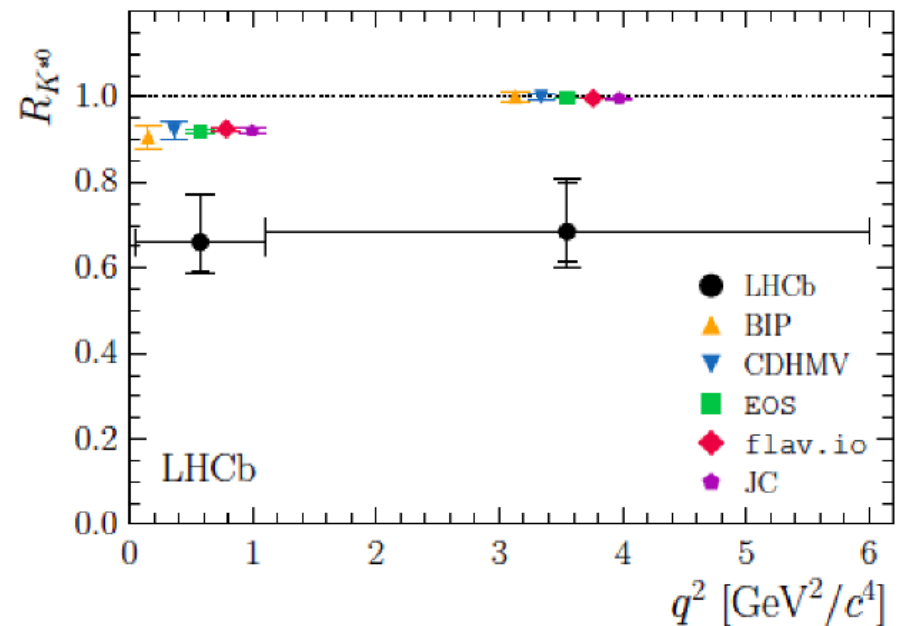
# Lepton flavour universality tests

- In SM couplings of the gauge bosons to leptons are independent of lepton flavour
- Ratios of the form:  $R_K = \frac{BR(B^+ \rightarrow K^+ \mu^+ \mu^-)}{BR(B^+ \rightarrow K^+ e^+ e^-)} \stackrel{\text{SM}}{\cong} 1$
- Free from QCD uncertainties that affect other observables
  - hadronic effects cancel, error is  $O(10^{-4})$
  - QED corrections can be  $O(10^{-2})$



**SM compatibility:**

**$\sim 2.5\sigma$  in  $1.1 < q^2 < 6.0 \text{ GeV}^2$**



**SM compatibility:**

**$\sim 2.2\sigma$  in low  $q^2$ ,  $\sim 2.5\sigma$  in central  $q^2$**

# Interpretation of the anomaly

- Most of measurements in good agreement with SM predictions
  - only a hint of disagreement in  $P_5'$  at low  $q^2$
- But, anyway: interesting local discrepancy in  $P_5'$ 
  - few others tensions less significant in other observables
- Possibly due to:
  - statistical fluctuation
  - SM theoretical prediction not fully correct  
(QCD effects not fully understood...)
- New Physics:
  - different value for some Wilson coefficients, e.g.  $C_9$ , or  $C_9$  and  $C_9'$ , including the possibility of  $Z'$  particle with a mass around few TeV

$\Delta F=1$ :  
Higgs penguins

# $B_s \rightarrow \mu^+ \mu^-$

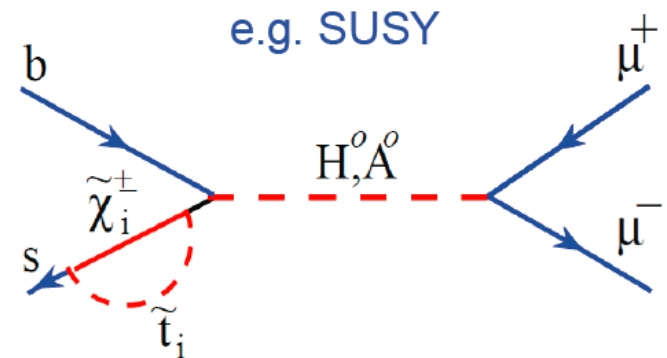
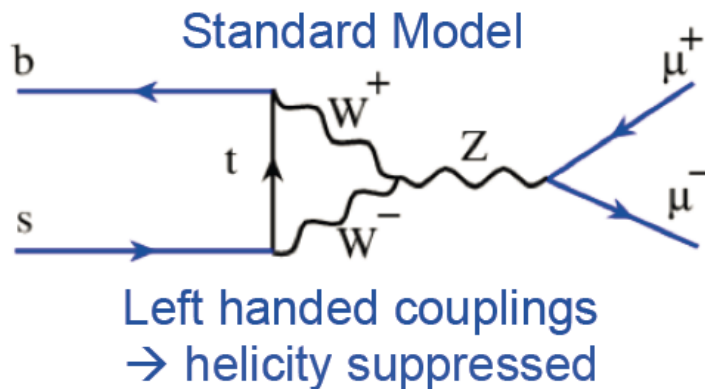
- Decay well predicted **theoretically**, and **experimentally** is exceptionally clean
- Within the SM**, the time-integrated predicted value is **very small**:

$$BR(B_s \rightarrow \mu^+ \mu^-)^{SM} = (3.3 \pm 0.3) \times 10^{-9}$$

- Huge NP enhancement ( $\tan\beta$  = ratio of Higgs vevs)

$$BR(B_s \rightarrow \mu^+ \mu^-)^{MSSM} \propto \tan^6 \beta / M_{A^0}^4$$

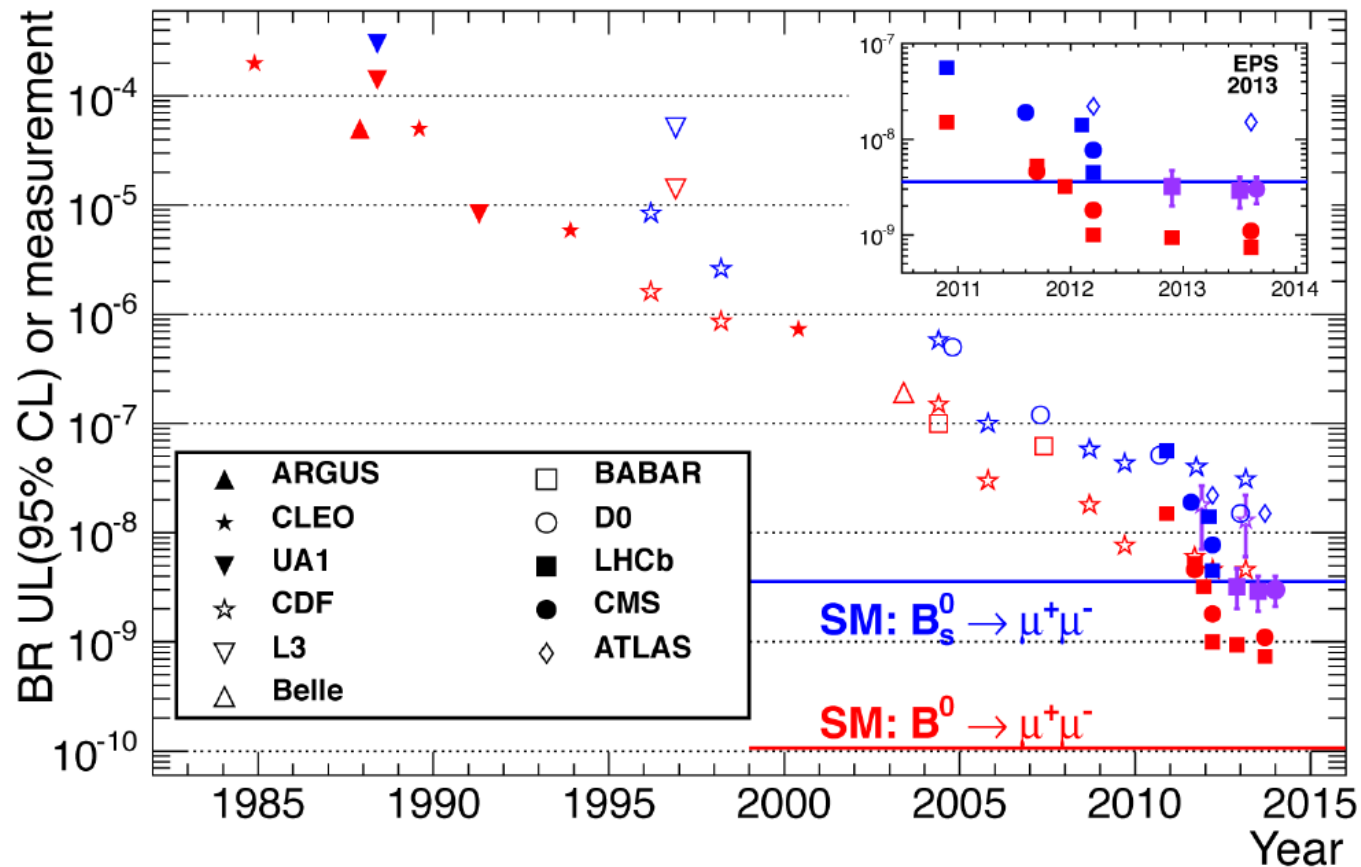
- Very **sensitive to an extended scalar sector** (e.g. extended Higgs, SUSY, etc.)
- Clean experimental signature**



**Killer for new physics discovery!**

$$B^0_{(s)} \rightarrow \mu^+ \mu^-$$

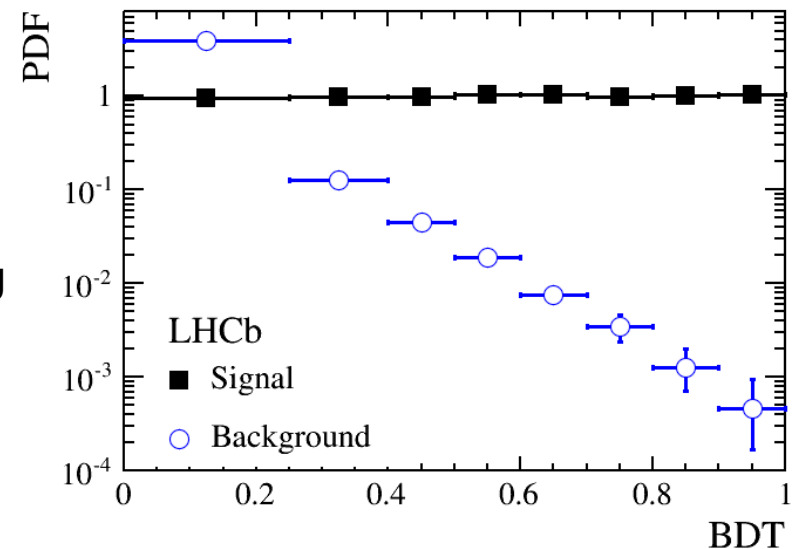
- It was considered one of the hottest channels for early NP discovery at LHC ( $B_d \rightarrow \mu^+ \mu^-$  also interesting...)



Searches over 30 years

# $B^0_{(s)} \rightarrow \mu^+\mu^-$ : analysis ingredients

- Produce a very large sample of B mesons
- Trigger efficiently on dimuon signatures
- Reject background
  - excellent vertex resolution (identify displaced vertex)
  - excellent mass resolution (identify B peak)
    - also essential to resolve  $B^0$  from  $B_s^0$  decays
  - powerful muon identification (reject background from B decays with misidentified pions)
  - typical to combine various discriminating variables into a multivariate classifier
    - e.g. Boosted Decision Trees algorithm

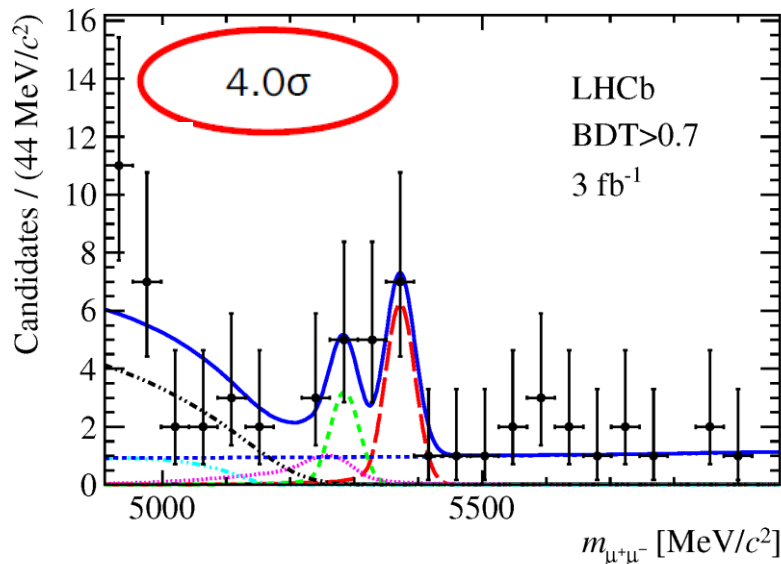


# $B_s \rightarrow \mu^+\mu^-$ : latest results from CMS & LHCb

Nov 2012: LHCb found the first evidence for  $B_s \rightarrow \mu^+\mu^-$  using  $2.1 \text{ fb}^{-1}$



- Update: full dataset:  $3 \text{ fb}^{-1}$ 
  - improved BDT
  - expected sensitivity:  $5.0\sigma$

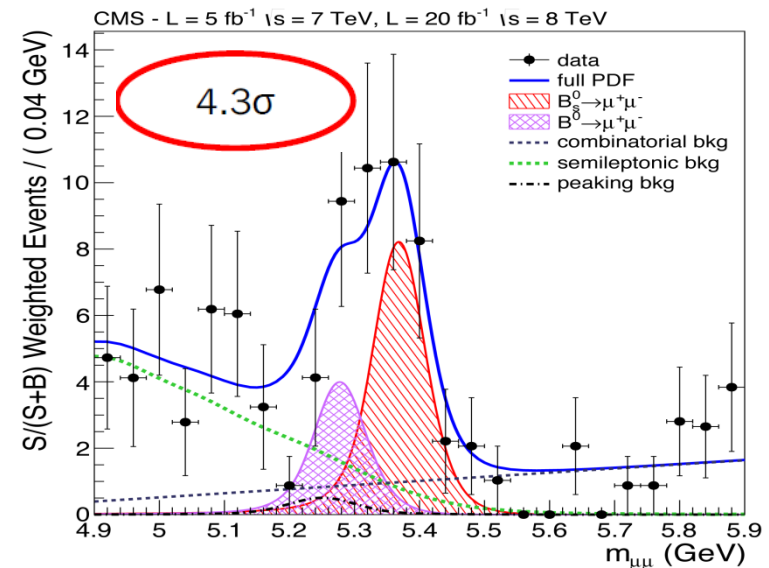


$$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) = (2.9_{-1.0}^{+1.1}) \times 10^{-9},$$

$$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-) = (3.7_{-2.1}^{+2.4}) \times 10^{-10}$$



- Update to  $25 \text{ fb}^{-1}$ 
  - cut based  $\rightarrow$  BDT based
  - improved variables
  - expected sensitivity:  $4.8\sigma$

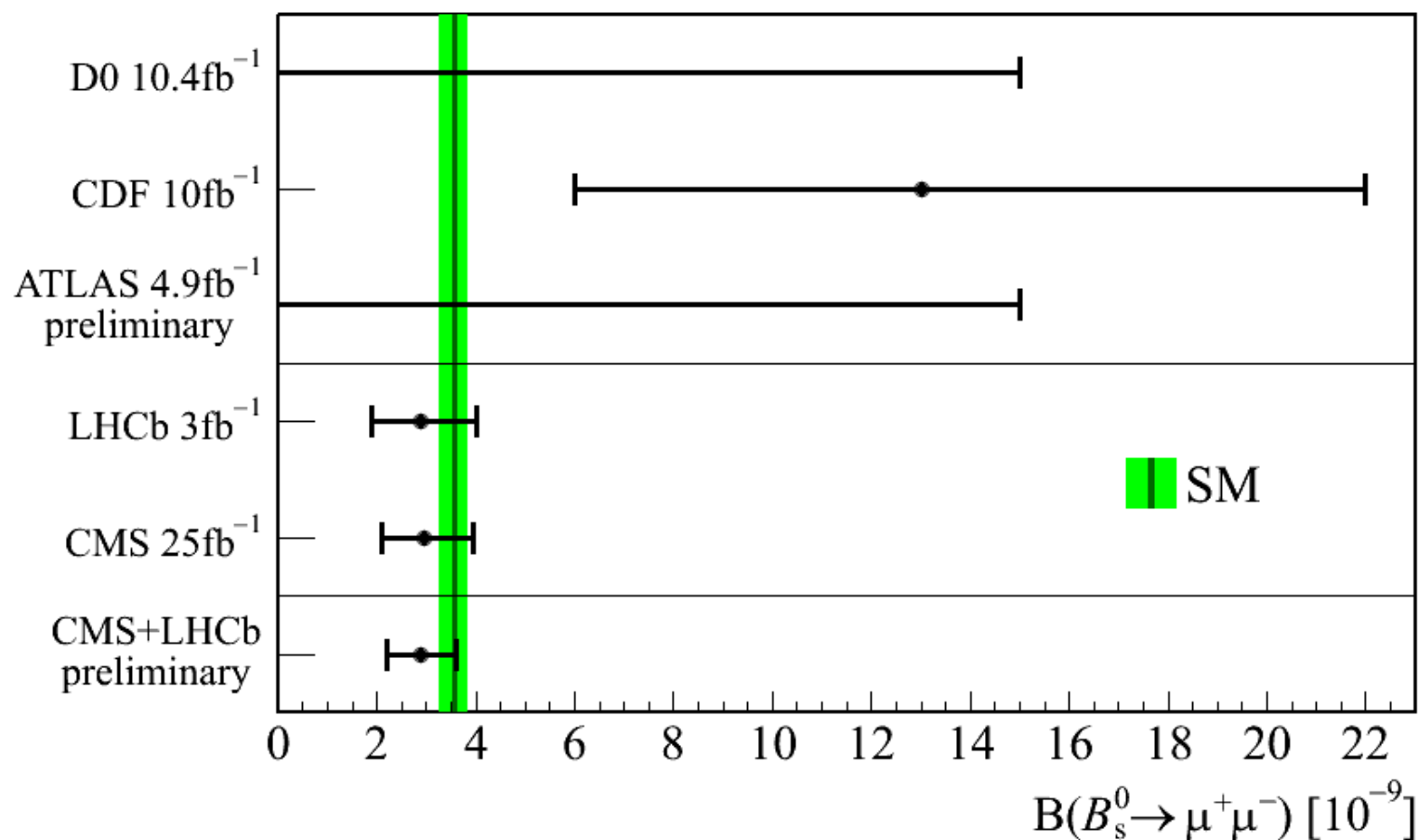


$$\mathcal{B}(B_s^0 \rightarrow \mu^+\mu^-) = (3.0_{-0.9}^{+1.0}) \times 10^{-9},$$

$$\mathcal{B}(B^0 \rightarrow \mu^+\mu^-) = (3.5_{-1.8}^{+2.1}) \times 10^{-10}$$

# $B_s \rightarrow \mu^+\mu^-$ : combined LHCb + CMS result

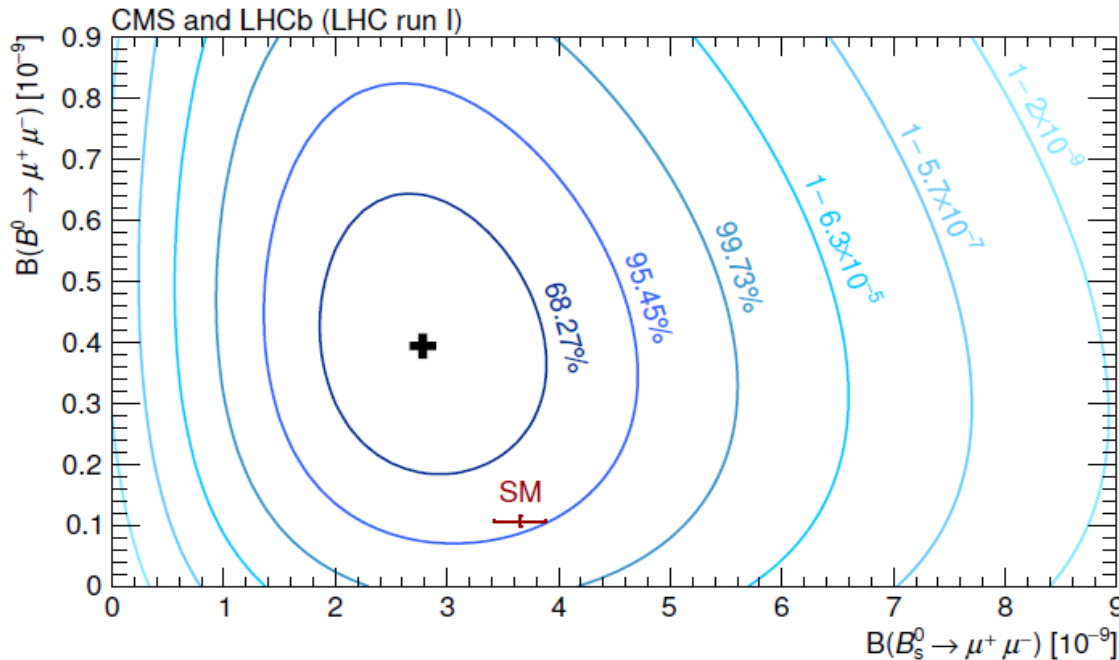
$$B(B_s^0 \rightarrow \mu^+\mu^-) = (2.9 \pm 0.7) \times 10^{-9}$$





# Implications of $B_s \rightarrow \mu^+\mu^-$

The measured BR is compatible with the SM prediction



**Strong constraints on many  
New Physics models**

→ together with direct  
searches:

**constrained MSSM  
models (almost) excluded**

Important key measurements:

- ratio of decay rates of  $B^0 \rightarrow \mu^+\mu^-$  /  $B_s \rightarrow \mu^+\mu^-$   
→ allows e.g. to test of „Minimal Flavour Violation” hypothesis
- lifetime of  $B_s \rightarrow \mu^+\mu^-$   
→ new, theoretically clean observable that is largely unconstrained