# Heavy flavour physics

# Lecture 1

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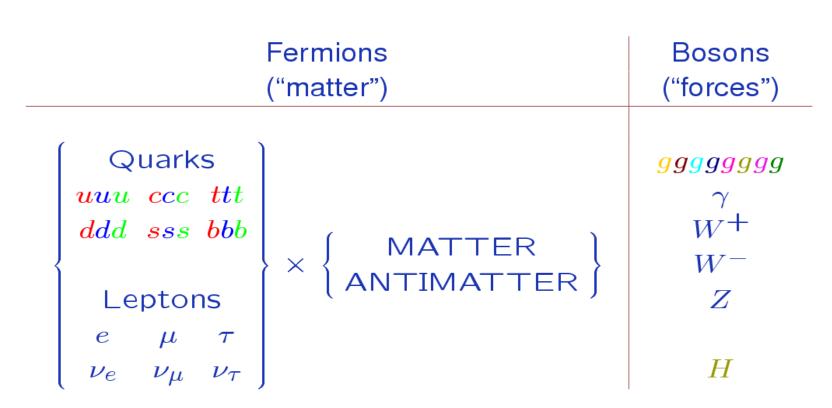
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# Contents

### Lecture 1

- What is flavour physics
- CKM mechanism
- SM flavour sector
- Flavour sector beyond the SM

# What is flavour physics?



### Flavour physics:

- transitions between different kinds of quarks
- its all about weak interactions...
- strong interactions as a "background"

# Parameters of the Standard Model

- 3 gauge couplings:  $\alpha_{EM}$ ,  $\alpha_{weak}$ ,  $\alpha_{strong}$
- 2 Higgs parameters: v, m<sub>H</sub>
- 6 quark masses:
- 3 quark mixing angles + 1 phase (CKM matrix)
- 3 (+3) lepton masses
- (3 lepton mixing angles + 1 phase) (PMNS matrix)

() = with Dirac neutrino masses

# Open questions in flavour physics

- Why are there so many different fermions?
- What is responsible for their organisation into generations / families?
- Why are there 3 generations / families each of quarks and leptons?
- Why are there flavour symmetries?
- What breaks the flavour symmetries?
- What causes matter-antimatter asymmetry?

# Flavour physics issues

### Families / generations

3 pairs of quarks	(are we sure?)

3 pairs of leptons (are we sure?)

### Hierarchies

m(t) > m(c) > m(u) m(b) > m(s) > m(d)

 $m(\tau) > m(\mu) > m(e)$ 

m(b) > m(s) > m(d) $m(v_{\tau}) > m(v_{u}) > m(v_{e}) ?$ 

### **Mixings & couplings**

hierarchy in quark mixings

what about lepton mixings?

### Mixings & couplings

universality

(no) flavour changing neutral currents (at tree level in the Standard Model)

### Symmetry principles & their violation

P violation / C violation

CP violation / T violation

baryon asymmetry of the universe

lepton flavour violation

### Unification

# Why is heavy flavour physics interesting?

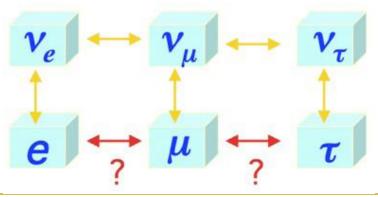
- Hope to learn something about the mysteries of the flavour structure of the Standard Model
- CP violation and its connection to the matter–antimatter asymmetry of the Universe
- Discovery potential far beyond the energy frontier via searches for rare or SM forbidden processes

# What breaks the flavour symmetries?

- In the Standard Model, the vacuum expectation value of the Higgs field breaks the electroweak symmetry
- Fermion masses arise from the Yukawa couplings of the quarks and charged leptons to the Higgs field (taking  $m_v = 0$ )
- The CKM matrix arises from the difference between weak eigenstates and mass eigenstates
- Consequently, the only flavour-changing interactions are the charged current weak interactions
  - → no flavour-changing neutral currents (GIM mechanism)
  - $\rightarrow$  not generically true in most extensions of the SM
  - $\rightarrow$  flavour-changing processes provide sensitive tests

# Lepton flavour violation

- No right-handed neutrinos in the SM, implies they are massless
  - $\rightarrow$  neutrinos only left-handed (chirality)
  - $\rightarrow$  antineutrinos only right-handed (chirality)
- Neutrino oscillations show they have small but finite masses
  - $\rightarrow$  where are the right-handed neutrinos?
  - $\rightarrow$  charged lepton flavour violation
  - $\rightarrow$  physics beyond the Standard Model
- Why do we not observe the decay  $\mu \rightarrow e\gamma$ ?
  - $\rightarrow$  exact (but accidental) lepton flavour conservation in the SM with  $m_{_{\!\rm V}}{=}0$
  - $\rightarrow$  SM loop contributions suppressed by  $(m_v / m_W)^4$
  - $\rightarrow$  LFV a mechanism beyond the SM needed



# What causes matter-antimatter asymmetry?

• The CKM matrix arises from the relative misalignment of the Yukawa matrices for the up- and down-type quarks

$$V_{CKM} = U_u U_d^+$$

(U - diagonalisation of mass matrices)

- It is a 3x3 complex unitary matrix
  - $\rightarrow$  described by 9 (real) parameters
  - $\rightarrow$  5 can be absorbed as phase differences between the quark fields
  - $\rightarrow$  3 can be expressed as (Euler) mixing angles
  - $\rightarrow$  the fourth makes the CKM matrix complex (i.e. gives it a phase)
    - weak interaction couplings differ for quarks and antiquarks
    - CP violation

# Reminder - 1964: CP violation

Both  $K^0 \rightarrow \pi\pi$  and anti- $K^0 \rightarrow \pi\pi$  occur

– K<sup>0</sup> may turn into its antiparticle, so are not mass eigenstates
 The mass eigenstates are:

$$|K_S^0\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle + |\bar{K}^0\rangle)$$
$$|K_L^0\rangle = \frac{1}{\sqrt{2}}(|K^0\rangle - |\bar{K}^0\rangle)$$

CP operator gives:

$$\mathbf{CP}|K^{0}\rangle = |\bar{K}^{0}\rangle, \mathbf{CP}|K_{S}\rangle = +|\bar{K}_{S}\rangle, \mathbf{CP}|K_{L}\rangle = -|\bar{K}_{L}\rangle$$

Thus:

only 
$$K_S \to \pi \pi$$
, but  $K_L \to 3\pi$ 

### **Under CP symmetry:**

 $K_S(CP=+1)$ : can only decay (hadronically) to  $2\pi$ 's (CP=+1)

 $K_L$ (CP=-1): can only decay (hadronically) to  $3\pi$ 's (CP=-1)

If CP conserved, should not see the decay  $K_L\!\to 2\pi's$ 

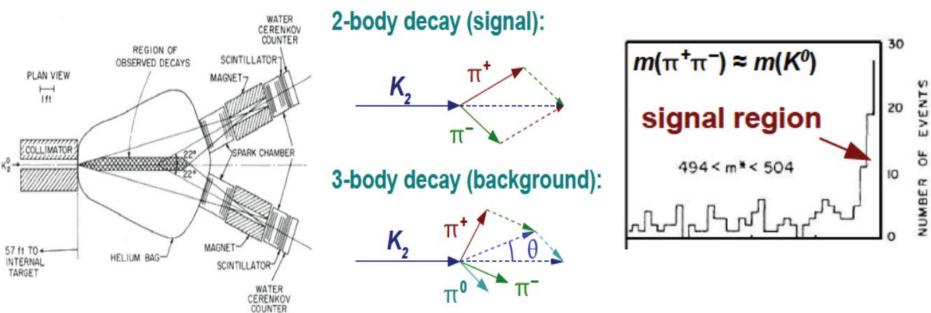
# Reminder - Cronin-Fitch experiment

**Observation of K<sub>2</sub>\rightarrow\pi^+\pi^-**  $\rightarrow$  Christenson, Cronin, Fitch, Turlay (1964)

The experiment shoot protons on a target to produce  $K^0$ , after a long enough trip in a vacuum pipe, they achieved a pure  $K_2$  beam.

Experimentally use invariant mass (energy conservation) and angle between  $K_2$  and  $\pi^+\pi^-$  (momentum conservation).

Find excess of ~56 events in the signal region:  $BF(K_2 \rightarrow \pi^+\pi^-) \sim 2 \times 10^{-3}$ 



 $\rightarrow$  CP violation!

# Reminder - 1963: Cabibbo mixing

### The weak coupling did not look to be universal:

$$s 
ightarrow u$$
 e.g.  $K^+ 
ightarrow \mu^+ v_\mu$ 

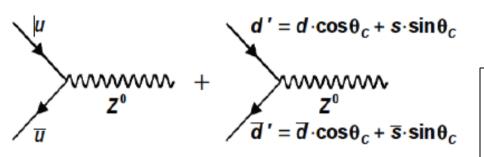
 $d \rightarrow u \quad \text{ e.g. } \quad \pi^+ \rightarrow \mu^+ v_\mu$ 

 $s \rightarrow u$  transitions suppressed by a factor  ${\sim}20$ 

$$\frac{\text{Pion decay}}{\pi^{-} \left\{ \begin{array}{c} d \\ \overline{u} \end{array} \right\} \xrightarrow{W^{-}} \\ \pi^{-} \left\{ \begin{array}{c} d \\ \overline{u} \end{array} \right\} \xrightarrow{W^{-}} \\ \pi^{-} \left\{ \begin{array}{c} d \\ \overline{u} \end{array} \right\} \xrightarrow{W^{-}} \\ \mu^{-} \end{array} \right\}$$

 $\mathbf{d'} = \mathbf{d} \cdot \cos \theta_{\rm c} + \mathbf{s} \cdot \sin \theta_{\rm c}$ 

 $\sin \theta_c = 0.22$  (empirically)



But, if the neutral weak currents also couples to d' expect large FCNC

 $K^{-}(s\bar{u}) \rightarrow \mu^{-} + \bar{v}_{\mu}$ 

Kaon decay

Experimentally, however, BR(K $\rightarrow$ µµ) ~ 7x10<sup>-9</sup>

# Reminder - 1970: GIM mechanism

$$\begin{split} &\mathsf{K}^+ \to \mu^+ v_\mu & \text{so why not} & \mathsf{K}^0 \to \mu^+ \mu^- \ ? \\ &\mathsf{K}^+ \to \pi^0 \mu^+ v_\mu & \text{so why not} & \mathsf{K}^0 \to \pi^0 \mu^+ \mu^- \ ? \\ &\mathsf{BR}(\mathsf{K}_L \to \mu^+ \mu^-) \sim 7 \cdot 10^{-9} & \mathsf{BR}(\mathsf{K}_L \to e^+ e^-) \sim 10^{-11} \\ &\mathsf{BR}(\mathsf{K}^0 \to \pi^0 \mu^+ \mu^-) < \sim 10^{-10} \end{split}$$

### GIM (Glashow, Iliopoulos, Maiani) mechanism (1970)

assume a **new (not yet observed) quark** in SU(2) quark doublets

no tree level flavour changing neutral currents

suppression of FCNC via loops

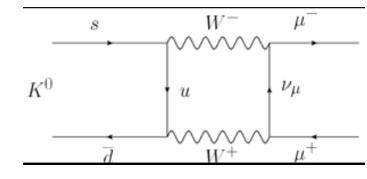
Requires that quarks come in pairs (doublets)

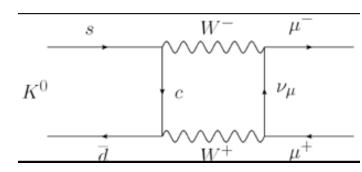
prediction of a **2nd** up-type quark

additional Feynman graph cancels the "u-box graph"

prediction of m(c)  $\approx$  1.5 GeV

 $\rightarrow$  Gaillard and Lee (1974)

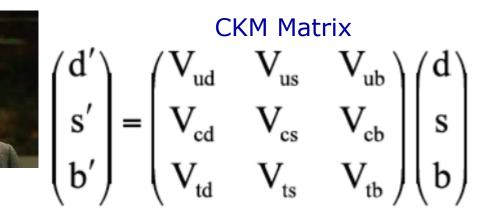




# Reminder - 1973: The CKM mechanism

1973: **Kobayashi & Maskawa** demonstrate that CP violation arises naturally from quark mixing if there are **3 generations of quarks** 







### **3x3 matrix of complex numbers**

- $\Rightarrow$  18 parameters
- unitary  $\Rightarrow$  9 parameters
- quark fields absorb unobservable phases  $\Rightarrow$  4 parameters

### 3 mixing angles and 1 phase allowing for CP violation

## Matter-antimatter asymmetry



- We know that the matter anti-matter symmetry in the Universe is broken: the Universe consists of matter.
- But, shortly after the Big Bang, there should have been equal amounts of matter and anti-matter

 $\rightarrow$  how did the Universe develop a preference of matter?

In 1966, Andrei Sakharov showed that necessary for evolution of matter dominated universe, from symmetric initial state, are:

- (1) baryon number violation
- (2) C & CP violation
- (3) thermal inequilibrium
- No significant amounts of antimatter observed!
- (N(baryon) N(antibaryon)) /  $N_v \sim 10^{-10}$



Standard Model CPV cannot explain matter asymmetry in the universe  $\rightarrow$  the only CP violating phase in SM leads to 10<sup>-17</sup>  $\Delta N_B/N_\gamma$ 

# SM flavour sector

# Flavour in Standard Model

- Higgs field was introduced to give masses to  $W^+$ ,  $W^-$  and  $Z^0$  bosons (after SBB)
- Since we have a Higgs field we can add (ad-hoc) interactions between the Higgs field φ and the fermions in a gauge invariant way (Yukawa couplings):

$$-L_{Yukawa} = Y_{ij} \begin{pmatrix} \downarrow & \downarrow & \text{singlet} \\ \psi_{Li} & \phi \end{pmatrix} \psi_{Rj} + h.c.$$

- The quark flavour structure within the SM is described by 6 couplings and 4 CKM params
- It is convenient to move the CKM matrix from Yukawa sector to the weak current sector
- We can diagonalize the  $Y_{ij}$  matrices, such that we arrive in the "mass basis"

However, then the Lagrangian of the charged weak current should also be rewritten:

$$-L_{W^{+}} = \frac{g}{\sqrt{2}} \left(\overline{u}, \overline{c}, \overline{t}\right)_{L} \left(V_{CKM}\right) \left(\begin{array}{c}d\\s\\b\end{array}\right)_{L} \gamma^{\mu} W_{\mu}^{+}$$
CKM matrix (rotation matrix)

 $V_{CKM}$  originates from the diagonalization of the Yukawa couplings

# Weak interactions in the SM

• After SSB, the charged current of a  $W^-$  exchange can be written as:

$$J^{\mu-} = (\overline{u}_L, \overline{c}_L, \overline{t}_L) \gamma^{\mu} V_{\text{CKM}} \begin{pmatrix} d_L \\ s_L \\ b_L \end{pmatrix}$$

- Weak interaction only couples to left-handed field
  - $\rightarrow$  left-handed quarks or right-handed anti-quarks
  - $\rightarrow$  manifestly violates parity

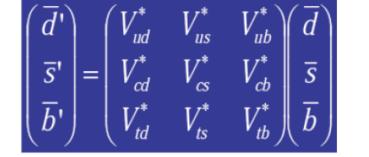
The weak eigenstates are related to the mass eigenstates by the CKM matrix:

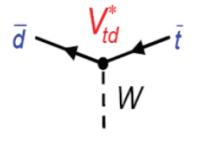
$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = V_{\rm CKM} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$
  
Weak eigenstates Mass eigenstates

# CP transformation & the weak interaction

Quarks

Anti-quarks:





CP

### CP violation requires complex matrix elements

### **Relative phases**

### Q: How many parameters does the CKM matrix have?

9 unitary conditions:  $V_{CKM} V_{CKM}^{\dagger} = 1$ 5 relative phases of the quark fields 4 parameters (\*)

(\*) 3 (real) Euler angles and 1 phase (single source of CP violation in the SM)

- with 2 generations there is only one real (Euler) angle: the Cabbibo angle
- CP violation requires 3 generations!

18 parameters (9 complex numbers):

When I do a phase transformation of the (left-handed) quark fields:

$$u_{Lj} \rightarrow e^{i\phi_j} u_{Lj} \qquad d_{Lk} \rightarrow e^{i\phi_k} d_{Lk}$$

And a simultaneous transformation of the CKM matrix:

$$V \rightarrow \begin{pmatrix} e^{-i\phi_{u}} & & \\ & e^{-i\phi_{c}} & \\ & & e^{-i\phi_{c}} & \\ & & & e^{-i\phi_{t}} \end{pmatrix} \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} e^{-i\phi_{d}} & & \\ & e^{-i\phi_{s}} & \\ & & e^{-i\phi_{s}} & \\ & & & e^{-i\phi_{b}} \end{pmatrix}$$

 $\int_{\phi_b} \text{ or } V_{jk} \rightarrow \exp\left(-i\left(\phi_j + \phi_k\right)\right) V_{jk}$ There are only 5

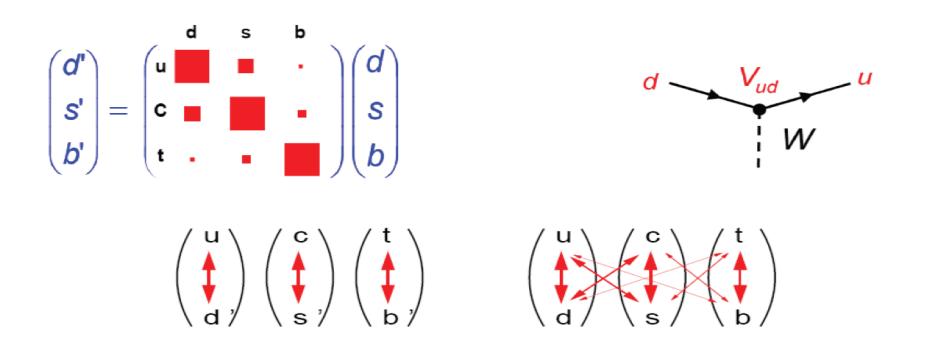
The charged current (i.e. the physics) remains invariant:

$$J^{\mu}_{CC} = u_{Li} \gamma^{\mu} V_{ij} d_{Lj}$$

There are only 5 relative phases (+ one overall phase) U d d C s b t

In other words, I can always absorb the 5 relative phases by redefining the quark fields  $\rightarrow$  **these 5 phases are unobservable** 

# Hierarchy in quark mixing



- Diagonal elements of CKM matrix are close to one
- Only small off-diagonal contributions
- Mixing between quark families is "CKM suppressed"

# Wolfenstein parametrization

Makes use of the fact that the off-diagonal elements are small compared to the diagonal elements

 $\rightarrow$  expansion in  $\lambda$   $\approx$   $V_{us}\text{,}$  A  $\approx$   $V_{cb}\text{ / }\lambda^2$  and  $\rho,$   $\eta$ 

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} \lambda \sim 0.22 \ (=\sin\theta_c, \ sine \ of \ Cabibbo \ angle) \\ A \sim 1 \ (actually \ 0.80) \\ \rho \sim 0.14 \\ \eta \sim 0.34 \end{pmatrix}$$
$$= \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix} + \mathcal{O}(\lambda^4)$$
$$\lambda^2 \equiv \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2} \qquad A^2\lambda^4 \equiv \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2} \qquad \bar{\rho} + i\bar{\eta} = -\frac{V_{ud}V_{ub}^*}{V_{cd}V_{cb}^*} \\ \rho + i\eta = \frac{\sqrt{1 - A^2\lambda^4(\bar{\rho} + i\bar{\eta})}}{\sqrt{1 - \lambda^2[1 - A^2\lambda^4(\bar{\rho} + i\bar{\eta})]}}$$

# CKM angles and unitarity triangle

Writing the complex elements explicitly:

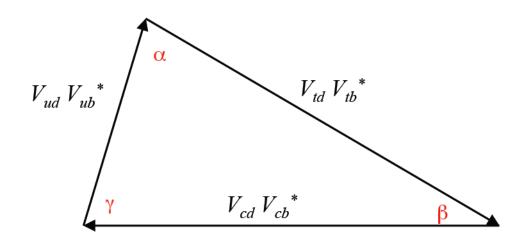
$$V_{\rm CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2 / 2 & \lambda & \sim \lambda^3 e^{-i\gamma} \\ -\lambda & 1 - \lambda^2 / 2 & \lambda \\ \sim \lambda^3 e^{-i\beta} & \sim -\lambda^2 e^{-i\beta_s} & 1 \end{pmatrix} + O(\lambda^4)$$

Definition of the angles:

$$\alpha = \arg\left(-\frac{V_{td}V_{tb}^{*}}{V_{ud}V_{ub}^{*}}\right)$$
$$\beta = \arg\left(-\frac{V_{cd}V_{cb}^{*}}{V_{td}V_{tb}^{*}}\right)$$
$$\gamma = \arg\left(-\frac{V_{ud}V_{tb}^{*}}{V_{cd}V_{cb}^{*}}\right)$$
$$\beta_{s} = \arg\left(-\frac{V_{us}V_{tb}^{*}}{V_{cs}V_{cb}^{*}}\right)$$

Using one of the 9 unitarity relations:  $V_{CKM} V_{CKM}^{\dagger} = 1$ Multiply first "d" column with last "b" column:

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



# CKM angles and unitarity triangle

Writing the complex elements explicitly:

$$V_{\rm CKM} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - \lambda^2 / 2 \\ -\lambda \\ -\lambda^3 e^{-i\beta} \\ \sim \lambda^3 e^{-i\beta} & -\lambda^2 e^{-i\beta_s} \\ -\lambda^2 e^{-i\beta_s} & 1 \end{pmatrix} + O(\lambda^4)$$

Definition of the angles:

$$\alpha \equiv \arg\left(-\frac{V_{td}V_{tb}^{*}}{V_{ud}V_{ub}^{*}}\right)$$
$$\beta \equiv \arg\left(-\frac{V_{cd}V_{cb}^{*}}{V_{td}V_{tb}^{*}}\right)$$
$$\gamma \equiv \arg\left(-\frac{V_{ud}V_{tb}^{*}}{V_{cd}V_{cb}^{*}}\right)$$
$$\beta_{s} \equiv \arg\left(-\frac{V_{ts}V_{tb}^{*}}{V_{cs}V_{cb}^{*}}\right)$$

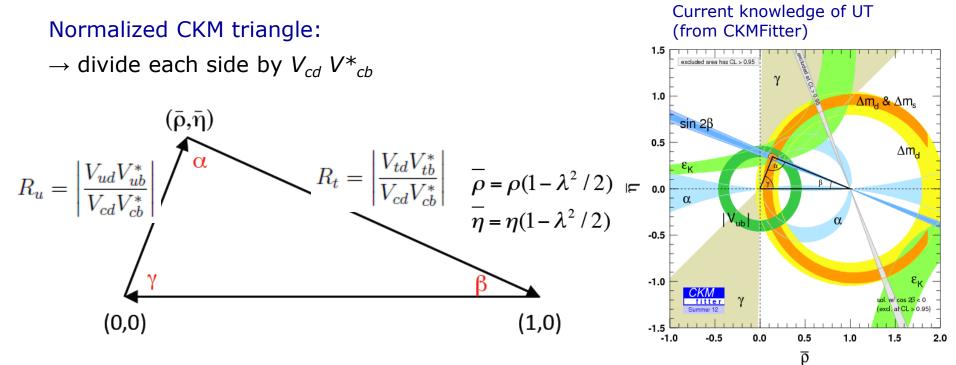
Using another unitarity relation:  $V_{CKM} V_{CKM}^{\dagger} = 1$ Multiply second "s" column with last "b" column:

$$V_{ub}V_{us}^* + V_{cb}V_{cs}^* + V_{tb}V_{ts}^* = 0$$

"Squashed unitarity triangle"

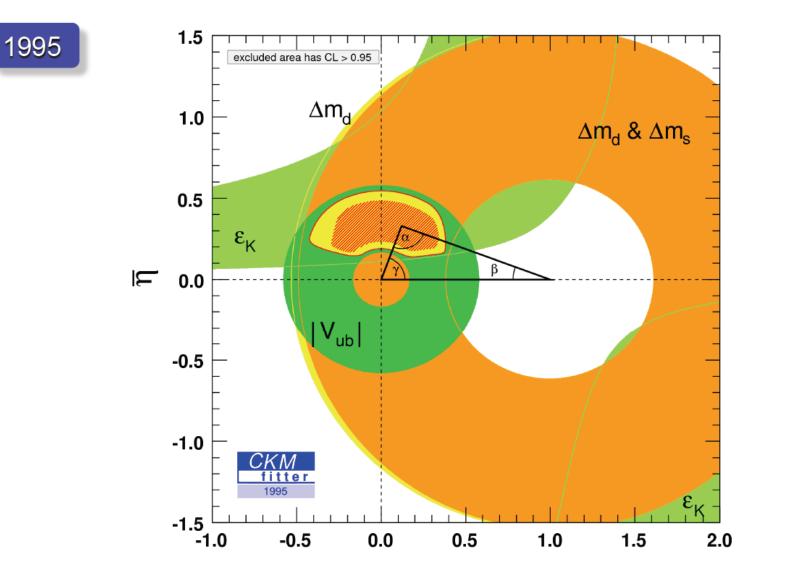
# CKM angles and unitarity triangle

- Imposing unitarity to the CKM matrix results in six equations that can be seen as the sum of three complex numbers closing a triangle in the complex plane
- Two of these triangles are relevant for study of CP-violation in B-physics and define the angles

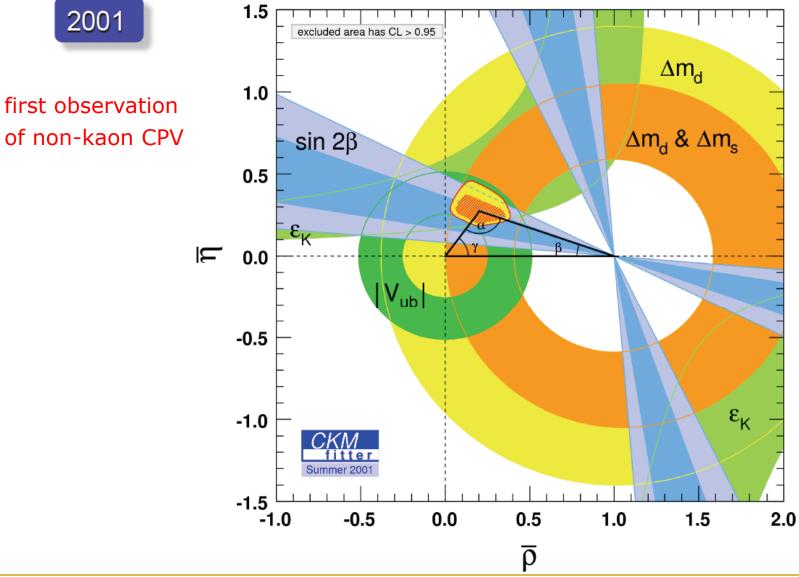


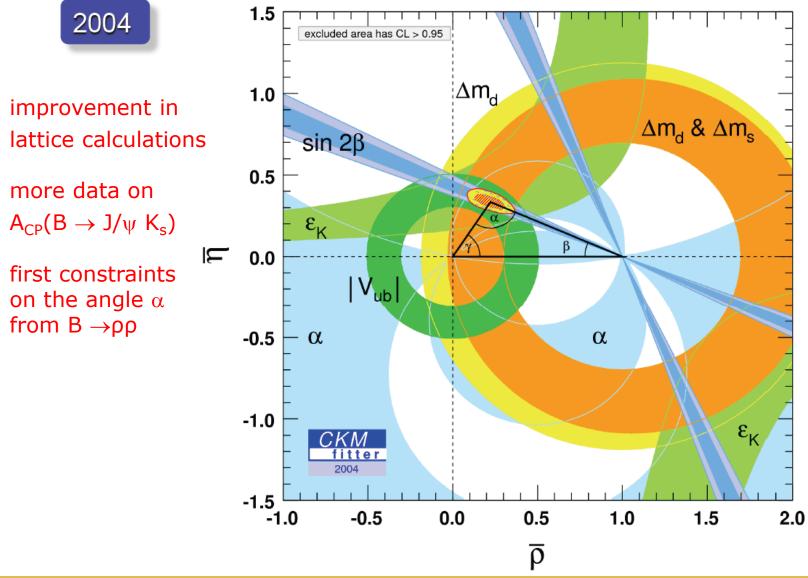
#### The unitarity triangle:

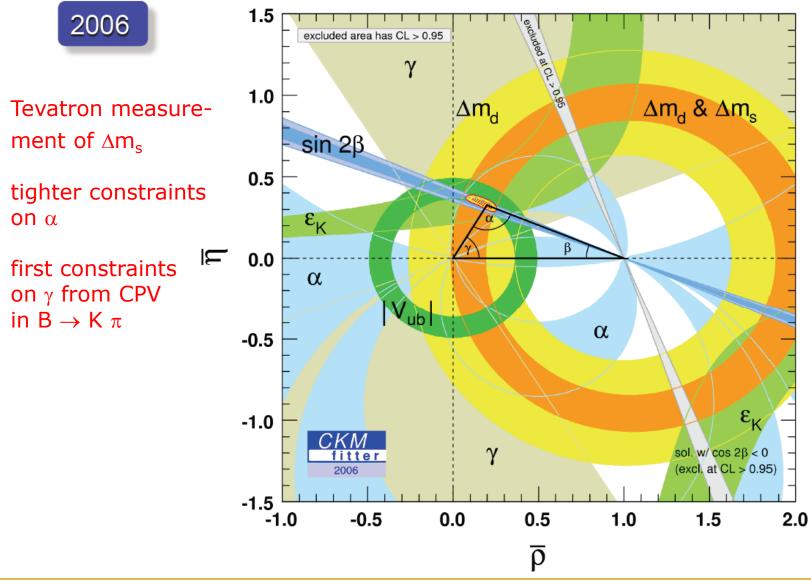
- Shows the size of the CP violation (no CPV means no triangle!)
- Presents our knowledge of CKM parameters
- Shows how consistent the measurements are!

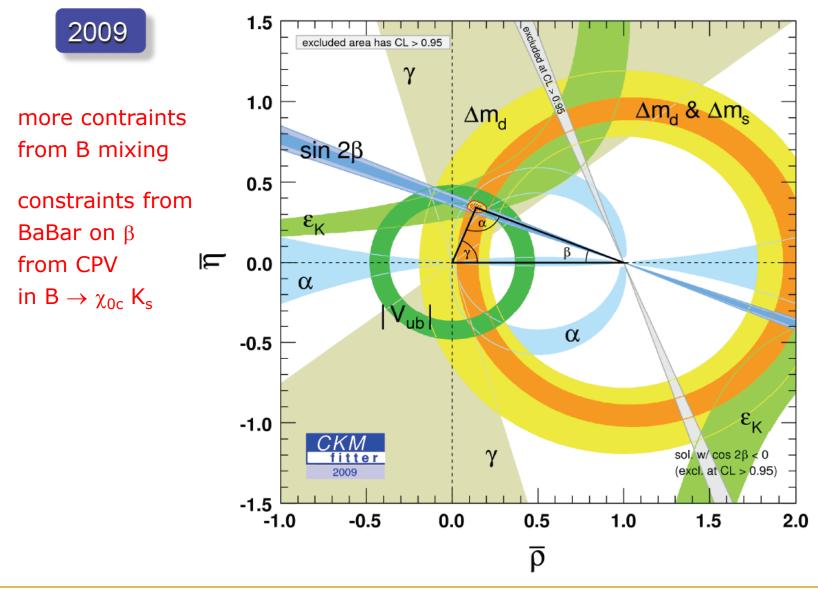


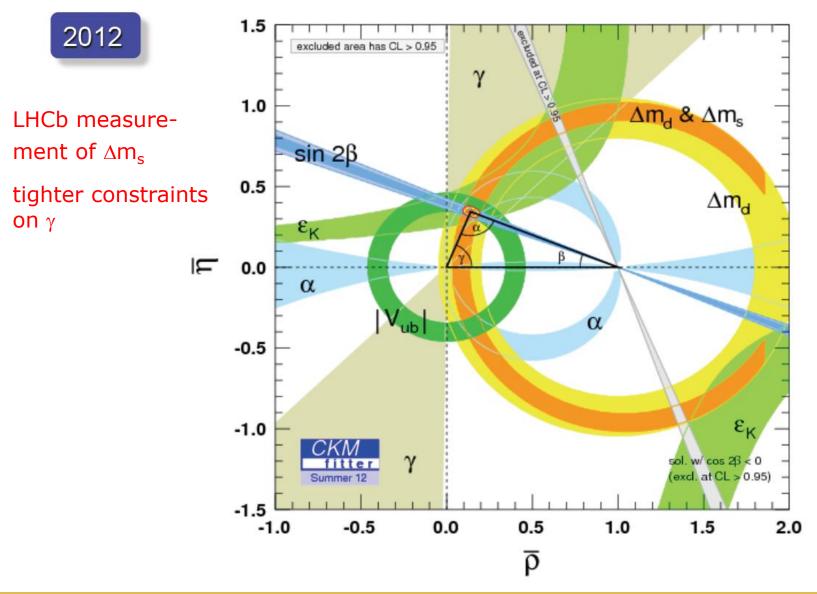
 $\overline{\rho}$ 





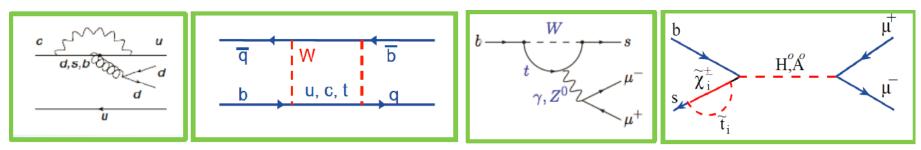






# FCNC loops in the SM

Map of flavour transitions and type of loop processes



QCD penguin

 $\Delta F=2 \text{ box}$ 

EW penguin

Higgs penguin

	b→s	b→d	c→u	s→d
QCD penguin	A <sub>CP</sub> (B <sub>s</sub> →hhh)	A <sub>CP</sub> (B⁰→hhh)	∆a <sub>cP</sub> (D→hh)	K→π <sup>0</sup> II ε΄/ε
∆F=2 box	<mark>∆M<sub>Bs</sub></mark> A <sub>CP</sub> (B <sub>s</sub> →J/ψφ)	$\Delta M_{Bd} = A_{CP}(B^0 \rightarrow J/\psi K_s)$	x,y, q/p	ΔM <sub>K</sub> ε <sub>K</sub>
EW penguin	<mark>Β→Κ(*)</mark> μμ Β→Χ <sub>s</sub> γ	Β→πμμ Β→Χγ	D→X <sub>u</sub> I I	K→ $π^0$ II K→ $π^{\pm}$ νν
Higgs penguin	B <sub>s</sub> →μμ	<b>Β</b> ⁰→μμ	D→µµ	K⁰→μμ

# Flavour sector beyond the SM

# Yukawa mechanism in the lepton sector

• in the SM the lepton Yukawa matrices can be diagonalized independently due to the global  $G_I$  symmetry of the Lagrangian, and therefore there are no FCNC

$$-\mathcal{L}_{\text{Yukawa}}^{\text{SM}} = Y_d^{ij} \bar{Q}_L^i D_R^j H + Y_u^{ij} \bar{Q}_L^i U_R^j H_c + Y_e^{ij} \bar{L}_L^i E_R^j H + \text{h.c.}$$
$$\mathcal{G}_q = SU(3)_{Q_L} \times SU(3)_{U_R} \times SU(3)_{D_R}, \qquad \mathcal{G}_\ell = SU(3)_{L_L} \otimes SU(3)_{E_R}$$

- however, the discovery that neutrinos oscillate (and are massive) implies that Lepton Flavour is not conserved
- the level of neutral Lepton Flavour Violation depends on the mechanism to generate neutrino masses (for instance **seesaw mechanism**)
- it could be just a copy of the quark sector, but it may be different due to the properties of the right-handed neutrino

## Seesaw mechanism

Simplification: one family:  $v_L$  and  $v_R$ 

• total mass term: Dirac and Majorana mass

$$\mathcal{L}_{mass} = -\frac{m(\bar{\nu}_L \nu_R + \bar{\nu}_R \nu_L)}{-\frac{1}{2}M(\nu_R^T C \nu_R + \bar{\nu}_R C \bar{\nu}_R^T)}$$

- diagonalization of the mass matrix:
  - $\rightarrow$  Majorana mass eigenstates of the neutrinos

for 
$$M >> m$$
 we get  $m_1 \approx \frac{m^2}{M} \quad m_2 \approx M$ 

one very heavy, practically right handed neutrino

• one very light, practically left handed neutrino

At energies small compared to M, Majorana mass term for left handed neutrino:

$$\mathcal{L}_{mass} = -\frac{1}{2} \frac{m^2}{M} \left( \nu_L^T C \nu_L + \bar{\nu_L} C \bar{\nu_L}^T \right)$$

Majorana mass is small if M >> m

## Seesaw mechanism

- In case of three families: Neutrino Mixing
- Compact notation for the Leptons:

$$\mathcal{N}_{L/R} = \begin{bmatrix} \nu_{e,L/R} \\ \nu_{\mu,L/R} \\ \nu_{\tau,L/R} \end{bmatrix} \quad \mathcal{E}_{L/R} = \begin{bmatrix} e_{L/R} \\ \mu_{L/R} \\ \tau_{L/R} \end{bmatrix}$$

• Dirac masses are generated by the Higgs mechanism: (as for the quarks)

$$\mathcal{L}_{DM}^{N} = -\mathcal{N}_{L}m^{N}\mathcal{N}_{R} + h.c.$$
  $\mathcal{L}_{DM}^{E} = -\mathcal{E}_{L}m^{E}\mathcal{E}_{R} + h.c.$ 

- $m^N$ : Dirac mass matrix for the neutrinos,  $m^E$ : (Dirac) mass matrix for e,  $\mu$ ,  $\tau$
- Right handed neutrinos  $\rightarrow$  Majorana mass term:

$$\mathcal{L}_{MM} = -\frac{1}{2} \left( N_R^T M C N_R + \bar{N}_R M C \bar{N}_R^T \right)$$

- M: (symmetric) Majorana Mass Matrix
- this term is perfectly  $SU(2)_L \otimes U(1)$  invariant

### Implementation of the seesaw mechanism:

• assume that all eigenvalues of *M* are large

Effective theory at low energies  $\rightarrow$  only light, practically left handed neutrinos

• effect of right handed neutrino: Majorana mass term for the light neutrinos

$$\mathcal{L}_{mass} = -\frac{1}{2} \left( N_L^T m^T M^{-1} m C N_L + \bar{N}_L m^T M^{-1} m C \bar{N}_L^T \right)$$

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# Lepton mixing: PMNS matrix

- we know there are FCNC in the lepton sector (analogous to the quark sector) because we have observed neutrino oscillations
- therefore the Yukawa couplings in lepton sector do contain also a mixing matrix

### Pontecorvo Maki Nakagawa Sakata Matrix

• almost like CKM: Three Euler angles  $\theta_{ij}$ 

$$U_{12} = \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix} , \quad U_{13} = \begin{bmatrix} c_{13} & 0 & s_{13} \\ 0 & 1 & 0 \\ -s_{13} & 0 & c_{13} \end{bmatrix} , \quad U_{23} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix}$$

- a Dirac phase  $\delta$  and two Majorana phases  $\alpha_1$  and  $\alpha_2$ 

$$U_{\delta} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & e^{-i\delta_{13}} \end{bmatrix} \quad U_{\alpha} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & e^{-i\alpha_{1}} & 0 \\ 0 & 0 & e^{-i\alpha_{2}} \end{bmatrix}$$

- PNMS parametrization:  $V_{\text{PMNS}} = U_{23}U_{\delta}^{\dagger}U_{13}U_{\delta}U_{12}U_{\alpha}$
- $V_{PMNS}$  is unitary like the CKM matrix
- left handed neutrinos are Majorana
  - $\rightarrow$  no freedom to rephase these fields!

### No hierarchy observed!

 $\begin{aligned} \theta_{12}[^{\circ}] &= 33.36^{+0.81}_{-0.78} \\ \theta_{23}[^{\circ}] &= 40.0^{+2.1}_{-1.5} \text{ or } 50.4^{+1.3}_{-1.3} \\ \theta_{13}[^{\circ}] &= 8.66^{+0.44}_{-0.46} \\ \delta_{\rm CP}[^{\circ}] &= 300^{+66}_{-138} \end{aligned}$ 

# Lepton mixing: PMNS matrix

- we know there are FCNC in the lepton sector (analogous to the quark sector) because we have observed neutrino oscillations
- therefore the Yukawa couplings in lepton sector do contain also a mixing matrix

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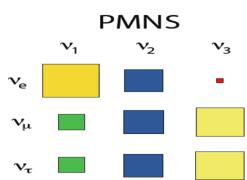
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# Lepton Flavour Violation

FCNC processes in the leptonic sector:

 $\tau \to \mu \gamma \quad \mu \to e \gamma \quad \tau \to e e e \text{ etc.}$  $\nu_{\tau} \to \nu_{e} \gamma \quad \nu_{\tau} - \nu_{e} \text{ mixing}$ 

### **Lepton Flavour Violation:**

- right handed neutrinos are Majorana fermions:
  - $\rightarrow$  no conserved quantum number corresponding to the rephasing of the right handed neutrino fields
- lepton flavour violation could feed via conserved B-L into baryon number violation
- if neutrinos are Dirac particles, expect very small (far from experimental sens.) LFV
- however, if neutrinos are Majorana particles and something like the seesaw mechanism is at work, large values (close to exp. sens.) are favoured
- in general, any extension of the SM with new states at the TeV scale generates large charged LFV

# Many flavour related open questions

- Our understanding of Flavour is unsatisfactory:
  - $\rightarrow$  22 (out of 27) free parameters of the SM originate from the Yukawa Sector (including Lepton Mixing)
  - $\rightarrow$  Why is the CKM Matrix hierarchical?
  - $\rightarrow$  Why is CKM so different from the PMNS?
  - $\rightarrow$  Why are quark masses (except top) so small compared with electroweak VEV?
  - $\rightarrow$  Why do we have three families?
- Why is CP Violation in flavour-diagonal processes not observed? (e.g. electric dipol moments of electron and neutron)
- Where is the CP violation needed to explain the matter-antimatter asymmetry of the Universe?

### **Strong CP remains mysterious**

- flavour diagonal CP Violation is well hidden
- $\rightarrow$  e.g electric dipole moment of the neutron:

$$\begin{array}{rcl} d_e &\sim & e \frac{\alpha_s}{\pi} \frac{G_F^2}{(16\pi^2)^2} \frac{m_t^2}{M_W^2} \, \mathrm{Im}\Delta \, \mu^3 \\ &\sim & 10^{-32} e \, cm \quad \mathrm{with} \, \mu \sim 0.3 \, \mathrm{GeV} \\ d_{\mathrm{exp}} &\leq & 3.0 \times 10^{-26} e \, cm \end{array}$$

# Many open questions

### **Standard Model**

- does not describe neutrino masses
- does not have a good DM candidate
- cannot explain the baryon asymmetry in the Universe
- no explanation for the **flavour structure**
- does not include gravity
- suffers from fine tuning issues in the Higgs sector

### **Possible extensions**

- SUSY, extra dimensions, hidden sectors, .....
- in general, the diagonalization of the mass matrix will not give diagonal Yukawa couplings  $\rightarrow$  **large FCNC**

### Needed

- precision measurements of flavour observables are generically sensitive to additions to the Standard Model
- precise measurements of the Higgs boson properties
- precise measurements of FCNC