
Non-Prompt J/psi Analysis

PbPb @ 5.02 TeV



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IFJ - ALICE Meetings

- Progress on Fitting for Non-prompt Fraction



Procedure

- Basic Idea to maximize

$$\ln L = \sum_{i=1}^N \ln F(x^i, m_{e^+e^-}^i) \quad (1)$$



- X = pseudo-proper decay length
- m=invariant mass reconstructed from pairs
- Observing either signal or bkg J/psi
-

$F(x^i, m_{e^+e^-}^i)$ → Likelihood Function
→ Probability of observing a J/ψ , given x^i and $m_{e^+e^-}^i$
 \sum → Sum over all the J/ψ candidates

- Unbinned 2-dim likelihood fit function

$$F(x, m_{e^+e^-}) = f_{sig} \cdot F_{sig}(x) \cdot M_{sig}(m_{e^+e^-}) + (1 - f_{sig}) \cdot F_{bkg}(x) \cdot M_{bkg}(m_{e^+e^-})$$

$$F_{sig} = f'_B \cdot F_B(x) + (1 - f'_B) \cdot F_{Prompt}(x)$$

X-distribution
for Prompt-
Jpsi

- Function to Fit :

$$F(x, m_{e^+e^-}) = f_{sig} \cdot [f'_B \cdot F_B(x) + (1 - f'_B) \cdot F_{Prompt}(x)] \cdot M_{sig}(m_{e^+e^-}) + (1 - f_{sig}) \cdot F_{bkg}(x) \cdot M_{bkg}(m_{e^+e^-})$$

f'_B & $f_{sig} (= \frac{S}{S+B})$ are free parameters.

All the PDFs are defined
in the Ana-note.

According to the previous slide (last bullet)

- We need 5 templates PDFs for the 2-dim (m_{ee} , x) fitting of the Likelihood function.
 - $M_{\text{sig}}(m_{ee})$: template for Invariant Mass of J/Ψ -Signal (taken from MC)
 - $M_{\text{bkg}}(m_{ee})$: template for Inv. Mass Combinatorial Background.
 - $R(x)$: Resolution function – depends on p_T , Hits on SPD's 1st layer (taken from MC)
 $\sim F_{\text{Prompt}}(x)$
 - $F_B(x)$: template for Non-prompt J/Ψ (from MC)
 - $F_{\text{bkg}}(x)$: template for fitting x -Background (on data)



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$\sim F_{Prompt}(x)$

- $F_B(x)$: template for Non-prompt J/Ψ (from MC)

- $F_{bkg}(x)$: template for fitting x-Background (on data)

$M_{sig}(m_{ee})$ Signal

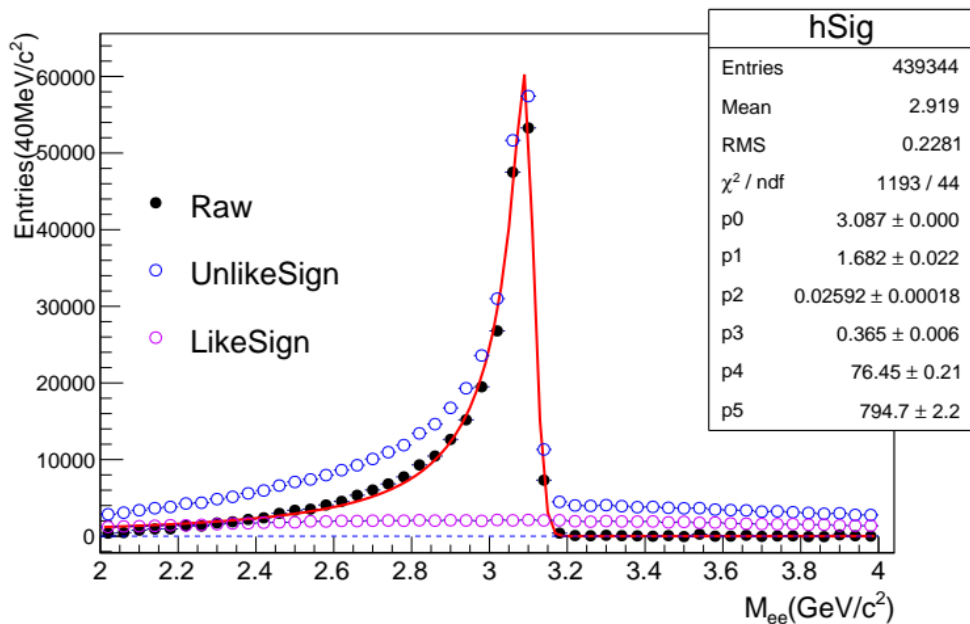
$$f(m^{e^+e^-}; \alpha, n, \bar{m}, \sigma, N) = N \cdot \begin{cases} \exp\left(-\frac{(m^{e^+e^-} - \bar{m})^2}{2\sigma^2}\right) & \text{for } \frac{m^{e^+e^-} - \bar{m}}{\sigma} > -\alpha \\ A \cdot \left(B - \frac{m^{e^+e^-} - \bar{m}}{\sigma}\right)^{-n} & \text{for } \frac{m^{e^+e^-} - \bar{m}}{\sigma} \leq -\alpha \end{cases}$$

and where the coefficients are:

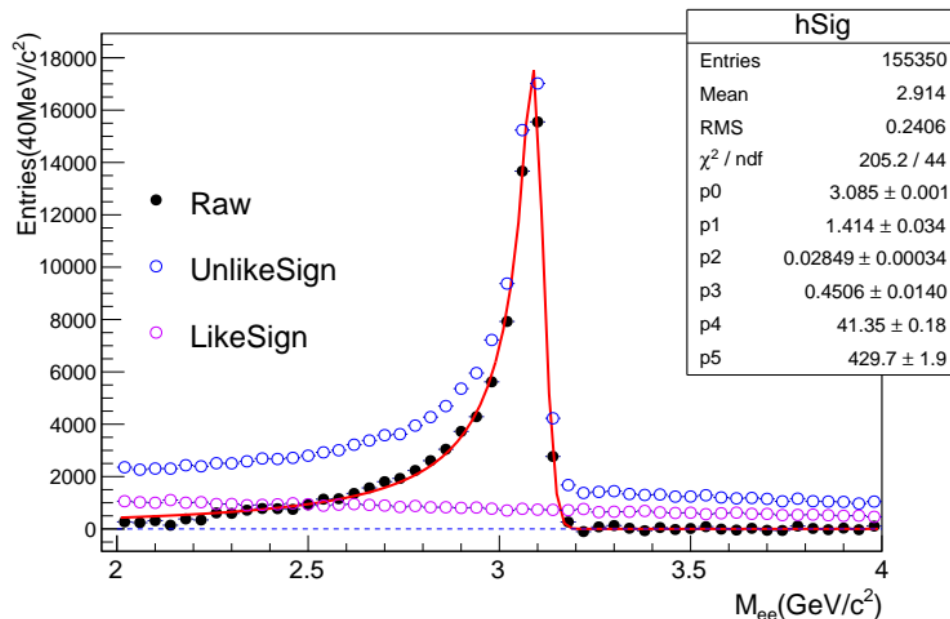
$$A = \left(\frac{n}{|\alpha|}\right)^n \cdot \exp\left(-\frac{|\alpha|^2}{2}\right) \quad B = \frac{n}{|\alpha|} - |\alpha|$$

- Fit on MC sample (with Injected Jpsi)

p0: Mean, p1: Sigma, p2: Alpha, p3: Norm,
p4: Norm of Exp = n



0 < pT < 3



3 < pT < 5



$M_{\text{sig}}(m_{ee})$ Signal

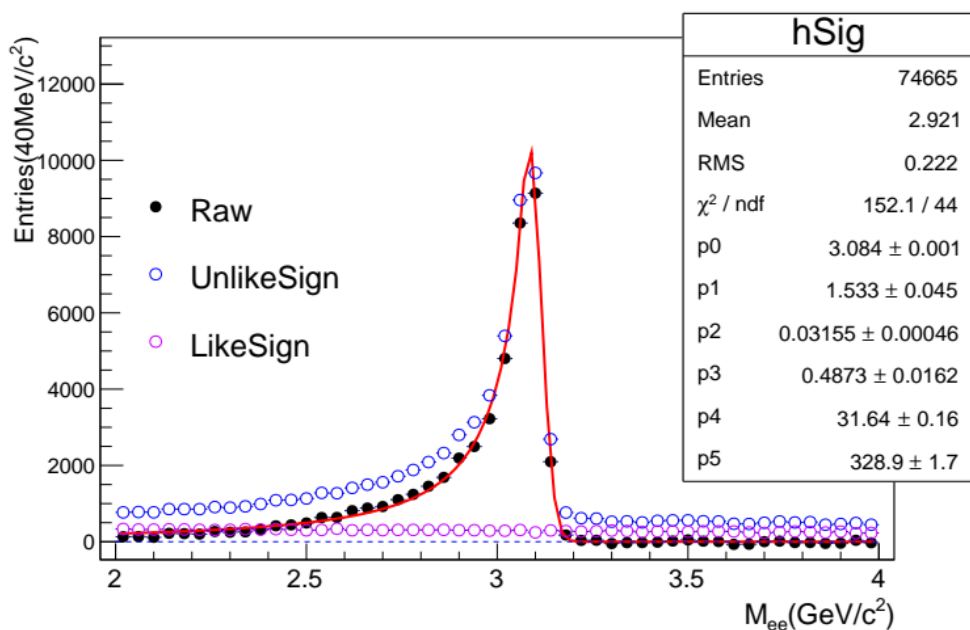
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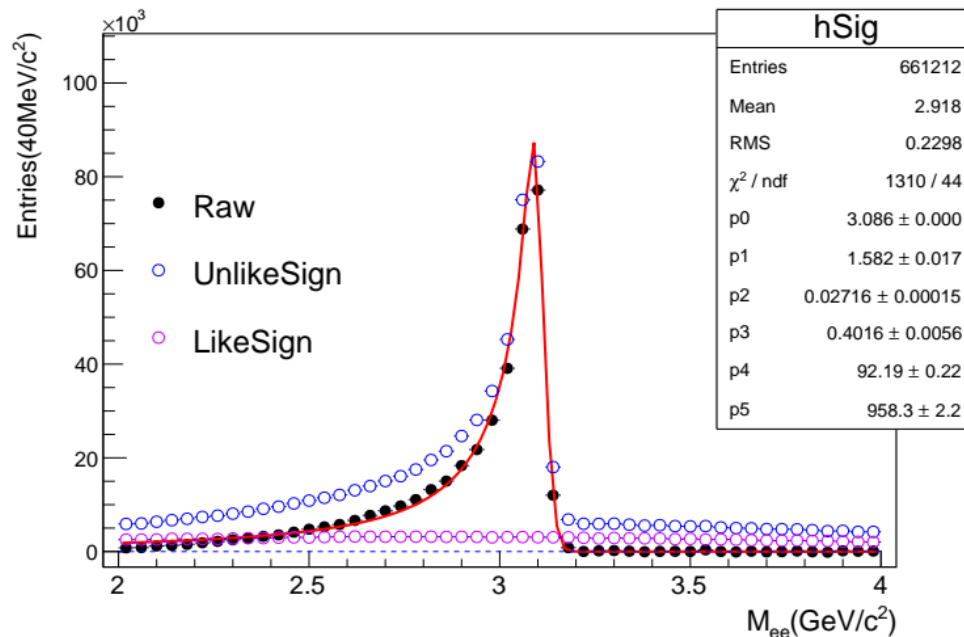
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- Fit on MC sample (with Injected Jpsi)

p0: Mean, p1: Sigma, p2: Alpha, p3: Norm,
p4: Norm of Exp = n



5 <pT< 15



0 <pT< 15



Fitting the Resolution Function R(x)

- **R(x) is measured as a function of pT(Jpsi) and type of J/psi.**
 - Transverse Impact parameter $d_0(r, \phi)$ resolution depends on the pT. (see backup)
- **Therefore, RMS of R(x) depends strongly on the pT of J/psi.**
 - Going from higher to lower pT, it increases
 - In lower pT, the $d_0(r, \phi)$ resolution is worse than high-pT.
- **Significantly, the hits in SPD layers varies the precision of tracking the daughters.**
- **Fitted on the x-distribution Reconstructed Prompt Jpsi in MC, In different pT regions.**
- **Fitted using BtoJPSI classes.**
- **Compared with the analysis pp 5TeV, 13TeV by Fiorella (pp Analysis-note)**

$$R(x) = w_1 \cdot G_1(x; \mu_1, \sigma_1) + w_2 \cdot G_2(x; \mu_2, \sigma_2) + w_3 \cdot f(x; \alpha, \lambda),$$

where the two functions G_1 and G_2 are gaussian functions:

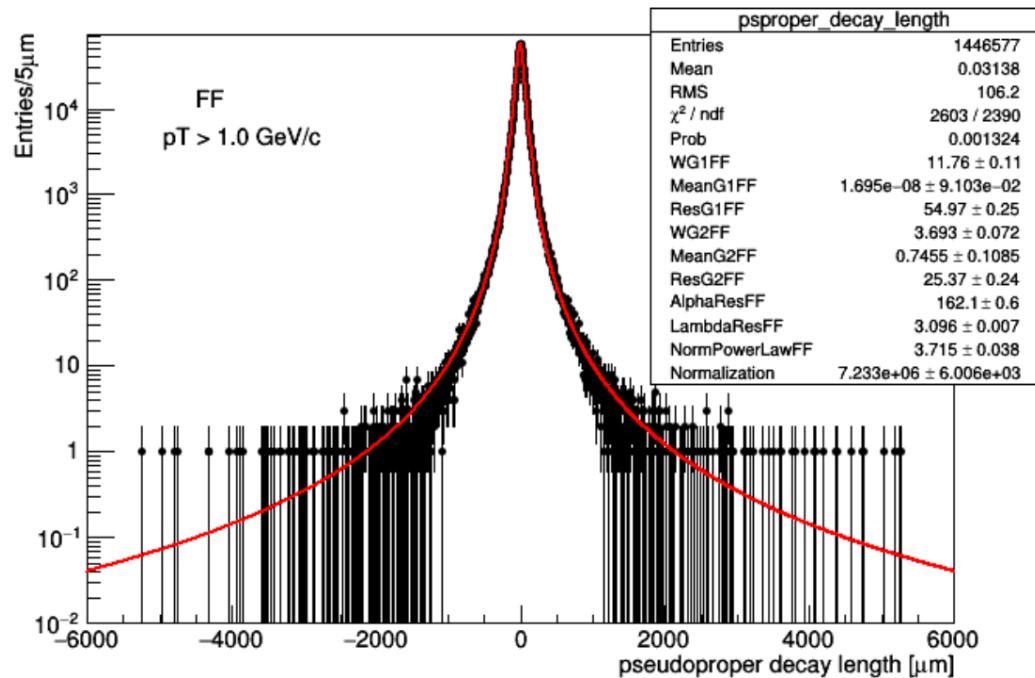
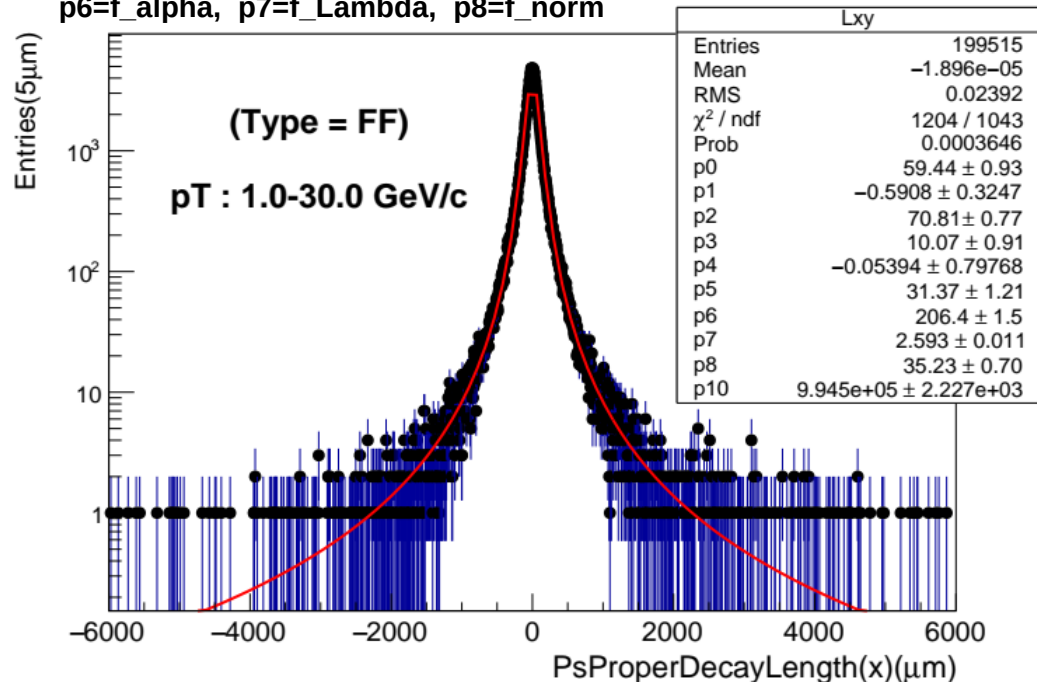
$$G(x; \mu, \sigma) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

while the symmetric power law term has the stepwise form:

$$f(x; \alpha, \lambda) = \begin{cases} \frac{\lambda-1}{2\alpha\lambda} & |x| < \alpha \\ \frac{\lambda-1}{2\alpha\lambda} \alpha |x|^{-\lambda} & |x| > \alpha \end{cases}$$

Resolution Function R(x) fitting to Prompt Jpsi x-distribution:

$p_0=G1norm$, $p_1=G1Mean$, $p_2=G1rms$,
 $p_3=G2norm$, $p_4=G2Mean$, $p_5=G2rms$,
 $p_6=f_alpha$, $p_7=f_Lambda$, $p_8=f_norm$

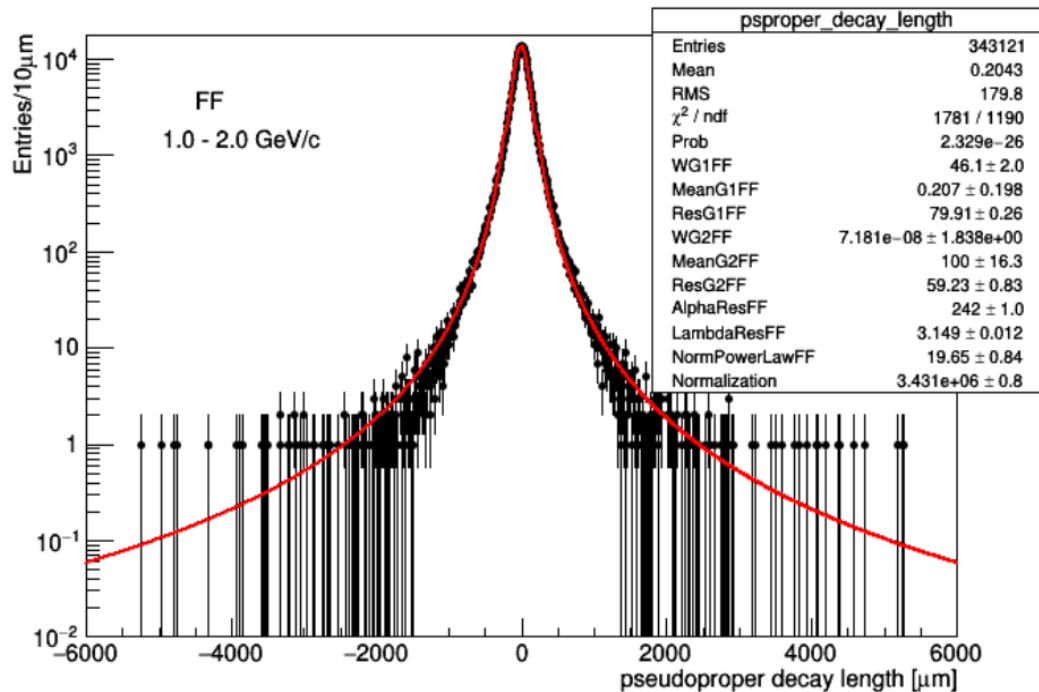
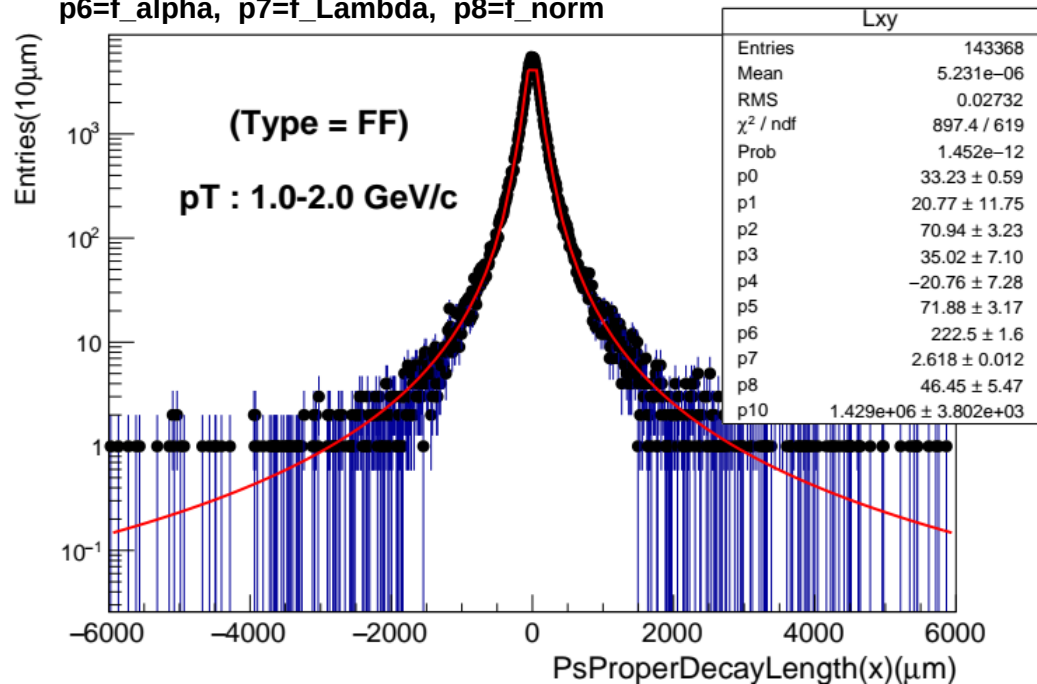


Fiorella pp-5-13TeV

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Fiorella pp-5-13TeV

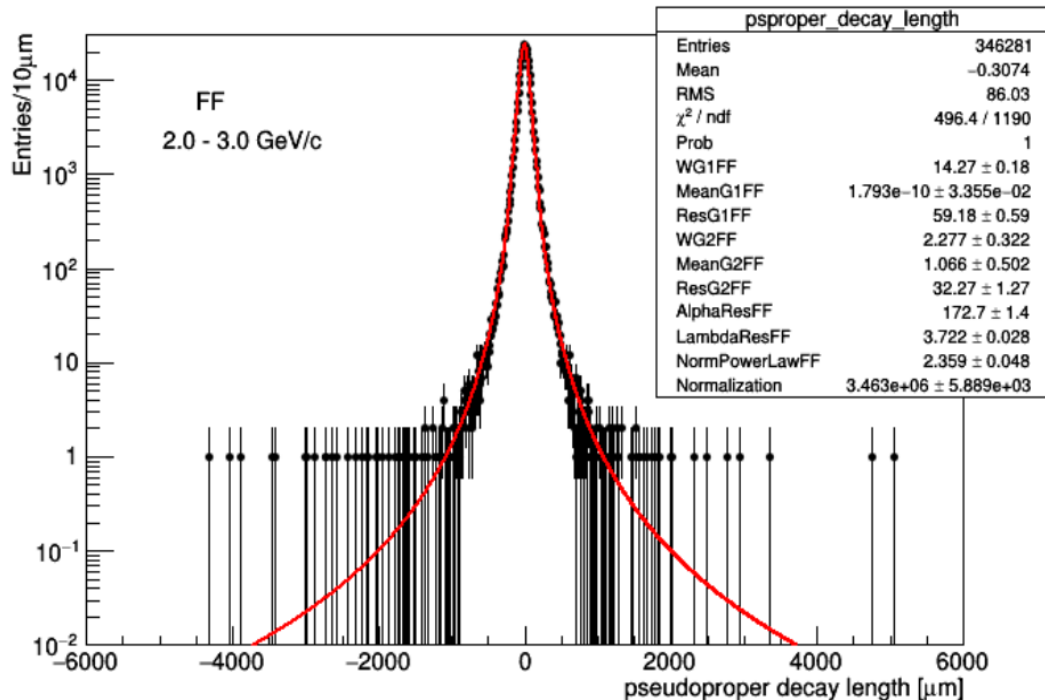
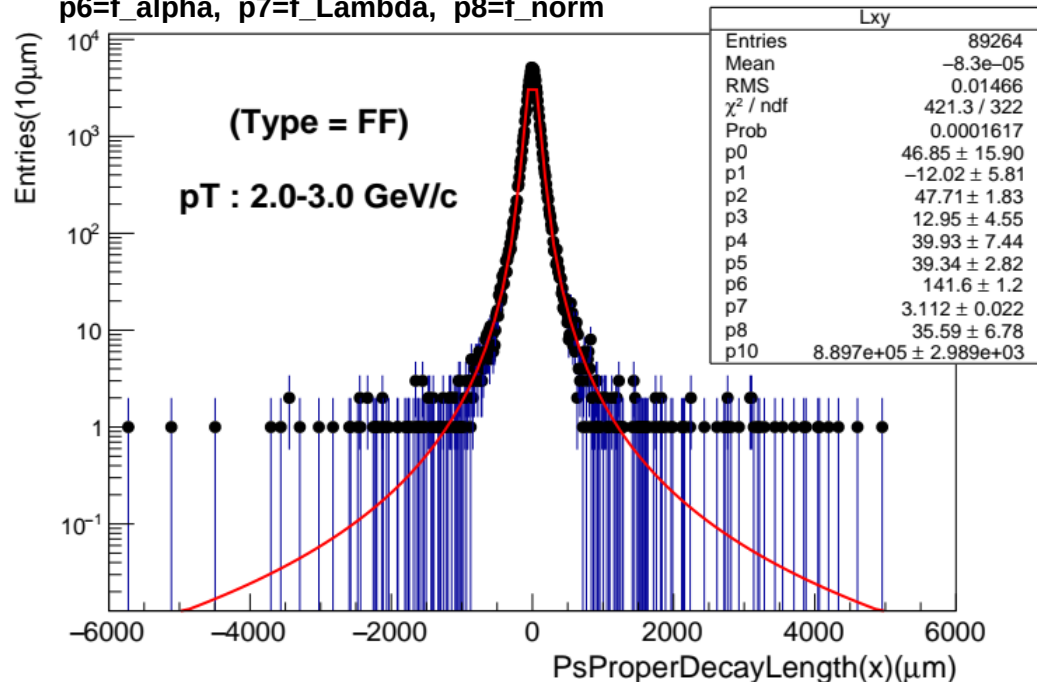


Resolution Function $R(x)$ fitting to Prompt $J\psi$ x -distribution:



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$p_0=G1norm$, $p_1=G1Mean$, $p_2=G1rms$,
 $p_3=G2norm$, $p_4=G2Mean$, $p_5=G2rms$,
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Fiorella pp-5-13TeV

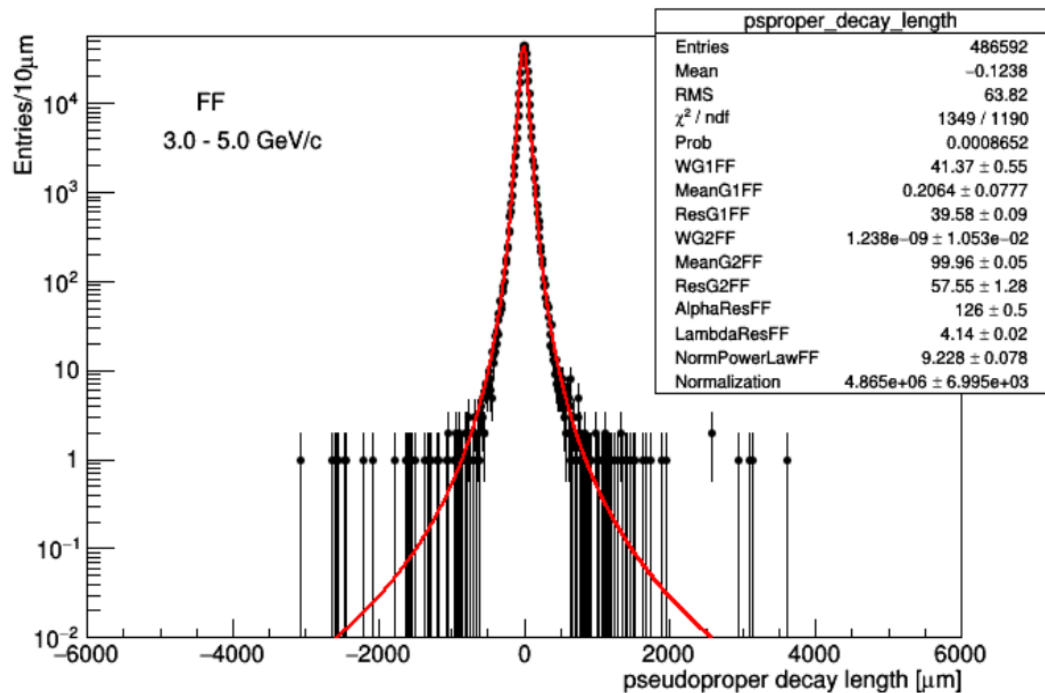
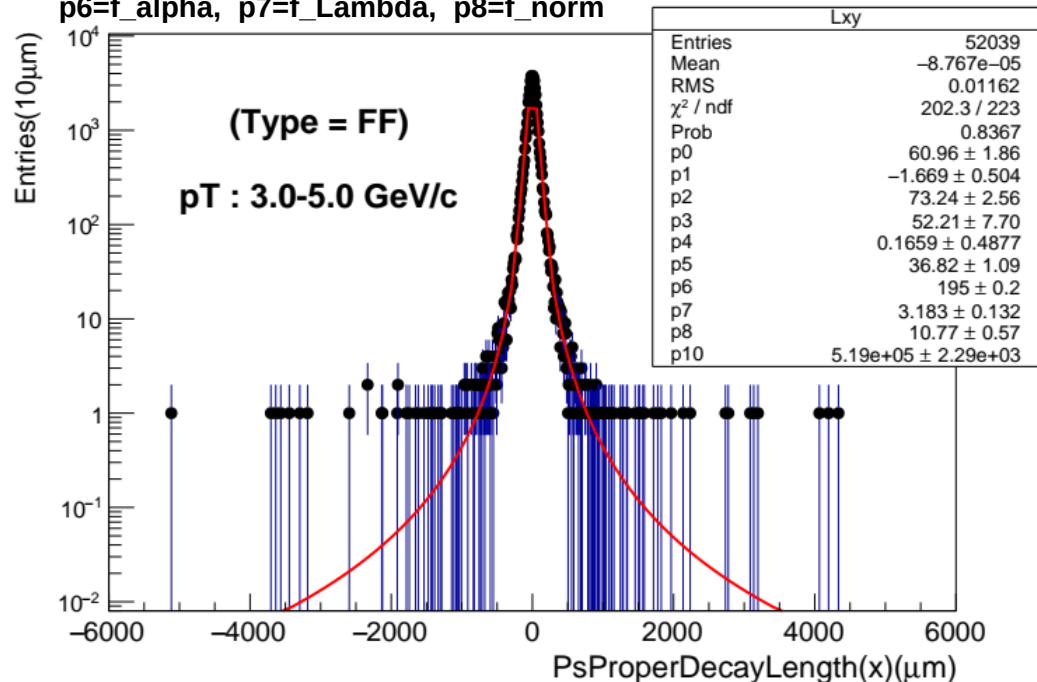


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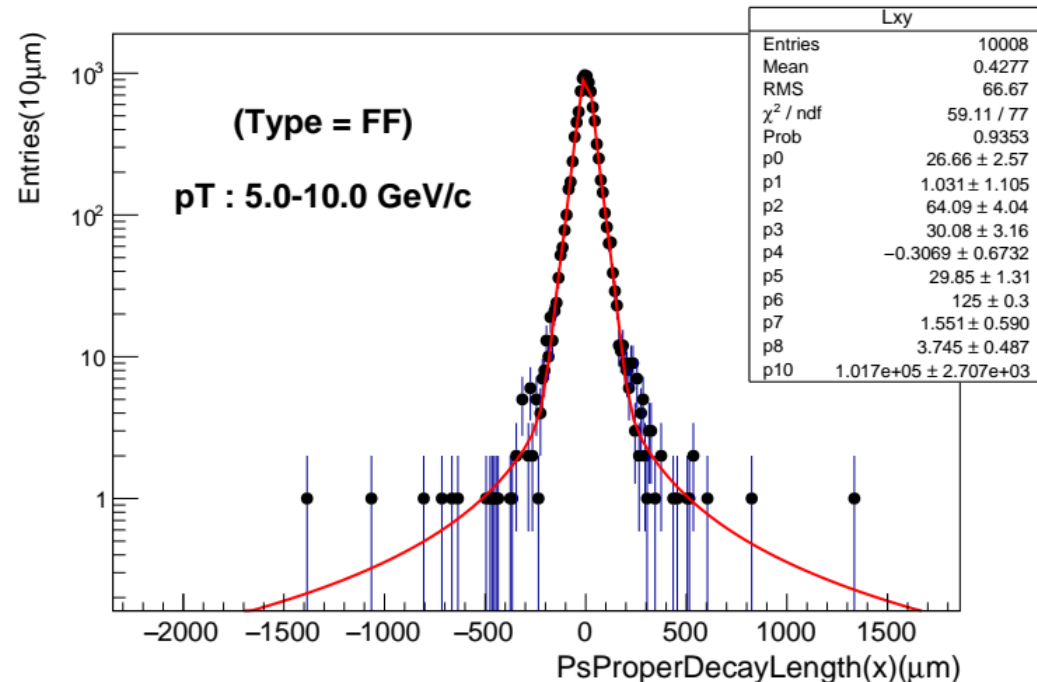
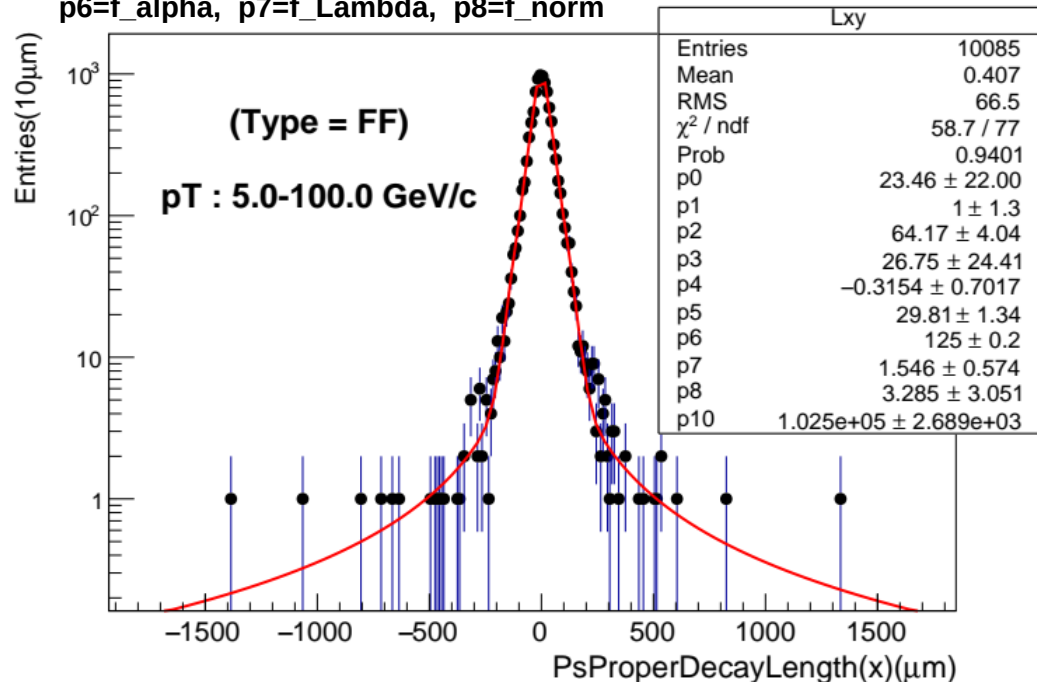


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ALICE

p0=G1norm, p1=G1Mean, p2=G1rms,
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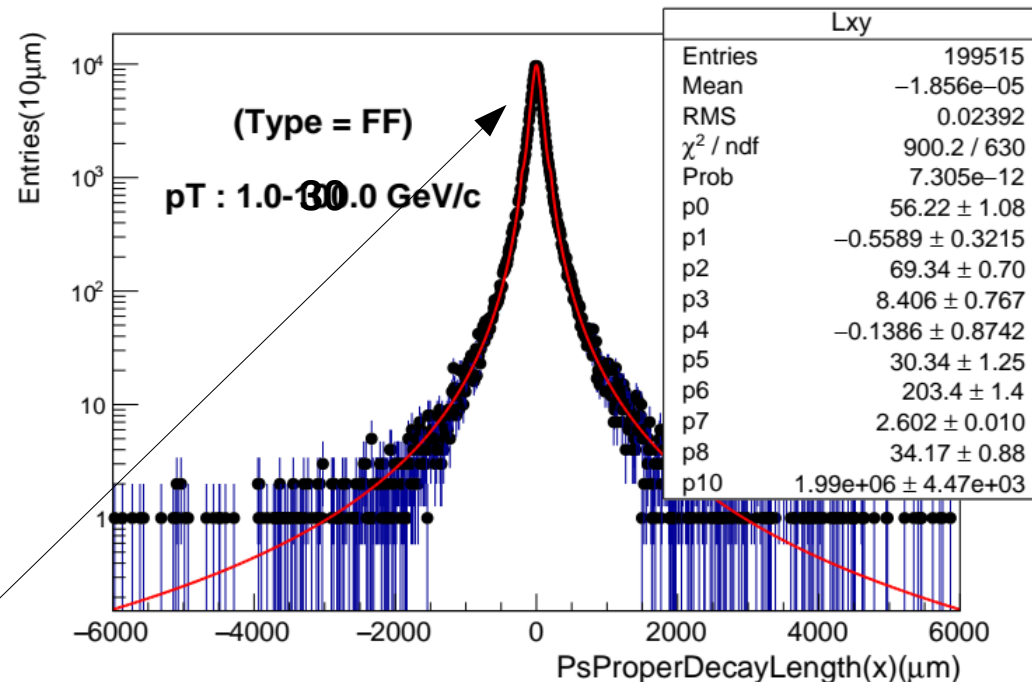
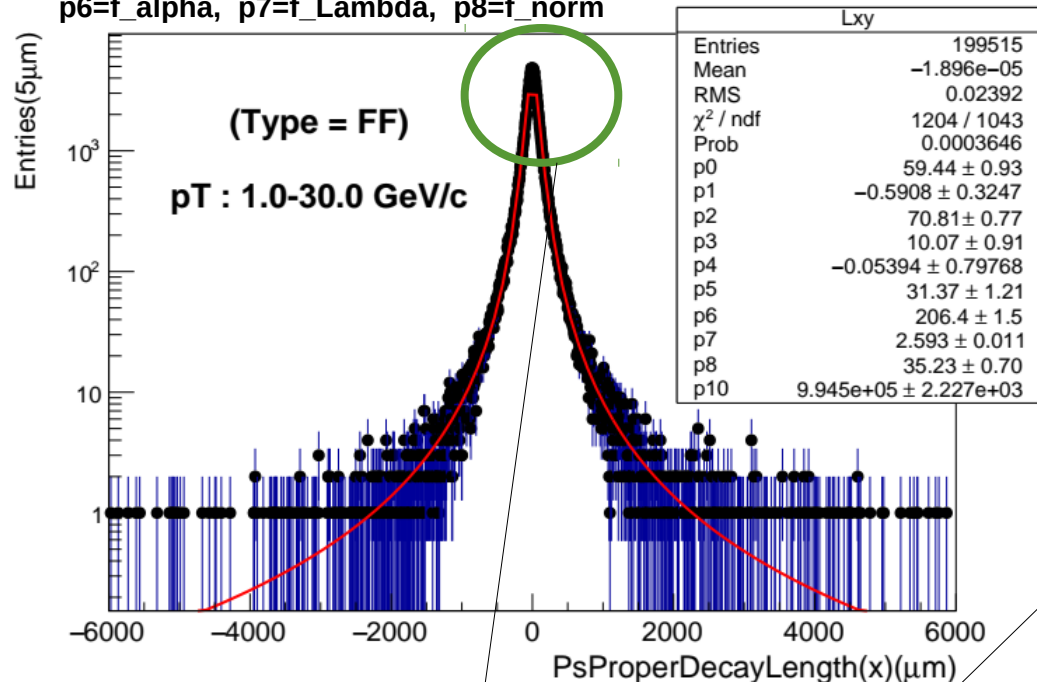


Resolution Function $R(x)$ fitting to Prompt Jpsi x-distribution:



ALICE

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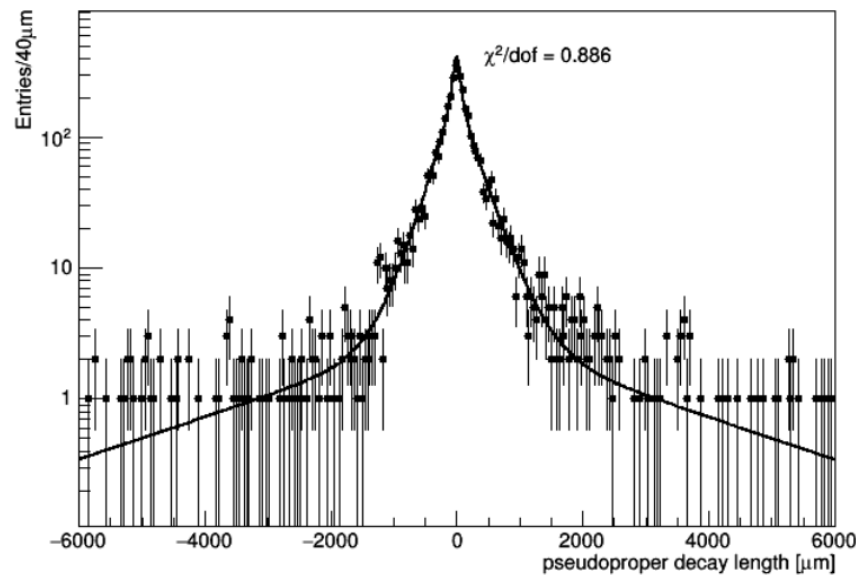


This is due to less # of points in function to draw, after increasing the # of points it is corrected!!!



- To obtain a good description of the data outside the signal region.
- We fit the x-distribution on both side of signal-mass region (LB, RB).
- Components:
 - Exp(+ve slope) λ_+ : describes the bkg from other long-lived b-hadrons producing ep-em pairs.

$$b \longrightarrow c e-X \quad c \longrightarrow e+X$$
 - Exp (-ve slope) λ_- and symmetric part: describes the remaining bkg from other sources.
 - Zero-life time components : same as resolution function.
 - f's are constants to normalize the distribution.



$$F_{Bkg[m_{inv}, p_T, type]}(x) = \left[\frac{f_+}{\lambda_+} e^{-\frac{x'}{\lambda_+}} \cdot \theta(x') + \frac{f_-}{\lambda_-} e^{\frac{x'}{\lambda_-}} \cdot \theta(-x') + \frac{f_{Sym}}{2\lambda_{Sym}} e^{-\frac{|x'|}{\lambda_{Sym}}} + (1 - f_+ - f_- - f_{Sym}) \cdot \delta(x') \right] \otimes R_{p_T, type}(x - x')$$

Example figure taken from
[AnaNote-957](#)





ALICE

Backup



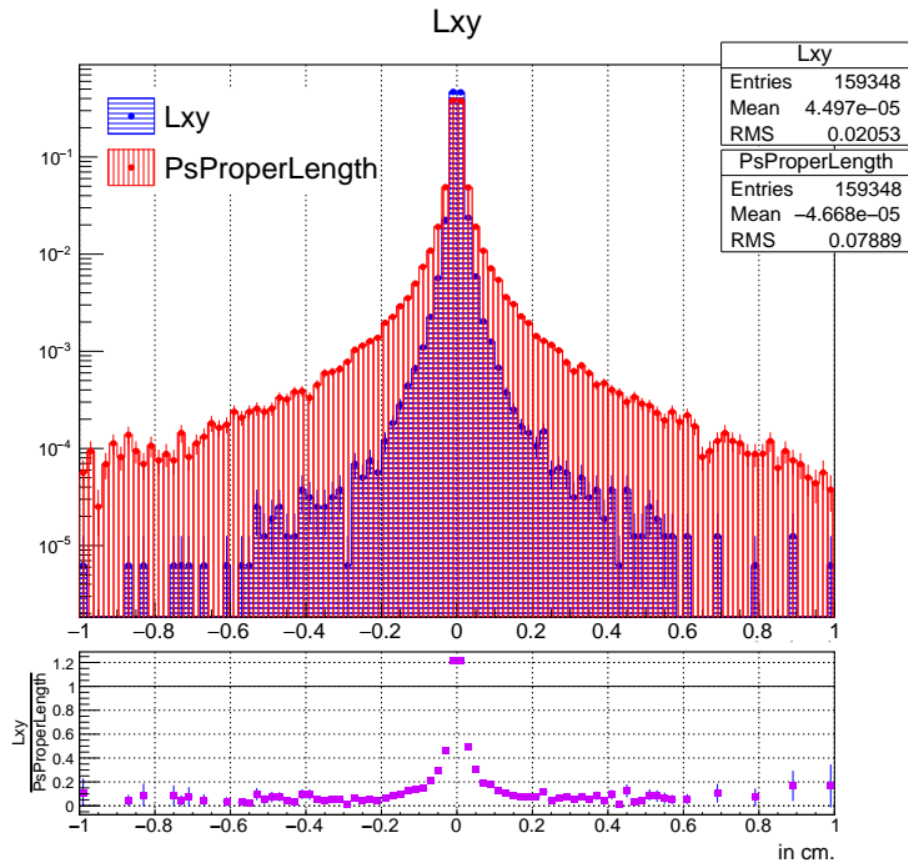
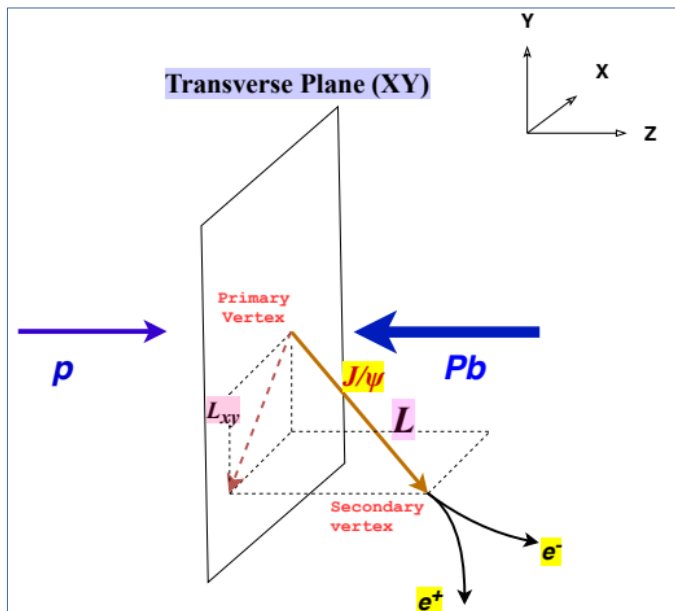
$$M_{Bkg}(m_{e^+e^-}; \lambda, A) = A \cdot e^{-\frac{(m_{e^+e^-})}{\lambda}} + B ,$$

A & Lambda are free parameters

L_{xy} to PsProper Decay Length (x)

$$L_{xy} = \vec{L} \cdot \vec{p}_T^{J/\psi} / p_T^{J/\psi}$$

$$x = \frac{c \cdot L_{xy} \cdot m_{J/\psi}}{p_T^{J/\psi}}$$



Comparison of L_{xy} and x -distributions for **Reconstructed true Prompt J/psi**

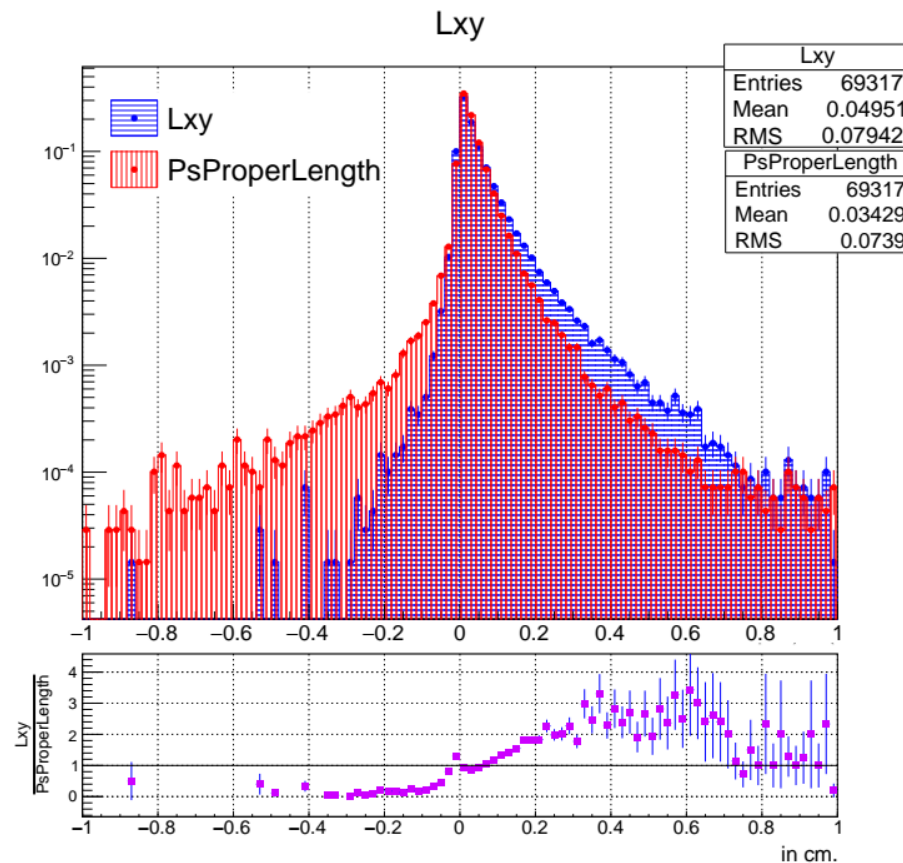
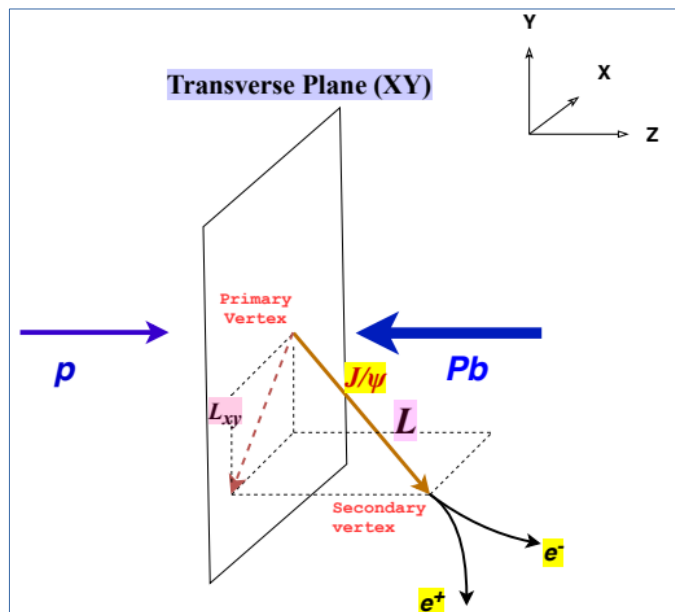
L_{xy} to PsProper Decay Length (x)



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Comparison of L_{xy} and x -distributions for **Reconstructed true NonPrompt J/psi**



Data vs MC $d_0(r\phi)$ resolution

