

# *Transversal momentum dependence and di-jets in $p$ - $p$ , $p$ -Pb and Pb-Pb collisions*



NCN



The Henryk Niewodniczański  
Institute of Nuclear Physics  
Polish Academy of Sciences

*Krzysztof Kutak*



*Based on*

*Phys.Lett. B795 (2019) 511-515*

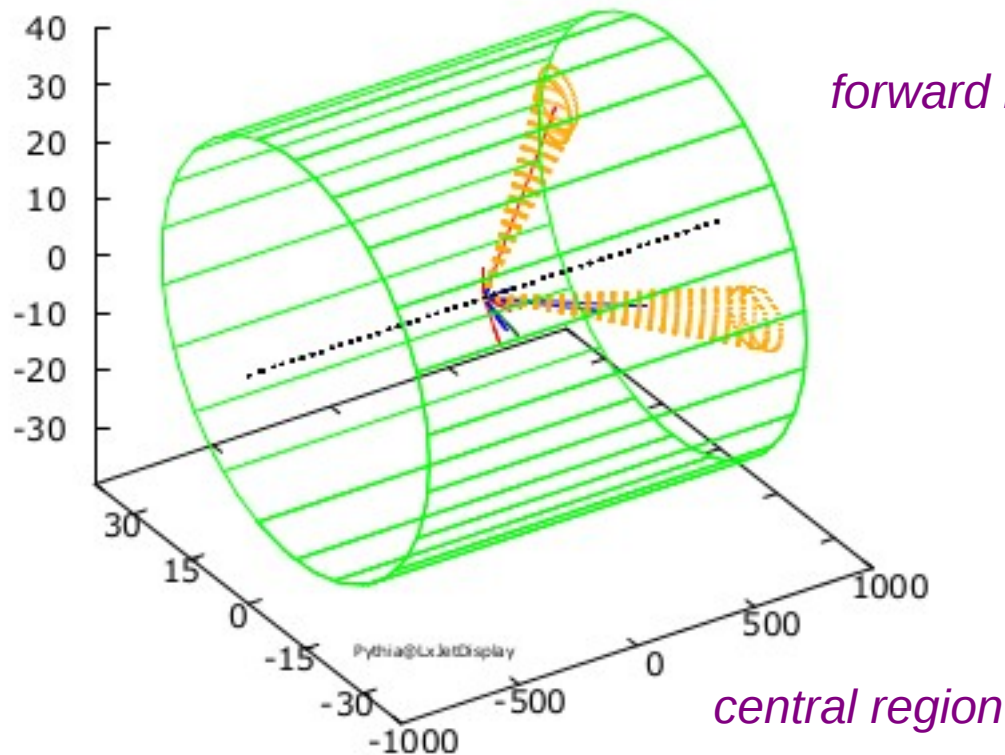
*A. van Hameren, P. Kotko, K. Kutak, S. Sapeta*

*1811.06390 by Kutak, Płaczek, Straka*

*1911. XXXX van Hameren, Kutak, Płaczek, Rohrmoser, Tywoniuk*

*p-p and p-Pb*

# $p - A$ (dilute-dense) forward-forward di-jets



*forward region*

*The collisions we consider:*

*e.g minimal  $p_T$  28 GeV*

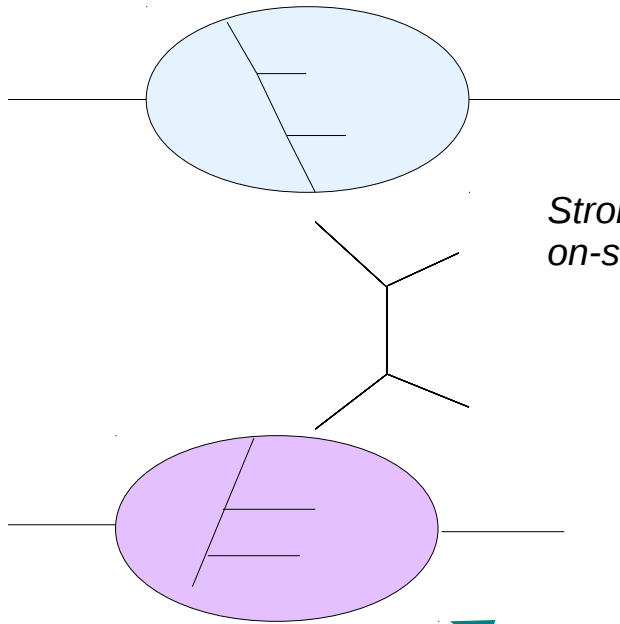
*both jets are forward  $\rightarrow 4 > y > 2.7$*

*central region*

*From: Piotr Kotko  
LxJet*

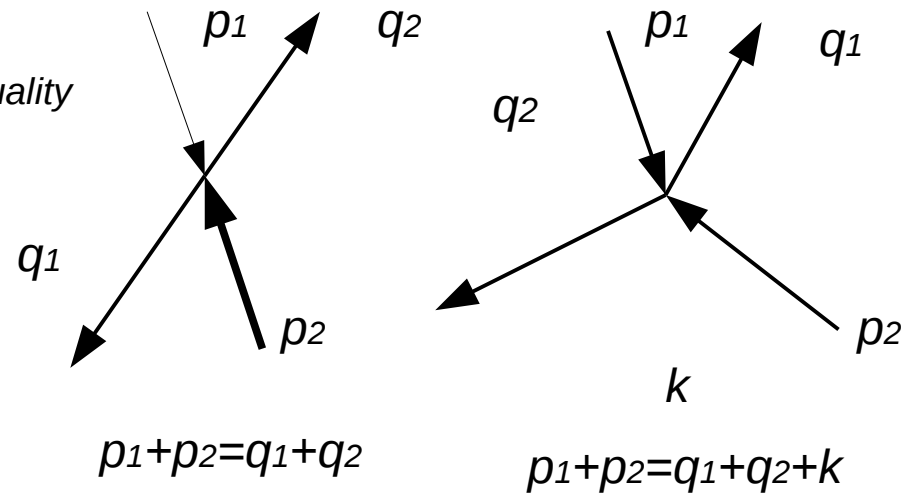
*There is certain class of processes where one can assume that partons in one of hadrons are just collinear with hadron and in other are not*

# QCD at high energies – hybrid factorization



Strongly decreasing in virtuality  
on-shell partons large  $x$

Strongly decreasing  
in longitudinal momentum  
fractions of off-shell partons



$$\frac{d\sigma_{\text{SPS}}^{P_1 P_2 \rightarrow \text{dijets} + X}}{dy_1 dy_2 dp_{1t} dp_{2t} d\Delta\phi} = \frac{p_{1t} p_{2t}}{8\pi^2 (x_1 x_2 s)^2} \sum_{a,c,d} x_1 f_{a/P_1}(x_1, \mu^2) |\overline{\mathcal{M}}_{ag^* \rightarrow cd}|^2 \mathcal{F}_{g/P_2}(x_2, k_t^2) \frac{1}{1 + \delta_{cd}}$$

New helicity based methods for ME

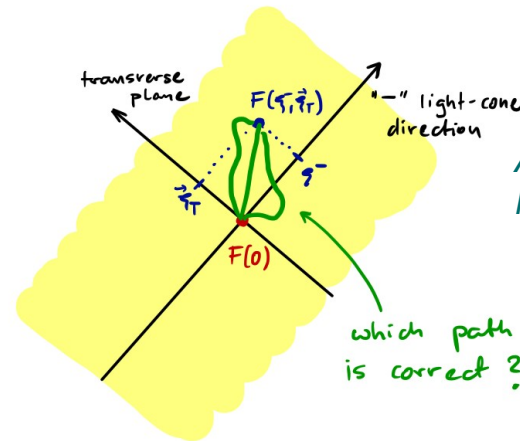
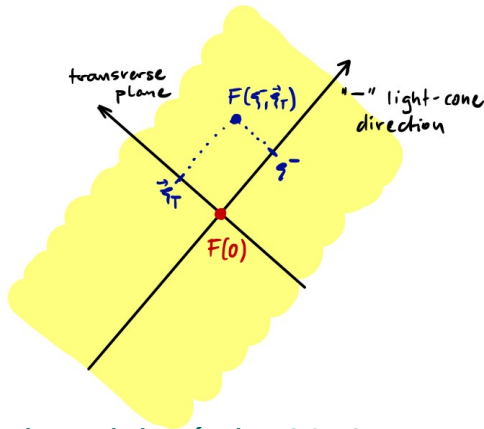
Kotko, K.K, van Hameren, '12

# Definition of TMD – gauge links

The formula for HEF is strictly valid for large transverse momentum and is kind of conjectured. The gluon density is defined in terms of evolution equation. Recent developments with formal approaches start from definition of what parton density is.

$$\mathcal{F}(x, k_T) = 2 \int \frac{d\xi^- d^2\xi_T}{(2\pi)^3 P^+} e^{ixP^+\xi^- - i\vec{k}_T \cdot \vec{\xi}_T} \langle P | \text{Tr} \left\{ \hat{F}^{i+}(0) \hat{F}^{i+}(\xi^+ = 0, \xi^-, \vec{\xi}_T) \right\} | P \rangle$$

naive definition of gluon distribution



A. Belitsky, X. Ji, F. Yuan  
Nucl.Phys. B656 (2003) 165-198

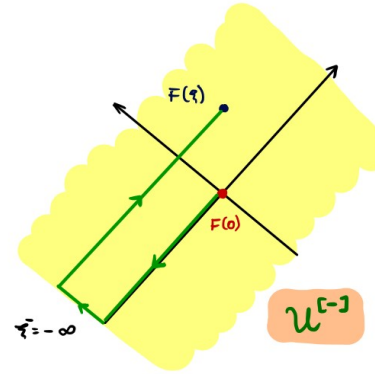
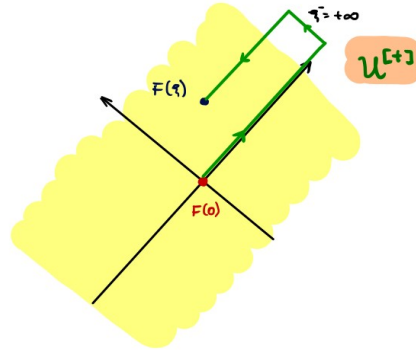
from P. Kotko, Białasówka 2019

One needs also gauge link which accounts for exchange of collinear gluons between the soft and hard parts

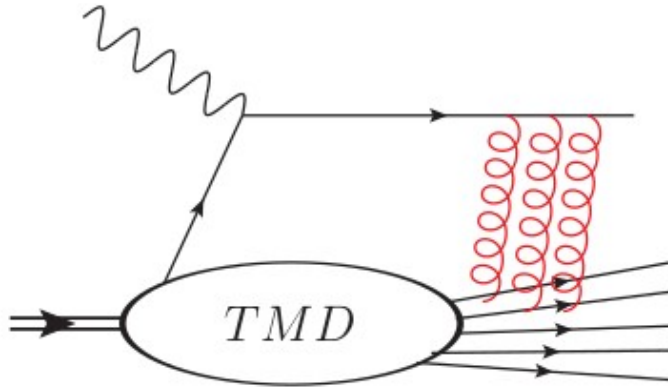
$$\mathcal{F}(x, k_T) = 2 \int \frac{d\xi^- d^2\xi_T}{(2\pi)^3 P^+} e^{ixP^+\xi^- - i\vec{k}_T \cdot \vec{\xi}_T} \langle P | \text{Tr} \left\{ \hat{F}^{i+}(0) \mathcal{U}_{C_1} \hat{F}^{i+}(\xi) \mathcal{U}_{C_2} \right\} | P \rangle$$

# Definition of TMD – gauge links

Two basic structures arise:

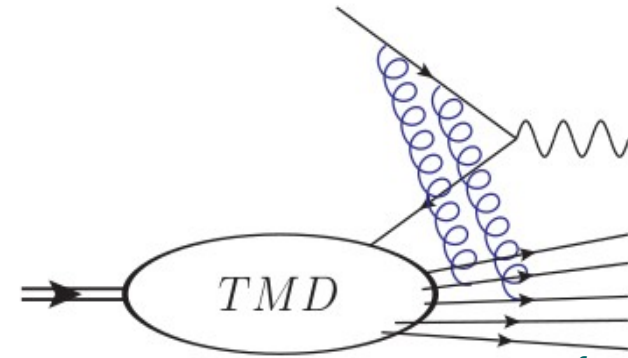


Semi Inclusive DIS



final state interactions

Drell-Yan



initial state interactions

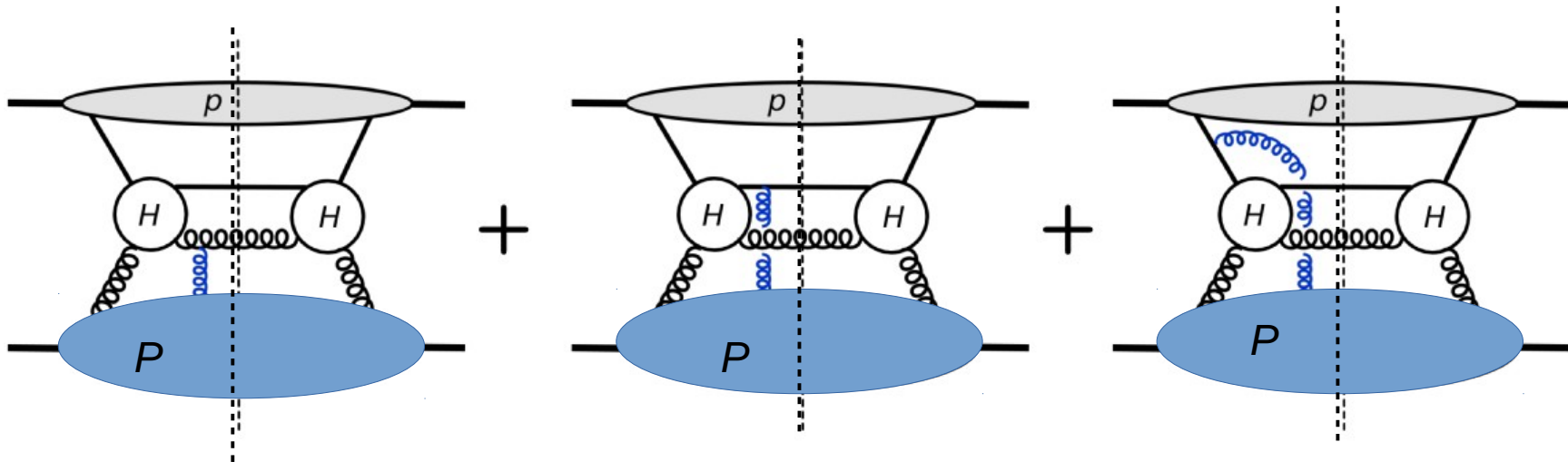
from R. Boussarie  
Initial Stages 2019

$$\Phi_q^{[+]}(x, p_T) = \int \frac{d(\xi \cdot P) d^2 \xi_T}{(2\pi)^3} e^{ip \cdot \xi} \langle H | \bar{\psi}(0) \mathcal{U}^{[+]} \psi(\xi) | H \rangle$$

C.J. Bomhof, P.J. Mulders, F. Pijlman  
Eur.Phys.J. C47 (2006) 147-162

$$\mathcal{U}^{[\pm]} = U_{[(0^-, \mathbf{0}_T); (\pm\infty^-, \mathbf{0}_T)]} U_{[(\pm\infty^-, \mathbf{0}_T); (\pm\infty^-, \infty_T)]} U_{[(\pm\infty^-, \infty_T); (\pm\infty^-, \xi_T)]} U_{[(\pm\infty^-, \xi_T); (\xi^-, \xi_T)]}$$

# Gauge links and dijets



+ similar diagrams with 2,3,...gluon exchanges.

All this need to be resummed

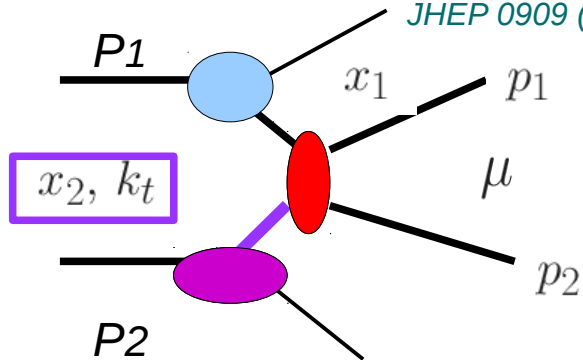
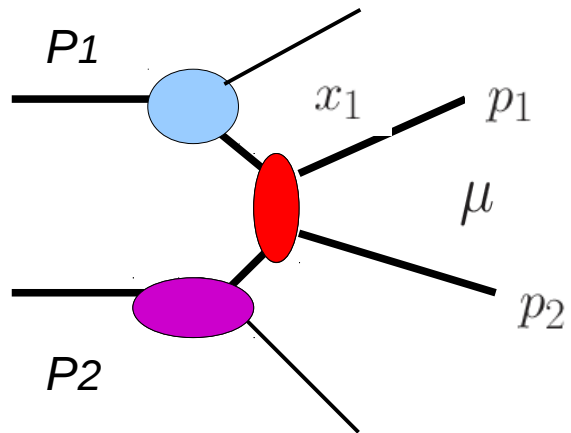
C.J. Bomhof, P.J. Mulders, F. Pijlman  
Eur.Phys.J. C47 (2006) 147-162

$$\mathcal{F}(x, k_T) = 2 \int \frac{d\xi^- d^2\xi_T}{(2\pi)^3 P^+} e^{ixP^+\xi^- - i\vec{k}_T \cdot \vec{\xi}_T} \langle P | \text{Tr} \left\{ \hat{F}^{i+}(0) \mathcal{U}_{C_1} \hat{F}^{i+}(\xi) \mathcal{U}_{C_2} \right\} | P \rangle$$

Hard part defines the path of the gauge link  $\mathcal{U}^{[C]}(\eta; \xi) = \mathcal{P} \exp \left[ -ig \int_C dz \cdot A(z) \right]$

# Improved Transversal Momentum Dependent Factorization

$$\frac{d\sigma_{\text{SPS}}^{P_1 P_2 \rightarrow \text{dijets} + X}}{dy_1 dy_2 dp_{1t} dp_{2t} d\Delta\phi} = \frac{p_{1t} p_{2t}}{8\pi^2 (x_1 x_2 s)^2} \sum_{a,c,d} x_1 f_{a/P_1}(x_1, \mu^2) |\overline{\mathcal{M}}_{ag^* \rightarrow cd}|^2 \mathcal{F}_{g/P_2}(x_2, k_t^2) \frac{1}{1 + \delta_{cd}}$$



A, Dumitru, A. Hayashigaki J. Jalilian-Marian  
Nucl.Phys. A765 (2006) 464-482 M. Deak,  
F. Hautmann, H. Jung, K. Kutak  
JHEP 0909 (2009) 121

Generalization of hybrid formula but no  $k_t$  in ME

Fabio Dominguez, Bo-Wen Xiao, Feng Yuan  
Phys.Rev.Lett. 106 (2011) 022301

F. Dominguez, C. Marquet, Bo-Wen Xiao, F. Yuan  
Phys.Rev. D83 (2011) 105005

Appropriate in back-to-back configuration

Using HEF motivated sum over polarization  
for low  $x$  gluons we included  $k_t$  in ME

Conjecture P. Kotko K. Kutak, C. Marquet, E. Petreska, S. Sapeta,  
A. van Hameren, JHEP 1509 (2015) 106

Appropriate in any configuration

gauge invariant amplitudes with  $k_t$  and TMDs

Example for  $g^* g \rightarrow g g$

$$\frac{d\sigma^{pA \rightarrow ggX}}{d^2 P_t d^2 k_t dy_1 dy_2} = \frac{\alpha_s^2}{(x_1 x_2 s)^2} x_1 f_{g/p}(x_1, \mu^2) \sum_{i=1}^6 \mathcal{F}_{gg}^{(i)} H_{gg \rightarrow gg}^{(i)}$$

Can be obtained from CGC

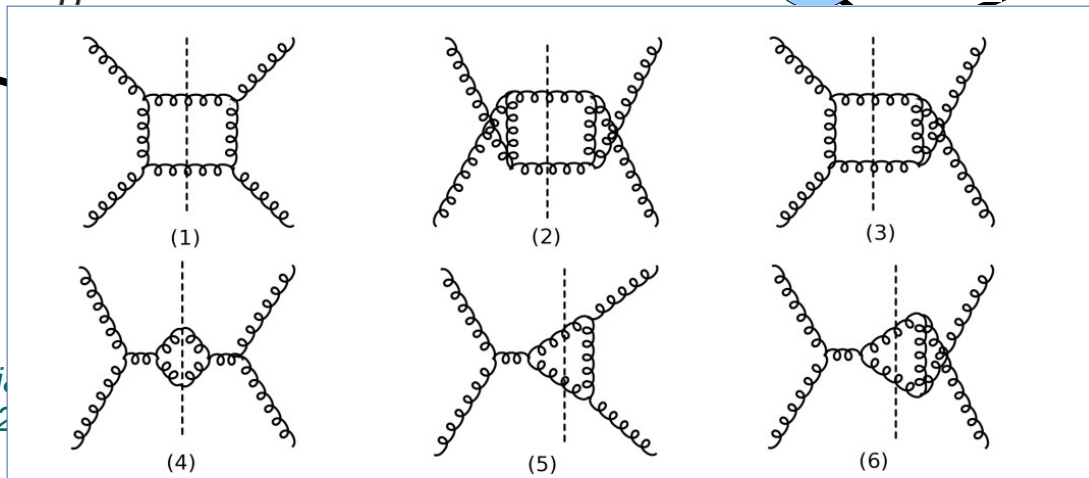
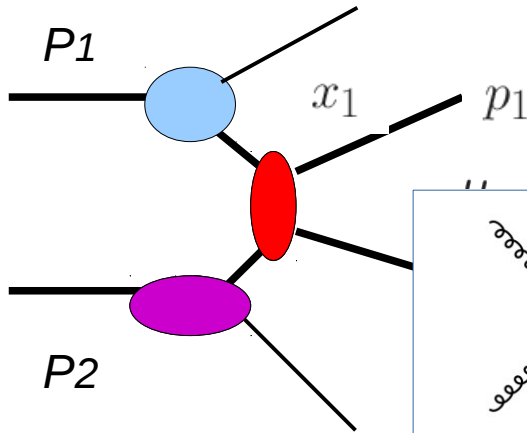
T. Altinoluk, R. Boussarie, Piotr Kotko JHEP 1905 (2019) 156



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 F. Hautmann, H. Jung, K. Kutak  
 JHEP 0909 (2009) 121



$p_2$   
 or polarization  
 in ME

Generalization of hybrid  
 ME  
 Fabio Dominguez, Bo-Wen Xi  
 Phys.Rev.Lett. 106 (2011) 022

F. Dominguez, C. Marquet, Bo  
 Phys.Rev. D83 (2011) 105005

Appropriate in back-to-back configuration

A. van Hameren, JHEP 1509 (2015) 106

Appropriate in any configuration

gauge invariant amplitudes with  $k_t$  and TMDs

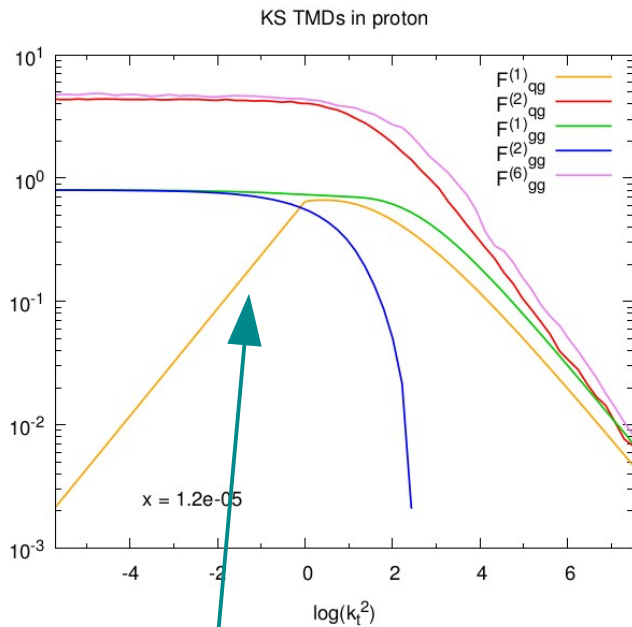
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# Plots of ITMD gluons



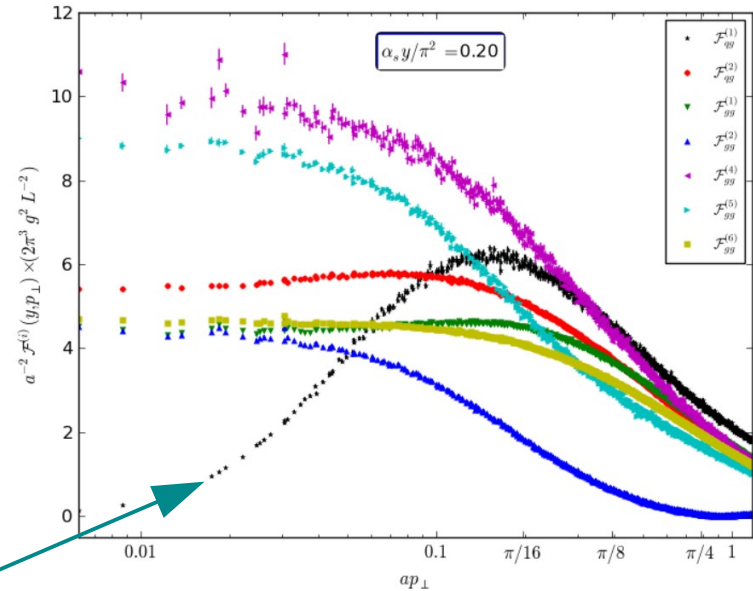
Calculation – in large  $N_c$  approximation with analytic model for dipole gluon density – all gluons can be calculated from the dipole one. KS gluon used.

Kotko, K.K, Marquet, Petreska, Sapeta, van Hameren  
 JHEP 1612 (2016) 034

**Standard HEF gluon density**

The other densities are flat at low  $k_t \rightarrow$  less saturation

Not negligible differences at large  $k_t \rightarrow$  differences at small angles

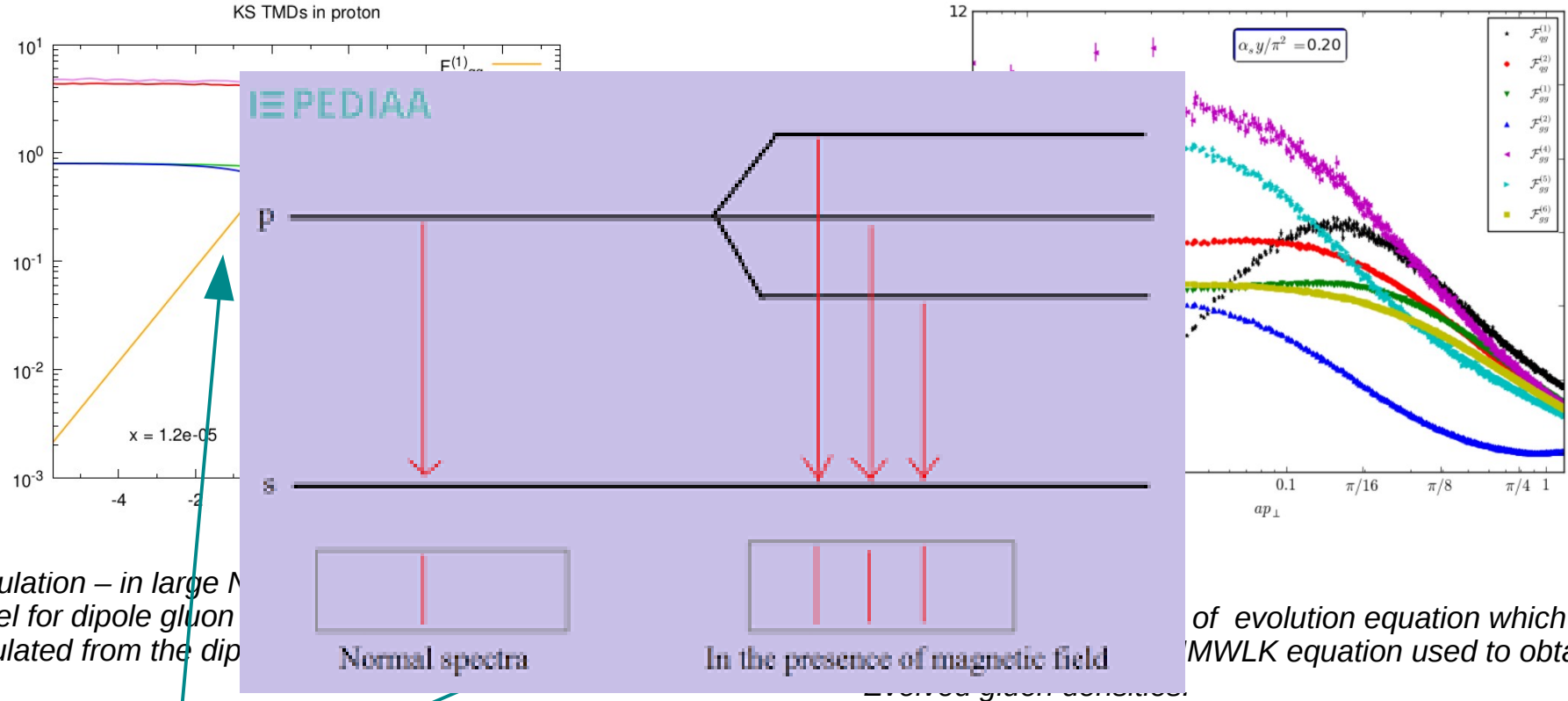


Obtained from solutions of evolution equation which accounts for finite  $N_c$ . JIMWLK equation used to obtain Evolved gluon densities.

The JIMWLK equation is a renormalization group equation for the Wilson lines, obtained by integrating out the quantum fluctuations at smaller and smaller Bjorken- $x$ .  
 C. Marquet, E. Petreska, C. Roiesnel  
 JHEP 1610 (2016) 065

# Plots of ITMD gluons

rough analogy to splitting of spectral lines  
in presence of a new scale



Calculation – in large  $N_c$  model for dipole gluon calculated from the dip

Kotko, K.K, Marquet, Petreska, Sapeta, van Hameren  
JHEP 1612 (2016) 034

Standard HEF gluon density

The other densities are flat at low  $k_t \rightarrow$  less saturation

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of evolution equation which MWLK equation used to obtain

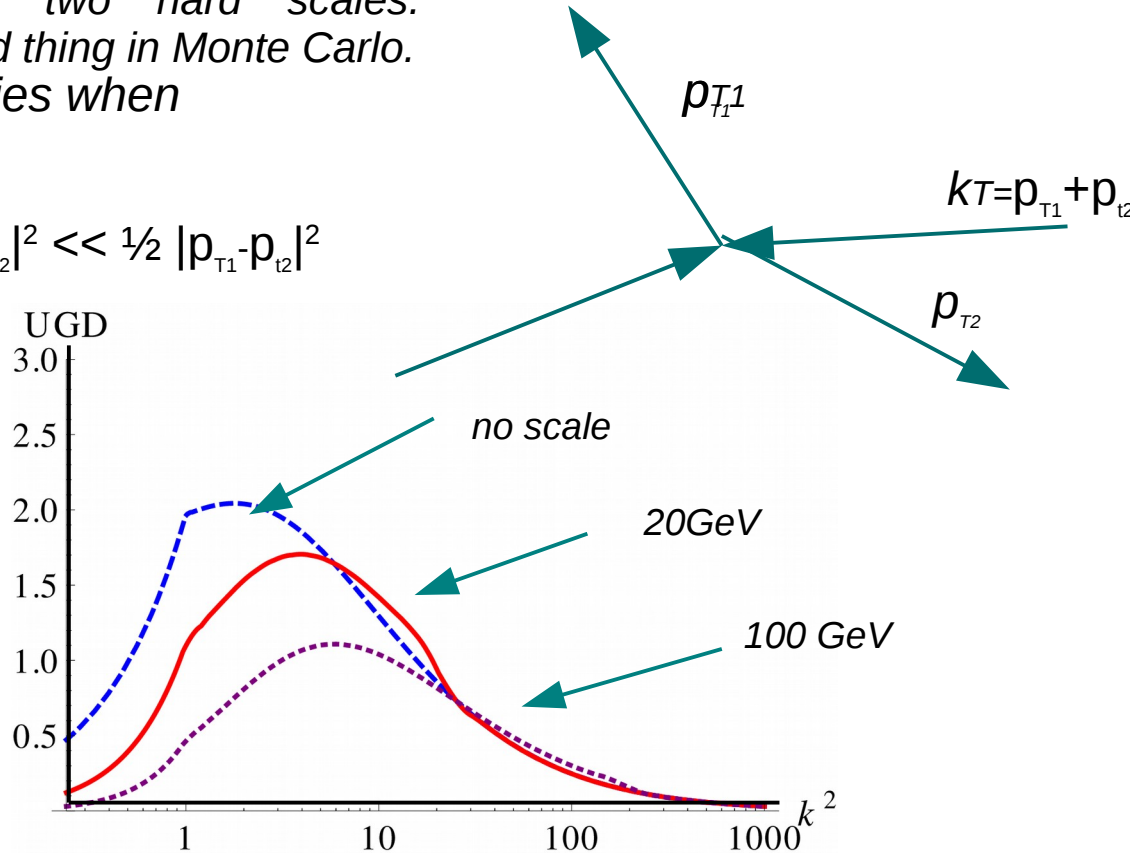
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# Forward physics and Sudakov form factor

Sudakov - no emission probability between two hard scales.  
Standard thing in Monte Carlo.  
Applies when

$$|p_{T1} + p_{T2}|^2 \ll \frac{1}{2} |p_{T1} - p_{T2}|^2$$

Low  $kt$  gluons are suppressed. The conservation of probability leads to change of shape of gluon density which depends on the hard scale



A. H. Mueller, Bo-Wen Xiao, Feng Yuan  
Phys.Rev.Lett. 110 (2013) no.8, 082301

Phys. Rev. D 88, 114010 (2013)  
A. H. Mueller, Bo-Wen Xiao, Feng Yuan

Phys.Lett. B737 (2014) 335-340  
A. van Hameren, P. Kotko, K. Kutak, S. Sapeta

K. Kutak  
Phys.Rev. D91 (2015) no.3, 034021

I. Balitsky, A. Tarasov  
JHEP 1510 (2015) 017

A.H. Mueller, Lech Szymanowski,  
Samuel Wallon, Bo-Wen Xiao, Feng Yuan  
JHEP 1603 (2016) 096

Nucl.Phys. B921 (2017) 104-126  
B. Xiao, F. Yuan, J. Zhou.

$$T_s(\mu^2, k^2) = \exp \left( - \int_{k^2}^{\mu^2} \frac{dk'^2}{k'^2} \frac{\alpha_s(k'^2)}{2\pi} \sum_{a'} \int_0^{1-\Delta} dz' P_{a'a}(z') \right)$$

Motivated by Catani, Ciafaloni, Fiorani Marchesini and  
Kwiecinski, Kimber, Martin, Stasto.

# Sudakov form factor

The relevance in low x physics at linear level recognized by:

Catani, Ciafaloni, Fiorani, Marchesini;  
Kimber, Martin, Ryskin;  
Collins, Jung

Sudakov - no emission probability. Resumes unresolved real and virtual emissions. Standard thing in Monte Carlo.

Comes from misscancelation of virtual and real diagrams

$\mu$  and  $k_t$

$\mu$

hard scale

Survival probability of the gap without emissions

A. H. Mueller, Bo-Wen Xiao, Feng Yuan  
Phys.Rev.Lett. 110 (2013) no.8, 082301

Phys. Rev. D 88, 114010 (2013)  
A. H. Mueller, Bo-Wen Xiao, Feng Yuan

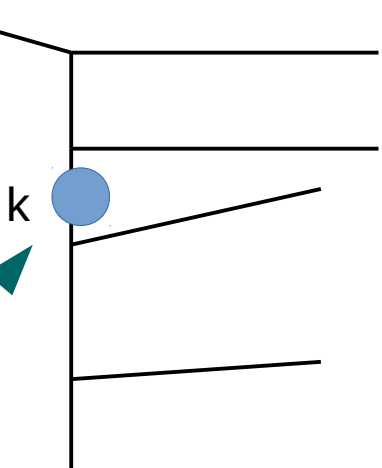
Phys.Lett. B737 (2014) 335-340  
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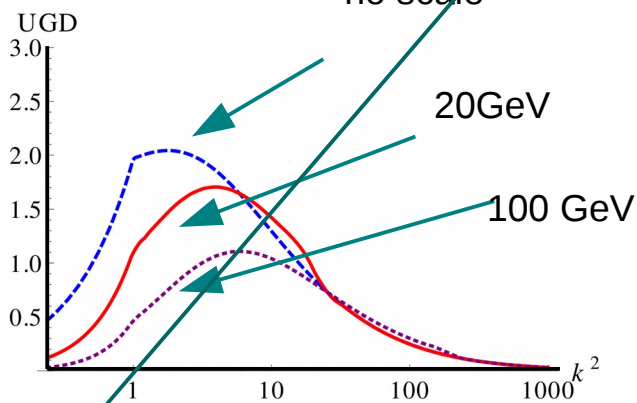
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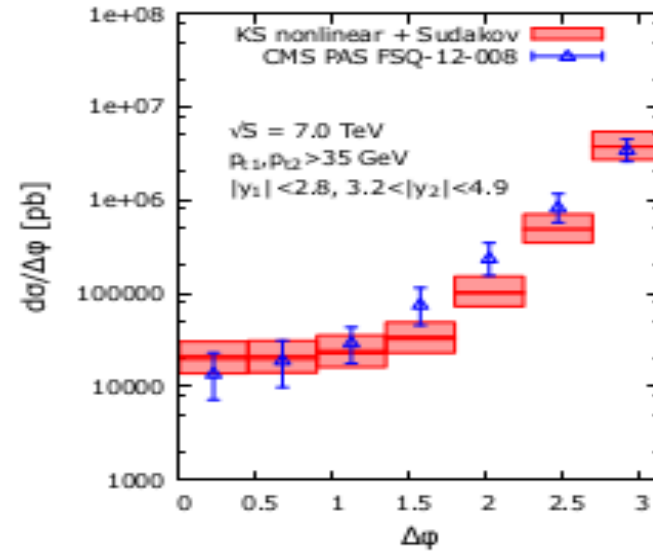
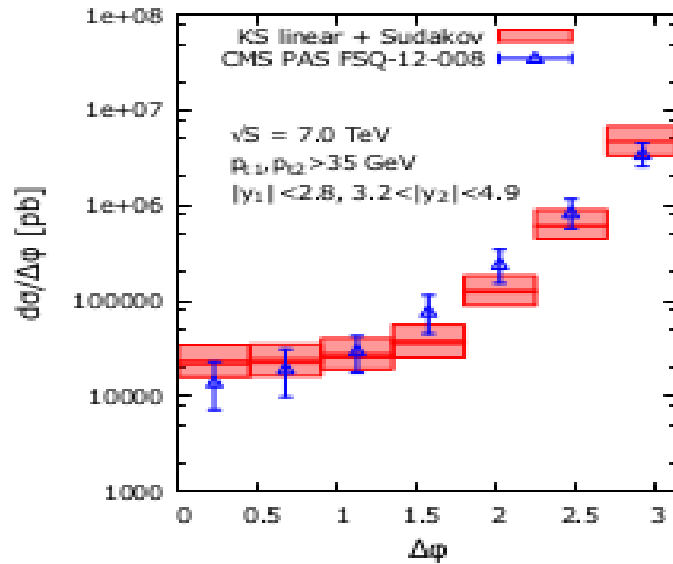


no scale

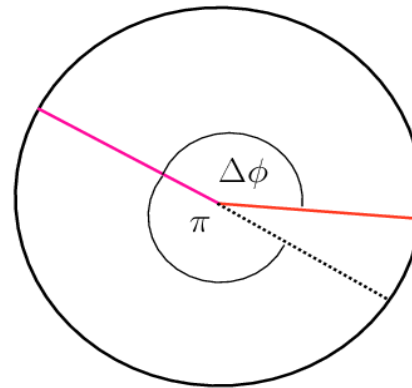
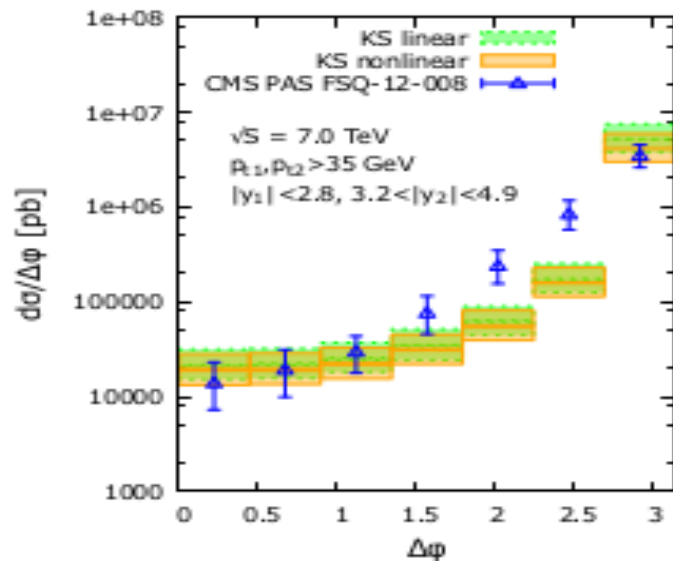


$$T_s(\mu^2, k^2) = \exp \left( - \int_{k^2}^{\mu^2} \frac{dk'^2}{k'^2} \frac{\alpha_s(k'^2)}{2\pi} \sum_{a'} \int_0^{1-\Delta} dz' P_{a'a}(z') \right)$$

# Decorelations inclusive scenario-central forward

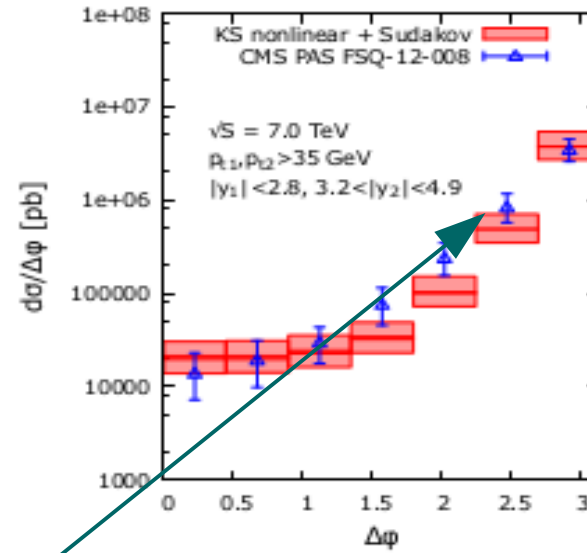
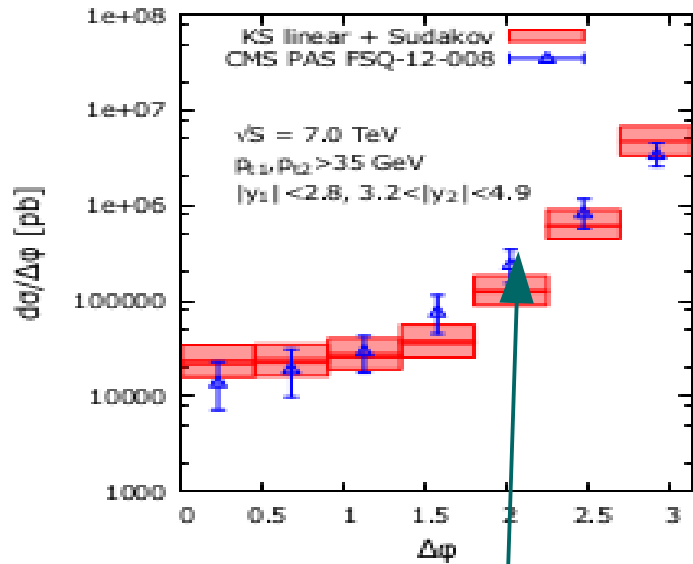


No saturation...  
visible Sudakov effects

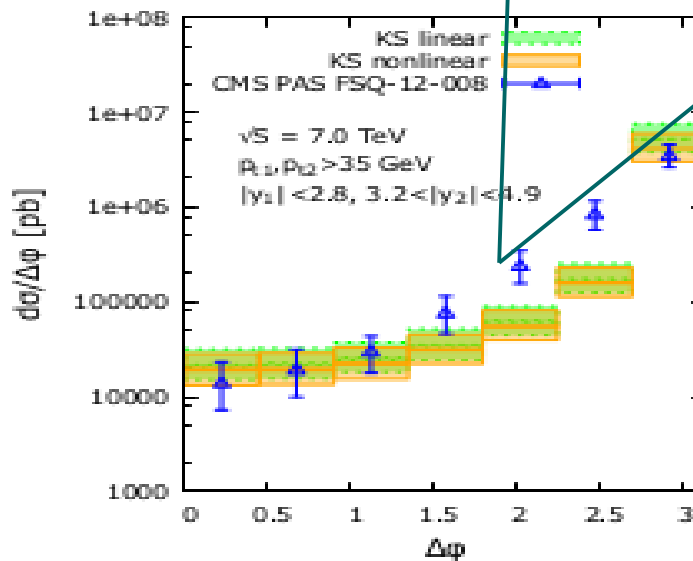


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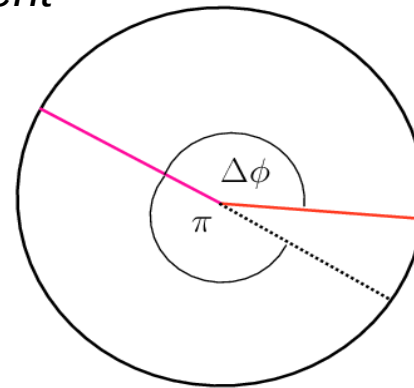
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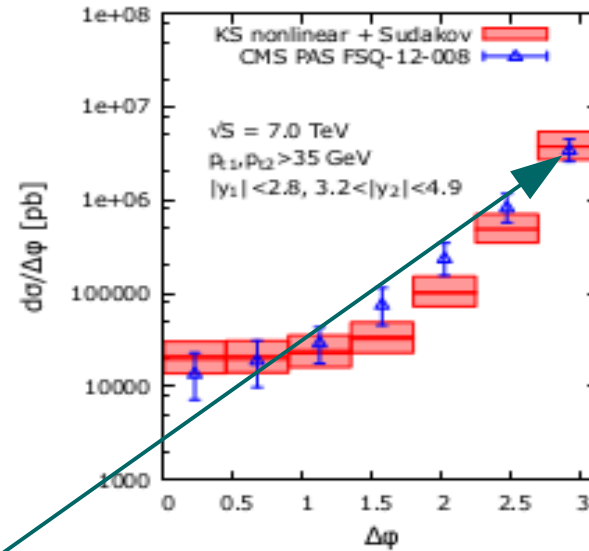
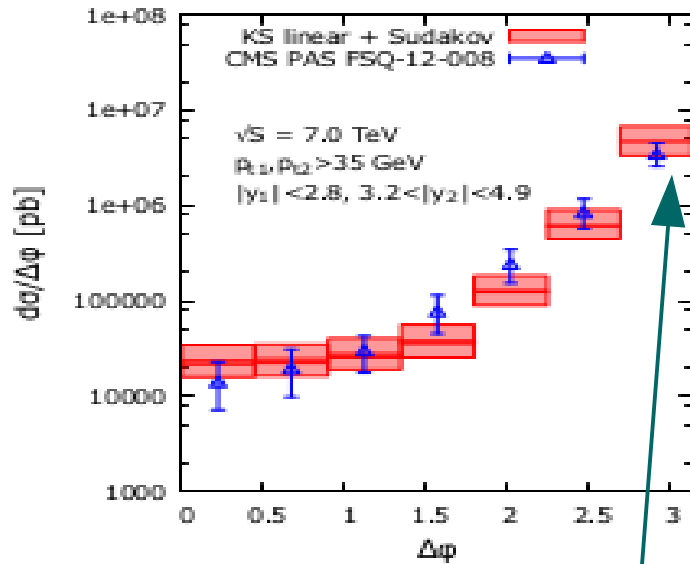
enhancement



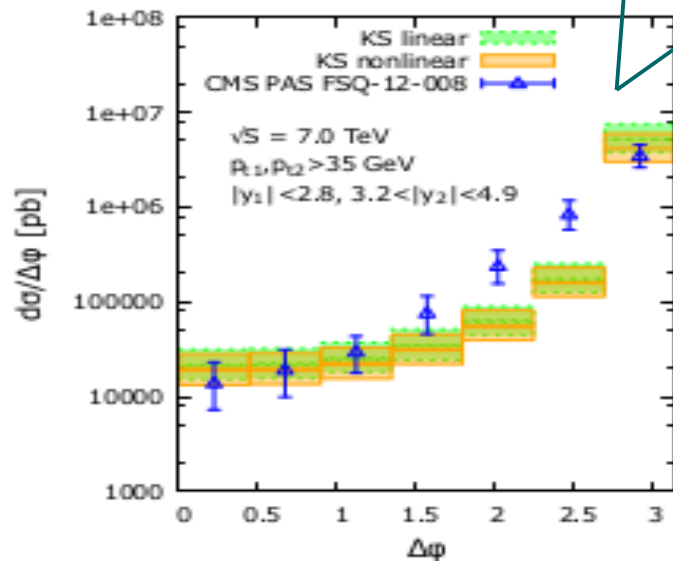
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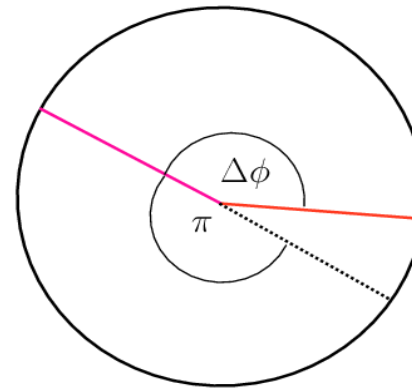
# Decorelations inclusive scenario-central forward



No saturation...  
visible Sudakov effects

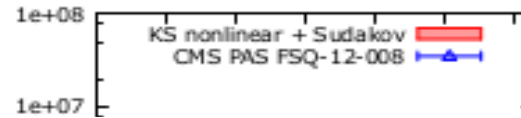
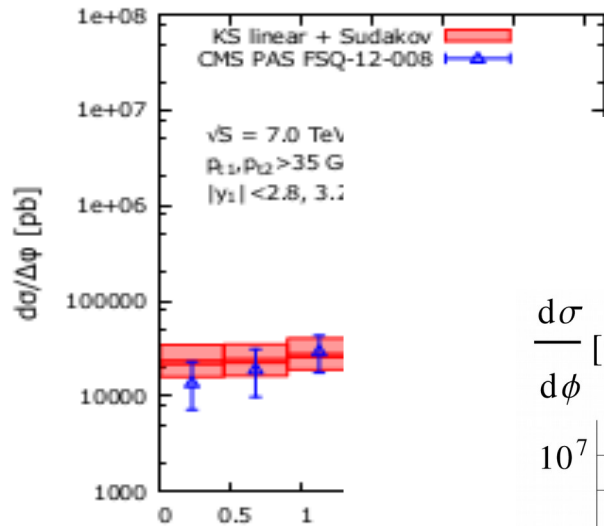


suppression

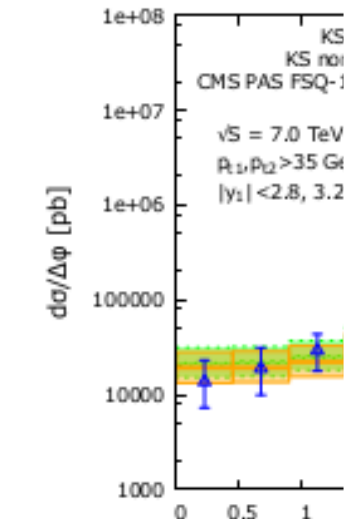




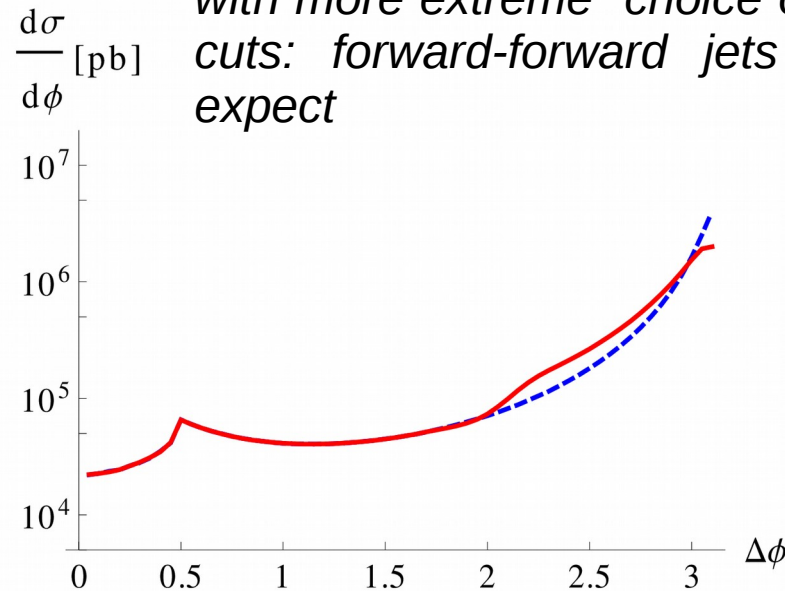
# Decorelations inclusive scenario



No saturation...  
visible Sudakov effects



with more extreme choice of rapidity cuts: forward-forward jets we can expect



K. Kutak  
Phys.Rev. D91 (2015) no.3, 034021

## *Forward-forward dijets- elements going into our prediction*

*The ITMD gluon's were obtained using:*

*Proton's KS gluon density – fitted to  $F_2$  proton HERA data Balitsky-Kovchegov equation + kinematical constraint + subleading in low  $x$ , low  $z$  parts of splitting function.*

*Lead's KS gluon density – normalized to number of nucleons. Modified radius as compared to proton's radius*

*The Sudakov:*

*It has been was obtained from exponentiation of DGLAP splitting function*

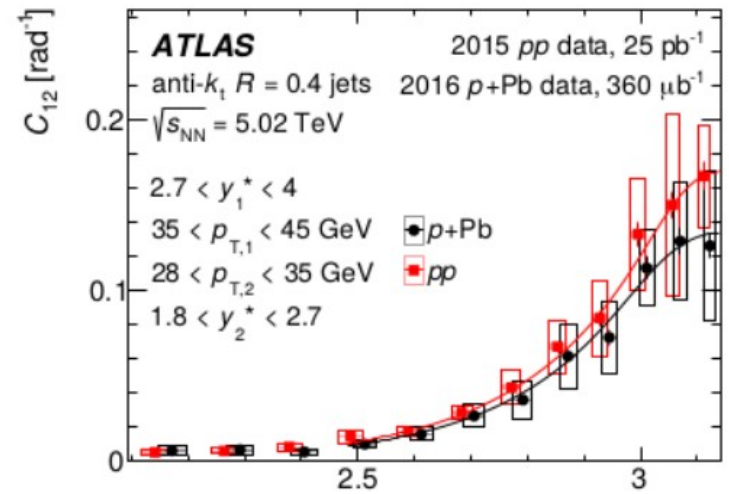
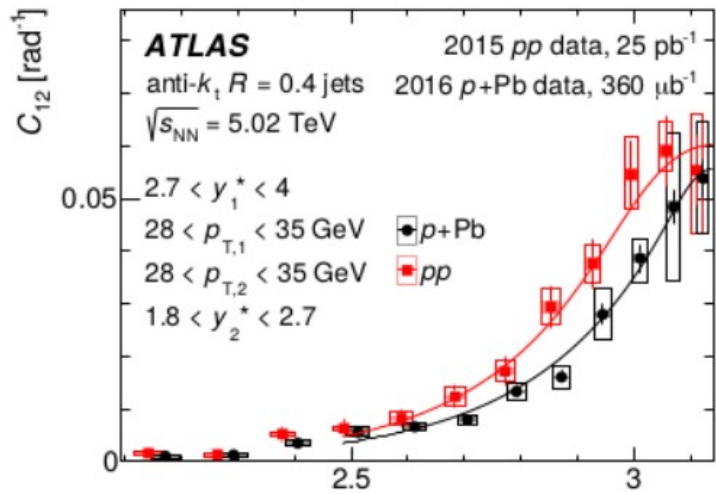
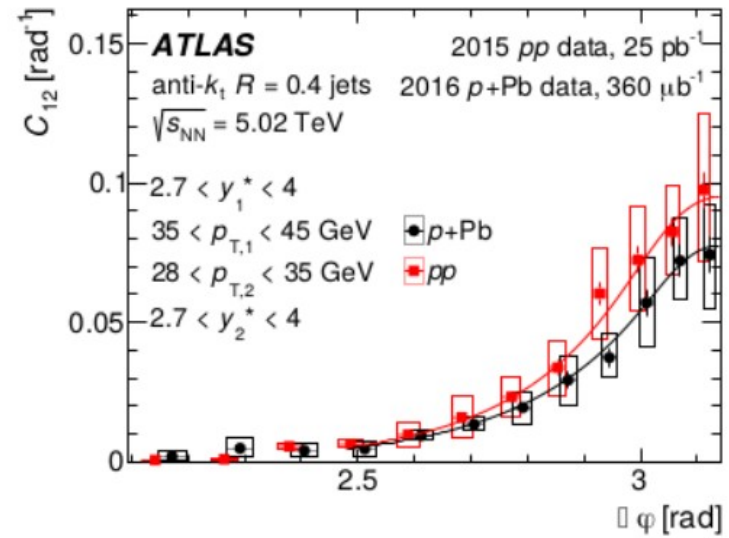
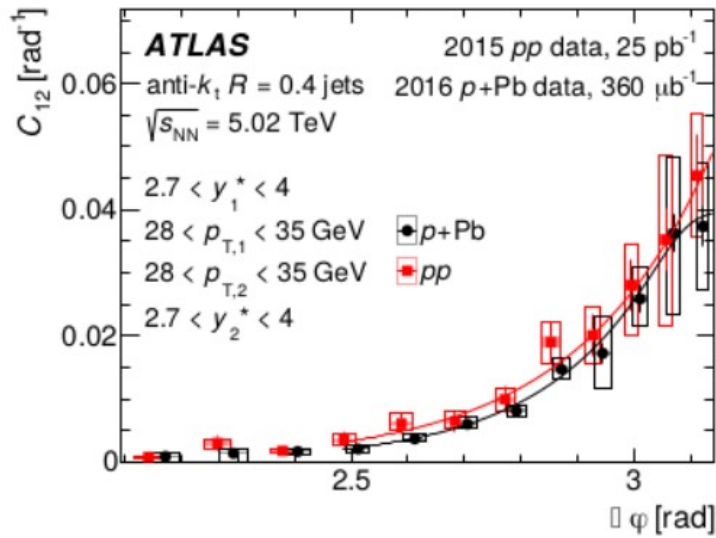
*Total cross section is unchanged. Cross section at large angles is suppressed. Events with moderate angles are enhanced.*

*The cross section:*

*was calculated using:*

- KaTie Monte Carlo (van Hameren Comput.Phys.Comm. 224 (2018) 371-380 )  
- MC for p-p, p-A, soon DIS and A-A, calculates  
matrix elements in kt factorization and ITMD, matrix elements agree with the once obtained  
from Lipatov effective action. Via merging with CASCADE accounts for ISR and FSR*
- cross-checked with LxJet Monte Carlo (Piotr Kotko) – dedicated MC for jets in kt factorization*

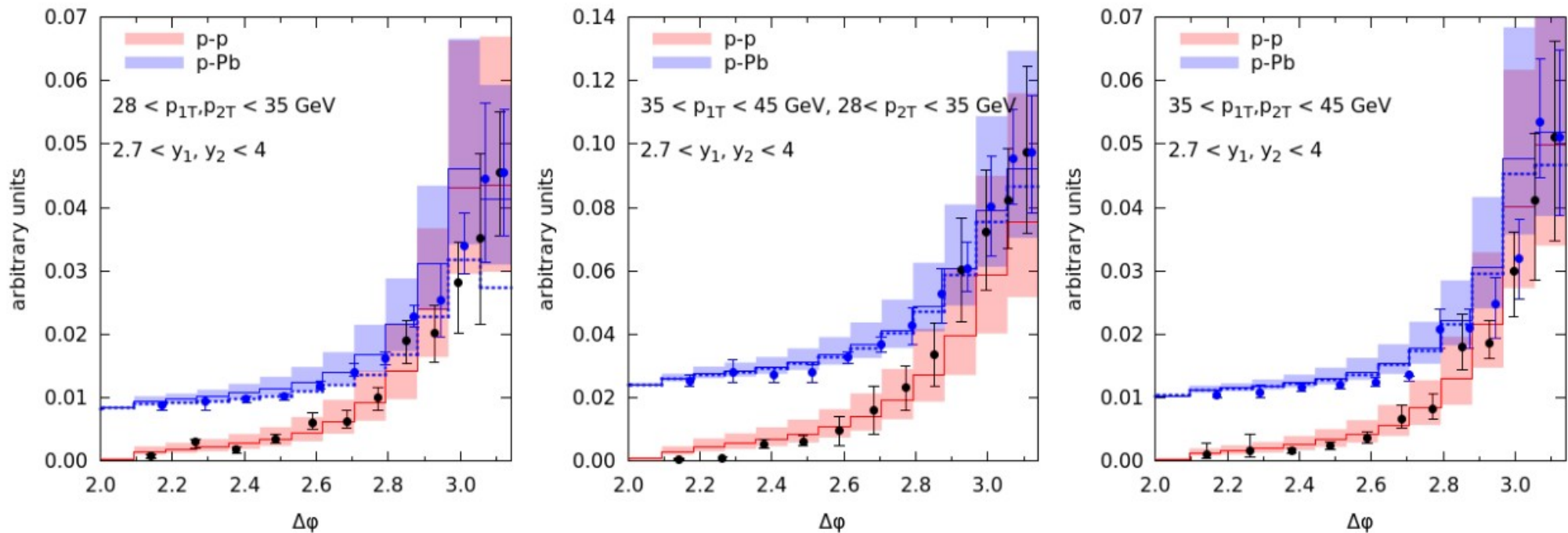
# Data



# Signature of broadening in forward-forward dijets

ATLAS Phys.Rev. C100 (2019) no.3, 034903

A. Hameren, P. Kotko, K. Kutak, S. Sapeta  
Phys.Lett. B795 (2019) 511-515



Data: number of dijets normalized to number of single inclusive jets. We can not calculate that. We can compare shapes.

Procedure: fit normalization to p-p data.

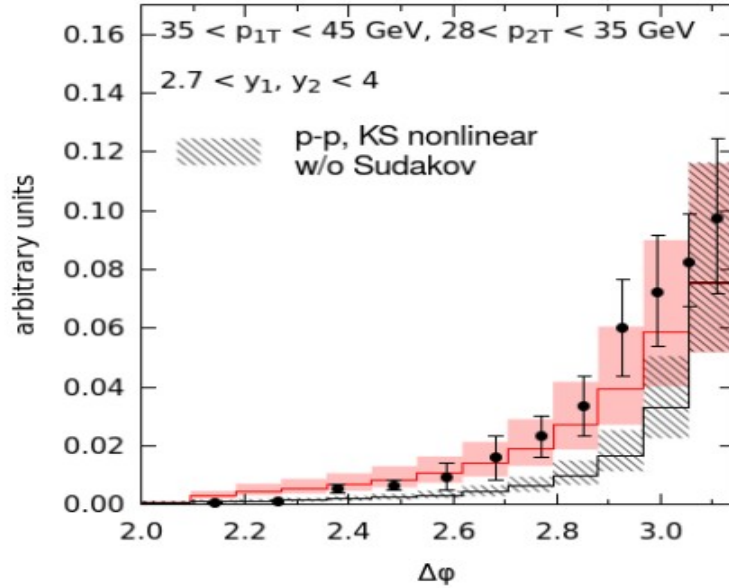
Use that both for p-p and p-Pb. Shift p-Pb data

The procedure allows for visualization of broadening

# Other approaches

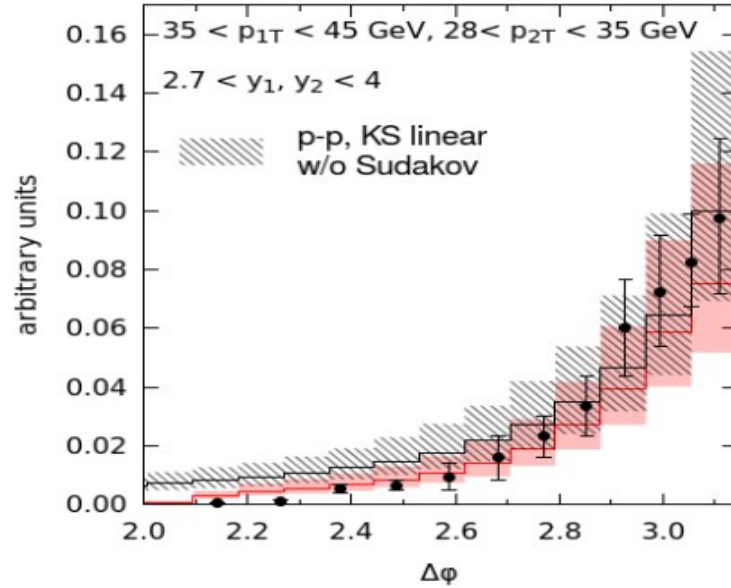
*nonlinearity  
no Sudakov*

*too narrow  
distribution*



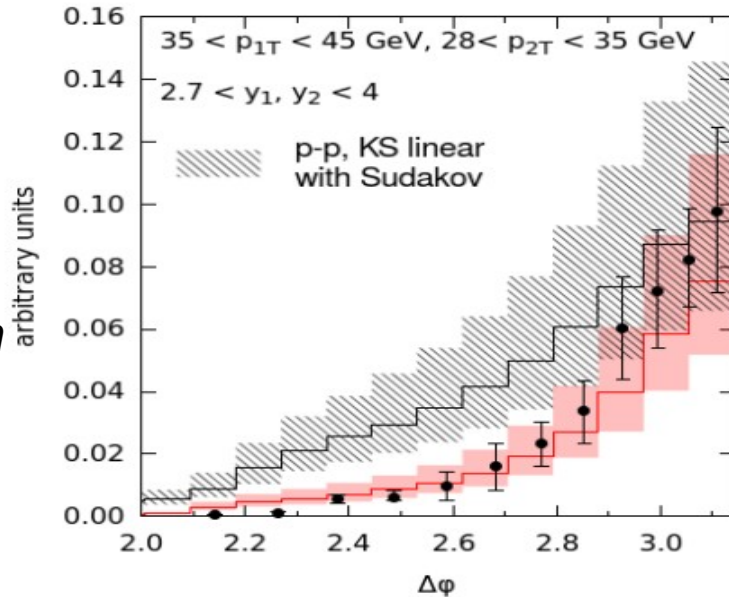
*linear  
no Sudakov*

*not too bad  
but  
different  
shape*



*linear*

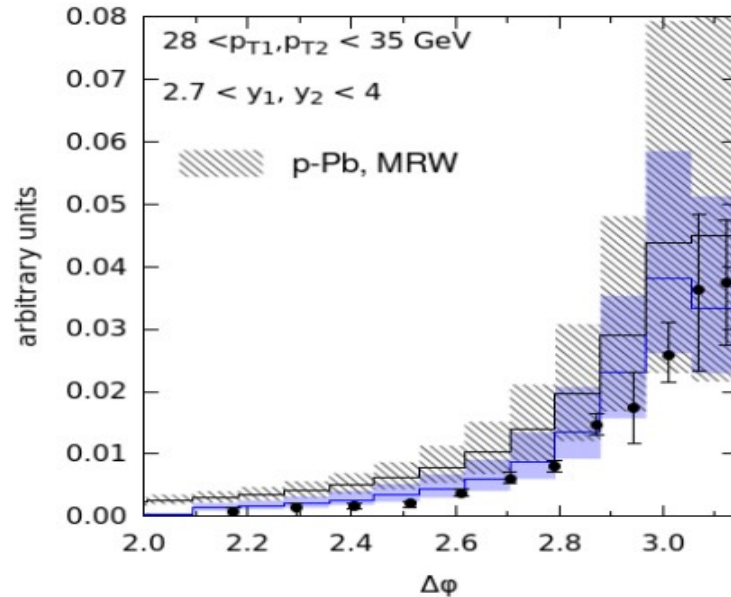
*too wide  
Sudakov  
acts too much*



*Linear +  
Sudakov*

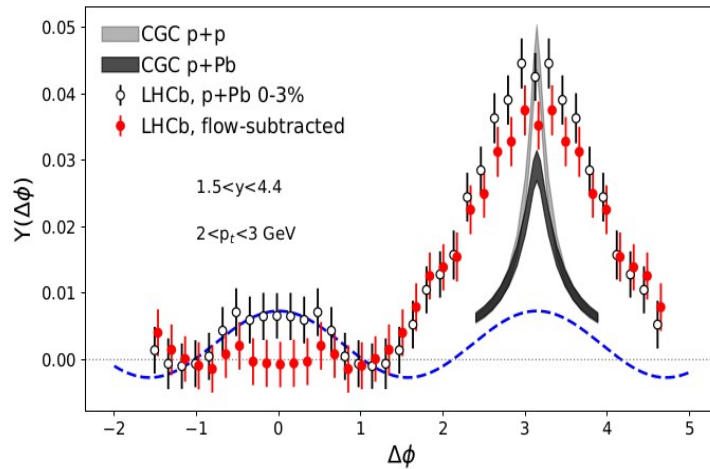
*Ordering in  
 $k_t$*

*not too bad  
but different  
shape*





# Other calculations which support our result - di-hadrons production

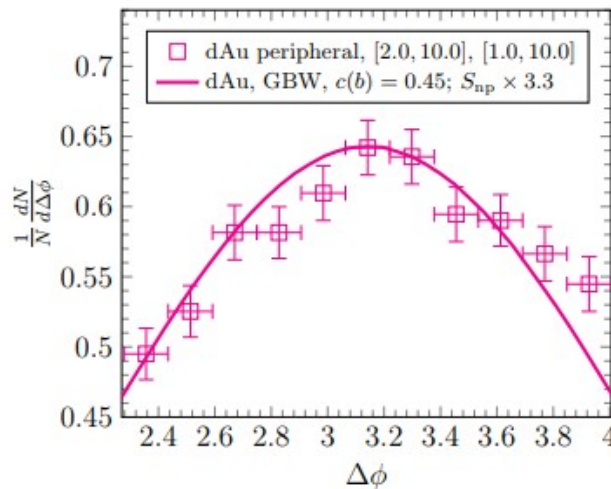
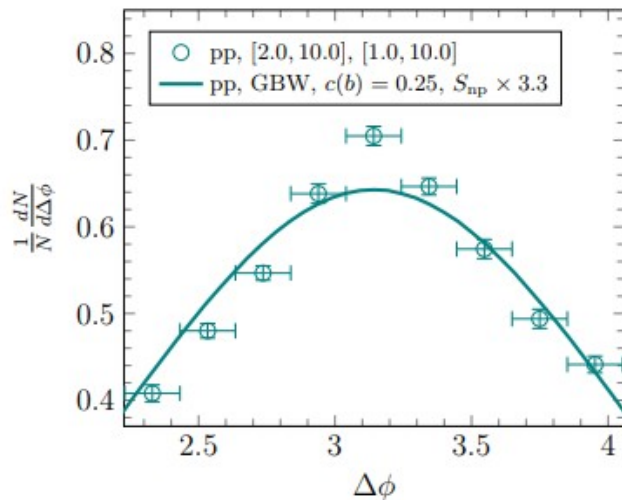


← ITMD, no Sudakov

Expectation:  
Sudakov  
will broaden the distribution

G. Giacalone, C. Marquet, M. Matas  
Phys.Rev. D99 (2019) no.1, 014002

J. Albacete, C. Marquet  
Phys.Rev.Lett. 105 (2010) 162301

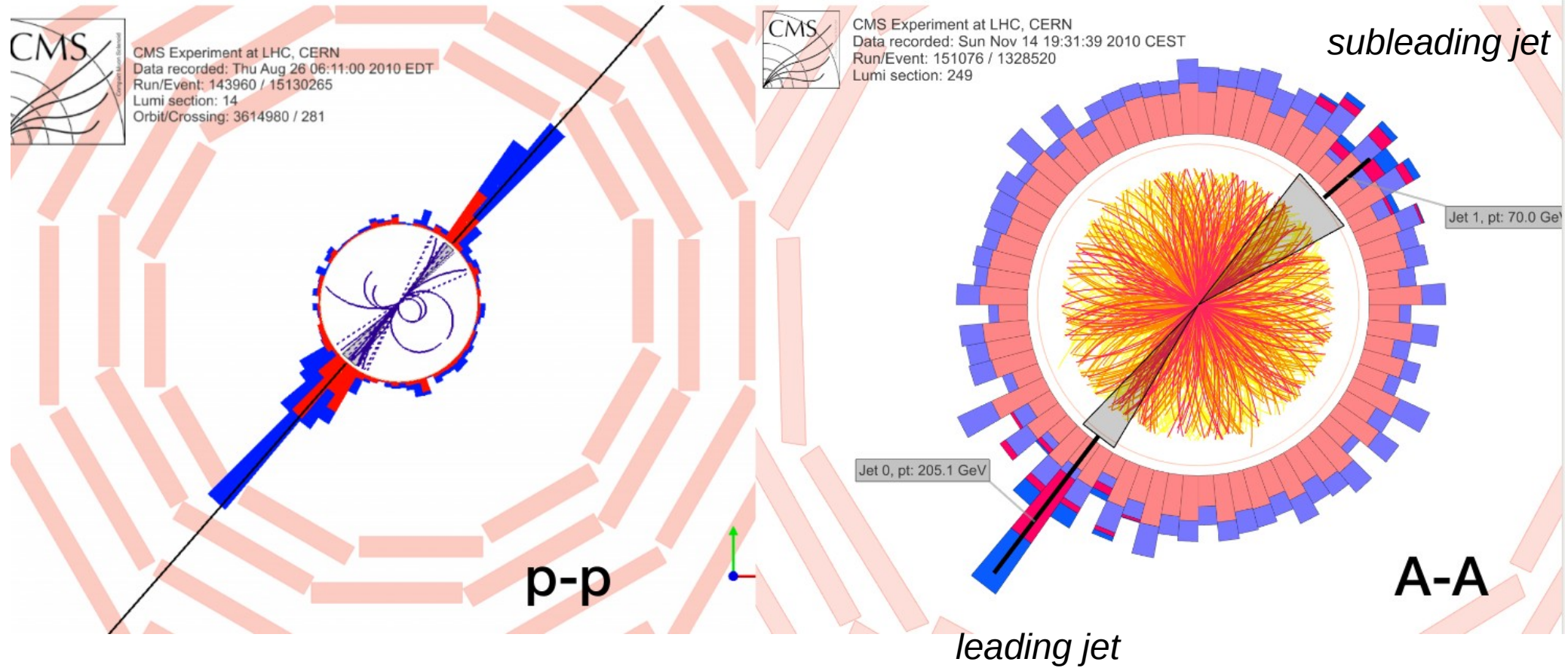


← Correlation limit of CGC  
+ Sudakov no  $k_t$  in ME

A.Stasto, S. Wei, B. Xiao, F. Yuan  
Phys.Lett. B784 (2018) 301-306

*Pb-Pb*

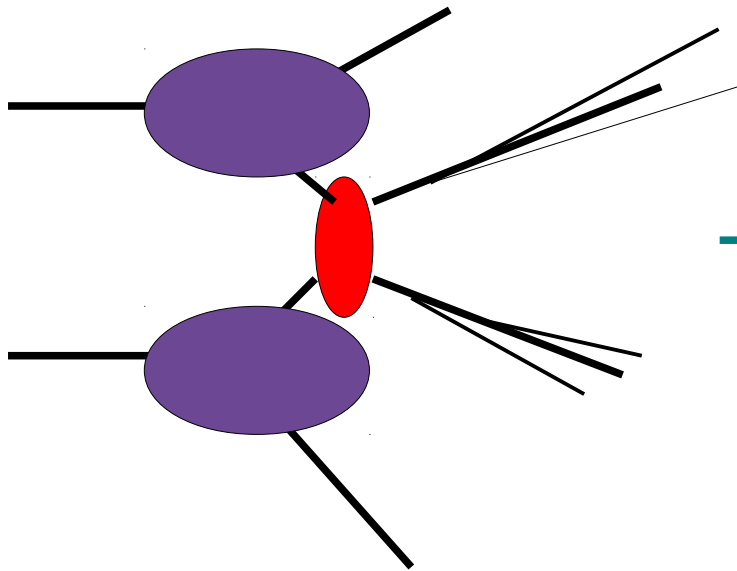
# Jet quenching





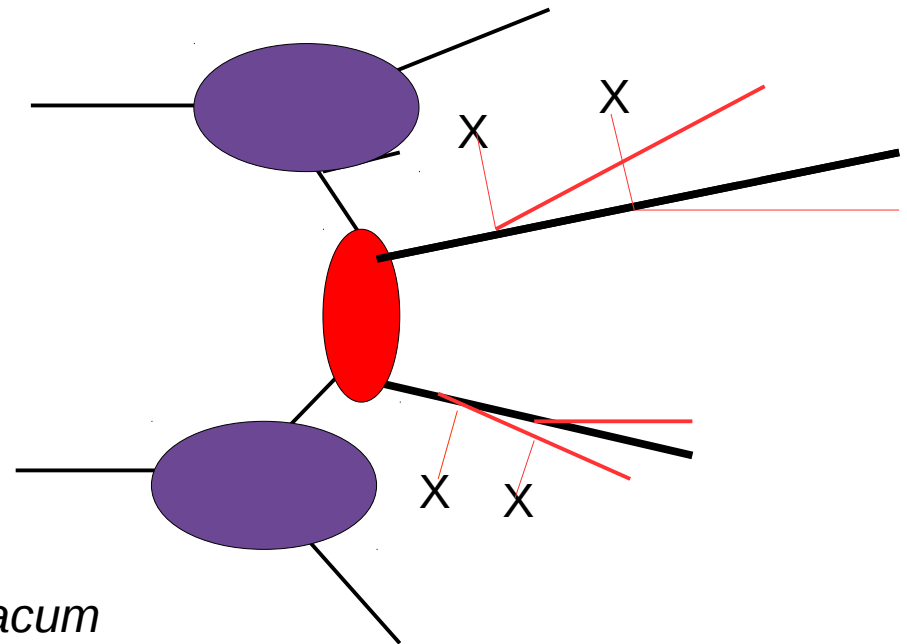
# From vacuum to medium

*vacuum*



*vacuum x-section = ME \* pdf \* fragmentaion in vacuum*

*medium*



*complete x-section = ME \* pdf \* fragmentaion in  
medium +  
ME \* pdf \* fragmentation in vacuum*

## LPM and BDMPS-Z

*Multiple soft scattering resummed to all orders. It is expected to be important for short mean free-path*

*Because medium-induced radiation can occur anywhere along the medium with equal probability, the radiation spectrum is expected to scale linearly with  $L$ .*

*Many scattering centers act coherently during the radiation over time  $t_{\text{coh}}$  ( $\ll t_{\text{mfp}}$ ).*

$$\omega \frac{dI}{d\omega} \simeq \alpha_s \frac{L}{t_{\text{coh}}} = \alpha_s \sqrt{\frac{\omega_c}{\omega}}$$

$$t_{\text{coh}} \equiv \sqrt{\frac{\omega}{\hat{q}}}$$

↑  
energy of observed gluon

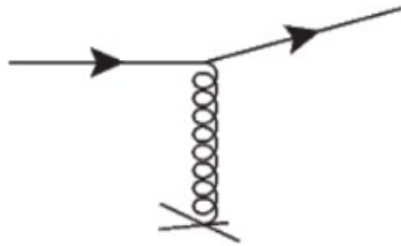
↖  
maximal energy that can be taken by single gluon

$$\omega \frac{dI_{\text{BH}}}{d\omega} \simeq \alpha_s \frac{L}{\ell_{\text{mfp}}} = \alpha_s N_{\text{scatt}}$$

↖  
if  $t_{\text{coh}} \sim t_{\text{mfp}}$  only one scattering is involved in radiation

# Jet medium interaction

scattering...



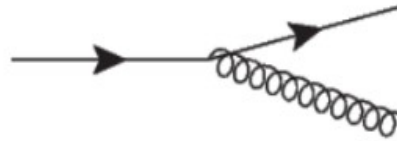
Transverse momentum transfer!

$$p \rightarrow p + k_T$$

Scattering Kernel:  $C(k_T)$

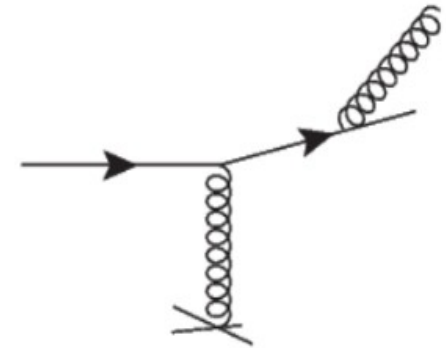
Average transfer:  $\hat{q}$

...splitting...



Bremsstrahlung as in vacuum.

...induced radiation



Momentum distribution:

$$p \rightarrow zp$$

+Momentum transfer:

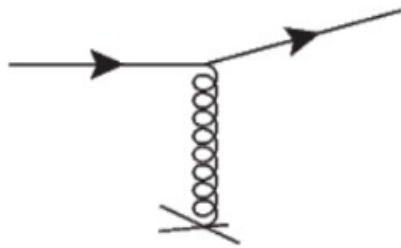
$$p \rightarrow zp + k_T$$

Kernel:  $\mathcal{K}(z, k_T)$

from Martin Rohmoser

# Jet medium interaction

scattering...



Transverse momentum transfer!

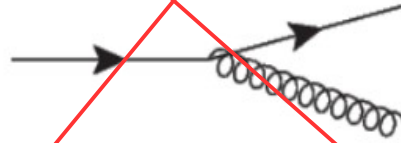
$$p \rightarrow p + k_T$$

Scattering Kernel:  $C(k_T)$

Average transfer:  $\hat{q}$

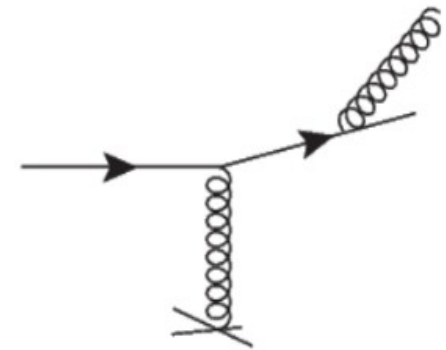
~~we do not account for this now~~

~~...splitting...~~



~~Bremsstrahlung as in vacuum.~~

...induced radiation



Momentum distribution:

$$p \rightarrow zp$$

+Momentum transfer:

$$p \rightarrow zp + k_T$$

Kernel:  $\mathcal{K}(z, k_T)$

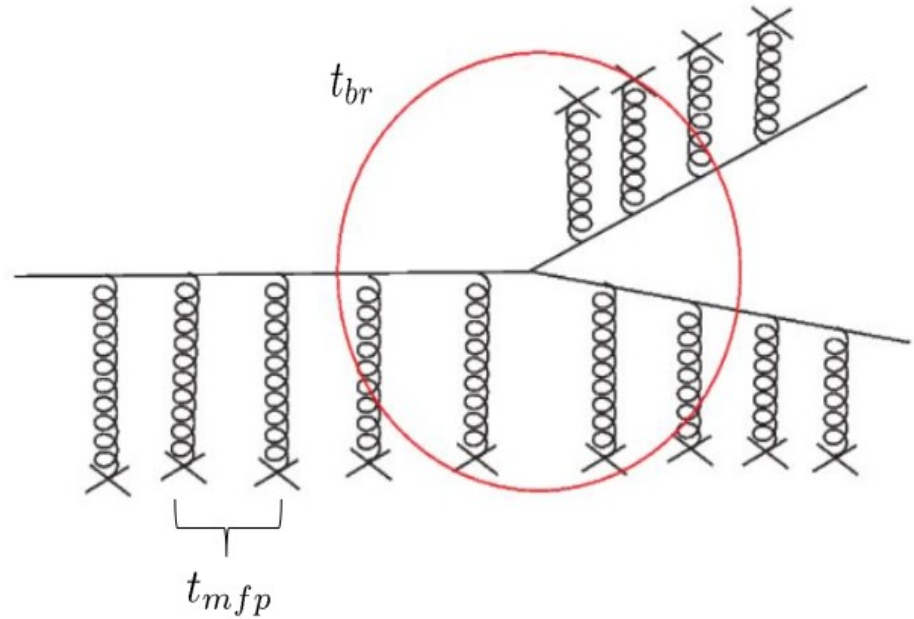
from Martin Rohmoser

# LPM and BDMPS-Z

$$t_{br} \sim \sqrt{\frac{2\omega}{\hat{q}}}$$

$t_{br} \sim t_{mfp}$  : one scattering + radiation  
...Bethe-Heitler spectrum

$t_{br} \gg t_{mfp}$  : coherent radiation



$$\omega \frac{dI}{d\omega} \sim \alpha_s \frac{L}{t_{br}} = \alpha_s \sqrt{\frac{\omega_c}{\omega}}$$

Look at range:  $\omega_{BH} < \omega < \omega_c$

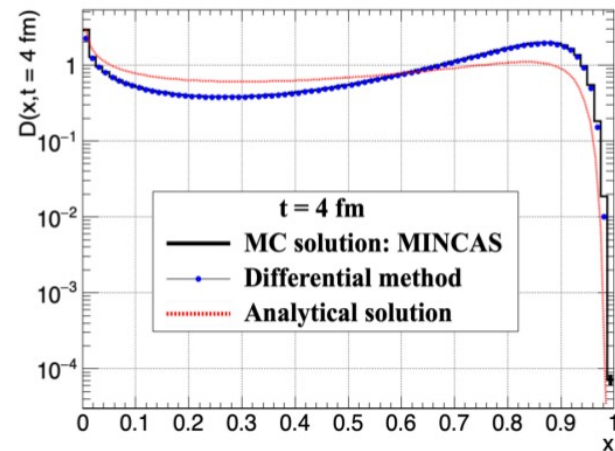
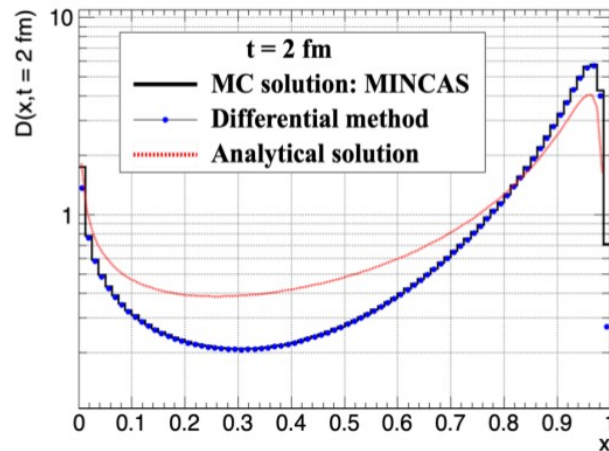
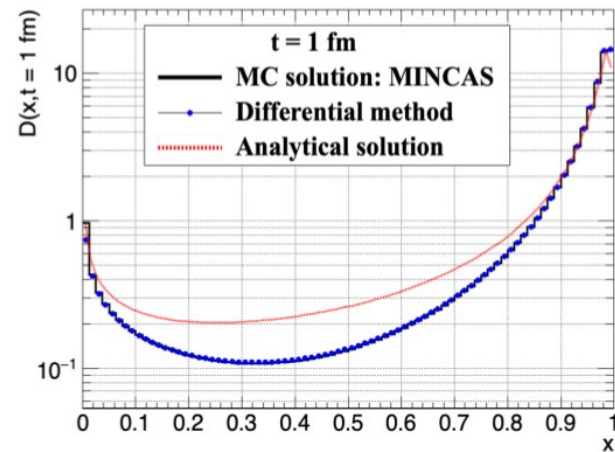
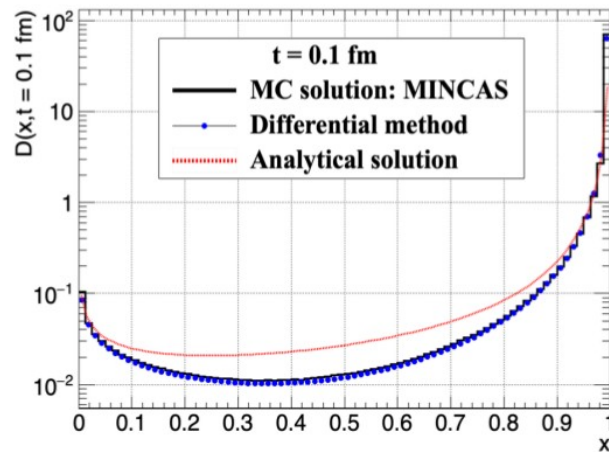
maximal energy that can be taken by single gluon

Energy distribution of radiated gluons

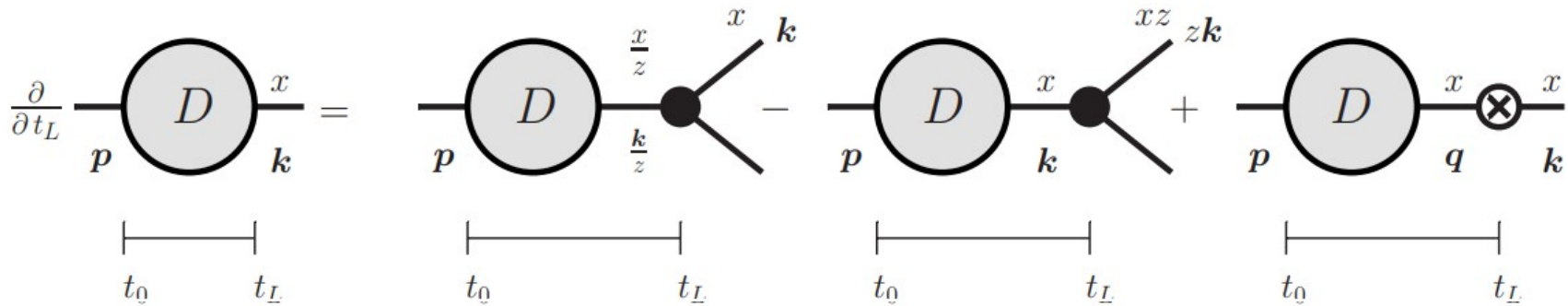
$$\frac{\partial}{\partial t} D(x, t) = \frac{1}{t^*} \int_0^1 dz \mathcal{K}(z) \left[ \sqrt{\frac{z}{x}} D\left(\frac{x}{z}, t\right) \theta(z - x) - \frac{z}{\sqrt{x}} D(x, t) \right]$$

# Solution for energy distribution

– simplified kernel vs. complete kernel



# The BDIM equation - generalization of BDMPS-Z



Blaizot, Dominguez, Iancu, Mehtar-Tani '12

$$\frac{\partial}{\partial t} D(x, \mathbf{k}, t) = \frac{1}{t^*} \int_0^1 dz \mathcal{K}(z) \left[ \frac{1}{z^2} \sqrt{\frac{z}{x}} D\left(\frac{x}{z}, \frac{\mathbf{k}}{z}, t\right) \theta(z-x) - \frac{z}{\sqrt{x}} D(x, \mathbf{k}, t) \right]$$

Inclusive gluon distribution  
as produced by hard jet

$$\frac{1}{t^*} = \frac{\bar{\alpha}}{\tau_{\text{br}}(E)} = \bar{\alpha} \sqrt{\frac{\hat{q}}{E}}$$

$$C(\mathbf{q}) = w(\mathbf{q}) - \delta(\mathbf{q}) \int d^2 \mathbf{q}' w(\mathbf{q}')$$

$$\mathcal{K}(z) = \frac{[f(z)]^{5/2}}{[z(1-z)]^{3/2}} \quad f(z) = 1 - z + z^2$$

Equation describes interplay of rescatterings and branching. This particular equation has  $k_t$  independent kernel. This is an approximation. The whole broadening comes from rescattering. Energy of emitted gluon is much larger than its transverse momentum

## Rearrangement of the equation for gluon density

procedure almost the same as for energy distribution

$$\frac{\partial}{\partial t} D(x, \mathbf{k}, t) = \frac{1}{t^*} \int_0^1 dz \mathcal{K}(z) \left[ \frac{1}{z^2} \sqrt{\frac{z}{x}} D\left(\frac{x}{z}, \frac{\mathbf{k}}{z}, t\right) \theta(z-x) - \frac{z}{\sqrt{x}} D(x, \mathbf{k}, t) \right] + \int \frac{d^2 \mathbf{q}}{(2\pi)^2} C(\mathbf{q}) D(x, \mathbf{k} - \mathbf{q}, t),$$

Kutak, Płaczek, Straka 19

Sudakov form factor resums virtual and unresolved real emissions



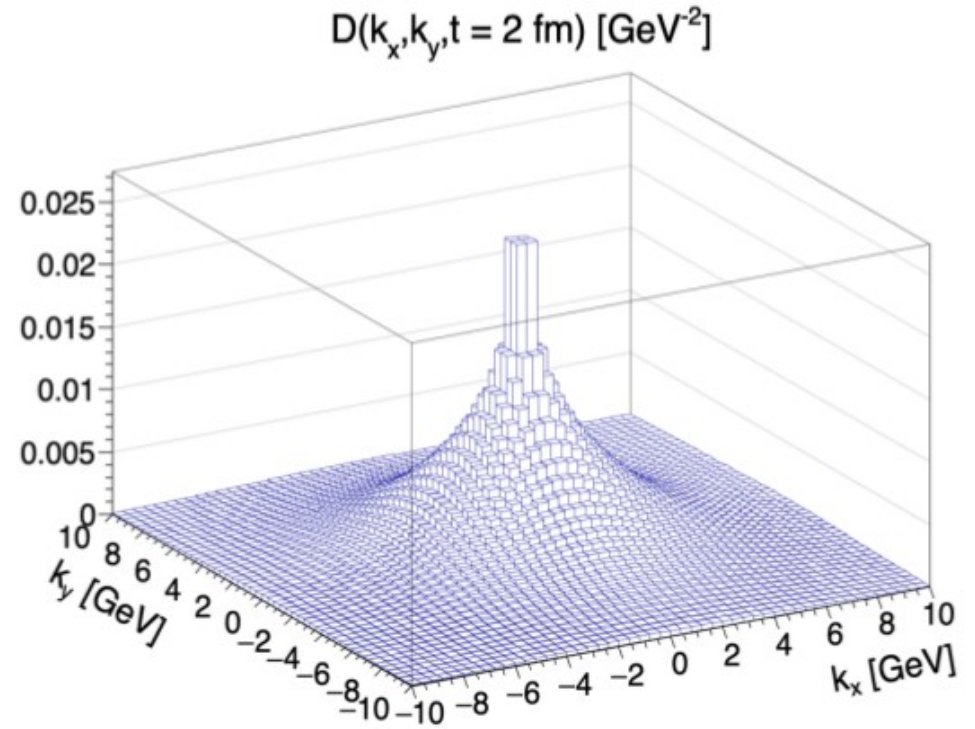
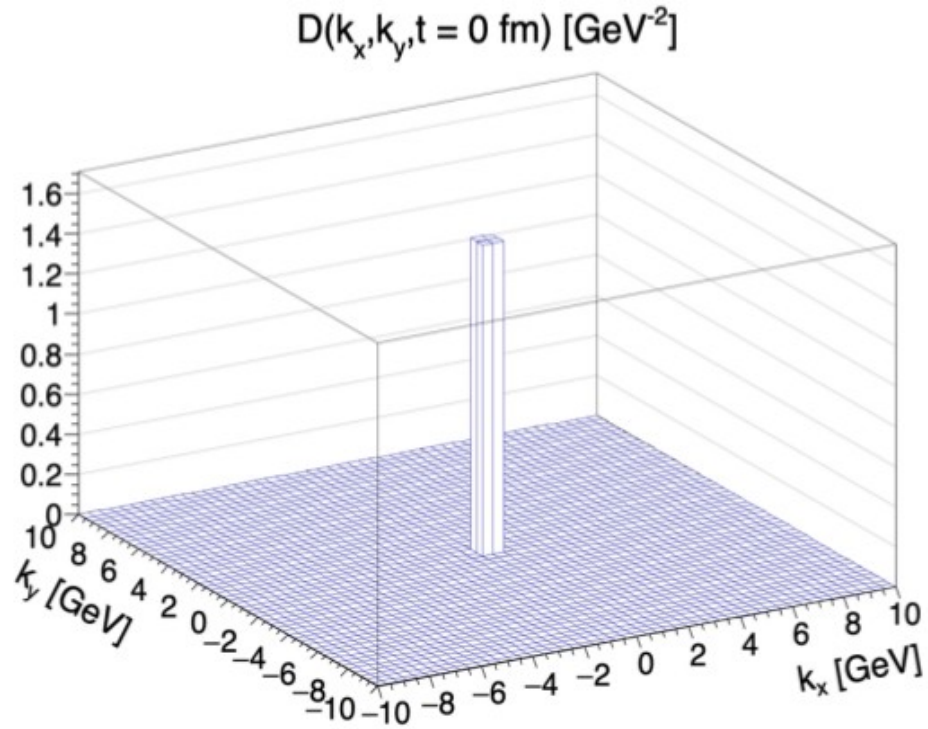
*mathematics:* transformation of differential equation to integral equation

*physics:* resummation of virtual and unresolved real emissions

$$D(x, \mathbf{k}, \tau) = e^{-\Psi(x)(\tau-\tau_0)} D(x, \mathbf{k}, \tau_0) + \int_{\tau_0}^{\tau} d\tau' \int_0^1 dz \int_0^1 dy \int d^2 \mathbf{k}' \int d^2 \mathbf{q} \mathcal{G}(z, \mathbf{q}) \times \delta(x - zy) \delta(\mathbf{k} - \mathbf{q} - z\mathbf{k}') e^{-\Psi(x)(\tau-\tau')} D(y, \mathbf{k}', \tau')$$

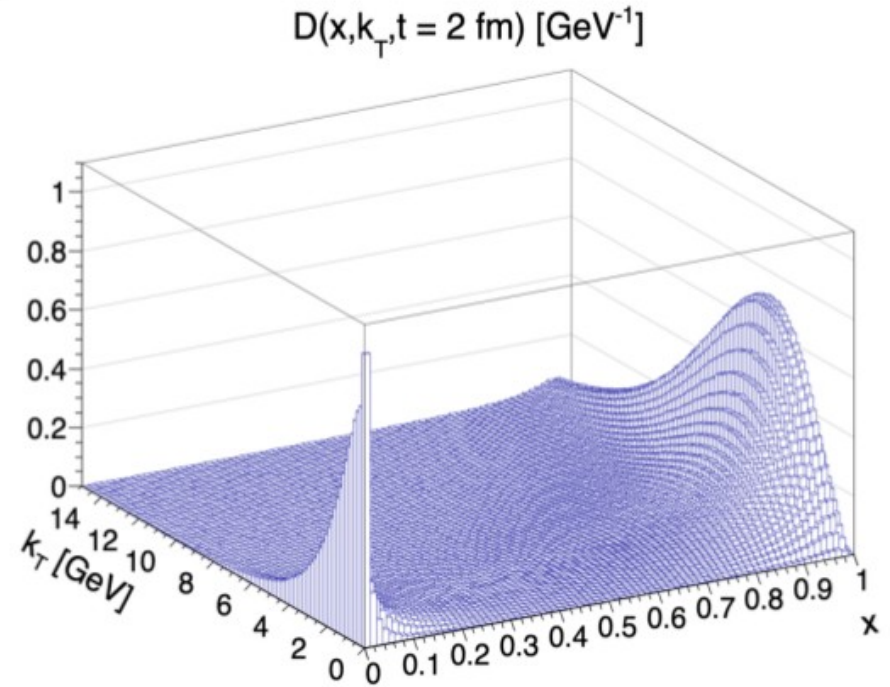
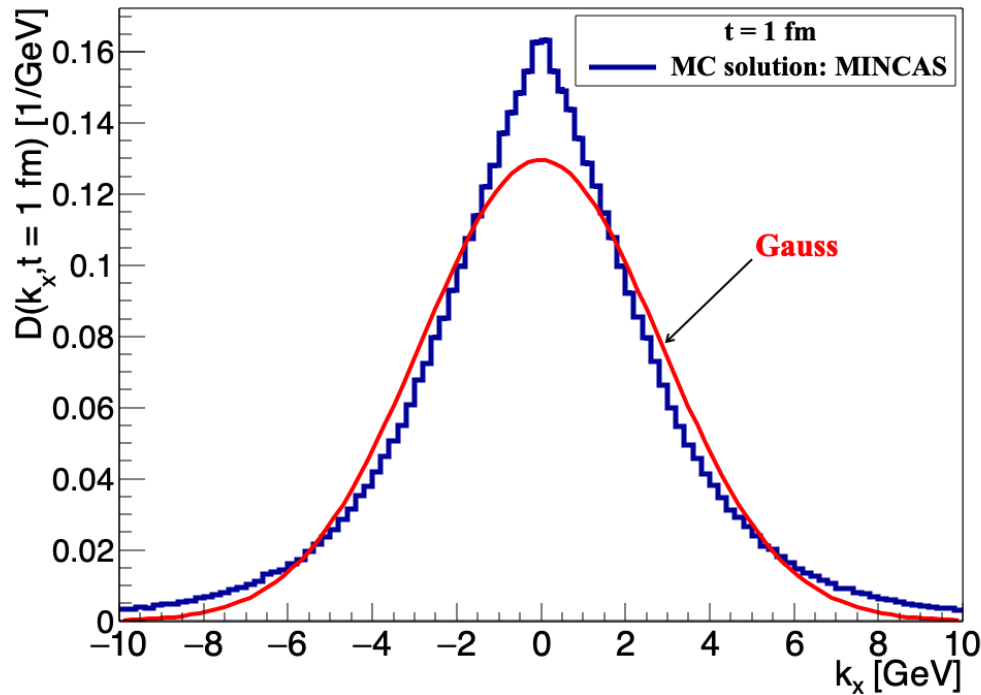


# Broadening of jet



*Such picture is not possible if you assume strongly coupled plasma*

# Non gaussianity



*Sum of many gaussians with different width.*

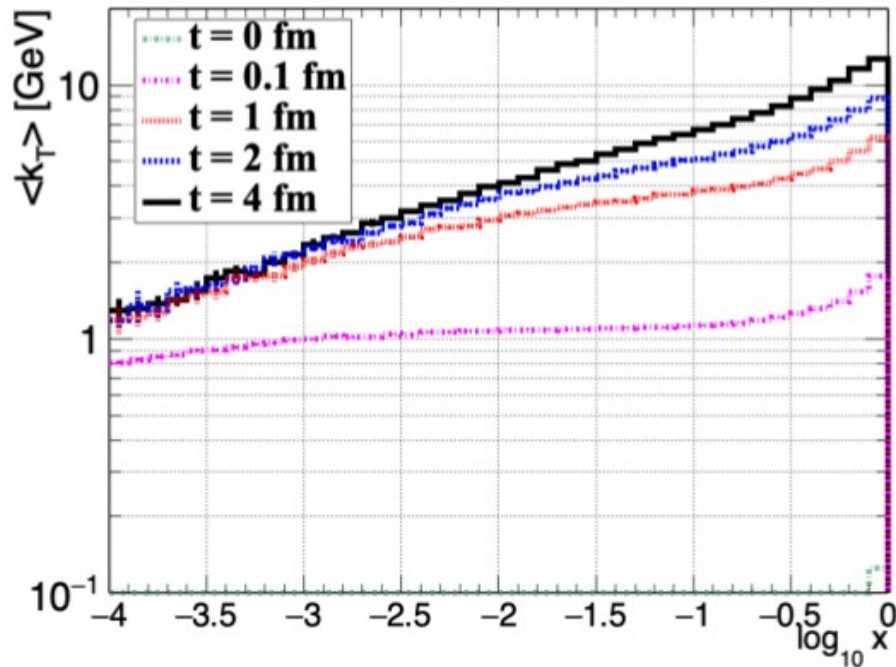
*This is a result of the exact treatment of the gluon transverse-momentum broadening due to an arbitrary number of the collisions with the medium together with its shrinking due an arbitrary number of the emission branching.*

# Quenching line

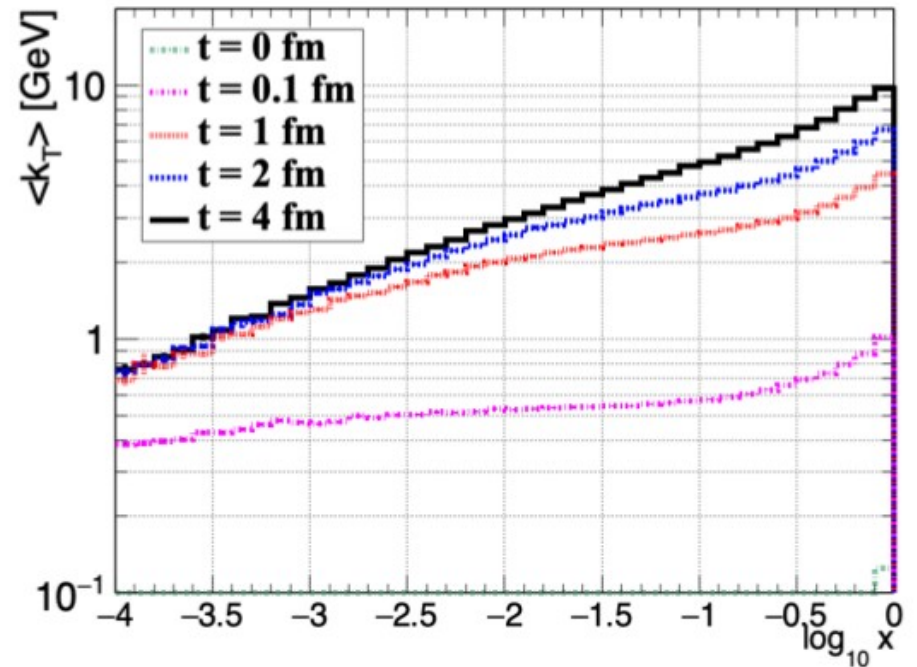
*Non-thermalized medium*

*Thermalized medium*

$$w(q) \sim 1/q^4$$



$$w(q) \sim 1/[q^2(q^2+m_D^2)]$$



*Thermalized medium suppresses jets stronger*

*Universal behavior at larger times*

*The jet gets delocalized in transverse in transverse plane and lower and lower "x"*

## From vacuum to medium

$$\frac{d\sigma_{pp}}{dy_1 dy_2 d^2q_{1T} d^2q_{2T}} = \int \frac{d^2k_{1T}}{\pi} \frac{d^2k_{2T}}{\pi} \frac{1}{16\pi^2 (x_1 x_2 s)^2} \overline{|\mathcal{M}_{g^*g^* \rightarrow gg}^{\text{off-shell}}|^2} \\ \times \delta^2(\vec{k}_{1T} + \vec{k}_{2T} - \vec{q}_{1T} - \vec{q}_{2T}) \mathcal{F}_g(x_1, k_{1T}^2, \mu_F^2) \mathcal{F}_g(x_2, k_{2T}^2, \mu_F^2)$$

$$\frac{d\sigma_{AA}}{d\Omega_{p_1} \Omega_{p_2}} = \int d^2\mathbf{q}_1 \int d^2\mathbf{q}_2 \int_0^1 \frac{d\tilde{x}_1}{\tilde{x}_1^2} \int_0^1 \frac{d\tilde{x}_2}{\tilde{x}_2^2} D(\tilde{x}_1, \mathbf{p}_1 - \mathbf{q}_1, \tau(p_1^+/\tilde{x}_1)) D(\tilde{x}_2, \mathbf{p}_2 - \mathbf{q}_2, \tau(p_2^+/\tilde{x}_2))$$

Our assumptions:

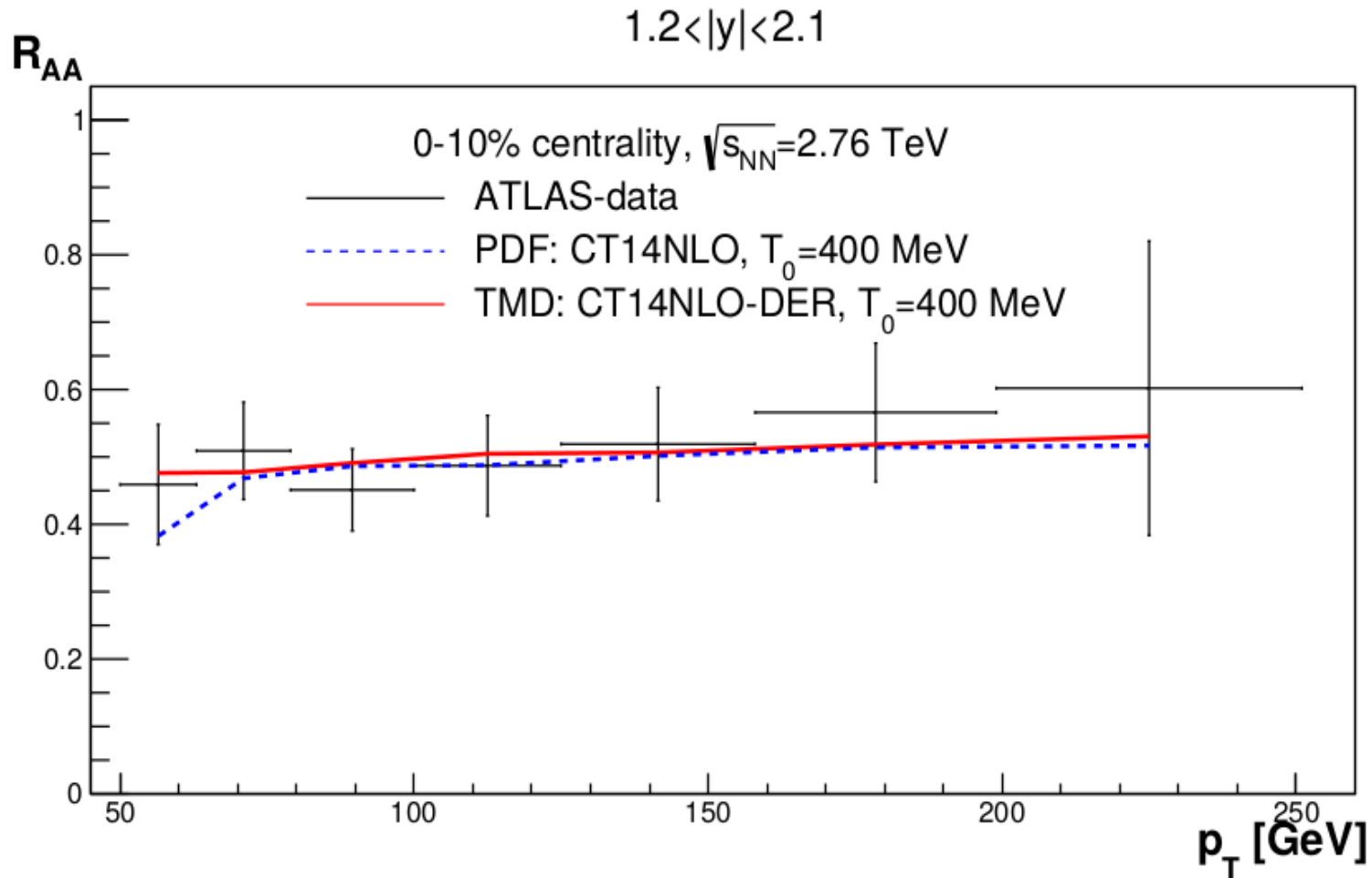
- only gluonic jets
- uniform plasma
- we neglect shower outside of plasma
- we neglect vacuum like emissions in plasma
- we assume bjorken model to tune the temperature to describe  $R_{AA}$

$$\left. \frac{d\sigma_{pp}}{dq_1^+ dq_2^+ d^2\mathbf{q}_1 d^2\mathbf{q}_2} \right|_{q_1^+ = p_1^+/\tilde{x}_1, q_2^+ = p_2^+/\tilde{x}_2}$$

# $R_{AA}$ nuclear modification ratio

1911.05463

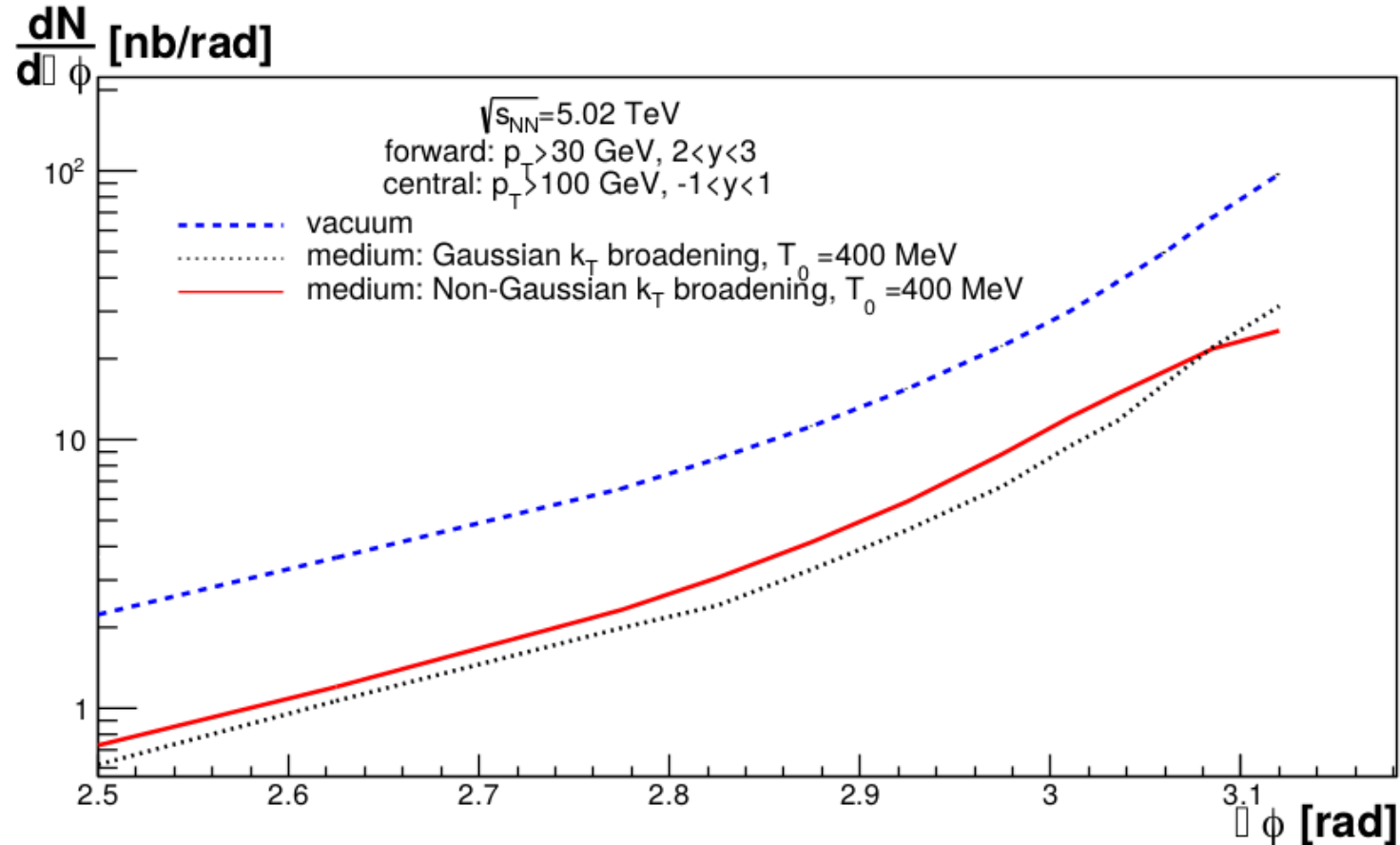
Van Hameren, Kutak, Placzek, Rohrmoser



# Azimuthal decorrelations

1911.05463

Van Hameren, Kutak, Placzek, Rohrmoser



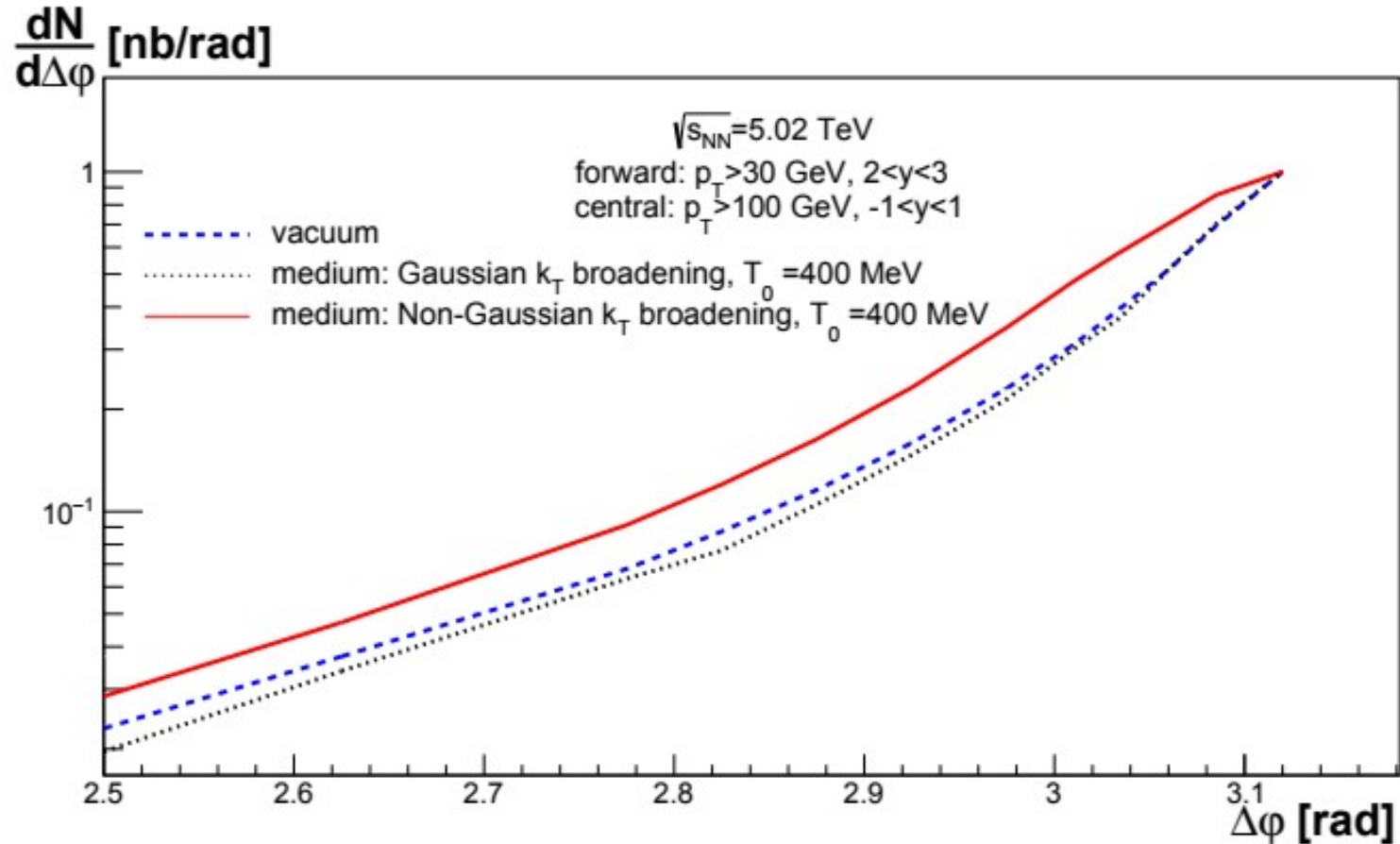
*Suppression at large angles*

*Enhancement at moderate angles*

# Azimuthal decorrelations - normalized to maximum

1911.05463

Van Hameren, Kutak, Placzek, Rohrmoser





# Summary and outlook

## *P-p, p-A*

*New factorization formula for dilute-dense collision has been obtained*

- *accounts for nonlinear evolution of low  $x$  gluon density*
- *accounts for correct gauge structure of the theory*
- *can be obtained from Color Glass Condensate in appropriate limit*

*Evidence for need for Sudakov and saturation in forward jets has been found – **visible broadening***

## *A-A*

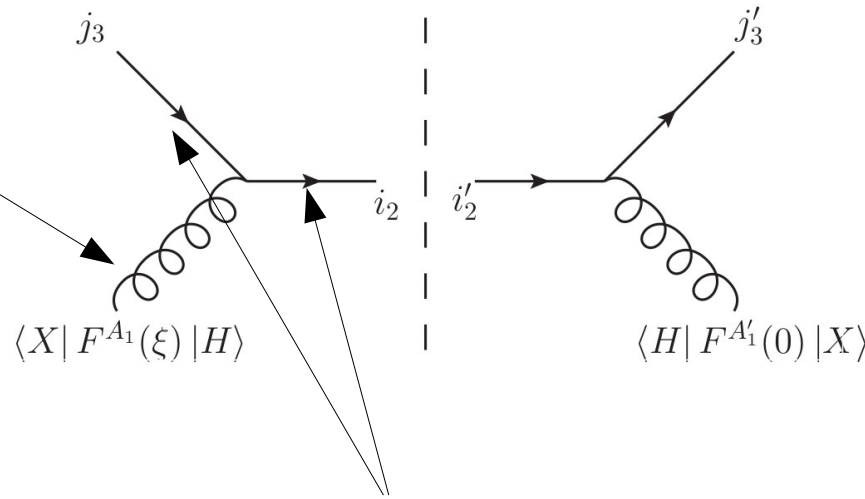
- *jet evolution based on coherent emission and scattering*
- *combination with of MINCAS with KATIE: allows for calculation of jet-observables*
- *results differ from pure Gaussian broadening...*

*In the future we want to study more forward processes and in particular combine jet quenching and saturation*



# Example $qg \rightarrow q$

We want to get TMD distribution of



Resummation

replacement of deltas with operators

We need to resum all collinear emissions from

$$\mathcal{M} = (t^{A_1})_{j_3}^{i_2} \mathcal{A}(2, 1, 3)$$

$$\mathcal{M}^* \mathcal{M} \delta^{i_2 i'_2} \delta_{j_3 j'_3} = (t^{A_1})_{j_3}^{i_2} (t^{A'_1})_{i'_2}^{j'_3} \delta^{A_1 A'_1} \delta^{i_2 i'_2} \delta_{j_3 j'_3} \mathcal{A}^*(2, 1, 3) \mathcal{A}(2, 1, 3)$$

$$\begin{aligned} (t^{A_1})_{j_3}^{i_2} (t^{A'_1})_{i'_2}^{j'_3} (U^{[+]})_{i'_2}^{i_2} (U^{[-]\dagger})_{j_3}^{j'_3} F^{A'_1}(0) F^{A_1}(\xi) &= \\ &= (F(\xi))_{j_3}^{i_2} (U^{[-]\dagger})_{j_3}^{j'_3} (F(0))_{i'_2}^{j'_3} (U^{[+]})_{i'_2}^{i_2} = \text{Tr} [F(\xi) U^{[-]\dagger} F(0) U^{[+]}] \end{aligned}$$

$$\mathcal{F}_{qg}^{(1)}(x, k_T) = 2 \int \frac{d\xi^- d^2 \xi_T}{(2\pi)^3 P^+} e^{ixP^+ \xi^- - i\vec{k}_T \cdot \vec{\xi}_T} \left\langle \text{Tr} [\hat{F}^{i+}(\xi) U^{[-]\dagger} \hat{F}^{i+}(0) U^{[+]}] \right\rangle$$