

# Cumulants of net-proton number fluctuations from ALICE at the LHC

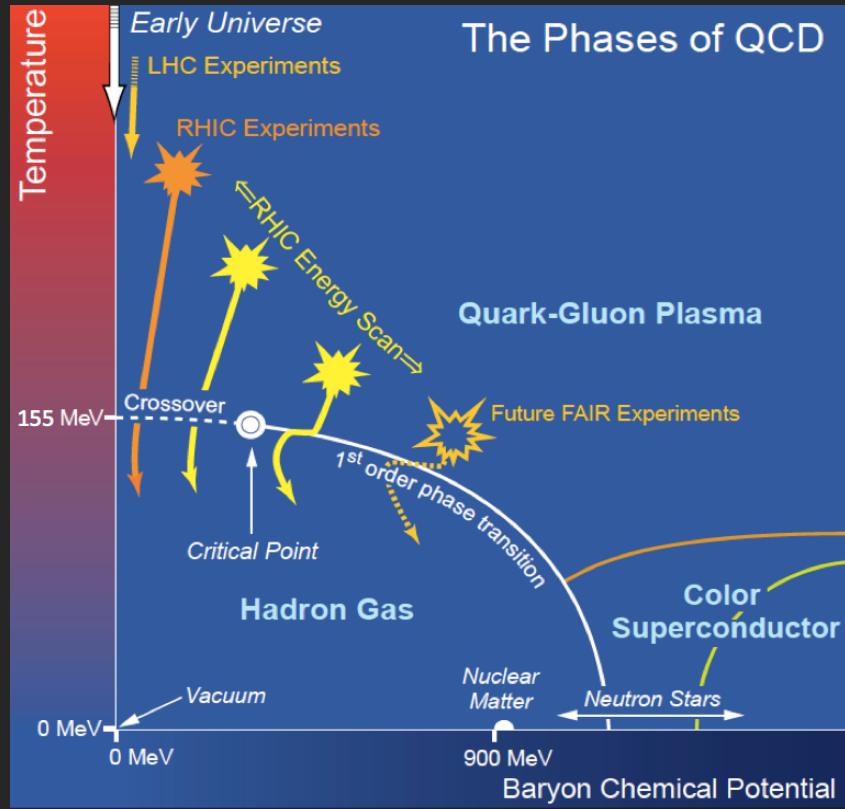
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for the ALICE collaboration

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# Motivation: To map the QCD phase diagram



(Y. Akiba et al, arXiv:1502.02730v1)

- At LHC energies,  $\mu_B \simeq 0$ .
- Lattice QCD:  $T_c \simeq 154 \pm 9$  MeV

Estimation from models with ALICE data:

- $T_{\text{freeze-out}}: \sim 156 \pm 3$  MeV  
[J. Stachel et al J. Phys. Conf. Ser. 509, 012019, (2014)]

➤ Chemical freeze-out line is close to the crossover line!

Precise determination of freeze-out parameters ( $T$  and  $\mu_B$ ) at the LHC can help to locate the phase boundary at  $\mu_B \simeq 0$ .

S. Borsányi *et al*, PRL 111, 062005 (2013), Frithjof Karsch, Central Eur.J.Phys. 10 (2012) 1234-1237

# Motivation: Connecting experiment with lattice QCD

In lattice QCD, the cumulants ( $C_n$ ) of the distributions of conserved charges (net-charge, net-baryon, net-strangeness) are related to the generalized quark-number susceptibilities ( $\chi_n^q$ )

We measure	We are interested in
	$C_n = VT^3 \chi_n^q$
Experiment	$\frac{C_4}{C_2} = \frac{\chi_4^q}{\chi_2^q}$
	$\frac{C_3}{C_2} = \frac{\chi_3^q}{\chi_2^q}$

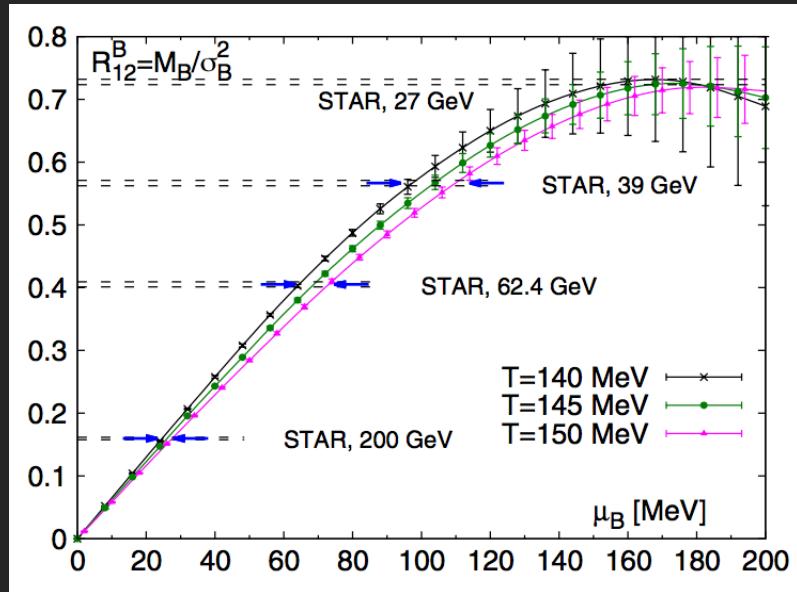
$$\chi_n^q = \frac{\partial^n (p/T^4)}{\partial(\mu_B/T)^n}$$

Lattice QCD

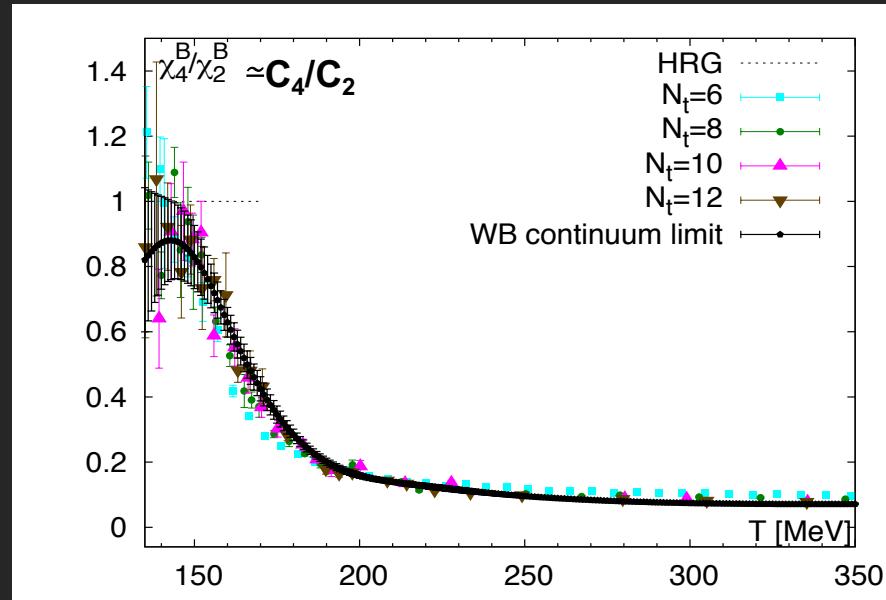
A direct comparison of experimental results with lattice QCD!

# Motivation: Connecting experiment with lattice QCD

Freeze-out temperature from the ratio of cumulants of net-baryons



S. Borsányi *et al* PRL 113, 052301 (2014)



S. Borsányi *et al* PRL 111, 062005 (2013)

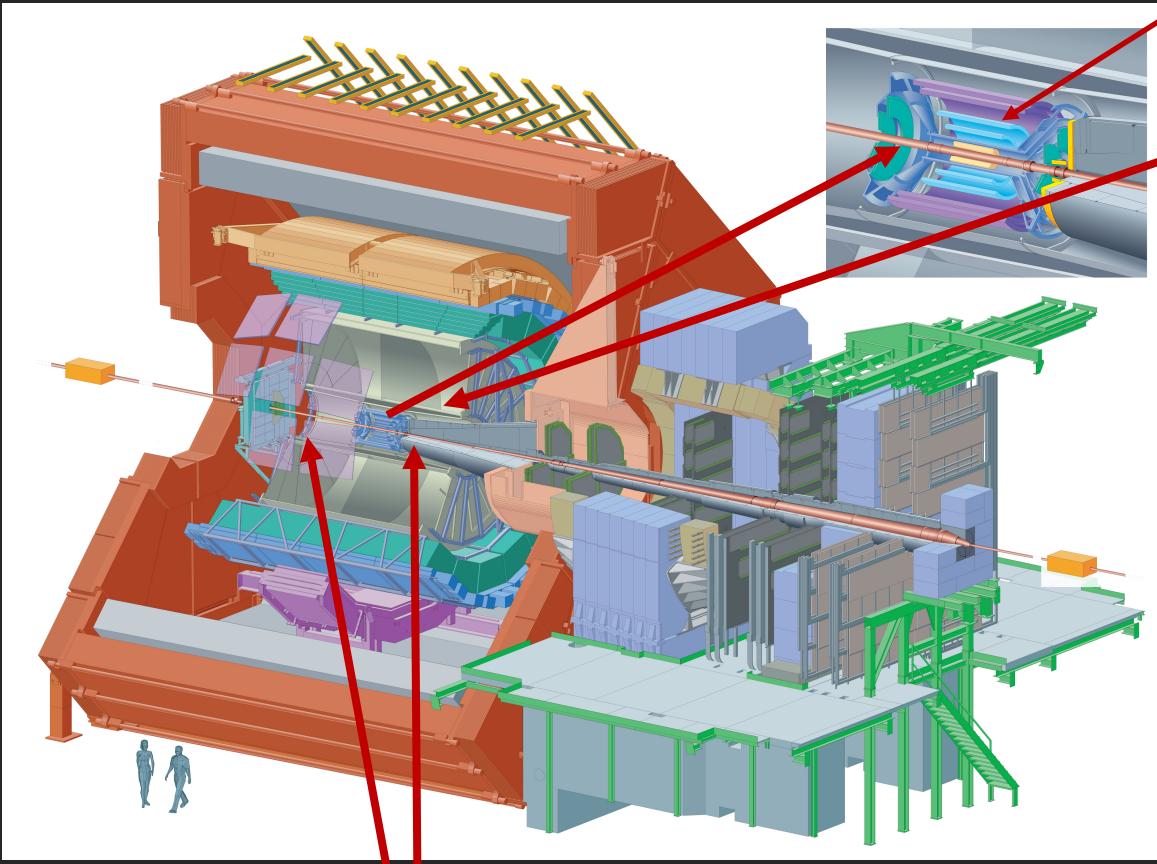
- From lattice QCD, freeze-out parameters can be extracted from experimental results at  $\mu_B = 0$ .
- Net-proton fluctuations are a good proxy for net-baryon number fluctuations.

[Y. Hatta, M.A. Stephanov, PRL 91 102003 (2003)]

Experimental measurements of the ratio of cumulants of net-protons at the LHC will help to constrain the lattice QCD predictions in a model independent way.

# Experimental setup and dataset

## ALICE detector



V0 detector:  
Trigger, centrality estimation  
V0A:  $2.8 < \eta < 5.1$ , VOC:  $-3.7 < \eta < -1.7$

Inner Tracking System (ITS): Vertex, tracking, PID

Time Projection Chamber (TPC): Tracking, PID

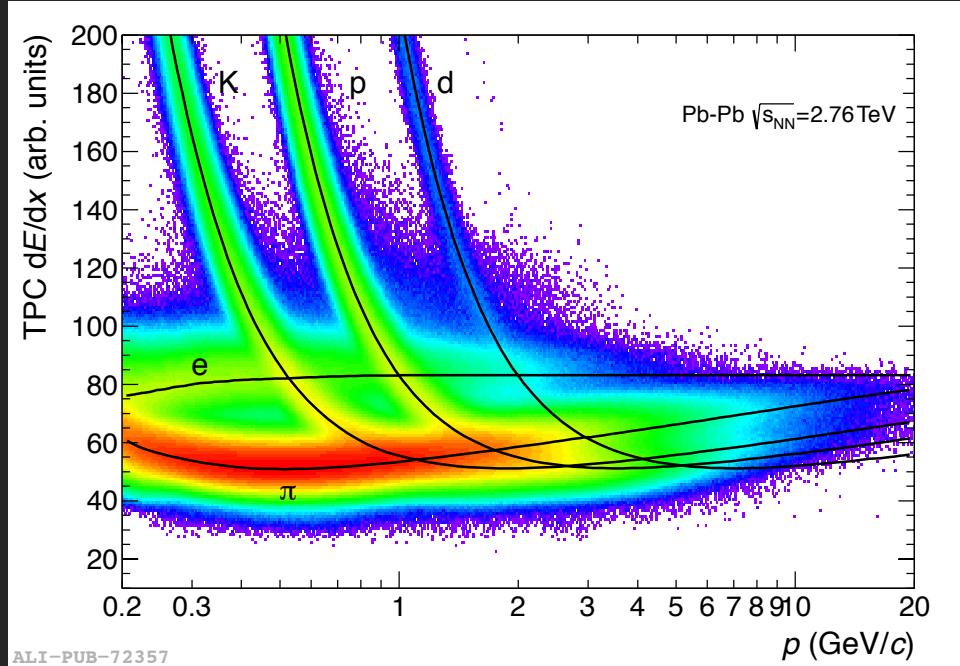
Minimum-bias Pb-Pb collision data

Collision energy	Pb-Pb 2.76 TeV (Run1)	Pb-Pb 5.02 TeV (Run2)
Number of events	$14 \times 10^6$	$59 \times 10^6$

- Kinematic cuts:  $0.4 < p_T < 1.0 \text{ GeV}/c$ ,  $|\eta| < 0.8$
- Proton identification: TPC (next slide)

# Proton Identification

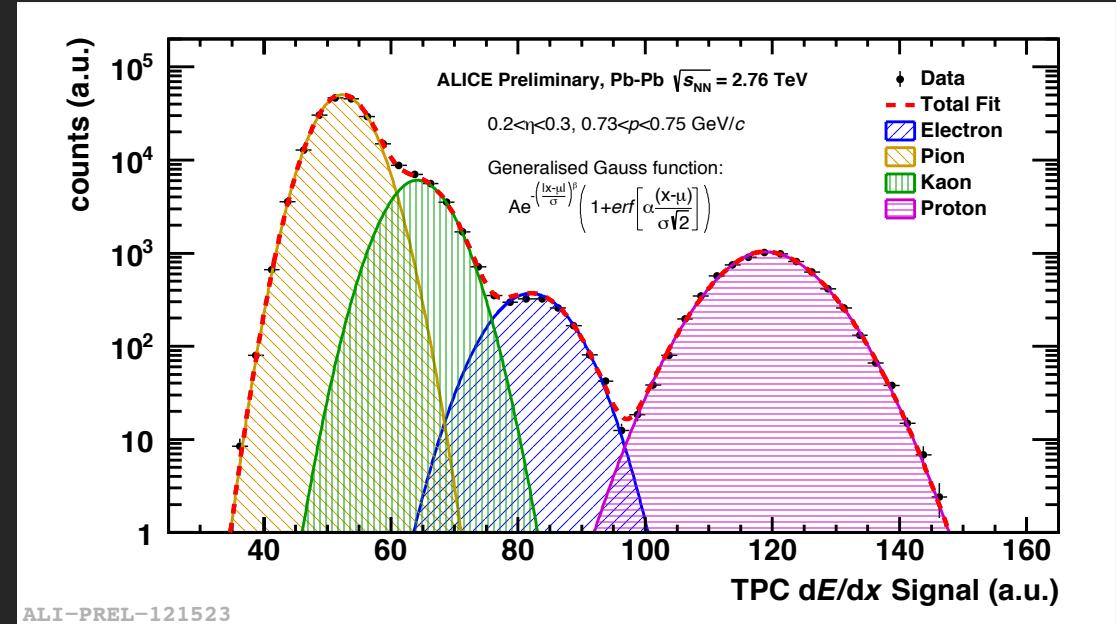
## Energy loss ( $dE/dx$ ) of particles in TPC gas



- (Anti-)Proton identified using the  $n\sigma$  cut around the expected value of energy loss of particles in TPC detector (this presentation).

C<sub>2</sub> results from both the methods agree with each other

## Generalized Gaussian fit to TPC $dE/dx$



- Proton identification using Identity method:  
Assign a Bayesian probability for each particle species.
- Get the true numbers using response matrix built from the parameterization of TPC  $dE/dx$ .

M. Gazdzicki et al., PRC 83, 054907 (2011)

M. I. Gorenstein, PRC 84, 024902 (2011)

A. Rustamov, M. I. Gorenstein, PRC 86, 044906 (2012)

# Higher moments and cumulants

- Measure net-proton numbers on event-by-event basis:  $\Delta\mathbf{p} = \mathbf{p} - \bar{\mathbf{p}}$
- The  $n^{\text{th}}$  moments:  $m'_n = <(\Delta p)^n>$

## Cumulants from moments

$$C_1 = m'_1$$

$$C_2 = m'_2 - m'_1^2$$

$$C_3 = m'_3 - 3m'_1 m'_2 + 2m'_1^3$$

$$C_4 = m'_4 - 4m'_1 m'_3 - 3 m'_2^2 + 12m'_1^2 m'_2 - 6m'_1^4$$

# Analysis methodology

## 1) Detector efficiency correction: method 1

- A. Bzdak and V. Koch, PRC 91, 027901 (2015).
- Assumption: detector efficiency follows Binomial distribution.

Factorial moments

$$F_{i,k} = \sum_{x_1, \dots, x_i} \sum_{\bar{x}_1, \dots, \bar{x}_k} \frac{a_{i,k}(x_1, \dots, x_i; \bar{x}_1, \dots, \bar{x}_k)}{\epsilon(x_1) \dots \epsilon(x_i) \bar{\epsilon}(\bar{x}_1) \dots \bar{\epsilon}(\bar{x}_k)}.$$

where

$$\begin{aligned} a_{i,k}(x_1, \dots, x_i; \bar{x}_1, \dots, \bar{x}_k) &= \langle n(x_1)[n(x_2) - \delta_{x_1, x_2}] \cdots [n(x_i) - \delta_{x_1, x_i} - \cdots - \delta_{x_{i-1}, x_i}] \\ &\quad \bar{n}(\bar{x}_1)[\bar{n}(\bar{x}_2) - \delta_{\bar{x}_1, \bar{x}_2}] \cdots [\bar{n}(\bar{x}_k) - \delta_{\bar{x}_1, \bar{x}_k} - \cdots - \delta_{\bar{x}_{k-1}, \bar{x}_k}] \rangle. \end{aligned}$$

Cumulants from factorial moments

$$\begin{aligned} K_1 &= \langle N_1 \rangle - \langle N_2 \rangle, \\ K_2 &= N - K_1^2 + F_{02} - 2F_{11} + F_{20}, \\ K_3 &= K_1 + 2K_1^3 - F_{03} - 3F_{02} + 3F_{12} + 3F_{20} - 3F_{21} + F_{30} \\ &\quad - 3K_1(N + F_{02} - 2F_{11} + F_{20}), \\ K_4 &= N - 6K_1^4 + F_{04} + 6F_{03} + 7F_{02} - 2F_{11} - 6F_{12} - 4F_{13} \\ &\quad + 7F_{20} - 6F_{21} + 6F_{22} + 6F_{30} - 4F_{31} + F_{40} \\ &\quad + 12K_1^2(N + F_{02} - 2F_{11} + F_{20}) - 3(N + F_{02} - 2F_{11} + F_{20})^2 \\ &\quad - 4K_1(K_1 - F_{03} - 3F_{02} + 3F_{12} + 3F_{20} - 3F_{21} + F_{30}), \end{aligned}$$

where

$$N \equiv \langle N_1 \rangle + \langle N_2 \rangle = F_{10} + F_{01}.$$

# Analysis methodology

## 1) Detector efficiency correction: method 2 (Used here)

- Recent method: T Nonaka et al ,PRC 95, 064912, (2017)
- Assumption: detector efficiency follows Binomial distribution.

$$\begin{aligned}\langle Q \rangle_c &= \langle q_{(1,1)} \rangle_c, \\ \langle Q^2 \rangle_c &= \langle q_{(1,1)}^2 \rangle_c + \langle q_{(2,1)} \rangle_c - \langle q_{(2,2)} \rangle_c, \\ \langle Q^3 \rangle_c &= \langle q_{(1,1)}^3 \rangle_c + 3\langle q_{(1,1)}q_{(2,1)} \rangle_c - 3\langle q_{(1,1)}q_{(2,2)} \rangle_c + \langle q_{(3,1)} \rangle_c - 3\langle q_{(3,2)} \rangle_c + 2\langle q_{(3,3)} \rangle_c, \\ \langle Q^4 \rangle_c &= \langle q_{(1,1)}^4 \rangle_c + 6\langle q_{(1,1)}^2q_{(2,1)} \rangle_c - 6\langle q_{(1,1)}^2q_{(2,2)} \rangle_c + 4\langle q_{(1,1)}q_{(3,1)} \rangle_c + 3\langle q_{(2,1)}^2 \rangle_c + 3\langle q_{(2,2)}^2 \rangle_c - 12\langle q_{(1,1)}q_{(3,2)} \rangle_c \\ &\quad + 8\langle q_{(1,1)}q_{(3,3)} \rangle_c - 6\langle q_{(2,1)}q_{(2,2)} \rangle_c + \langle q_{(4,1)} \rangle_c - 7\langle q_{(4,2)} \rangle_c + 12\langle q_{(4,3)} \rangle_c - 6\langle q_{(4,4)} \rangle_c,\end{aligned}$$

Moments

where

$$q_{(r,s)} = q_{(a^r / p^s)} = \sum_{i=1}^M (a_i^r / p_i^s) n_i.$$

$a_i = 1$  for proton,  $-1$  for anti-proton

$p_i$  = Efficiency in  $i^{\text{th}}$   $p_T$  bin.

$n_i$  = Number of observed (anti-) proton

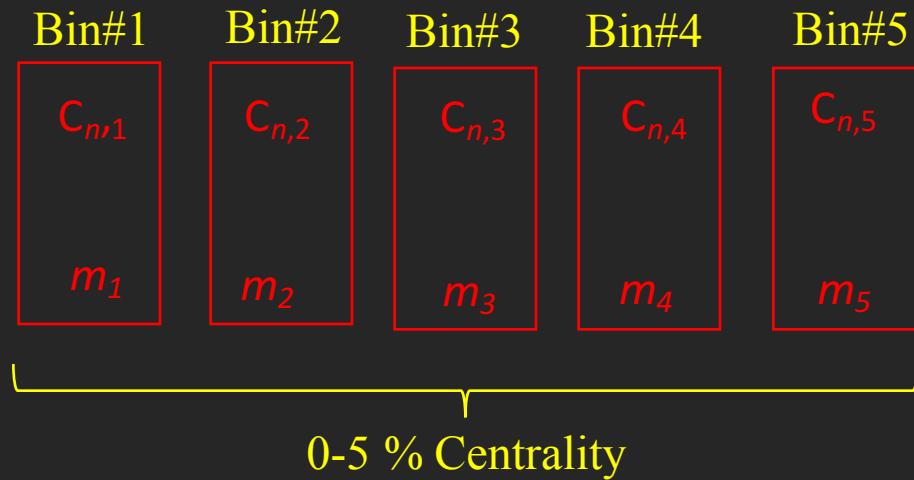
$M$  = Total Number of  $p_T$  bins

- Simpler and faster than method 1.
- Method 1 and 2 give the same results!

# Analysis methodology

## 2) Centrality bin-width correction (CBWC):

- To minimize the impact parameter (or volume) variations due to the finite centrality bin. [X. Luo et al J. Phys. G 40, 105104 (2013)]



$$C_n = \frac{\sum_{i=1}^k m_i C_{n,i}}{\sum_{i=1}^k m_i}$$

$C_{n,i}$  =  $n^{\text{th}}$  order cumulant measured in  $i^{\text{th}}$  centrality bin

$m_i$  = number of events in  $i^{\text{th}}$  centrality bin

$k$  = numbers of centrality bins

- With or without CBWC, the results are consistent for ALICE measurements.
- Cumulants up to 3<sup>rd</sup> order are not sensitive to volume fluctuations!

[P. Braun-Munzinger, A. Rustamov, J. Stachel, NPA 960, 114 (2017) ]

# Analysis methodology

## 3) Statistical error estimation:

- Subgroup method: Divide the data sample into ‘ $k$ ’ subsamples randomly.

$$C_n = \frac{\sum_i^k C_n^i}{k}$$

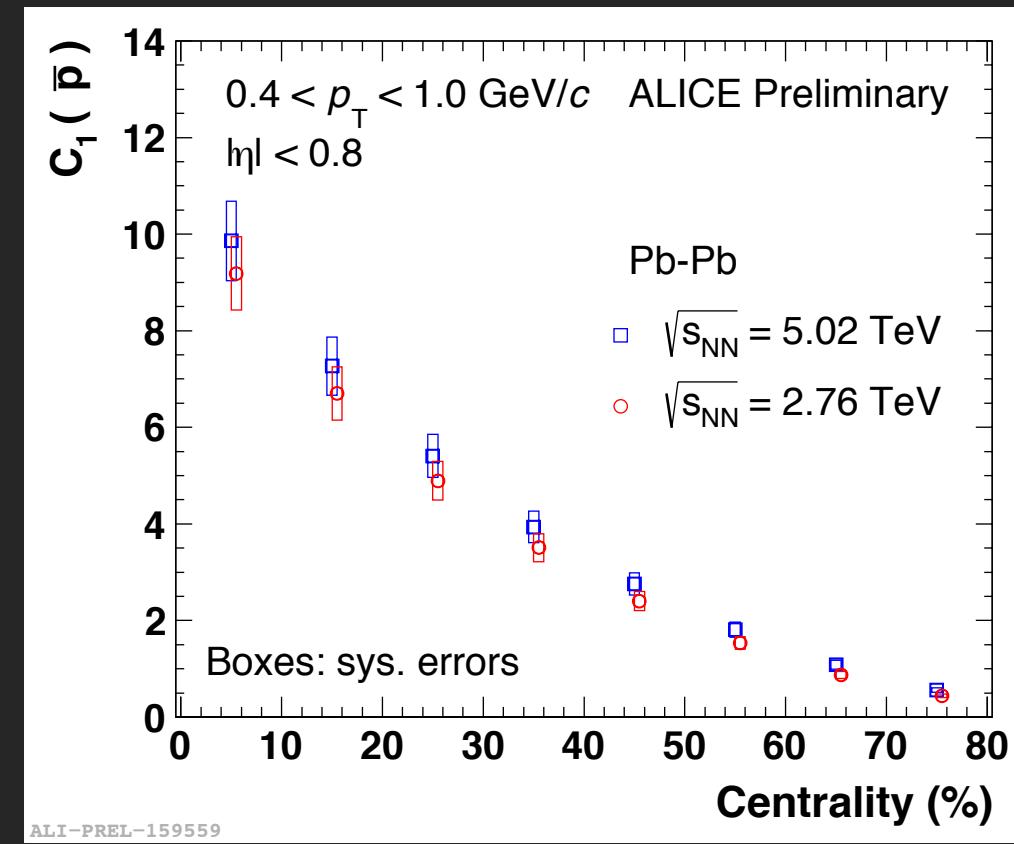
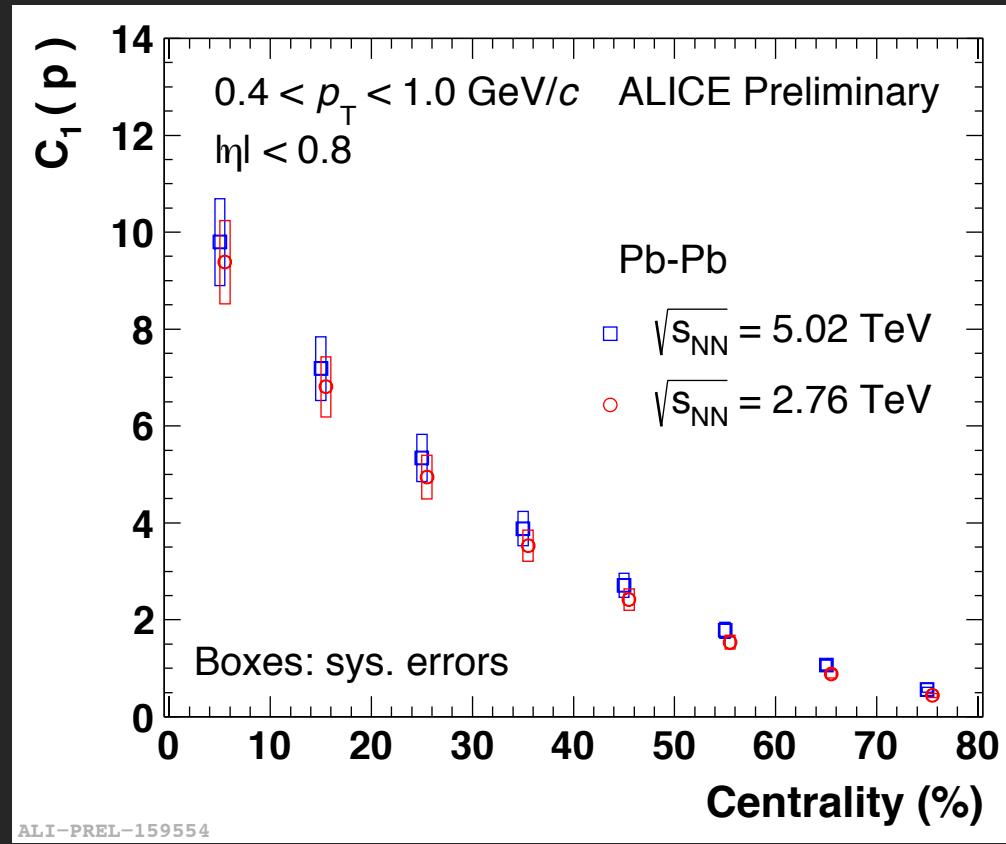
Statistical error  $\delta C_n = \frac{\sigma}{\sqrt{k}}$

where

$$\sigma = \sqrt{\frac{\sum_{i=1}^k (C_n^i - \langle C_n \rangle)^2}{k - 1}}$$

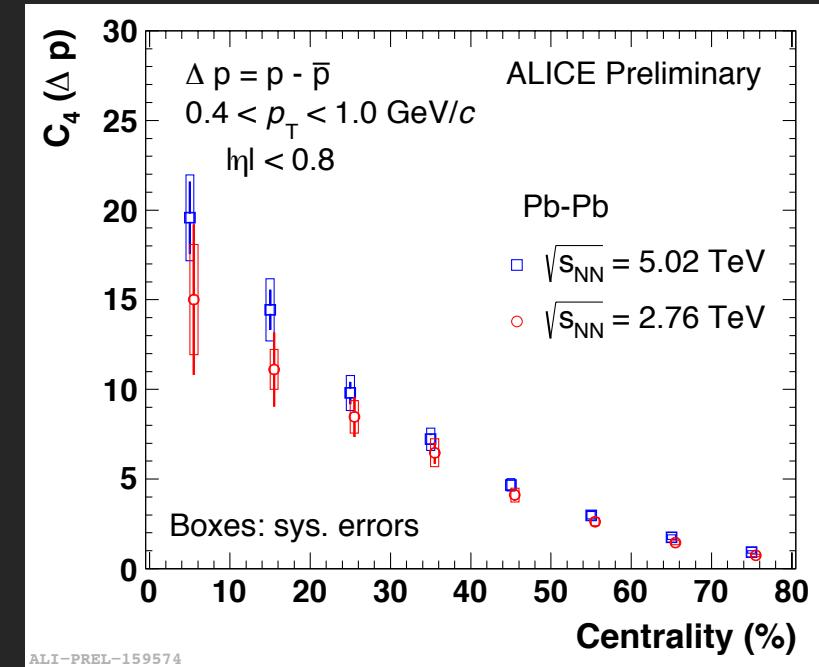
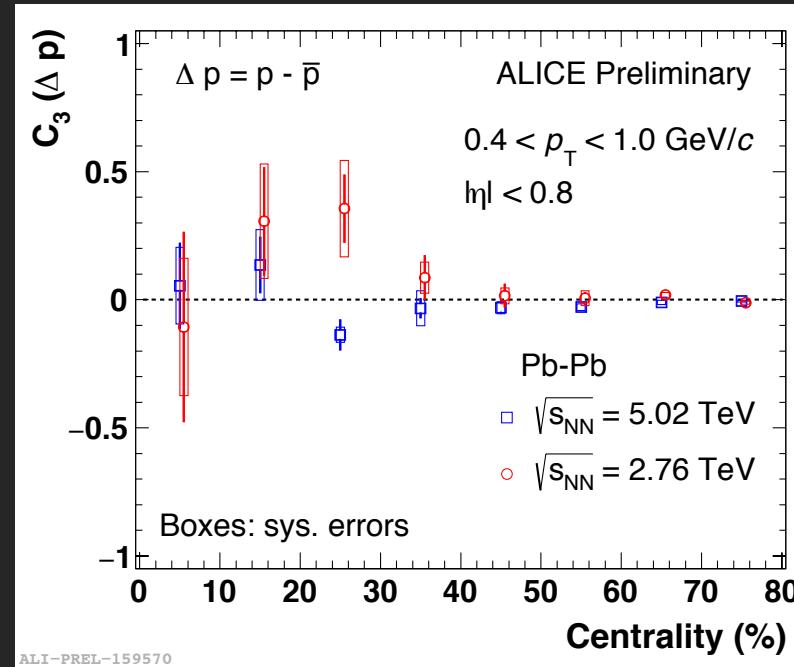
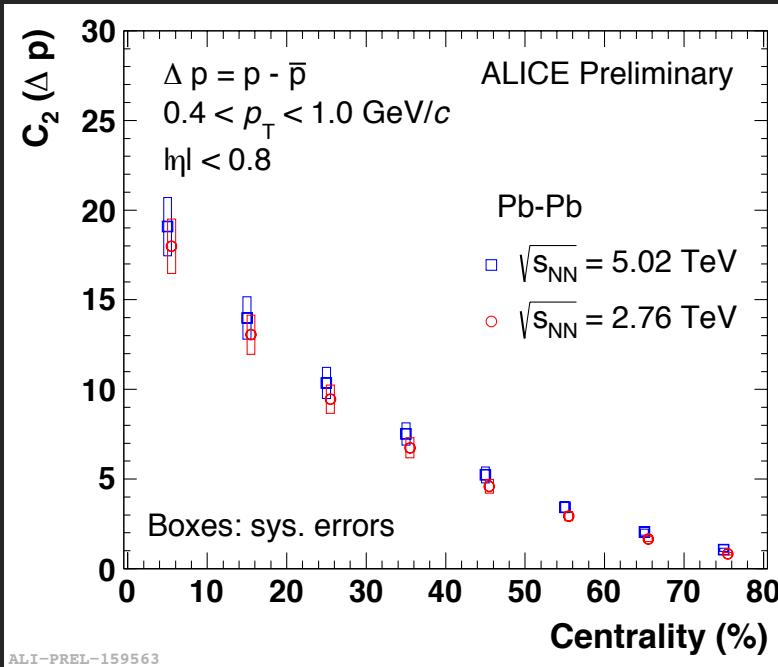
- Number of subsamples used : 30
- Statistical errors estimated from Bootstrap and Subgroup method agree with each other.

# Results: proton and anti-proton $C_1$



- For both energies, proton and anti-proton numbers are similar within systematic errors.

# Results: Cumulants of net-proton distributions

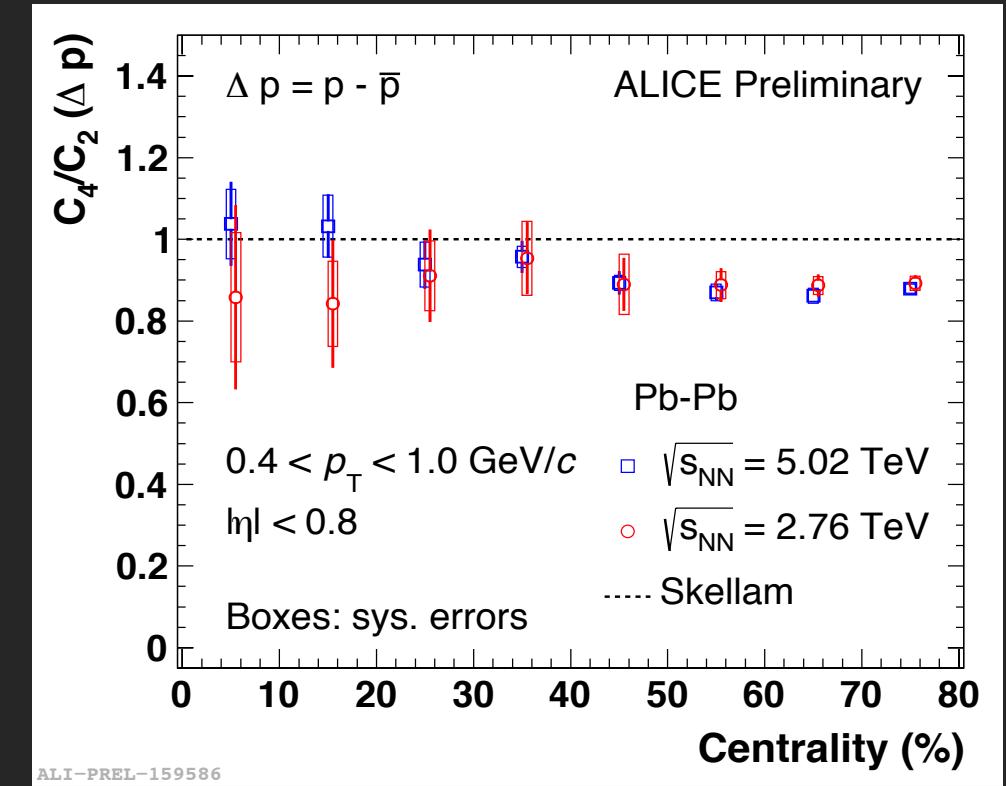
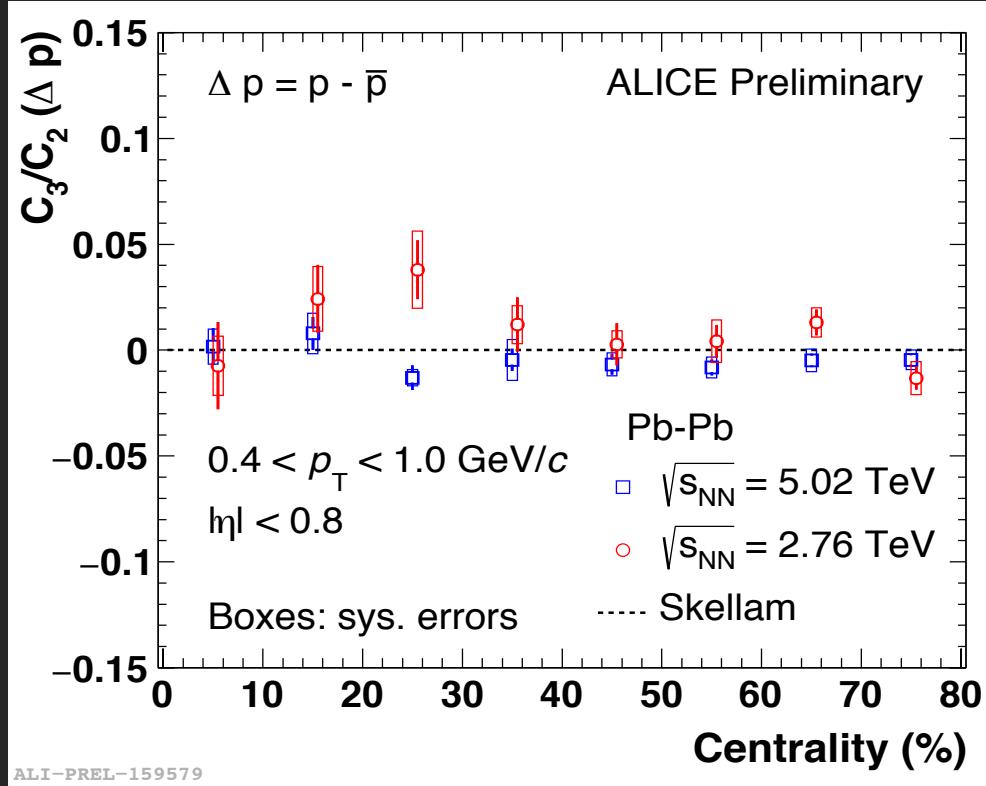


- Cumulants of net-proton distributions for both energies are the same within statistical and systematic errors.
- C<sub>2</sub> results are consistent with Identity method. [ A. Rustamov NPA, 967 (2017) 453–456 (QM 2017)]

# Baseline estimation

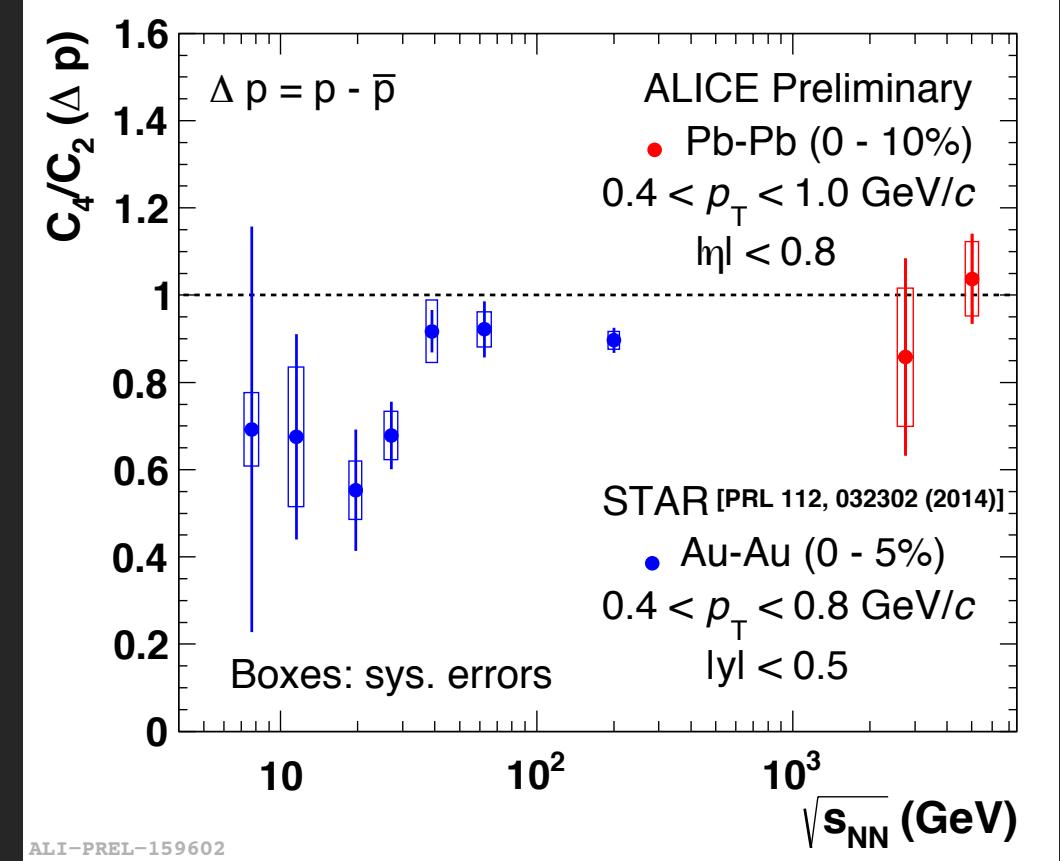
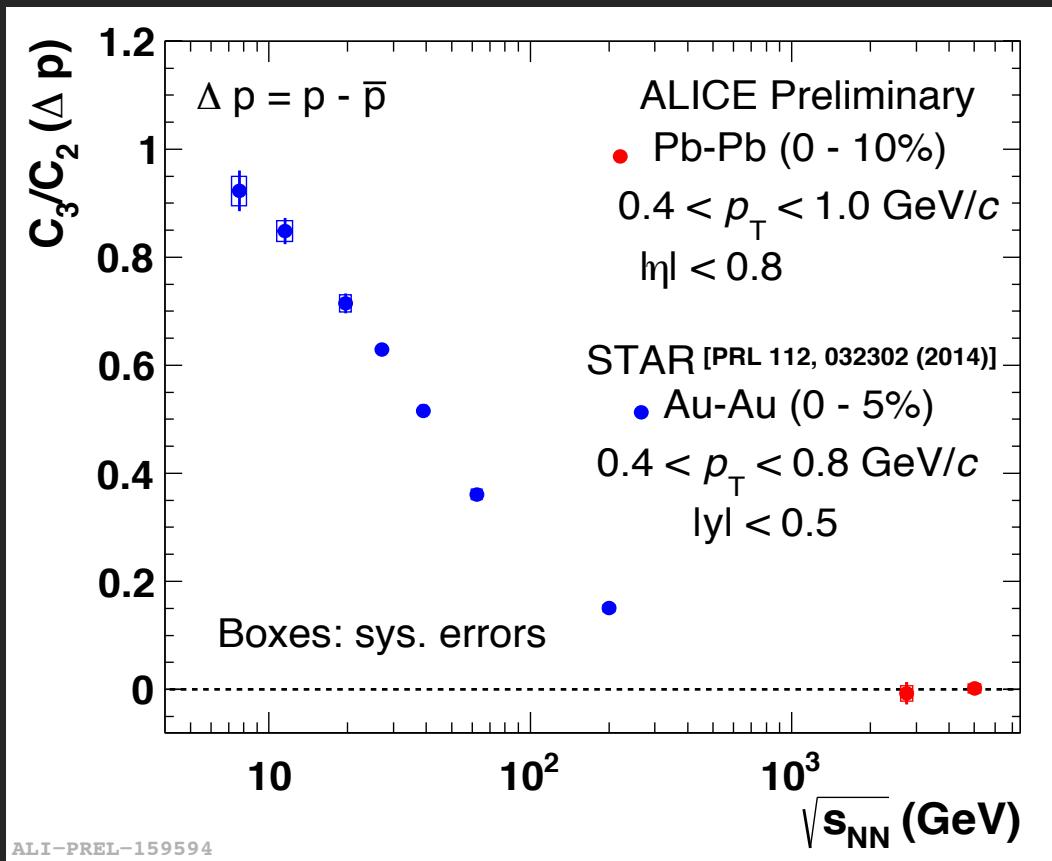
- Assume proton and anti-proton distributions are independent Poissonian distributions => net-proton distribution is a Skellam distribution.
- $C_n(\text{Skellam}) = C_1(p) + (-1)^n C_1(\bar{p})$
- $C_1(\Delta p) = C_3(\Delta p) = C_1(p) - C_1(\bar{p})$
- $C_2(\Delta p) = C_4(\Delta p) = C_1(p) + C_1(\bar{p}) \Rightarrow C_4/C_2 = 1.$
- Used in Hadron Resonance Gas (HRG) model calculations.  
[P. Braun-Munzinger *et al* PLB 747, 292 (2015), P. Garg *et al* PLB 726, 691 (2013)]

# Results: Ratio of cumulants of net-proton distributions



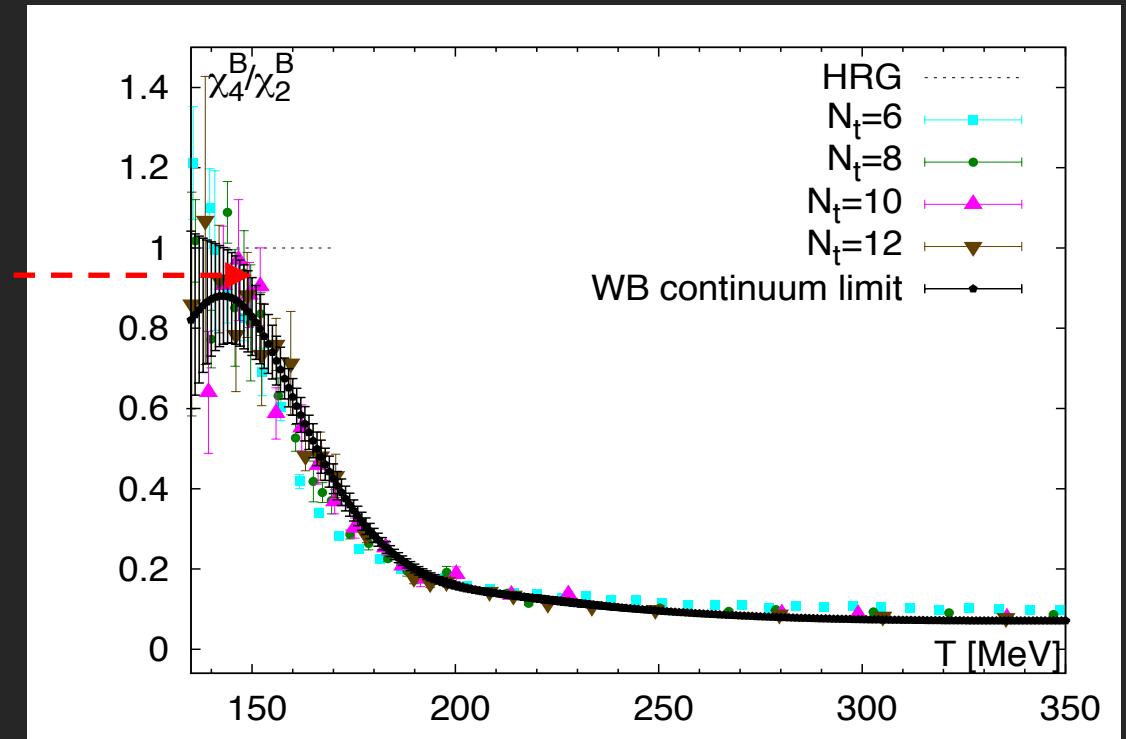
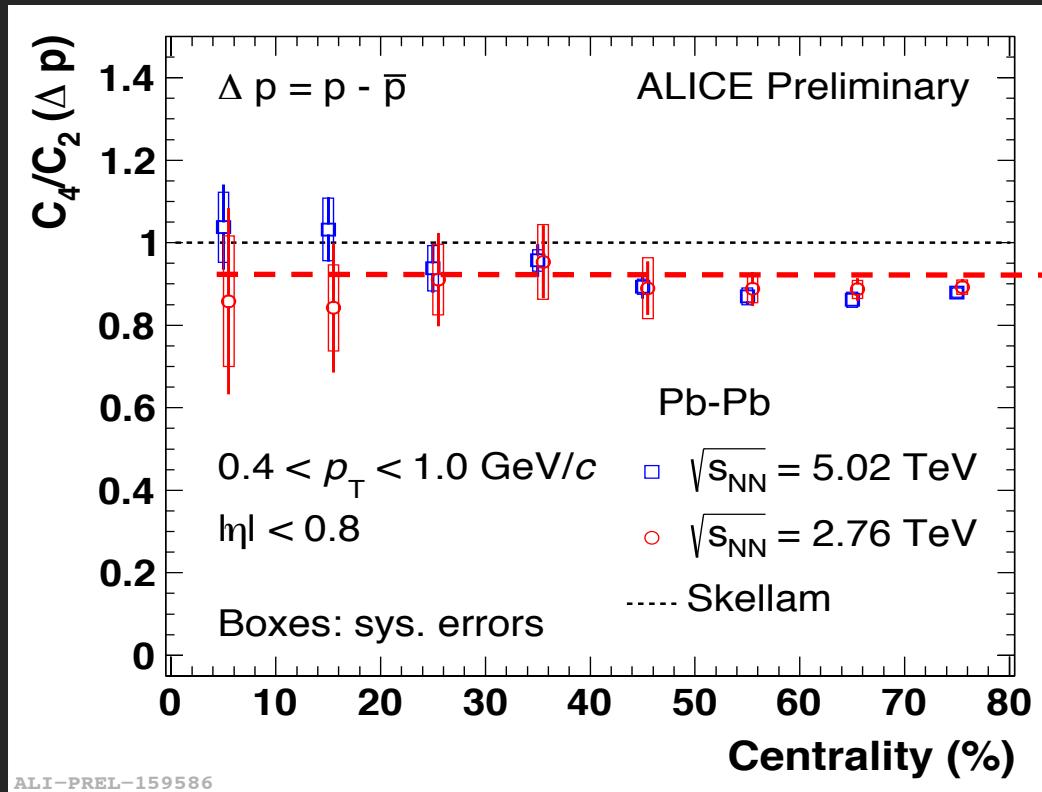
- $C_3/C_2$  and  $C_4/C_2$  results for 2.76 TeV and 5.02 TeV are the same within the statistical error bars.
- $C_3/C_2$  and  $C_4/C_2$  of central events agree with Skellam expectations within statistical errors.

# Results: RHIC to LHC



- $C_3/C_2$  follows a decreasing trend as a function of collision energy.
- Within experimental uncertainties  $C_4/C_2$  at the LHC agrees with the Skellam baseline.

# Freeze-out temperature at the LHC



S. Borsányi *et al* PRL 111, 062005 (2013)

Implied freeze-out temperature from  $C_4/C_2$  consistent with thermal fits to particle yields.  
(assuming net-protons are good proxy to net-baryons on the lattice)

- Need more precise data to further constrain the freeze-out temperature.

# Summary

- The net-proton higher order cumulants up to 4<sup>th</sup> order and their ratios in Pb-Pb collisions at 2.76 and 5.02 TeV are presented as a function of centrality.
- $C_3, C_4$  and their ratios with respect to  $C_2$  generally agree with Skellam expectations within the uncertainties.
- From RHIC to LHC the ratios of cumulants approach the Skellam baseline.
- The results may be used in conjunction with lattice calculations to estimate the freeze-out temperature.
- News: Second cumulants of net- $\Lambda$  fluctuations are measured in ALICE (see A. Ohlson talk in QM 2018)

# Outlook

- The analysis will be extended for higher  $p_T$  ( up to 2 GeV/c) and for other particle species in different pseudo-rapidity windows.
- Measurement of net-proton higher order cumulants with Identity method.
- Off-diagonal cumulants of net-particles.
- The upcoming dedicated Pb-Pb run at 5.02 TeV will increase the statistics to further constrain the freeze-out parameters.

**THANK YOU**

# Backup slides

# Efficiency correction method

$$N_{rec.} = N_{rec.primary} + N_{cont.}$$

where  $N_{cont.} = N_{material} + N_{secondary} + N_{mis.Identified}$

$$\text{Now } N_{rec.primary} = N_{rec} - N_{cont.}$$

$$\Rightarrow N_{gen.primary} = N_{rec.} \frac{(1 - \delta)}{\varepsilon}$$

where contamination factor ( $\delta$ ) =  $\frac{N_{cont.}}{N_{rec.}}$

$$\text{Efficiency } (\varepsilon) = \frac{N_{rec.primary}}{N_{gen.primary}}$$

$$\Rightarrow N_{gen.primary} = \frac{N_{rec.}}{\omega}$$

$$\text{correction factor } \omega = \frac{\varepsilon}{(1 - \delta)}$$