Production of $p\overline{p}$ pairs in UPC at the LHC

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Plan

1) $\gamma \gamma \rightarrow p \overline{p}$ reaction

- non-resonant proton exchange contribution
- *f*₂ meson contribution
- hand-bag approach
- 2) results for $\gamma \gamma \rightarrow p \overline{p}$
 - comparison with data from e^+e^- collisions
- 3) predictions for *Pb Pb* \rightarrow *Pb Pb* $p\overline{p}$

Based on:

M. Kłusek-Gawenda, P. Lebiedowicz, O. Nachtmann, and A. Szczurek, From the $\gamma\gamma \rightarrow p\overline{p}$ reaction to the production of $p\overline{p}$ pairs in ultraperipheral ultrarelativistic heavy-ion collisions at the LHC, Phys. Rev. D96 (2017) 094029

Nuclear reaction



The quantities \overline{b}_x , \overline{b}_y are the components of the b_1 and b_2 vectors which mark a point (distance from first and second nucleus) where photons collide and particles are produced.

$\gamma \gamma \rightarrow p \overline{p}$ reaction

nonresonant proton exchange



• s-channel tensor meson exchange – $f_2(1270)$ and $f_2(1950)$



• hand-bag mechanism (M. Diehl, P. Kroll, C. Vogt, Eur. Phys. J. C26 (2003) 567)



+ diagram with photon vertices interchanged

Proton exchange contribution



 F_1 and F_2 are Dirac and Pauli form factors of proton, respectively; for real photons: $F_1(0) = 1$ and $F_2(0) = \kappa_p = 1.7928$

 Virtual protons are off-shell. We take the off-shell dependences into account via multiplication of "bare" amplitude by an extra form factor

$$\mathcal{M}^{(p \text{ exchange})} = \mathcal{M}_{\text{bare}}^{(p \text{ exchange})} F(t, u, s); \qquad F(t, u, s) = \frac{[F(t)]^2 + [F(u)]^2}{1 + [\tilde{F}(s)]^2}$$

$$[M.Poppe, \text{ Int.J.Mod.Phys.A1 (1986) 545}]$$

$$F(t) = \exp\left(\frac{t - m_p^2}{\Lambda_p^2}\right), \quad \tilde{F}(s) = \exp\left(\frac{-(s - 4m_p^2)}{\Lambda_p^2}\right), \quad F(m_p^2, m_p^2, 4m_p^2) = 1$$

Our amplitude satisfied the gauge-invariance and the Bose-symmetry relations. 3

Comparison with Belle data



- Clearly, the proton exchange contribution is not sufficient to describe the Belle data [C.C.Kuo *et al.* (Belle Collaboration) Phys. Lett. B621 (2005) 41]
- Pauli-type coupling is very important, enhances the cross section considerably. Large interference effect of Dirac- and Pauli-type terms in the amplitude

Angular distributions



Closer to the threshold energy the angular distributions become flatter and flatter

• We find dominance of the amplitudes ψ_1 and ψ_2 . Contributions of ψ_3 , ψ_4 , ψ_5 , and ψ_6 , are suppressed in $\cos\theta = \pm 1$. This is clear from angular momentum conservation.

f_2 meson contribution

$$\gamma(k_{1}) \bigvee_{\gamma(k_{2})} \int_{p_{s}} \int_{p_{s}} \int_{p(p_{4})} \int_{p(p_{4})}$$

• $f_2 \gamma \gamma$ vertex

$$i\Gamma^{(f_2\gamma\gamma)}_{\mu\nu\kappa\lambda}(k_1,k_2) = i\left[2a_{f_2\gamma\gamma}F^{(f_2\gamma\gamma)}_a(s)\Gamma^{(0)}_{\mu\nu\kappa\lambda}(k_1,k_2) - \frac{b_{f_2\gamma\gamma}}{b_{f_2\gamma\gamma}}F^{(f_2\gamma\gamma)}_b(s)\Gamma^{(2)}_{\mu\nu\kappa\lambda}(k_1,k_2)\right]$$

where *a* and *b* parametrise the so-called helicity 0 and helicity 2 $f_2 \rightarrow \gamma \gamma$ amplitudes [C.Ewerz, M. Maniatis, O. Nachtmann, Annals Phys. 342 (2014) 31]

• $f_2 pp$ vertex $i\Gamma_{\kappa\lambda}^{(f_2p\bar{p})(1)}(p_3,p_4) = -i\frac{g_{f_2pp}^{(1)}}{M_0} \left[\frac{1}{2}\gamma_\kappa(p_3-p_4)_\lambda + \frac{1}{2}\gamma_\lambda(p_3-p_4)_\kappa - \frac{1}{4}g_{\kappa\lambda}(\not\!p_3-\not\!p_4)\right] F^{(f_2p\bar{p})(1)}(s)$ $i\Gamma_{\kappa\lambda}^{(f_2p\bar{p})(2)}(p_3,p_4) = -i\frac{g_{f_2pp}^{(2)}}{M_{\star}^2} \left[(p_3 - p_4)_{\kappa}(p_3 - p_4)_{\lambda} - \frac{1}{4}g_{\kappa\lambda}(p_3 - p_4)^2 \right] F^{(f_2p\bar{p})(2)}(s)$ Here $g_{f_{2}nn}^{(j)}$ (j = 1, 2) are dimensionless coupling constants and $M_0 \equiv 1$ GeV. The complete $f_2 p \bar{p}$ vertex function is given by $i\Gamma_{\kappa\lambda}^{(f_2p\bar{p})}(p_3,p_4) = \sum i\Gamma_{\kappa\lambda}^{(f_2p\bar{p})(j)}(p_3,p_4)$ • f_2 propagator $i\Delta^{(f_2)}_{\alpha\beta,\kappa\lambda}(p_s) = iP^{(2)}_{\alpha\beta,\kappa\lambda}(p_s)\Delta^{(2)}(p_s^2)$ $= i \left[\frac{1}{2} \left(\hat{g}_{\alpha\kappa} \hat{g}_{\beta\lambda} + \hat{g}_{\alpha\lambda} \hat{g}_{\beta\kappa} \right) - \frac{1}{3} \hat{g}_{\alpha\beta} \hat{g}_{\kappa\lambda} \right] \frac{1}{p_s^2 - m_{f_s}^2 + i m_{f_2} \Gamma_{f_2}}$

Helicity amplitudes for $\gamma \gamma \rightarrow f_2 \rightarrow p\overline{p}$

 $\langle p(s_3), \bar{p}(s_4) | \mathcal{T} | \gamma(m_1), \gamma(m_2) \rangle \equiv \langle 2s_3, 2s_4 | \mathcal{T} | m_1, m_2 \rangle,$ $2s_3, 2s_4, m_1, m_2 \in \{+1, -1\}$

$$\begin{split} \langle 2s_{3}, 2s_{4} | \mathcal{T} | +, + \rangle &= \langle 2s_{3}, 2s_{4} | \mathcal{T} | -, - \rangle \\ &= -\frac{1}{2} s^{2} \sqrt{s - 4m_{p}^{2}} \Delta^{(2)}(s) \, a_{f_{2}\gamma\gamma} \, F_{a}^{(f_{2}\gamma\gamma)}(s) \\ &\times \Big\{ \frac{g_{f_{2}pp}^{(1)}}{M_{0}} F^{(f_{2}p\bar{p})(1)}(s) \Big[- 2m_{p} \Big(\cos^{2}\theta - \frac{1}{3} \Big) \, \delta_{s_{3}s_{4}} - \sqrt{s} \sin \theta \cos \theta \, \varepsilon_{s_{3}s_{4}} \Big] \\ &+ \frac{g_{f_{2}pp}^{(2)}}{M_{0}^{2}} F^{(f_{2}p\bar{p})(2)}(s) \, (s - 4m_{p}^{2}) \Big(\cos^{2}\theta - \frac{1}{3} \Big) \, \delta_{s_{3}s_{4}} \Big\} \\ \langle 2s_{3}, 2s_{4} | \mathcal{T} | \pm, \mp \rangle \\ &= -\frac{1}{2} s \sqrt{s - 4m_{p}^{2}} \Delta^{(2)}(s) \, b_{f_{2}\gamma\gamma} \, F_{b}^{(f_{2}\gamma\gamma)}(s) \\ &\times \Big\{ \frac{g_{f_{2}pp}^{(1)}}{M_{0}} F^{(f_{2}p\bar{p})(1)}(s) \Big[- 2m_{p} \sin^{2}\theta \, \delta_{s_{3}s_{4}} + \sqrt{s} \sin \theta \cos \theta \, \varepsilon_{s_{3}s_{4}} \pm \sqrt{s} \sin \theta \, \delta_{s_{3}, -s_{4}} \Big] \\ &+ \frac{g_{f_{2}pp}^{(2)}}{M_{0}^{2}} F^{(f_{2}p\bar{p})(2)}(s) \, (s - 4m_{p}^{2}) \sin^{2}\theta \, \delta_{s_{3}s_{4}} \Big\} \end{split}$$

• We assume the same form for the form factors

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 $F(s) = rac{\Lambda_{f_2,pow}^4}{\Lambda_{f_2,pow}^4 + (s - m_{f_2}^2)^2}$

Angular distributions



Here the model parameters (form factors, coupling constants) are fixed arbitrarily. Only the ψ_1 and ψ_2 amplitudes (solid line in left panel) are favored by the Belle data.

Hand-bag approach



The $\gamma\gamma \rightarrow p\overline{p}$ amplitude factorizes into a hard $\gamma\gamma \rightarrow q\overline{q}$ subprocess and a matrix element describing the soft $q\overline{q} \rightarrow p\overline{p}$ transition. [M. Diehl, P. Kroll, C. Vogt, Eur. Phys. J. C26 (2003) 567]

$$\widetilde{\mathcal{M}}_{s_3s_4,m_1m_2} = \mathcal{A}_{s_3s_4,m_1m_2} + \frac{m_p}{\sqrt{s}} \Big[2s_3\mathcal{A}_{-s_3s_4,m_1m_2} + 2s_4\mathcal{A}_{s_3-s_4,m_1m_2} \Big] + \mathcal{O}(m_p^2/s)$$

$$\mathcal{A}_{s_3s_4,+-} = -(-1)^{s_3-s_4} \mathcal{A}_{-s_3-s_4,-+} = 4\pi\alpha_{em} \frac{s}{\sqrt{tu}} \left\{ \delta_{s_3,-s_4} \frac{t-u}{s} R_V(s) + 2s_3 \delta_{s_3,-s_4} \left[R_A(s) + R_P(s) \right] - \frac{\sqrt{s}}{2m_p} \delta_{s_3s_4} R_P(s) \right\}$$

The $q\overline{q} \rightarrow p\overline{p}$ transition form factors $R_{V}(s)$, $R_{A}(s)$ and $R_{p}(s)$ were determined phenomenologically. We neglect the term with $R_{V}(s)$ and assume $\frac{\sqrt{s}}{2m_{p}}$

 $\frac{\sqrt{s}}{2m_p} \left| \frac{R_P(s)}{R_A(s)} \right| = 0.37.$ [formula (45) of DKV]

We parametrize $R_A(s) = C_A/s$ with C_A a parameter of dimension GeV² which we shall determine from a fit to the Belle data.

Due to different phase conventions we have: $\langle 2s_3, 2s_4 | \mathcal{T} | \pm, \mp \rangle_{hb} = 2s_4 \widetilde{\mathcal{M}}_{s_3 s_4, \pm \mp}$

We cut off the region of small |t| and |u| where the hand-bag approach does not apply. We multiply the hand-bag amplitudes by a purely phenomenological factor:

$$F_{corr}(t,u) = \left(1 - \exp\left(\frac{t}{\Lambda_{hb}^2}\right)\right) \left(1 - \exp\left(\frac{u}{\Lambda_{hb}^2}\right)\right)$$

Comparison with experimental data



One can observe the dominance of the $f_2(1950)$ resonance term at low energies. We slightly underestimate the Belle data around $W_{yy} = 2.6$ GeV.

Comparison with experimental data



Comparison with Belle data



Predictions for nuclear reaction



- $f_2(1950)$ contribution dominates at low $W_{\gamma\gamma} \equiv M_{pp}$ and at z=0, ±1
- *p*-exchange contribution is concentrated mostly at larger $M_{p\bar{p}}$ and $z = \pm 1$
- cross section is concentrated at $y_p \simeq y_{\overline{p}}$

Predictions for nuclear reaction



 σ = 500 µb (CMS cuts), 160 µb (ATLAS cuts), 100 µb (ALICE cuts), 104 µb (LHCb cuts)

We predict 46 events for |y| < 0.9, $p_t > 1$ GeV, and $L_{int} = 95 \mu b^{-1}$ (ALICE)

→ important background for coherent $J/\psi \rightarrow p\overline{p}$ photoproduction

Conclusions

- To describe the dynamics of the $\gamma\gamma \rightarrow p\overline{p}$ process we take into account not only the non-resonant proton exchange contribution but also the *s*-channel tensor meson exchange contributions and the hand-bag mechanism.
- In our calculation of non-resonant contribution we have included both Dirac- and Pauli-type couplings of the photon to the nucleon and form factors for exchanged off-shell protons. We have found that the Pauli-type coupling is very important, enhances the cross section considerably, and cannot be neglected.
- We have shown that the Belle data for low $\gamma\gamma$ energies can be nicely described by including the $f_2(1950)$ resonance.
- Having described the angular distributions for the $\gamma\gamma \rightarrow p\overline{p}$ process we made predictions for Pb-Pb collisions. Both, the total cross section and several differential distributions including experimental cuts were presented.
- We predict large cross sections (e.g., 100 μb for ALICE cuts, 500 μb for CMS cuts).

This opens a possibility to study the $\gamma\gamma \rightarrow p\overline{p}$ process in UPC at the LHC and may provide new information compared to the presently available data from e^+e^- collisions, in particular, if structures of y_{diff} distribution can be observed.

Extra Slides



Comparison with experimental data



One can observe the dominance of the $f_2(1950)$ resonance term at low energies. We slightly underestimate the Belle data around $W_{yy} = 2.6$ GeV.

parameter for	eq.	value (set A)	value (set B)
non-resonant $p\bar{p}$			
κ_p		1.7928	1.7928
Λ_p		$1.08 {\rm GeV}$	$1.07 {\rm GeV}$
$f_2(1270)$			
$a_{f_2\gamma\gamma}$		$\frac{e^2}{4\pi}$ 1.45 GeV ⁻³	$\frac{e^2}{4\pi}$ 1.45 GeV ⁻³
$b_{f_2\gamma\gamma}$		$\frac{e^2}{4\pi}$ 2.49 GeV ⁻¹	$\frac{e^2}{4\pi} 2.49 \text{ GeV}^{-1}$
M_0		1 GeV	1 GeV
$g_{f_2pp}^{(1)}$		11.04	11.04
$g_{f_2nn}^{(\bar{2})}$		0	0
$\Lambda_{f_2,pow}^{f_2pp}$		$1.15~{\rm GeV}$	$1 { m GeV}$
$f_2(1950)$			
$a_{f_2\gamma\gamma}g^{(2)}_{f_2pp}$		$\frac{e^2}{4\pi}$ 13.05 GeV ⁻³	$\frac{e^2}{4\pi}$ 12 GeV ⁻³
$b_{f_2\gamma\gamma}$		0	0
$g_{f_2nn}^{(1)}$		0	0
$\Lambda_{f_2,pow}^{_{J2PP}}$		$1.15~{\rm GeV}$	$1.15~{\rm GeV}$
hand-bag contribution			
C_A	$R_A(s) = C_A/s$	$0.14~{ m GeV^2}$	
\tilde{C}_A	$R_A(s) = \tilde{C}_A/s^2$		$2.5~{ m GeV^4}$
$ \qquad \Lambda_{hb}$		$0.85~{ m GeV}$	$0.85~{ m GeV}$

Table 1: Model parameters and their numerical values used.

Resonances that may contribute to $\gamma\gamma \rightarrow p\overline{p}$ reaction

Meson	m (MeV)	Γ (MeV)	$\Gamma_{p\bar{p}}/\Gamma$	$\Gamma_{\gamma\gamma}/\Gamma$
$f_2(1270)$	1275.5 ± 0.8	$186.7^{+2.2}_{-2.5}$		$(1.42 \pm 0.24) \times 10^{-5}$
$f_2(1950)$	1944 ± 12	472 ± 18	seen	seen
$\eta_c(1S)$	2983 ± 0.5	31.8 ± 0.8	$(1.50 \pm 0.16) \times 10^{-3}$	$(1.59 \pm 0.13) \times 10^{-4}$
$\chi_{c0}(1P)$	3414.75 ± 0.31	10.5 ± 0.6	$(2.25 \pm 0.09) \times 10^{-4}$	$(2.23 \pm 0.13) \times 10^{-4}$
$\chi_{c2}(1P)$	3556.20 ± 0.09	1.93 ± 0.11	$(7.5 \pm 0.4) \times 10^{-5}$	$(2.74 \pm 0.14) \times 10^{-4}$
$\eta_c(2S)$	3639.2 ± 1.2	$11.3^{+3.2}_{-2.9}$	$ $ $< 2 \times 10^{-3}$	$(1.9 \pm 1.3) \times 10^{-4}$

- Above we listed also the sub-threshold $f_2(1270)$ resonance
- The meson masses, their total widths and branching fractions are taken from PDG
- Our knowledge about the $f_2(1950)$ resonance comes from the BES and the CLEO analyses for $\psi(2S) \rightarrow \gamma f_2(1950) \rightarrow \gamma p \overline{p}$
- The tensor mesons were also needed to describe the Belle data for $\gamma\gamma \rightarrow \pi\pi$ processes [see e.g. M. Kłusek-Gawenda and A. Szczurek, Phys. Rev. C87 (2013) 054908]
- The charmonium states (η_c , χ_{c0}) have small total widths thus they will appear as narrow peaks [see e.g. P. Lebiedowicz and A. Szczurek, Phys. Lett. B772 (2017) 330] for $\gamma\gamma \rightarrow \gamma\gamma$ reaction

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