

# Interferometry correlations in central p+Pb collisions

based on: <https://doi.org/10.1140/epjc/s10052-017-5482-5> (with P. Bożek)

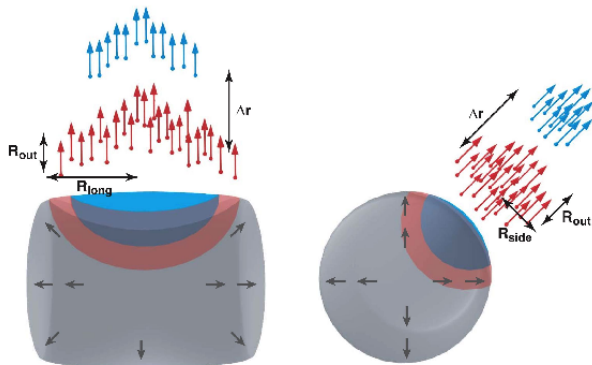
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XIII Workshop on Particle Correlations and Femtoscopy,  
Kraków 2018

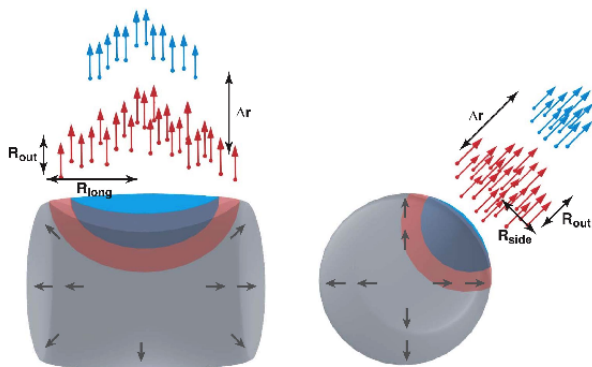
# HBT radii and Bersch – Pratt coordinate system

M. A. Lisa and S. Pratt (2008), arXiv:0811.1352



# HBT radii and Bersch – Pratt coordinate system

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$$k_T = \frac{p_1 + p_2}{2} \quad q = p_1 - p_2$$

$$C(q) = 1 + \lambda \exp(-R_o^2 q_o^2 - R_s^2 q_s^2 - R_l^2 q_l^2)$$

# Form of correlation function:

$$C(q, k) = \frac{\int d^4x_1 d^4x_2 S(x_1, p_1) S(x_2, p_2) |\Psi(q, x_1 - x_2)|^2}{\int d^4x_1 S(x_1, p_1) \int d^4x_2 S(x_2, p_2)}$$

$$C(p^a, p^b) = \frac{\frac{dN^{ab}}{d^3p^a d^3p^b}}{\left(\frac{dN^a}{d^3p^a}\right) \left(\frac{dN^b}{d^3p^b}\right)}$$

$$C(q_a, k_b) = \frac{\frac{1}{N_{pairs,num}} \sum_{j=1}^{N_h} \sum_{l \neq m=1}^{N_e} \sum_{s=1}^{M_l} \sum_{f=1}^{M_m} \delta_{q_a} \delta_{k_b} |\Psi(q, x_1 - x_2)|^2}{\frac{1}{N_{pairs,den}} \sum_{i \neq j=1}^{N_h} \sum_{l,m=1}^{N_e} \sum_{s=1}^{M_l} \sum_{f=1}^{M_m} \delta_{q_a} \delta_{k_b}}$$

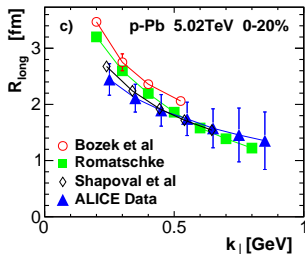
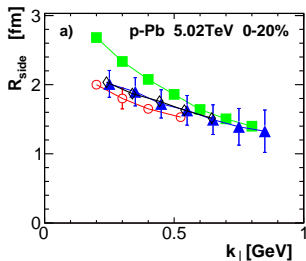
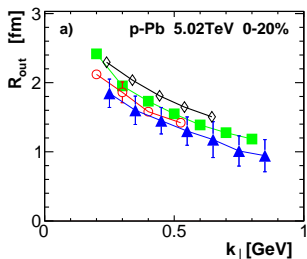
numerator: pion pairs from events generated from **the same** hypersurface

denominator: pion pairs from events generated from **different**

hypersurfaces ( $i \neq j$ ) – combinatorical background

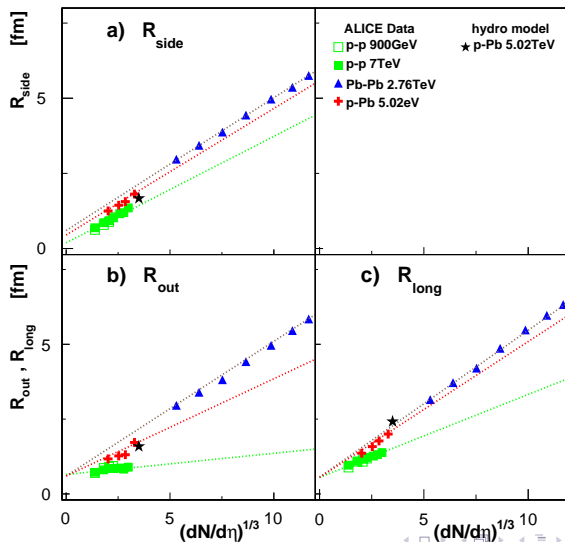
# 3 standard HBT radii in hydro

Hydro works in small systems



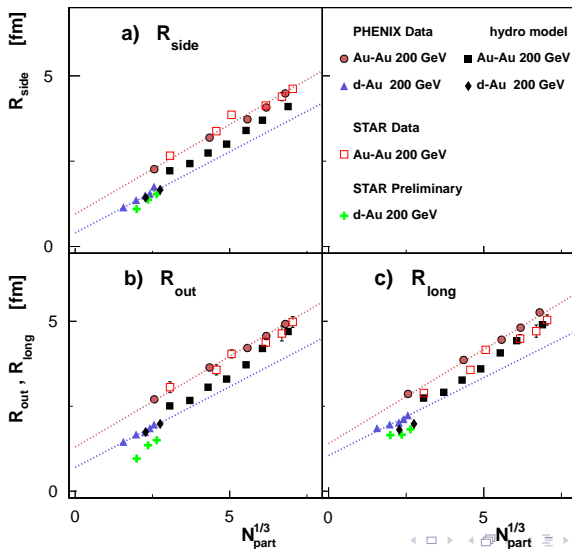
# 3 standard HBT radii in hydro – various systems

$R_{out}$ ,  $R_{side}$ ,  $R_{long}$  are fairly well reproduced by hydro models.



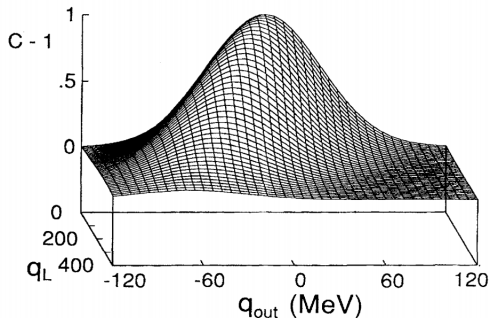
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# $R_{out-long}$ cross term

Proposed in *S. Chapman, et al, Phys. Rev. Lett. 74,4400 (1995)*.

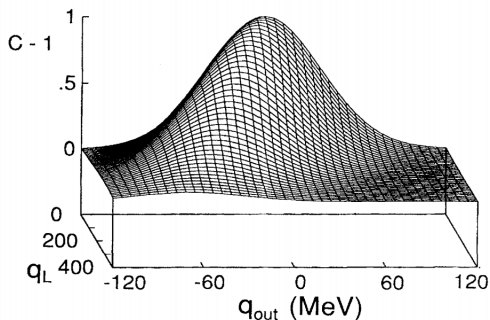


$$C(\mathbf{q}) = 1 + \lambda \exp \left( -R_o^2 q_o^2 - R_s^2 q_s^2 - R_l^2 q_l^2 - 2R_{ol}^2 q_o q_l \right)$$



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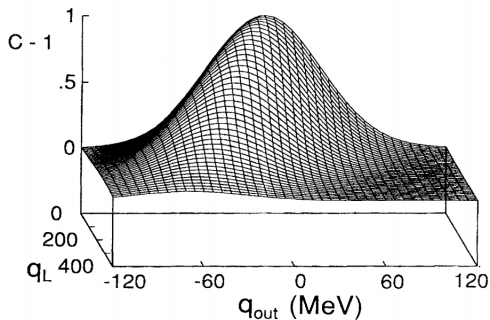
$$C(\mathbf{q}) = 1 + \lambda \exp \left( -R_o^2 q_o^2 - R_s^2 q_s^2 - R_l^2 q_l^2 - 2R_{ol}^2 q_o q_l \right)$$

In symmetric systems:  $R_{ol} = 0$  in central rapidity.

$R_{ol} \neq 0$  in non-central rapidity.

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$R_{ol} \neq 0$  also for asymmetric systems.

# Cross terms

In azimuthally sensitive analyses (*arXiv:1408.1264*) :

$$R_{0l}^2 = H_1 + I_1 - G_0\beta_{\perp} + (I_1 + I_3 - H_1 + H_3)\cos(2\Phi)$$

where,  $G_i, H_i, I_i$ :

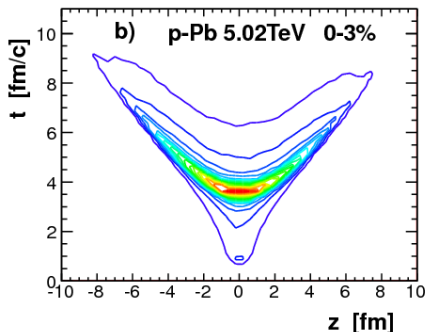
$$\langle tz \rangle - \langle t \rangle \langle z \rangle = G_0 + 2 \sum_{n=2,4,\dots} G_n \cos(n\Phi)$$

$$\langle xz \rangle - \langle x \rangle \langle z \rangle = 2 \sum_{n=1,3,\dots} H_n \cos(n\Phi)$$

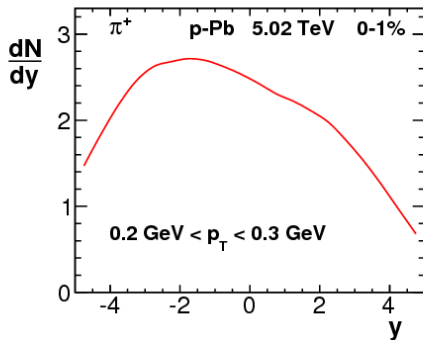
$$\langle yz \rangle - \langle y \rangle \langle z \rangle = 2 \sum_{n=1,3,\dots} I_n \sin(n\Phi)$$

Most significant among angle independent terms is  $G_0$ , appearing in Fourier expansion of time – beam-along moment of the emission function  $S(x, k)$

$R_{out-long}$  – consequence of asymmetry in time evolution of source  $\Rightarrow$   
it results in not boost invariant  $y$  distribution



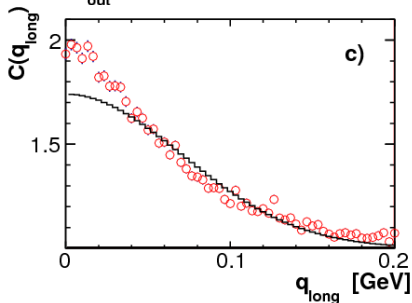
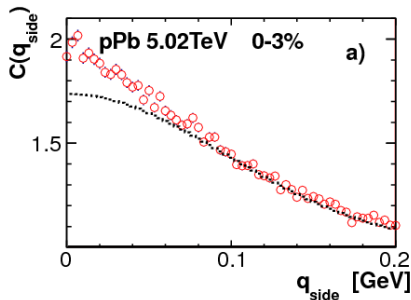
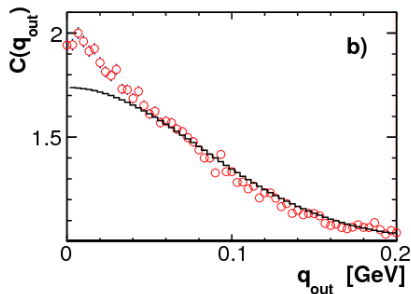
*hydrodynamic emission source  
in asymmetric p+Pb collisions*



$$\langle tz \rangle - \langle t \rangle \langle z \rangle \neq 0$$

## Gaussian parameterization:

$$C(q, k) = 1 + \lambda \exp(-R_o^2 q_o^2 - R_s^2 q_s^2 - R_l^2 q_l^2 - 2R_{ol}^2 q_o q_l)$$



# Non – gaussian parametrization used by ATLAS

- First measurements including out-long coupling
- First time radii as a function of rapidity

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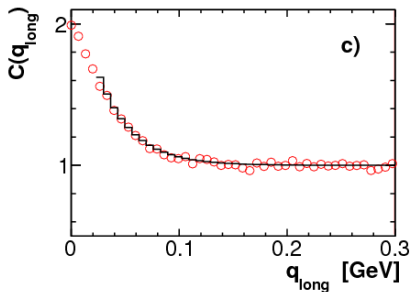
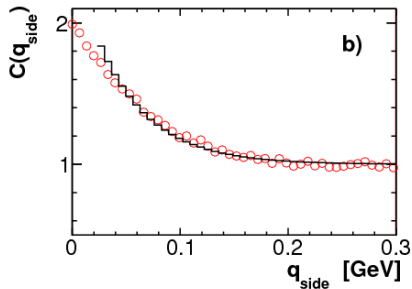
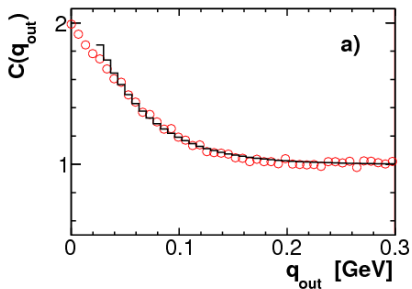
- First measurements including out-long coupling
- First time radii as a function of rapidity

$$C(\mathbf{q}) = 1 + \lambda \exp(-\|R \mathbf{q}\|)$$

$$\|R \mathbf{q}\| = \left[ \left( R_{out}^E q_{out} + R_{mix}^E q_{long} \right)^2 + \left( R_{side}^E q_{side} \right)^2 + \left( R_{long}^E q_{long} + R_{mix}^E q_{out} \right)^2 \right]^{1/2}$$

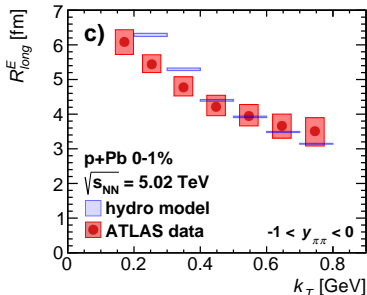
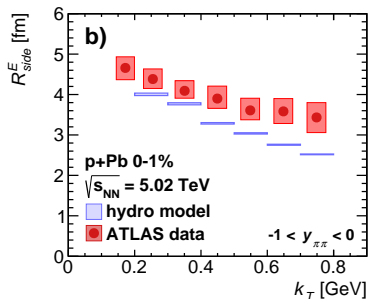
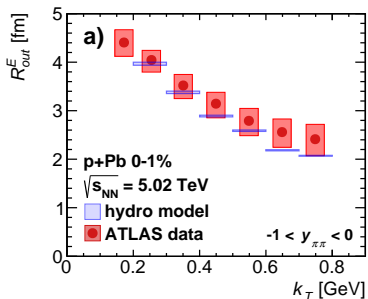
$$\|R \mathbf{q}\| = \left[ \left( R_{out}^E{}^2 + R_{mix}^E{}^2 \right) q_{out}^2 + R_{side}^E{}^2 q_{side}^2 + \left( R_{long}^E{}^2 + R_{mix}^E{}^2 \right) q_{long}^2 + 2 \left( R_{out}^E + R_{long}^E \right) R_{mix}^E q_{out} q_{long} \right]^{1/2}$$

# Non – gaussian parametrization used by ATLAS

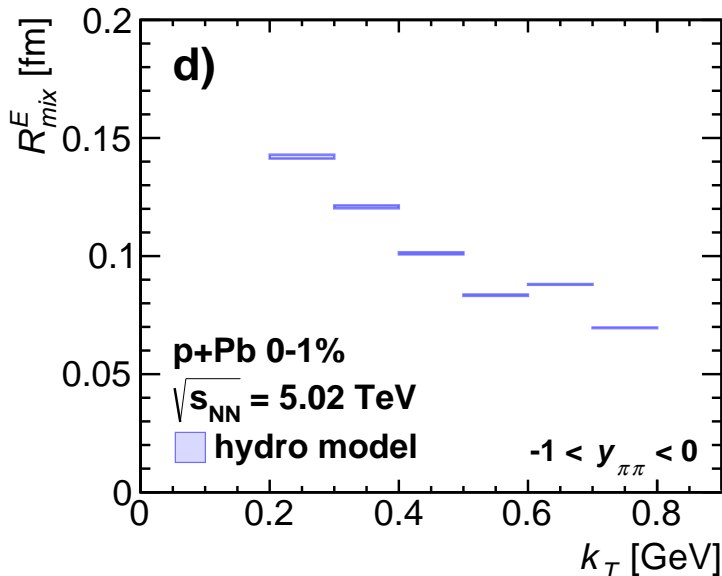




# Results – $R_{o,s,l}^E(k_T)$

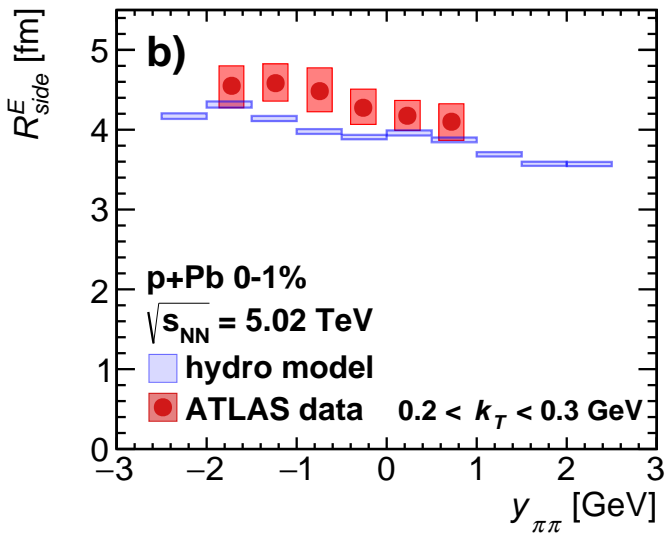


# Results – $R_{mix}^E(k_T)$



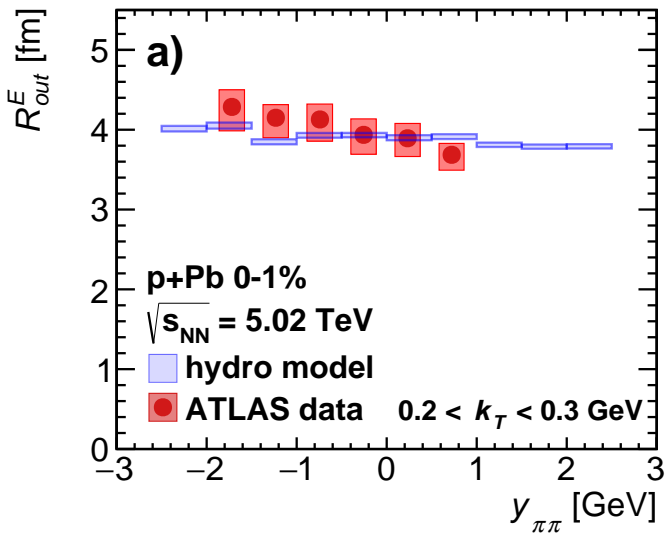
# Results – $R_{side}^E(y)$

first measurement of  $y$ -dependent HBT radii



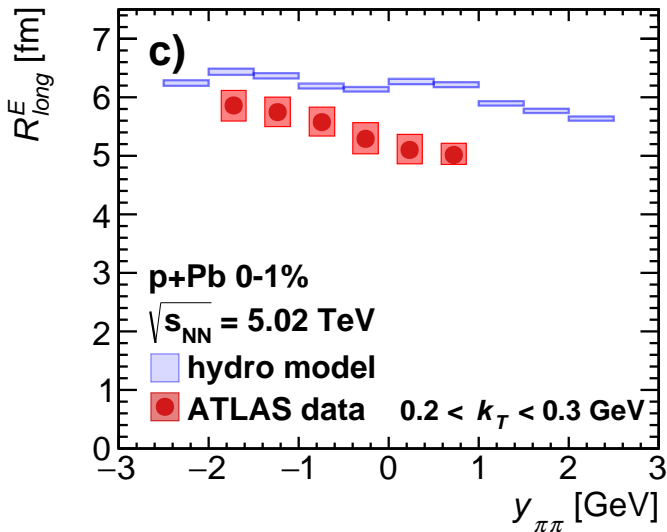
# Results – $R_{out}^E(y)$

first measurement of  $y$ -dependent HBT radii

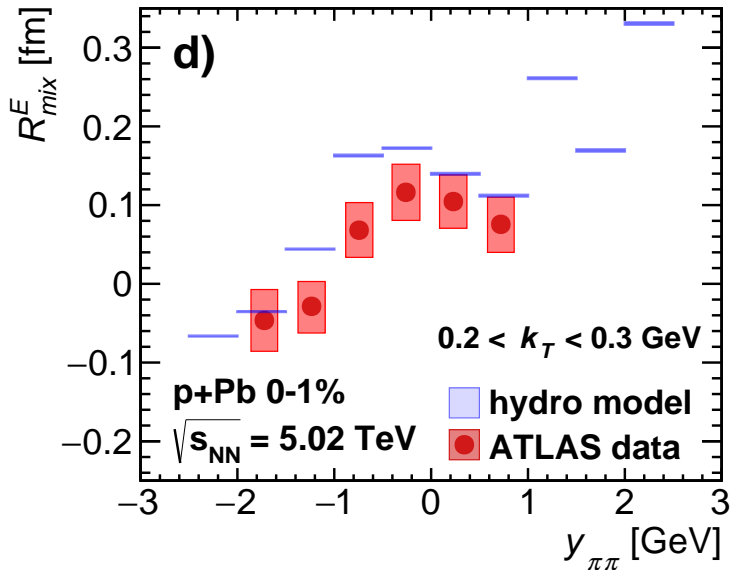


# Results – $R_{long}^E(y)$ :

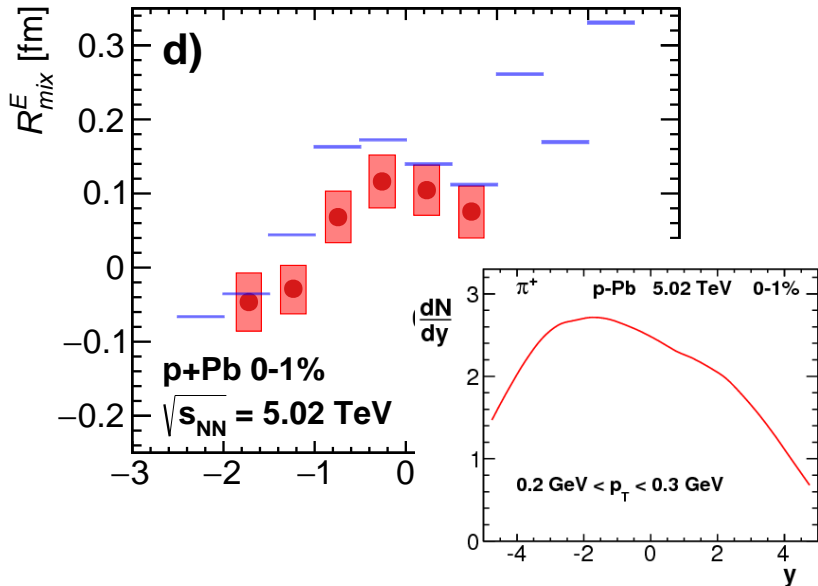
first measurement of  $y$ -dependent HBT radii



# Results – $R_{mix}^E(y)$



# Results – $R_{mix}^E(y)$



# Conclusions

- hydrodynamic models can describe (semi-)quantitatively HBT radii dependence on  $k_T$  in pPb collisions – both in gaussian and exponential parametrization
- rapidity dependence of HBT radii can be reproduced partly-qualitatively in simulations
- hydro models can explain out-long cross term in asymmetric collisions