



LumiBelle2, a fast luminosity monitor for beam tuning and feedback at the interaction point of SuperKEKB

Philip Bambade
IJCLab – Orsay

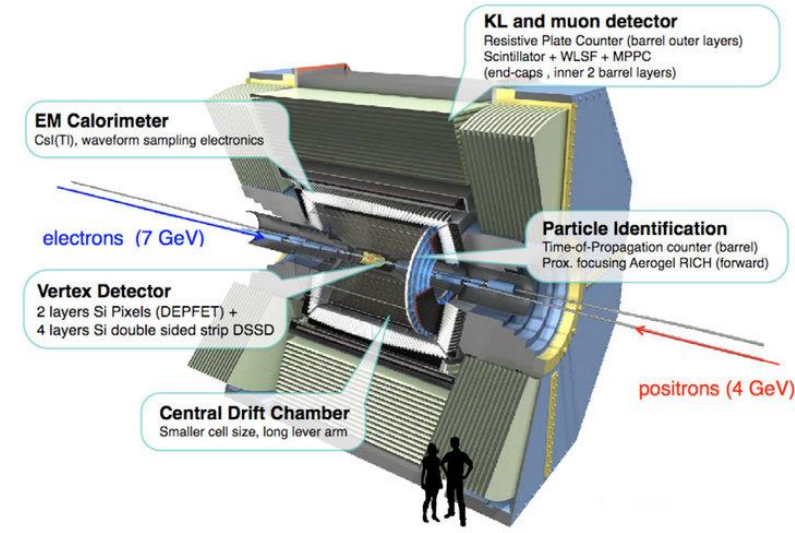
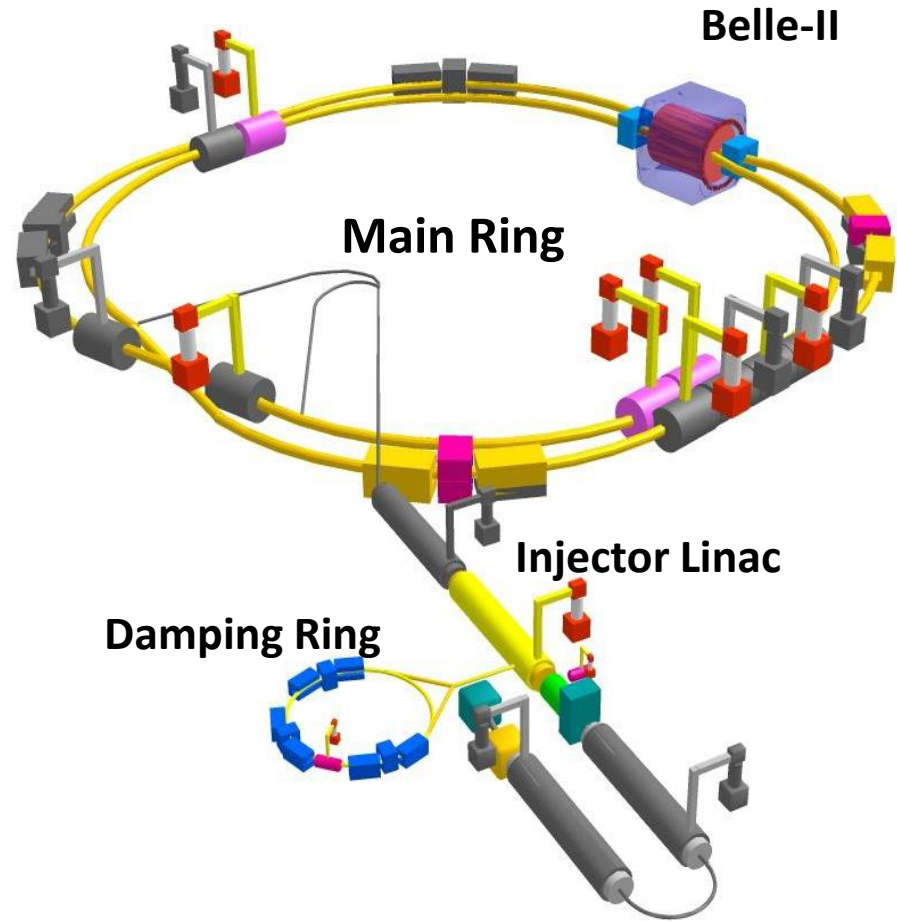
Acknowledgements: Y. Funakoshi, M. Masuzawa, H. Nakayama, Y. Ohnishi, S. Uehara (KEK – Tsukuba)

D. El Khechen (2013-2016), C.-G. Pang (2016-2019), S. Di Carlo (2017-2019), M. Li (2023-present), S. Wallon (2019-present)

The SuperKEKB/Belle II project

SuperKEKB (Electron-Positron Collider)
 C.M.S. Energy: $\sqrt{s} = 10.58 \text{ GeV}$
 Luminosity: $L = 8 \times 10^{35} \text{ cm}^{-2}\text{s}^{-1}$
 (Luminosity Frontier Machine)

	Electron	Positron
Energy (GeV)	7	4
Current (A)	3.6	2.6



Belle II (General purpose detector)

Vertex detectors: Pixel Vertex Detector (PXD),
 Silicon strip Vertex Detector (SVD)

Tracking: Central Drift Chamber (CDC)

Calorimeter: Electromagnetic CaLorimeter (ECL)

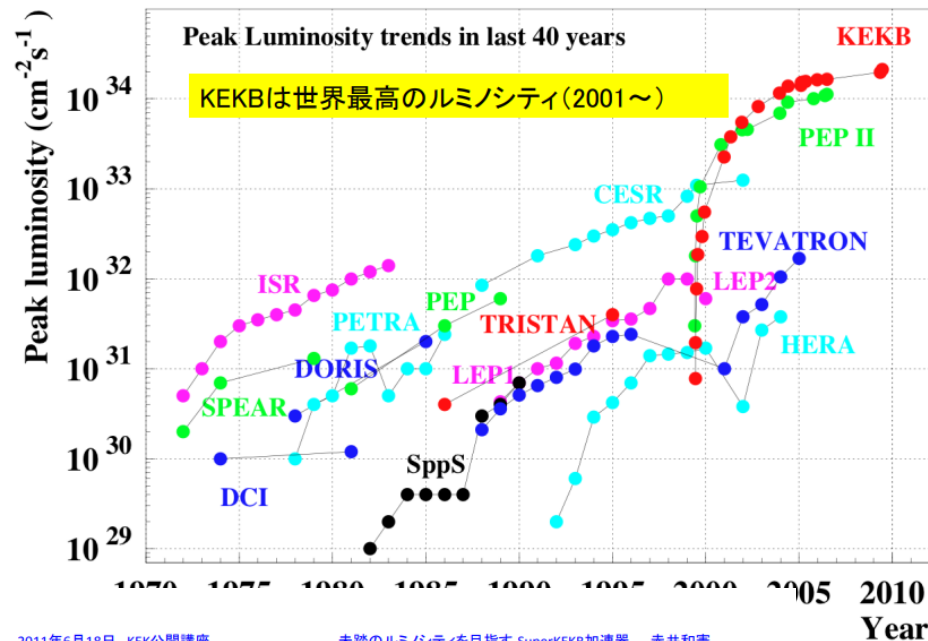
Particle ID: Aerogel Ring Image Cherenkov detector (ARICH)
 K-Long and Muon detector (KLM)
 Time-Of-Propagation counter (TOP)

Luminosity Frontier

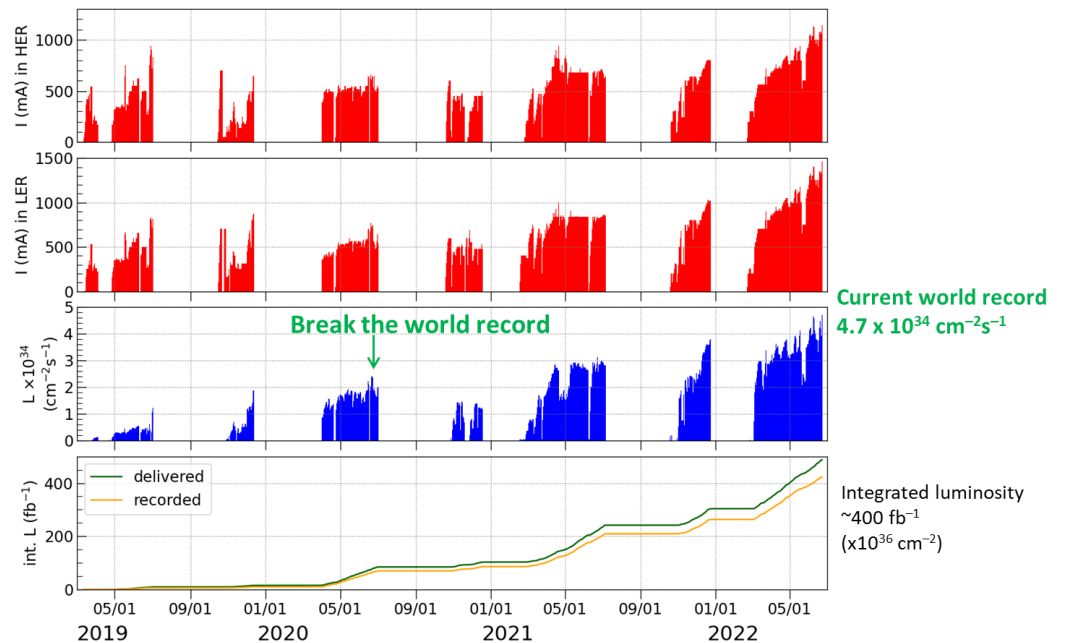
B-pair production rate (pair/sec) : $N = \sigma \times L$

σ = cross-section for B pair production = 1.1nb L = luminosity.
 \rightarrow 110 pairs of B mesons produced / second for $L = 10^{35} \text{ cm}^{-2}\text{s}^{-1}$.

World's history before SuperKEKB



Our history, current record: $4.7 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$



SuperKEKB \rightarrow uncharted luminosity territory \rightarrow new techniques

KEKB \leftrightarrow SuperKEKB parameters

		KEKB		SuperKEKB		Units
		LER (e^+)	HER (e^-)	LER (e^+)	HER (e^-)	
Beam energy	E	3.5	8.0	4.0	7.007	GeV
Circumference	C	3016.262		3016.315		m
Half crossing angle	θ_x	0(11 ^(*))		41.5		mrاد
Piwinski angle	ϕ_{piv}	0	0	24.6	19.3	rad
Horizontal emittance	ϵ_x	18	24	3.2(1.9)	4.6(4.4)	nm
Vertical emittance	ϵ_y	150	150	8.64	12.9	pm
Coupling		0.83	0.62	0.27	0.28	%
Beta function at IP	β_x^*/β_y^*	1200/5.9	1200/5.9	32/0.27	25/0.30	mm
Horizontal beam size	σ_x^*	147	170	10.1	10.7	μm
Vertical beam size	σ_y^*	940	940	48	62	nm
Horizontal betatron tune	ν_x	45.506	44.511	44.530	45.530	
Vertical betatron tune	ν_y	43.561	41.585	46.570	43.570	
Momentum compaction	α_p	3.3	3.4	3.20	4.55	10^{-4}
Energy spread	σ_E	7.3	6.7	7.92(7.53)	6.37(6.30)	10^{-4}
Beam current	I	1.64	1.19	3.60	2.60	A
Number of bunches	n_b	1584		2500		
Particle/bunch	N	6.47	4.72	9.04	6.53	10^{10}
Energy loss	U_0	1.64	3.48	1.76	2.43	MeV
Long. damping time	τ_z	21.5	23.2	22.8	29.0	msec
RF frequency	f_{RF}	508.9		508.9		MHz
Total cavity voltage	V_c	8.0	13.0	9.4	15.0	MV
Total beam power	P_b	~ 3	~ 4	8.3	7.5	MW
Synchrotron tune	ν_s	-0.0246	-0.0209	-0.0245	-0.0280	
Bunch length	σ_z	~ 7	~ 7	6.0(4.7)	5.0(4.9)	mm
beam-beam parameters	ξ_x/ξ_y	0.127/0.129	0.102/0.090	0.0028/0.088	0.0012/0.081	
Luminosity	L	2.108×10^{34}		8×10^{35}		$\text{cm}^{-2}\text{s}^{-1}$
Integrated luminosity	$\int L$	1.041		50		ab^{-1}

$\times 1/20 \beta_y$

$\sigma_y \approx 50\text{-}60 \text{ nm}$

(similar as ILC/ATF2)

$\times 2\text{-}3$ beam currents

similar beam-beam strength
(tune-shift)

\rightarrow up to $\times 40$ peak luminosity

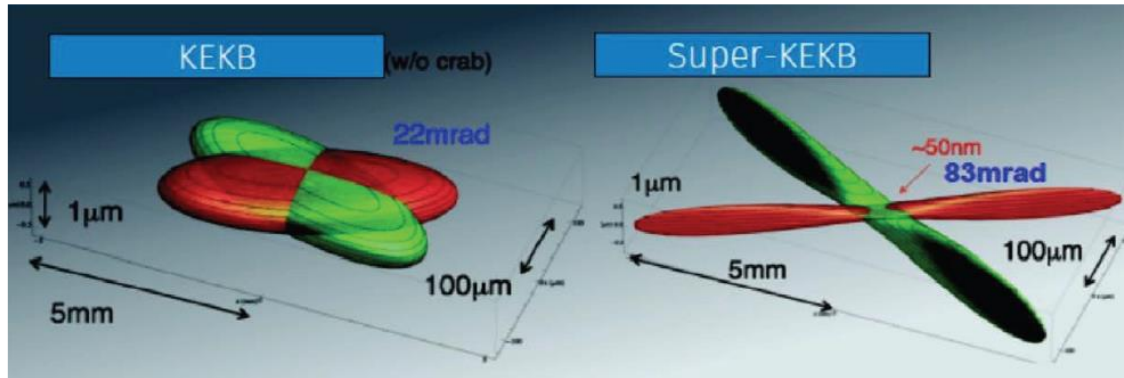
Nanobeam collision scheme

Opportunities

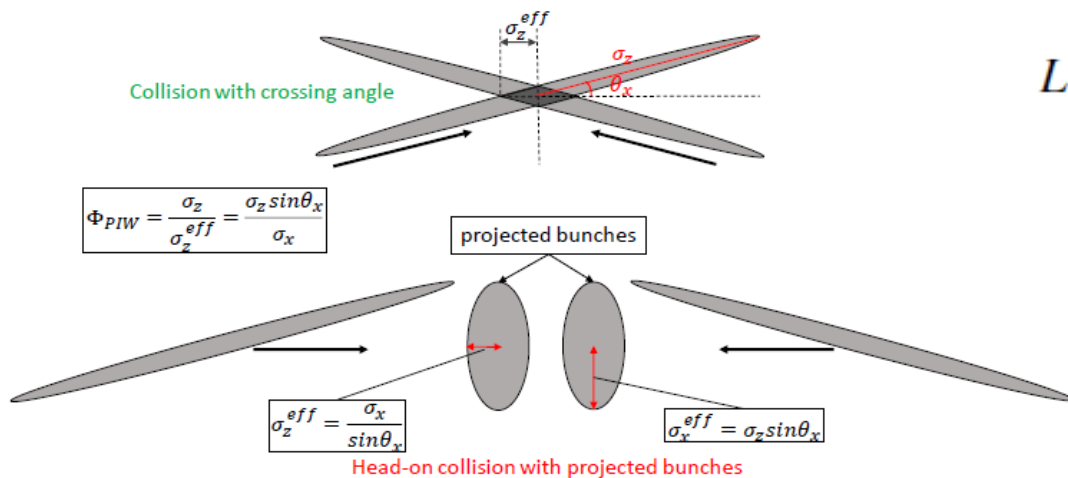
- ✓ Very small β_y avoids “hour-glass” limitation (effective bunch length \approx depth of field of the optics)
- ✓ Collide more charge @ tiny vertical beam size with similar **beam-beam tune-shift strength** parameter

Challenges

1. Optical aberrations near IP must be cancelled to achieve / maintain tiny beam spots
2. Control beam-beam tune-shift with more complex IP beam-beam dynamics + optical aberrations
3. Continuously inject intense beams in strongly demagnified IP optics \rightarrow **injection backgrounds**... beam tails...



$$\xi_{xy\pm} = \frac{r_e}{2\pi\gamma_{\pm}} \frac{N_{\mp}\beta_{xy}^*}{\sigma_{xy}^*(\sigma_x^* + \sigma_y^*)} R_{\xi_{xy}}$$



$$L = \frac{\gamma_{\pm}}{2er_e} \left(1 + \frac{\sigma_y^*}{\sigma_x^*}\right) \left(\frac{I_{\pm}\xi_{y\pm}}{\beta_{y\pm}^*}\right) \left(\frac{R_L}{R_{\xi_y}}\right)$$

$\times 1/20 \beta_y$

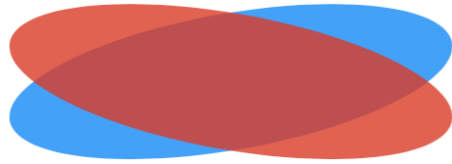
$\times 2-3$ beam currents

$$L = \frac{N_1 N_2 f n_b}{4\pi\sigma_x\sigma_y} R_L$$

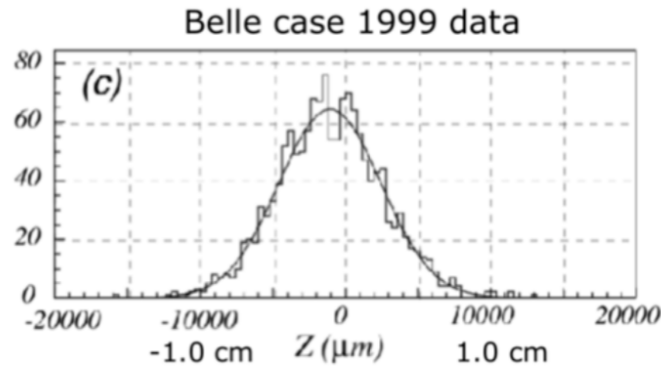
$\times 1/20 \sigma_y$

Nanobeam scheme reduced bunch overlap visible on reconstructed track vertex Z distribution

Ordinary collision KEKB



Z vertex distribution

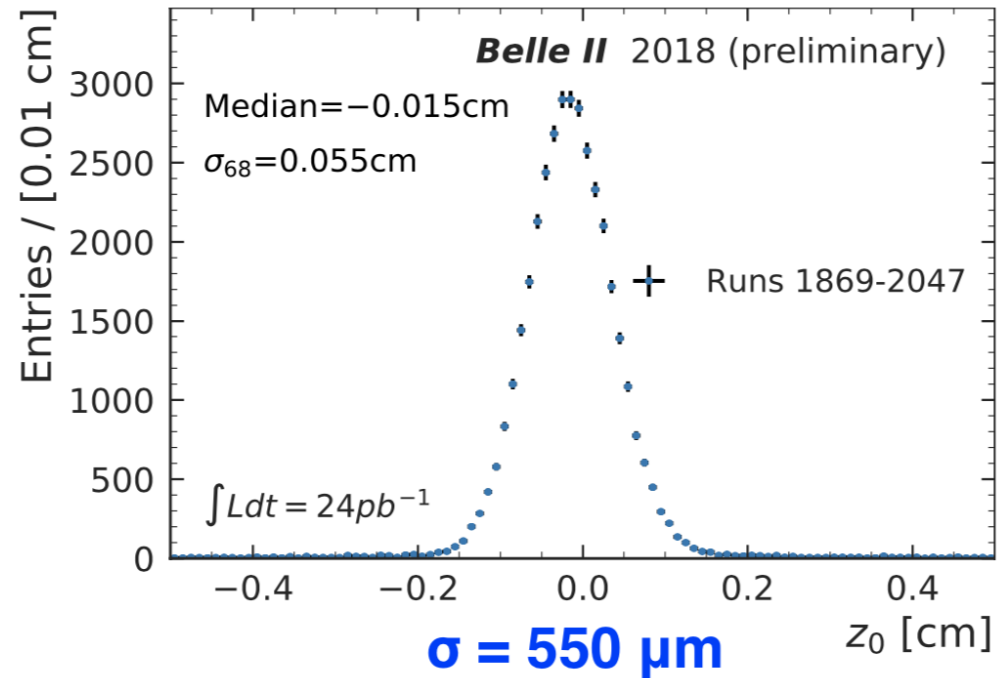


Nano-Beam (SuperKEKB)



Z vertex distribution

Belle II case 2018 data



IP optical aberrations blowing up the beam size are unavoidable

→ reliable measurement for correction only possible at the IP...

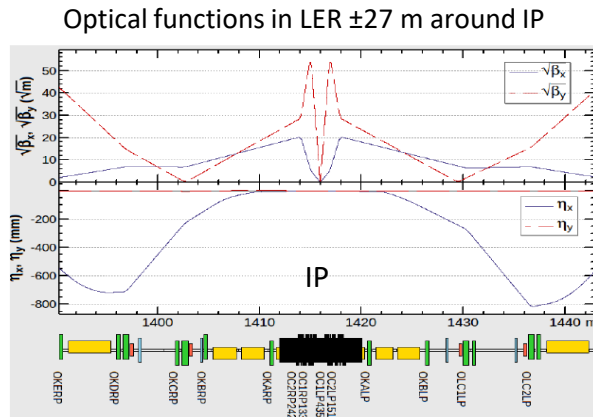
$$\sigma_y^2 = \underbrace{\mu^2 \varepsilon_y \left(\beta_y + \frac{\Delta s^2}{\beta_y} \right)}_{\text{ideal spot waist shift}} + \left\{ \frac{(R_2 + R_4 \Delta s)^2}{\beta_x} + \beta_x (R_1 + R_3 \Delta s)^2 \right\} + (\eta_y \sigma_\delta)^2$$

+ higher order terms
(geometric & chromo-geometric)

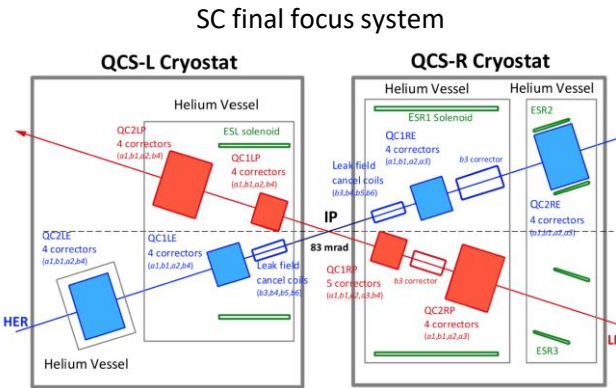
ideal spot waist shift

linear x-y coupling

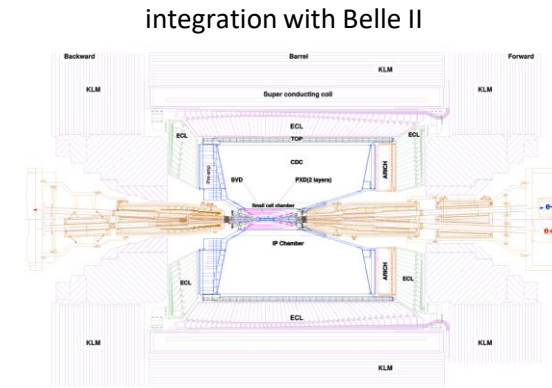
linear dispersion



Optical functions in LER ±27 m around IP

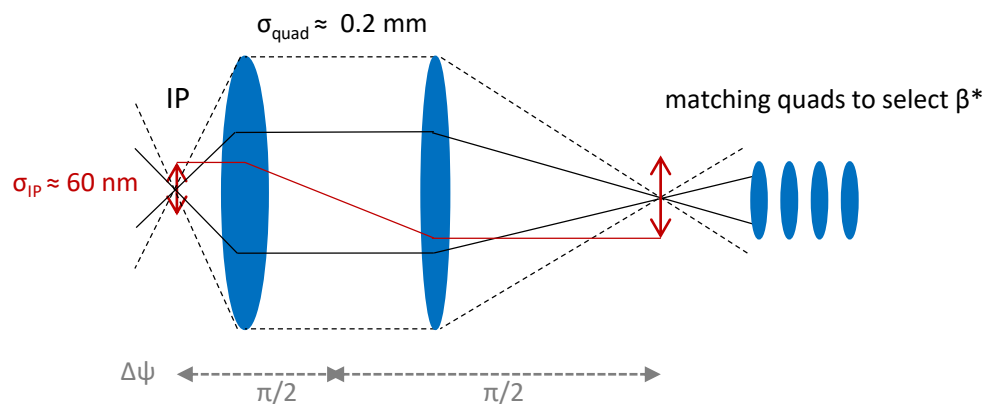


SC final focus system



integration with Belle II

quad strength tolerance for waist shift $< \beta^* / L^* \approx 3 \cdot 10^{-4}$



$$M(s_2|s_1) = \begin{pmatrix} \sqrt{\frac{\beta_2}{\beta_1}} (\cos \psi + \alpha_1 \sin \psi) & \sqrt{\beta_1 \beta_2} \sin \psi \\ -\frac{1 + \alpha_1 \alpha_2}{\sqrt{\beta_1 \beta_2}} \sin \psi + \frac{\alpha_1 - \alpha_2}{\sqrt{\beta_1 \beta_2}} \cos \psi & \sqrt{\frac{\beta_1}{\beta_2}} (\cos \psi - \alpha_2 \sin \psi) \end{pmatrix}$$

$$\Delta \psi = \int \frac{ds}{\beta(s)} \approx \pi/2 \text{ except near a waist}$$

Propagate IP aberration in low- β insertion
→ no visibility (except, possibly, at a secondary waist)

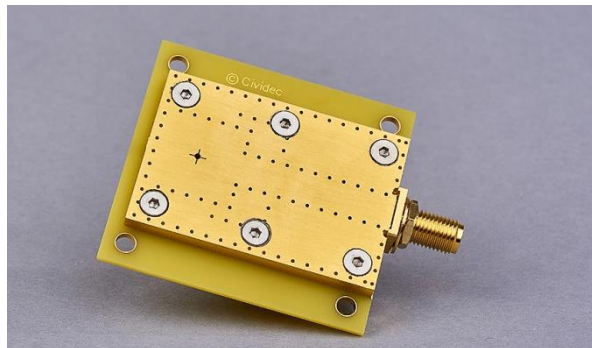
Must tune directly at IP (luminosity...)

Two complementary techniques for fast luminosity measurements

- compare / collaborate / mutually supporting
- share simulation, mechanics, some data...
- since 2012

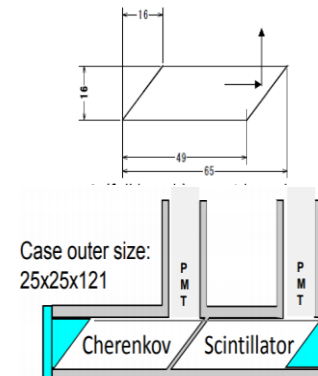
LumiBelle2 / IJCLab

- single crystal CVD diamond sensors
- $4 \times 4 \times 0.5/0.14 \text{ mm}^3$
- Fast charge/current amplifiers
- Digital electronics and processing



ZDLM (Zero Degree Luminosity Monitor) / KEK

- Cherenkov and scintillator detectors
- $15 \times 15 \times 64 \text{ mm}^3$ LGSO non-organic scintillator and ES-crystal (quartz)
- Photomultipliers
- Analog & digital processing



What for / specs ?

➤ “Dithering” feedback

- Correct for few Hz horizontal motion
- 79 Hz orbit “dithering” + luminosity sampling @ 1 kHz → reconstruct baseline freq. + 2nd harmonic
- Efficient separation from other “slow” variations
- **1% relative precision @ 1 kHz** sufficient (cf. C.-G. Pang et al., J.Phys.Conf.Ser. 1067 (2018) no.7, 072023)
- Provide analog signal as input to lock-in amplifier

➤ Bunch by bunch luminosity diagnostic

- Nominally 4 ns bunch separation → need **short signal pulses**, ideally < 4 ns
- **1% or better relative precision @ 1 Hz**

➤ IP vertical beam size measurement + tuning **at very low currents**

1. Single beam orbit + optics corrections in two rings
2. Vertical e+ and e- beam size optical tuning → suppress local aberrations in nanobeam final focus



Very low current → avoid confusion from beam-beam induced blowup

3. Control of beam-beam blowup → find best spot in tune diagram
- Dynamic range $L \approx 10^{32} \rightarrow 10^{36} \text{ cm}^{-2} \text{ s}^{-1}$
 - Non luminosity scaling contamination < 1% (e.g. beam gas bremsstrahlung and Touschek losses)
 - Manage radiation damage at highest luminosity

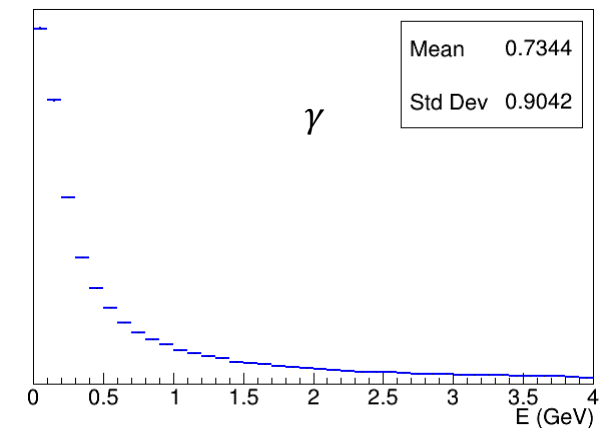
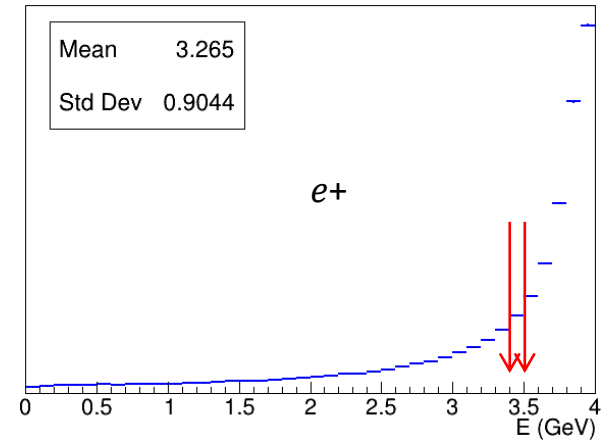
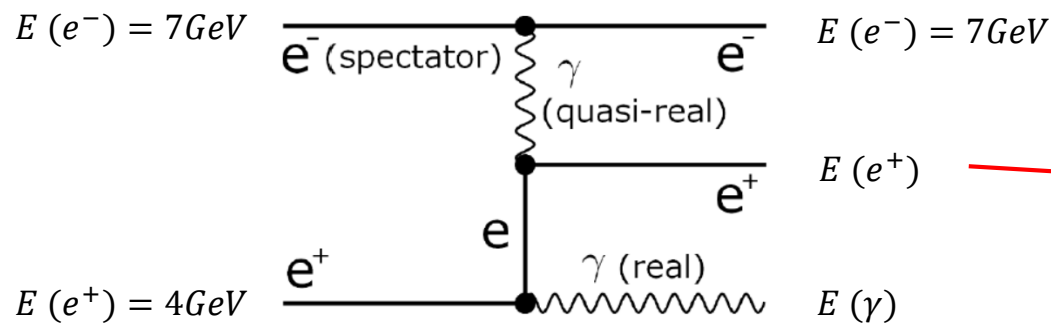
Bhabha process at vanishing scattering angle

a.k.a. Single Bremsstrahlung

Dima El Khechen et al., PRAB 22, 062801 (2019)

Large cross section $\sigma \approx 150 - 200 \text{ mbarn}$ for $E(\gamma) > 1\% E(\text{beam})$

- 1) e^+ rate in LER 10 m after IP (part of energy spectrum near $E(e^+) \approx 3.5 \text{ GeV}$ after large bend)
- 2) γ rate in HER 30 m after IP (part of 0.1-0.3 mrad IP beam angular spread due to geometry)



Only relative luminosity $\rightarrow L \propto \frac{dN}{dt}$ with certain conditions...

1. Acceptance depends on choice of sensor / location
2. Also some variation with beam parameters...
3. $\sigma_{\text{Bhabha@zero-degree}}$ not precisely computed in QED

- \rightarrow OK for usage on "short" enough time-scales
- \rightarrow care for beam parameter dependence

Theoretical prediction for small transverse beam size and large beam offset

- Finite scattering angle interaction cross-section does not depend on beam size and offset \Rightarrow ECL measurements
- Zero scattering angle interaction can occur over a range extending beyond beam size \Rightarrow ZDLM and LB2 measurements
 - ZDLM/ECL and LB2/ECL cross section ratios are suppressed for typical beam sizes of SuperKEKB, (**Fig -1-*)
 - ZDLM and LB2 counting rates decrease more slowly than ECL when beams are separated, (***Fig -2-*)

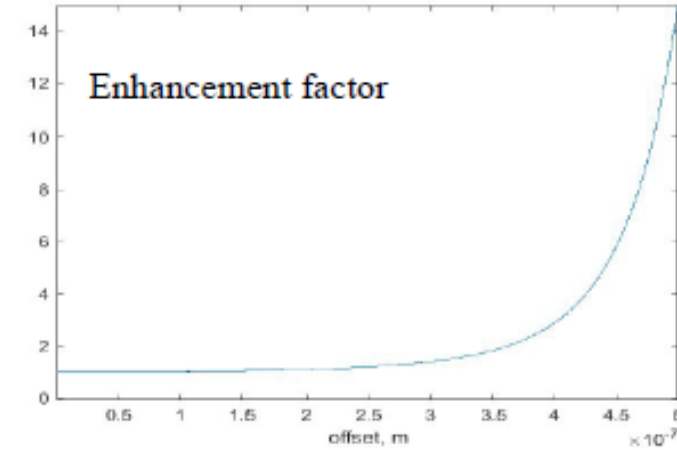
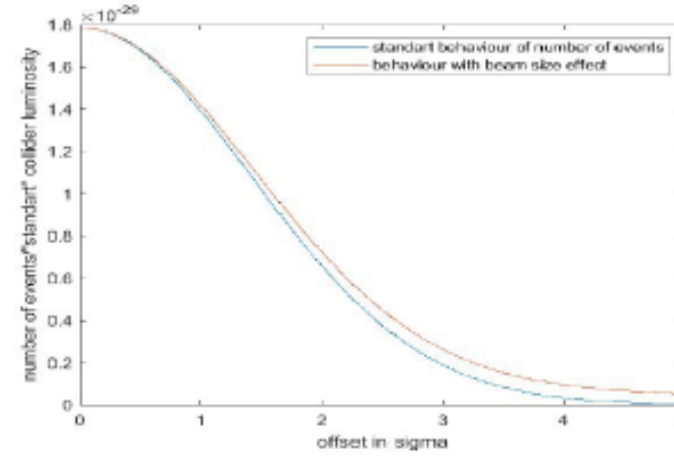
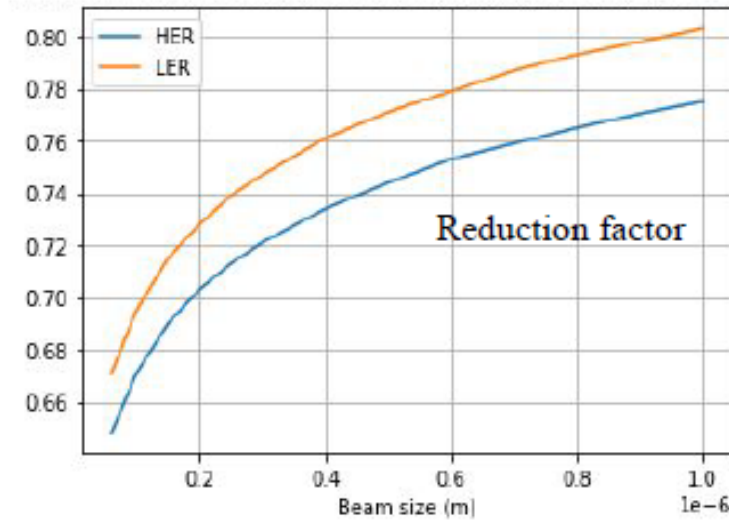


Fig -2- Left : Plots of the number of events for relative luminosity compared to absolute luminosity. Right : Plots of the ratio of number of events for LB2/ZDLM over number of events for ECL.

Fig -1- Plots of the ratio of the reduced and classical cross section with the beam size variation for positron (LER) and electron (HER) beams.

- Experimental study :
 - Comparing ZDLM and LB2 counting rate with respect to ECL during vertical beam offset scan
- Previously this effect has been studied at VEPP***

* Made by Thibaut OTTMANN, based on : "Beam-size effect and particle losses at B-factories KEKB and PEP-II, G.L. Kotkin, V.G. Serbo, NIM B 227 (2005) 137-142"

** Made by Vladyslav VINNICHENKO, based on : " V.N. Baler, V.M. Katkov and V.M. Strakhovenko, pre-print INP 81-59 (Novosibirsk, 1981) https://inp.nsk.su/images/preprint/1981_059.pdf"

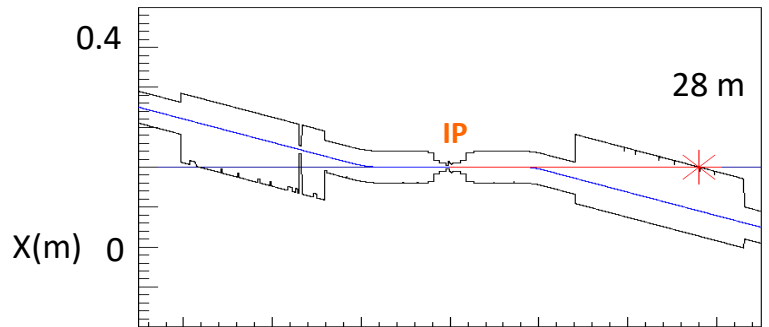
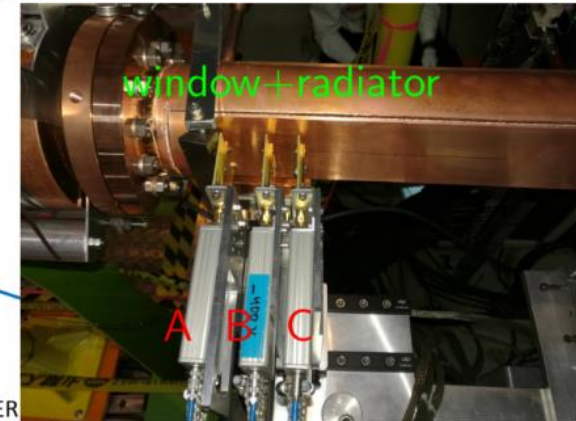
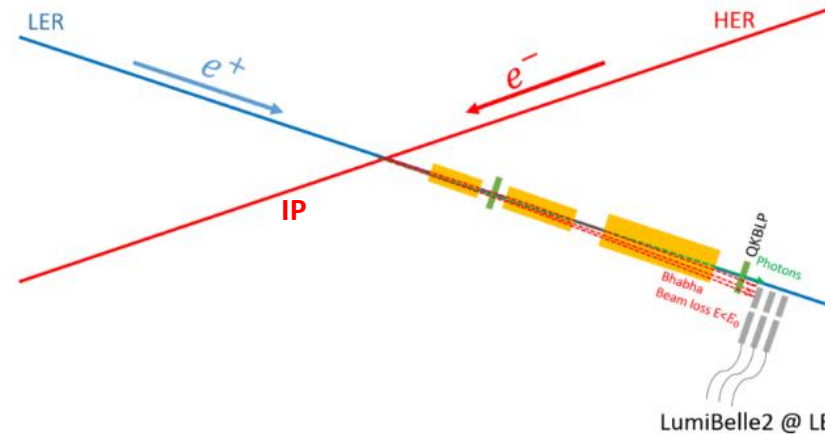
***LARGE IMPACT PARAMETER CUT-OFF IN THE PROCESS $e+e \rightarrow e+e-\gamma$, VEPP, Yury Eidelman et al. , Physics Letters B, 1982

Implementation in LER and HER

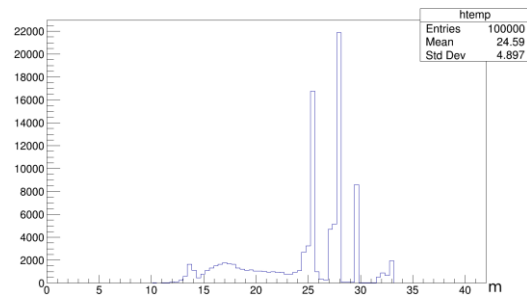
Cheng Guo Pang et al., Nucl.Instrum.Meth. A931 (2019) 225-235

POSITRON RING (measure e^+)

- Optimal position found at 10 m behind IP using SAD
- Over-bent Bhabha positrons \rightarrow vacuum chamber
- Special beam pipe with window + Tungsten radiator
- Start-to-end simulation (GuineaPig++, SAD, GEANT4)

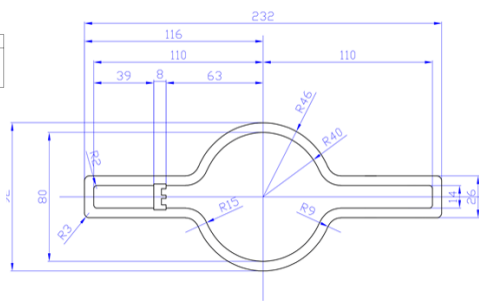


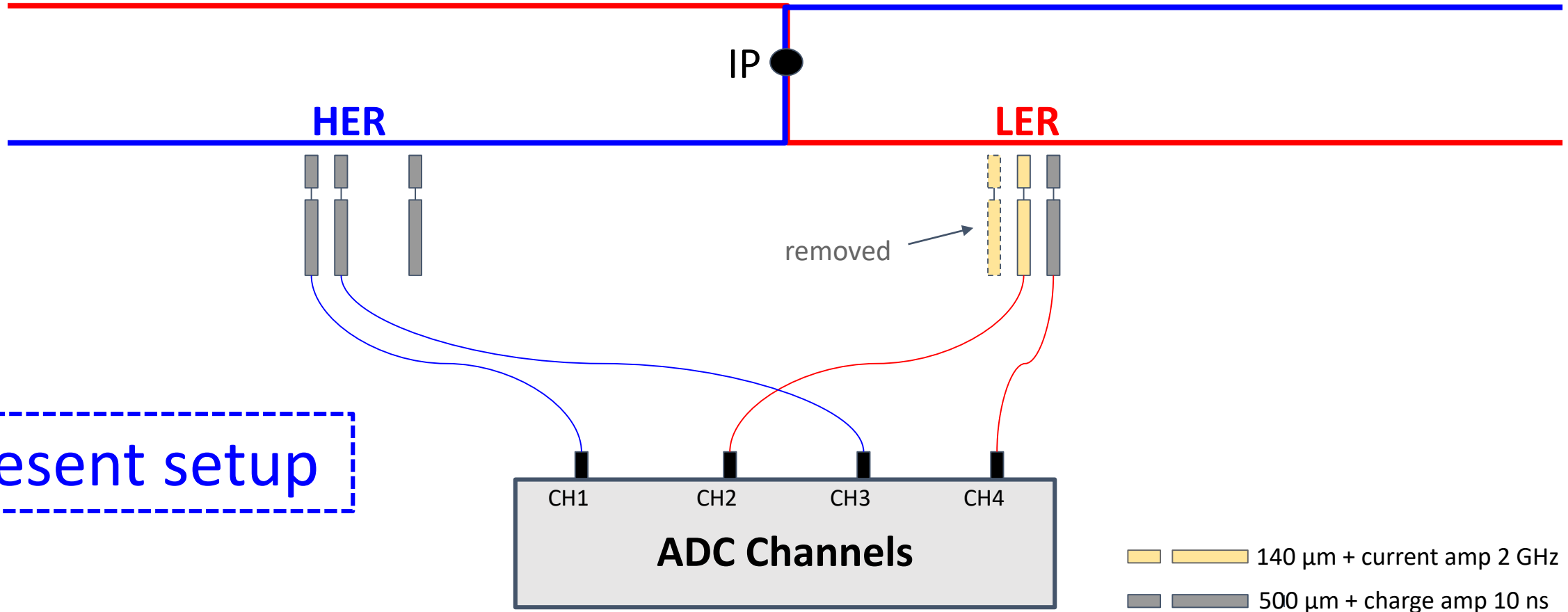
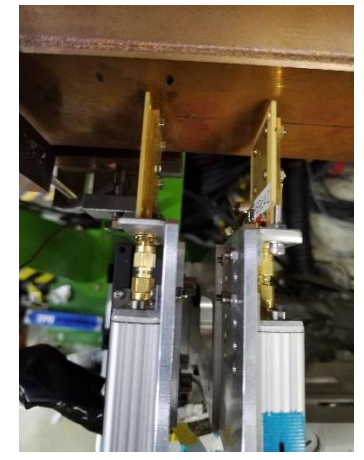
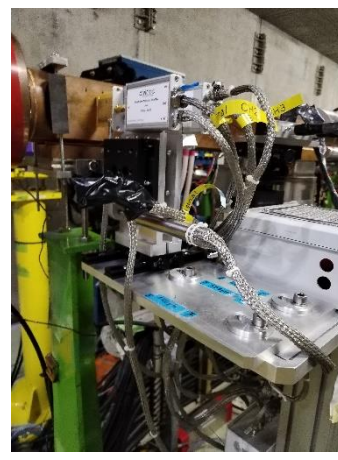
loss position distribution



ELECTRON RING (measure γ)

- Photon ray-tracing in detailed vacuum chamber geometry + GEANT4
- Original position at 30 m (2018)
- New optimal position found at 28 m with \approx 10 times higher rate





LumiBelle2 diamond sensor signals

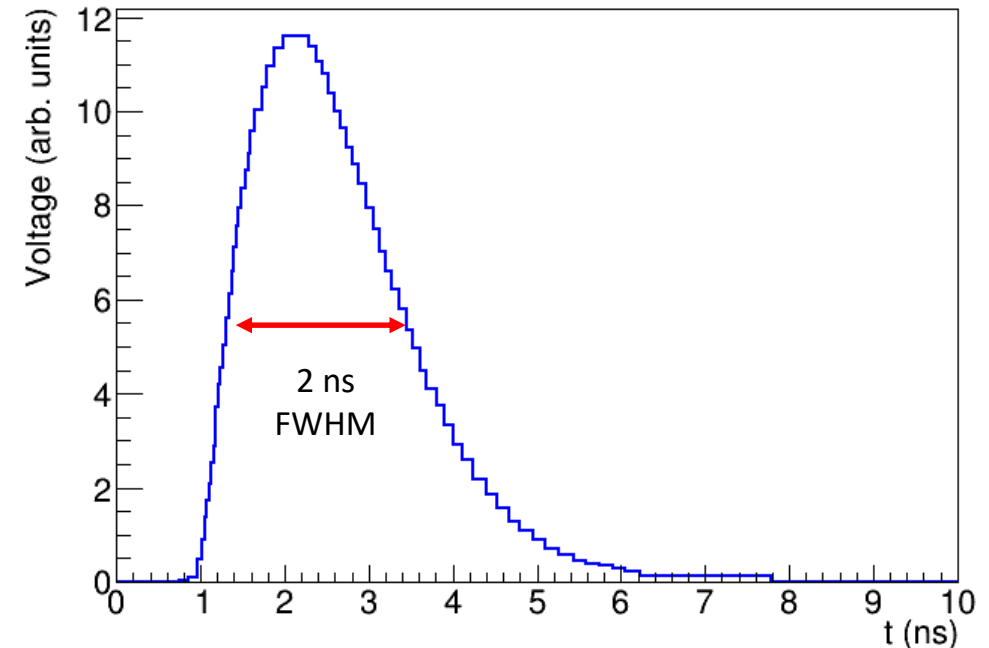
High charge carrier mobility → fast signal formation

Wide band-gap (5.5 eV) → good radiation tolerance

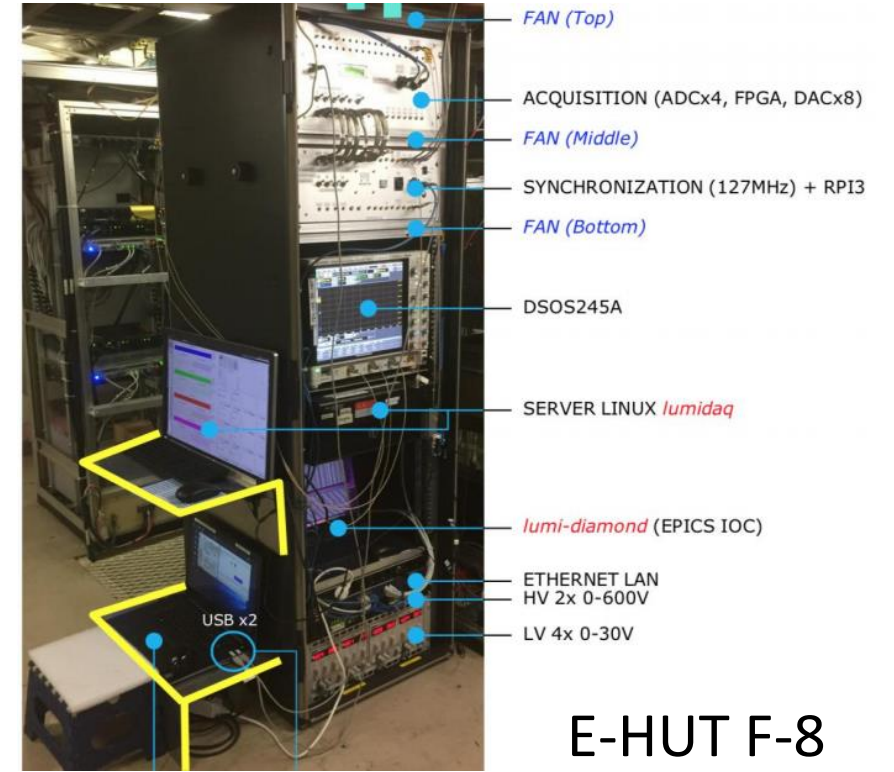
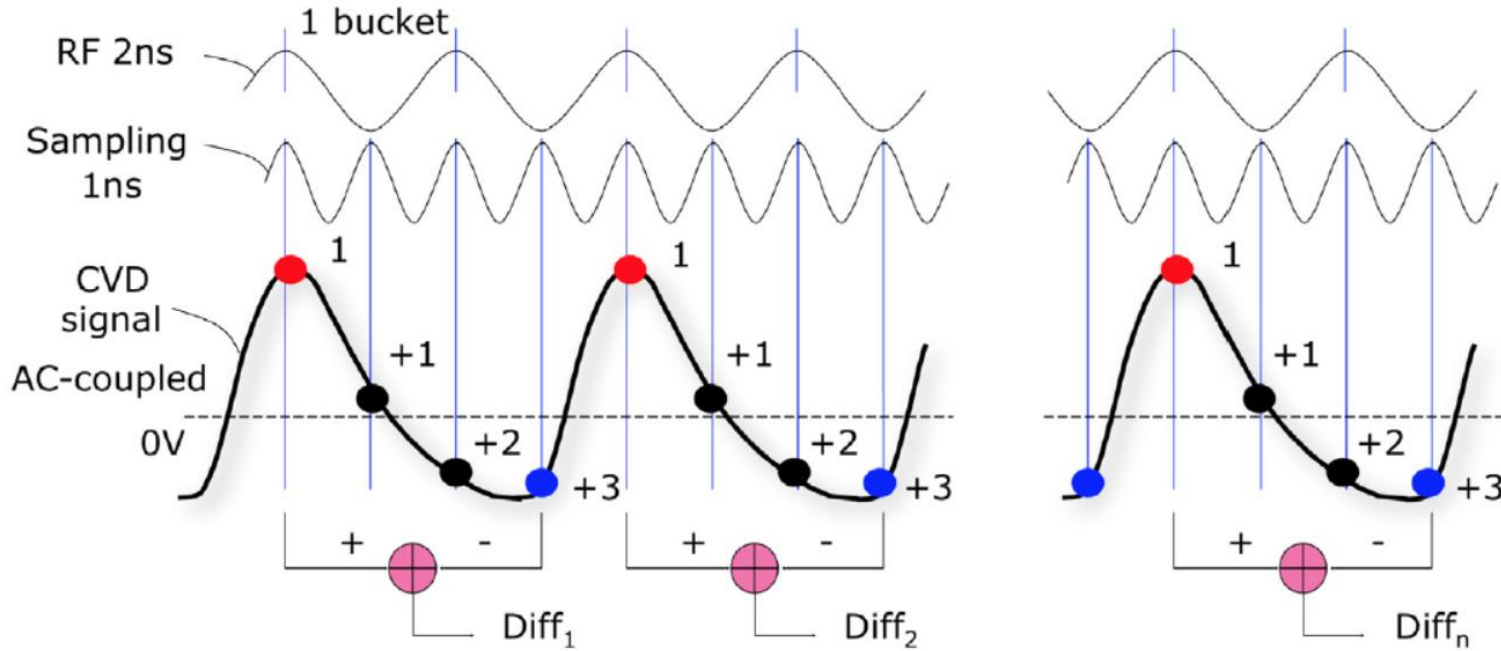


SuperKEKB nominal collision spacing = 4 ns

- Monitor bunch-by-bunch luminosity → easier with pulse width < 4 ns
- 140 μm thick diamond + fast 2 GHz current amplifier → 2 ns FWHM



LumiBelle2 signal processing



E-HUT F-8

- 2 / 10 ns FWHM signals from 140 / 500 μm with 2 GHz current / low noise charge amp sampled every 1 ns
- Synchronized to RF clock → continuous monitoring, averaging at 1 kHz and 1 Hz (bunch by bunch and all bunches together)
- Luminosity proportional to amplitude of signal peaks
 1. ADC is AC-coupled → record difference between peak and baseline → “TIL” & “BIL”
 2. Raw sum of all samples also ∝ luminosity and recorded → “RAWSUM”
 3. Number of peaks also recorded (constant fraction discriminator) → “COUNT”

$$BIL[j] = \sum_0^{1s} Diff_{n,j}, \quad \text{if } Diff_{n,j} > Threshold_1$$

$$TIL = \sum_0^{1s} Diff_{f_i}, \quad \text{if } Diff_{f_i} > Threshold_1$$

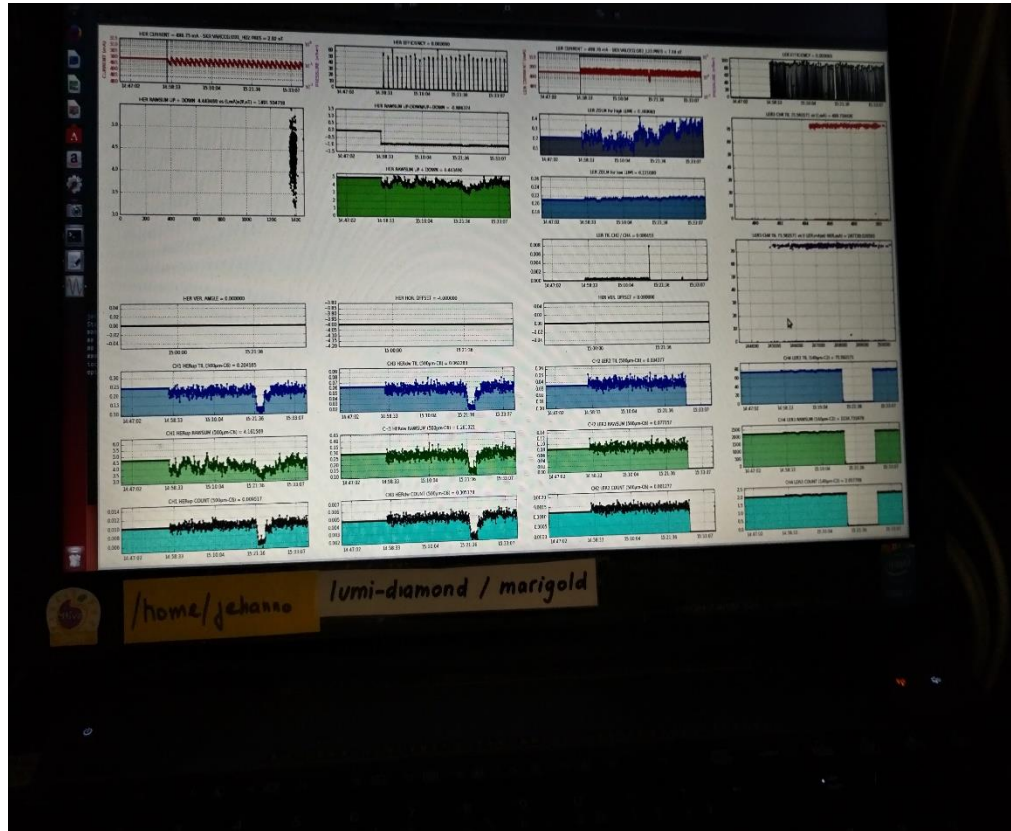
$$Count = Count + 1, \quad \text{if } Diff_{f_i} > Threshold_1$$

$$RAWSUM = \sum_0^{1ms} (Sample_i - Threshold_2), \quad \text{if } Sample_i - Threshold_2 > 0$$

→ EPICS broadcasting @ 1 Hz → “1 Hz, 1 KHz, bunch-by-bunch, bunch-current” data streams transferred daily for archiving

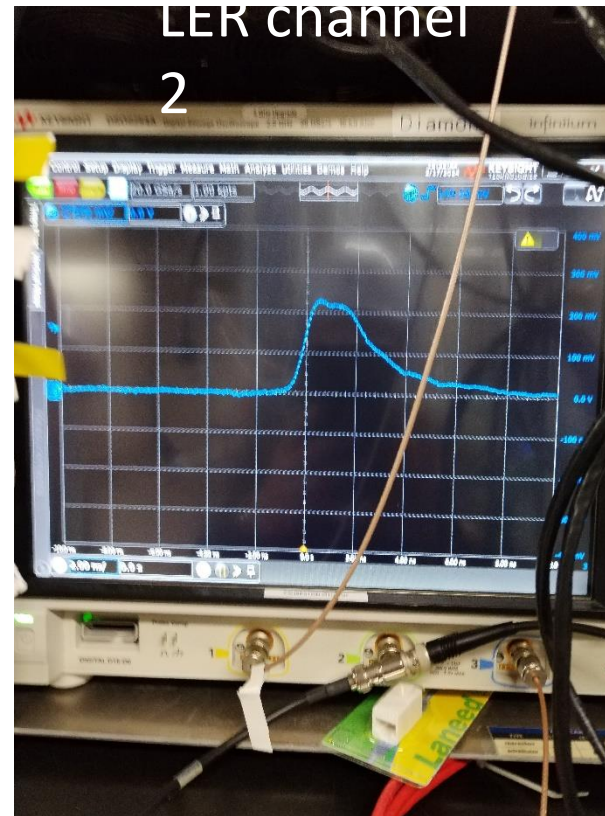
LER 400 mA single beam vacuum scrubbing – 17/02/2024 (beam gas Bremsstrahlung events)

E-HUT / lumi-diamond PC

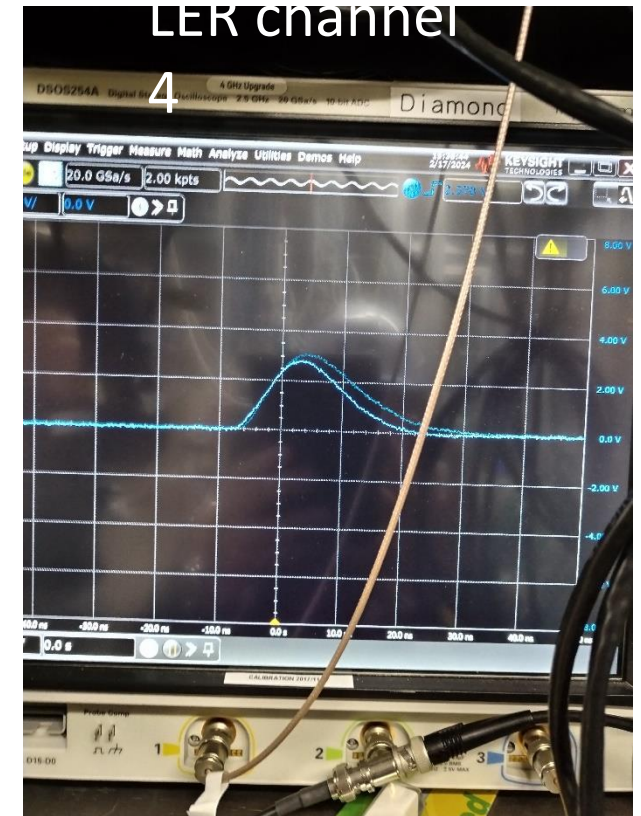


On-line EPICS data plotter

E-HUT / Keysight digital scope



140 μm diamond
2 GHz current amp



500 μm diamond
10 ns charge amp

Signal formation and DAQ simulation

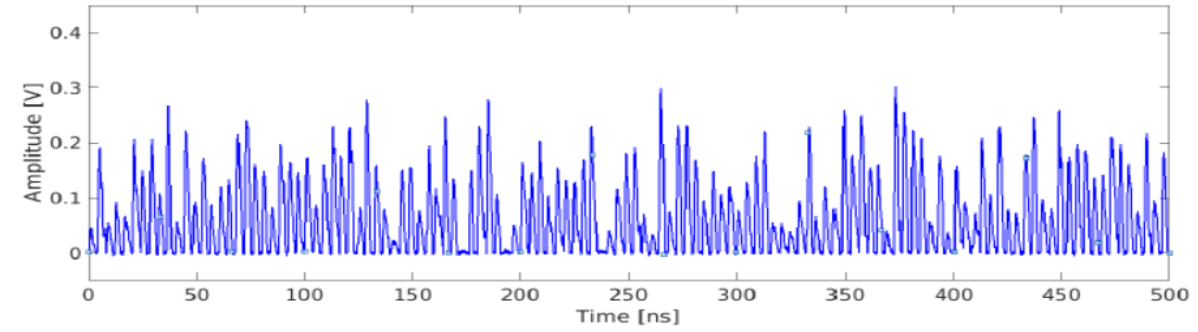
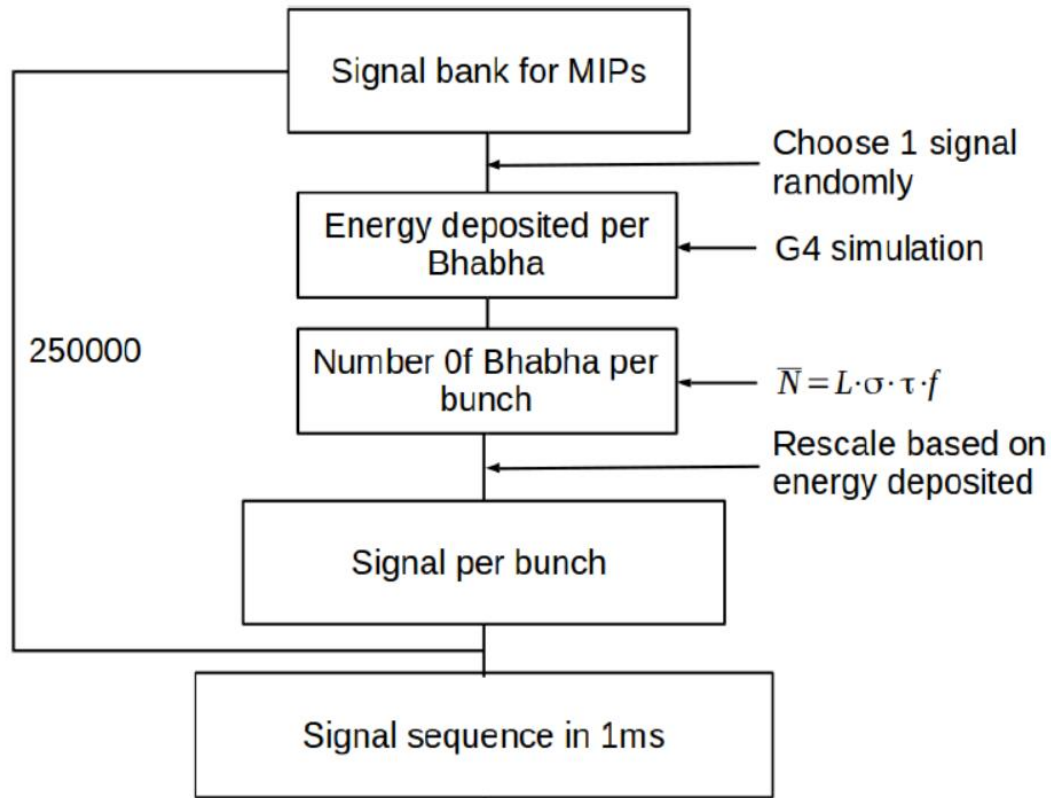


Figure 4.20: Example of signal sequence for the diamond detector with thickness of 140 μm coupled with the C2 broadband current amplifier in the nominal luminosity case.

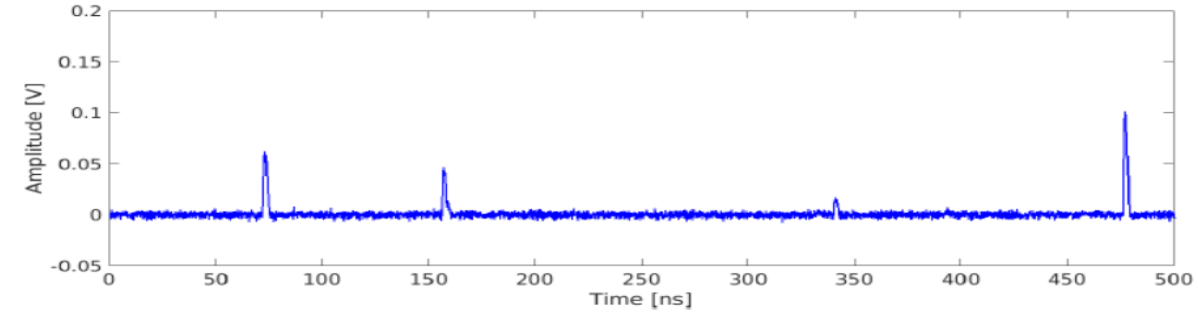


Figure 4.21: Example of signal sequence for the diamond detector with thickness of 140 μm coupled with the C2 broadband current amplifier for Phase-2 target luminosity case: $1 \times 10^{34} \text{ cm}^{-2} \text{ s}^{-1}$.

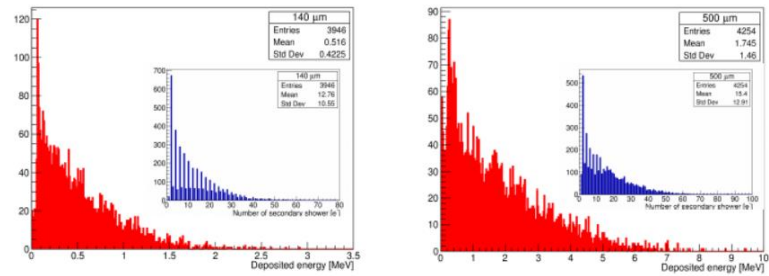
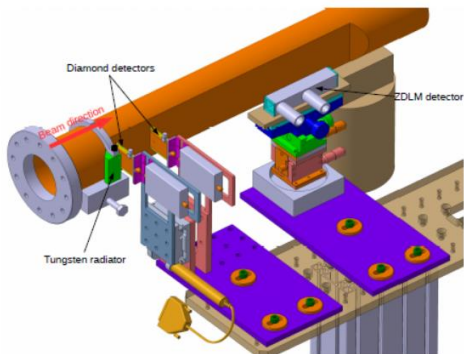


Figure 4.17: Histogram of deposited energy and number of secondary electrons for the diamond detector with thickness of 140 μm on l.h.s and 500 μm on r.h.s.

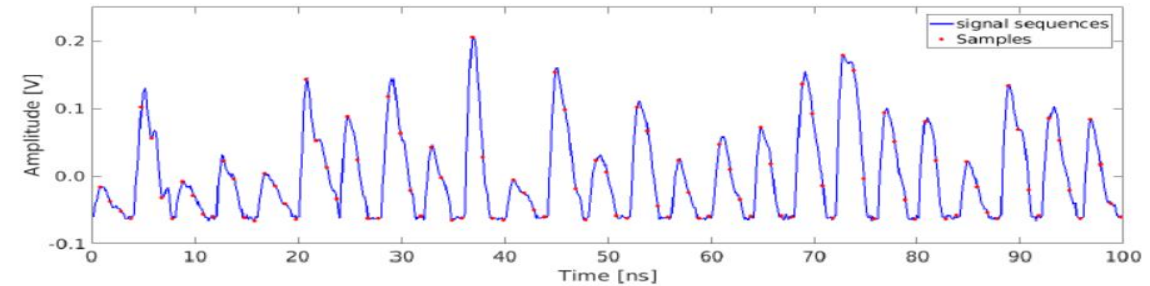


Figure 4.22: Example of sampling of constructed signal sequences for the expected fill pattern at the nominal luminosity of SuperKEKB after phase adjustment to get the maximum amplitude for each signal (the first 100 ns of the 1 ms sequence are shown).

Background study

SIMULATION FEATURES:

- Bremsstrahlung, Coulomb, and Touschek scattering included
- Use of SAD for tracking and Geant4 for particle detection
- Detailed simulation of pressure profile and chemical composition of vacuum gas ($Z_{eff} \approx 4.2 - 4.5$) from previous study (J.Carter, M.Ady)

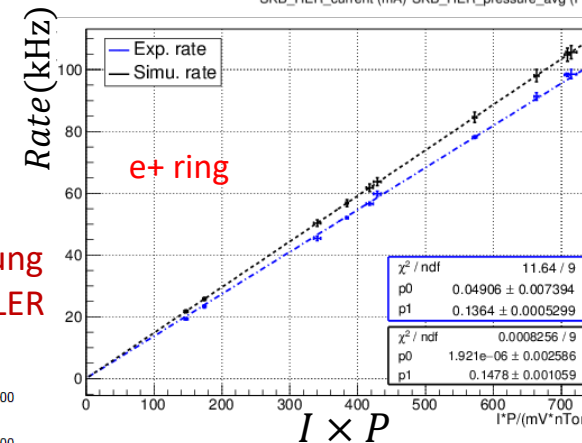
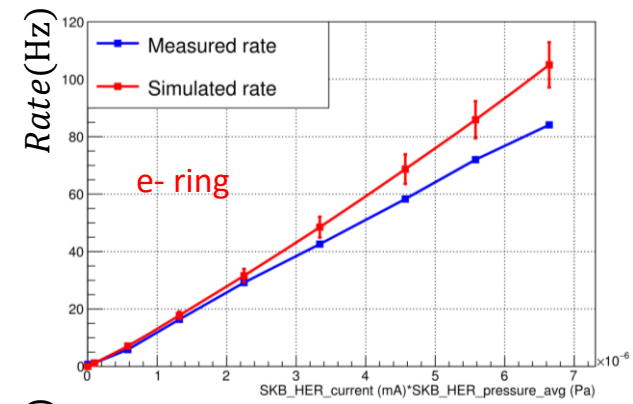
HER (e- ring):

- Dominant rate from **Bremsstrahlung photons**
- Electron rates from Bremsstrahlung, Coulomb, and Touschek scattering are negligible ($\ll 1\text{Hz}$)

LER (e+ ring):

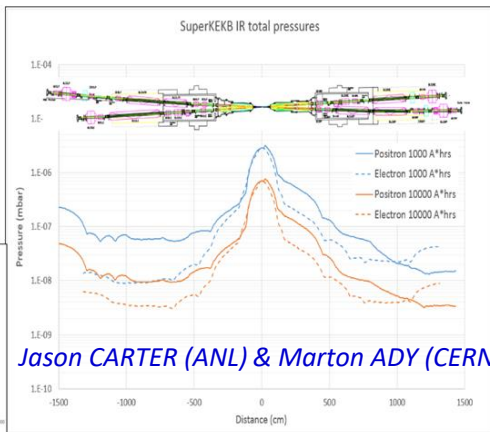
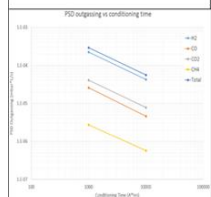
- Dominant rate from **Bremsstrahlung positrons**
- $\sim 10\%$ of the rate from Touschek scattering
- Positron rate from Coulomb scattering is negligible

Measurement vs Simulation



Total pressures at 1000, 10000 A*hrs, I = 3.6 A

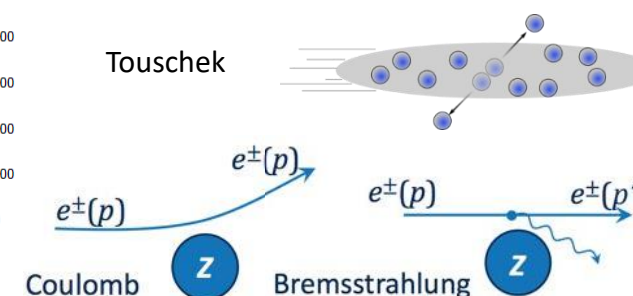
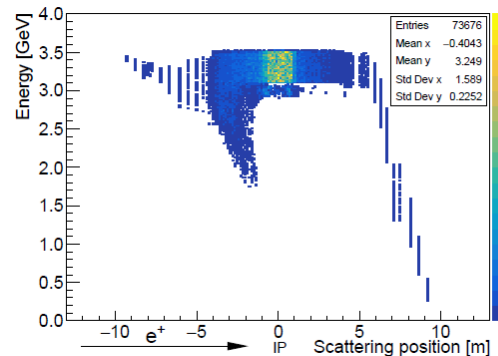
- Total indicates sum of H_2 , CO , CO_2 , and CH_4 partial pressures
- Asymmetric because of synchrotron radiation



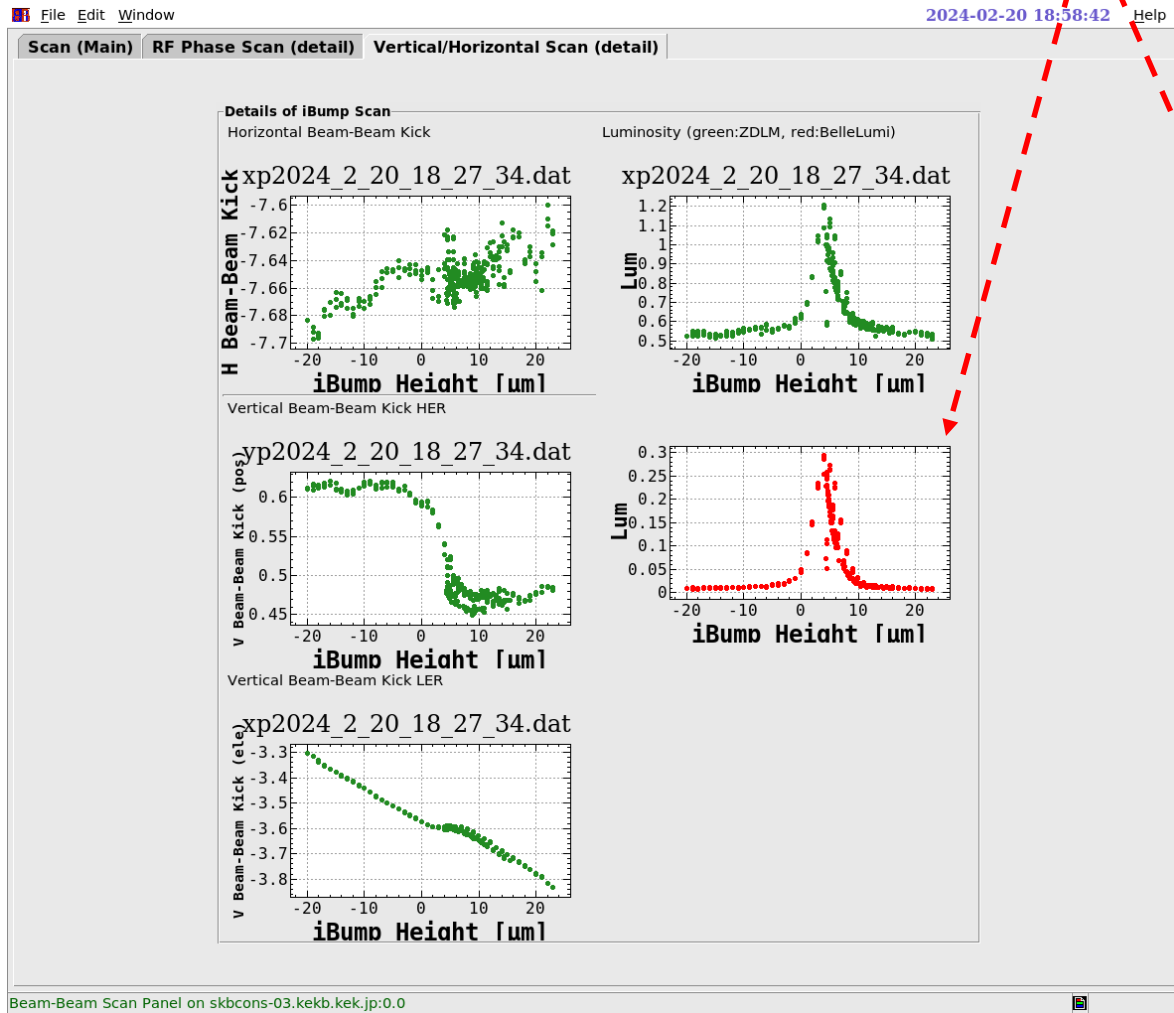
Jason CARTER (ANL) & Marton ADY (CERN)

Simulated vacuum profile in IR

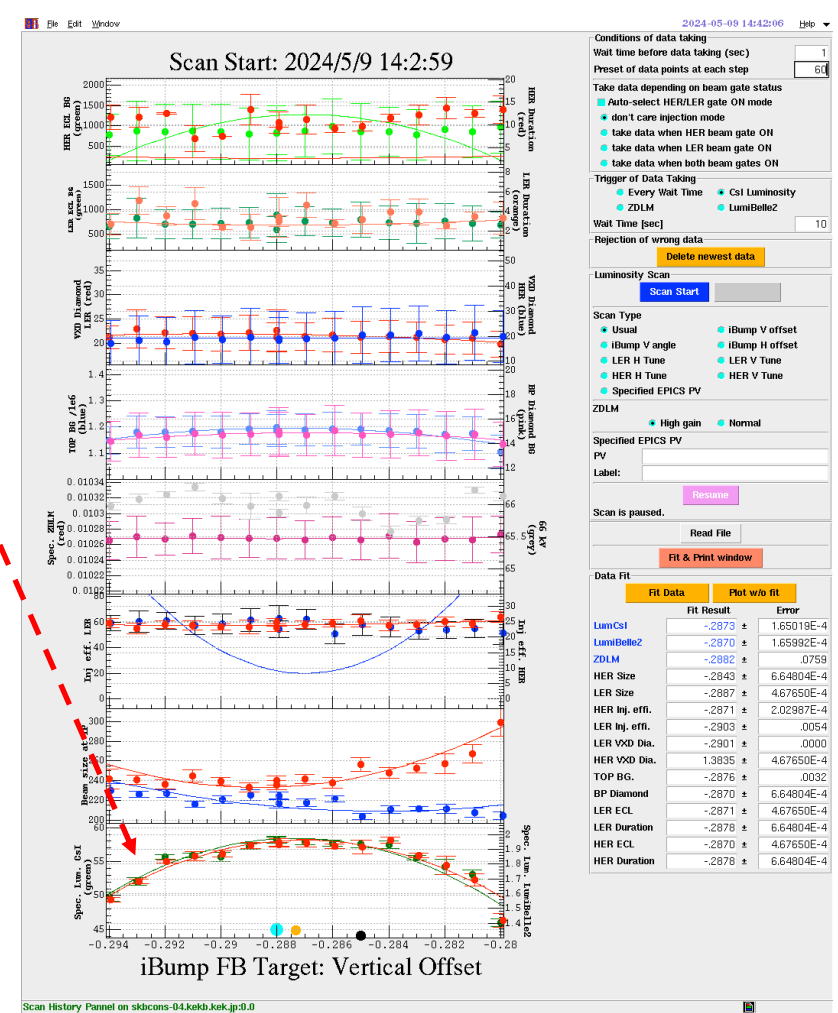
Scattering position of Bremsstrahlung particles detected in LumiBelle2 / LER



Setting up and optimizing beam collision with LumiBelle2

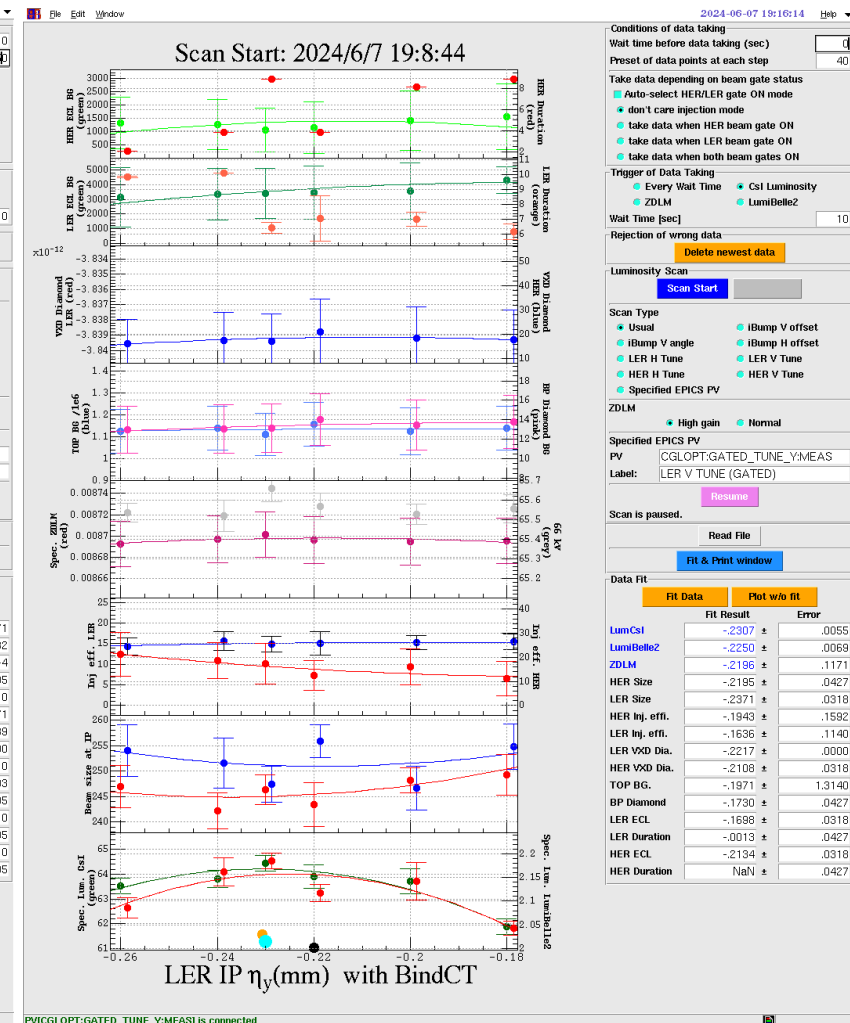
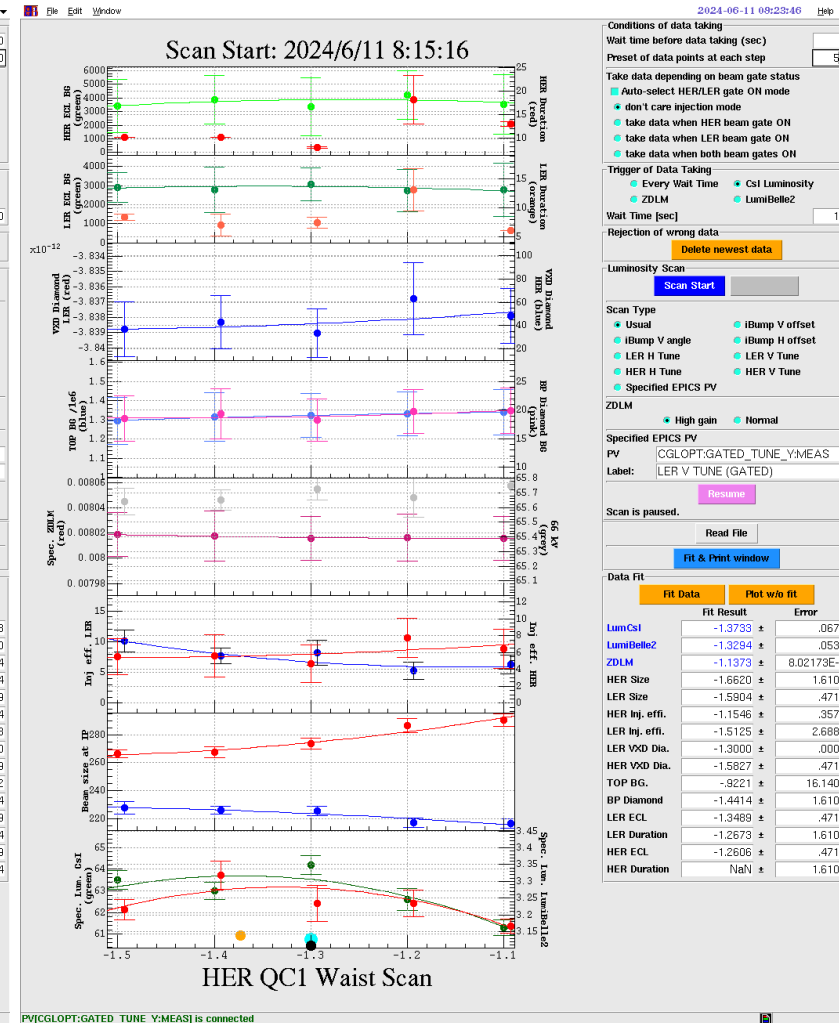
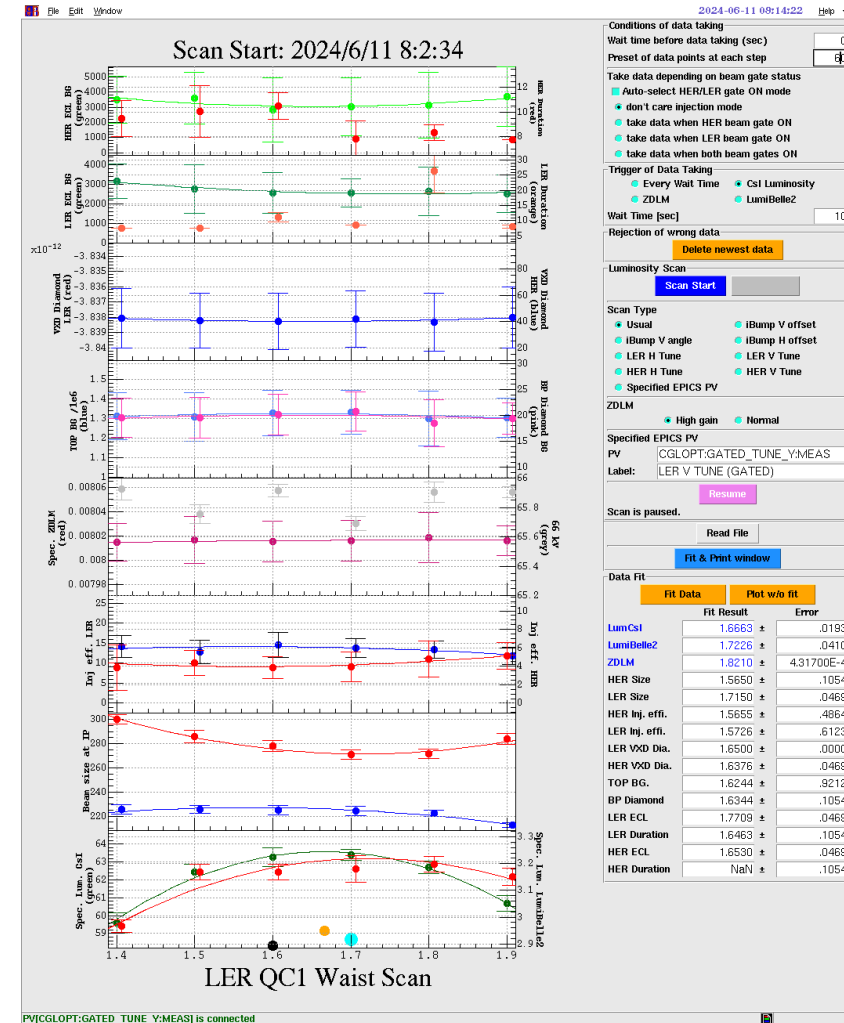


Initial scanning of IP beam offset to enable collisions at very beginning of the run...



Regularly optimizing IP beam offset to maximize luminosity...

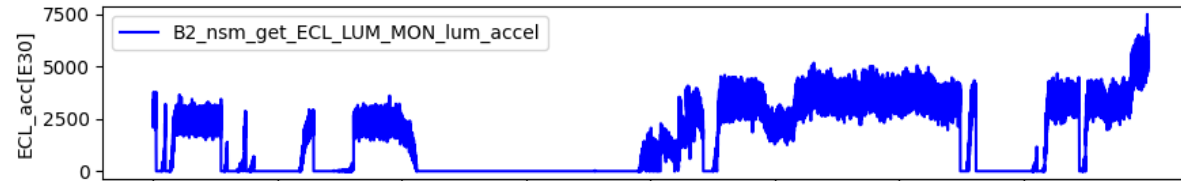
Minimising electron and positron IP beam sizes with LumiBelle2...



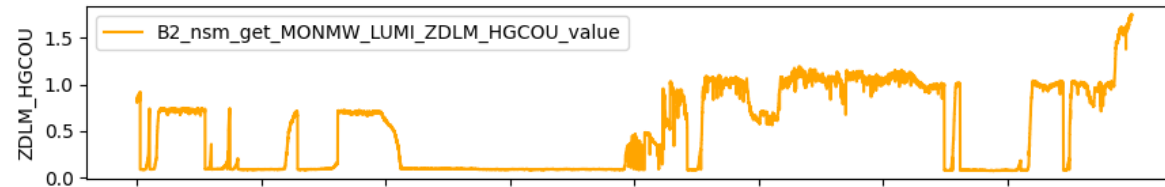
Comparing luminosity measuring channels in 24 hour period

2024-10-25:08:00 – 2024-10-26:08:00

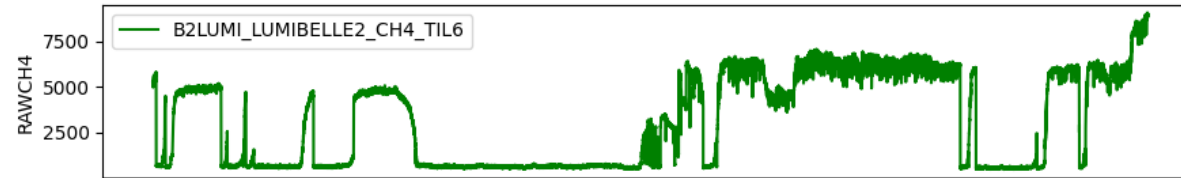
Belle II ECL end-caps



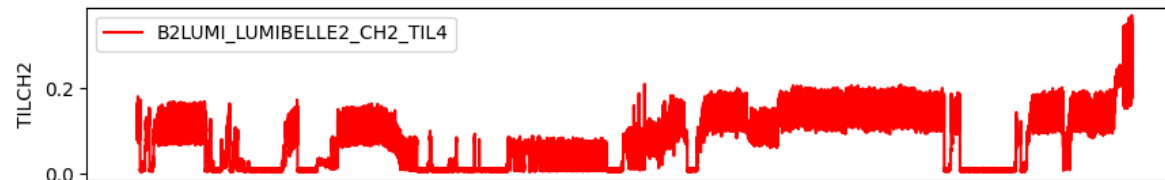
Belle II ZDLM



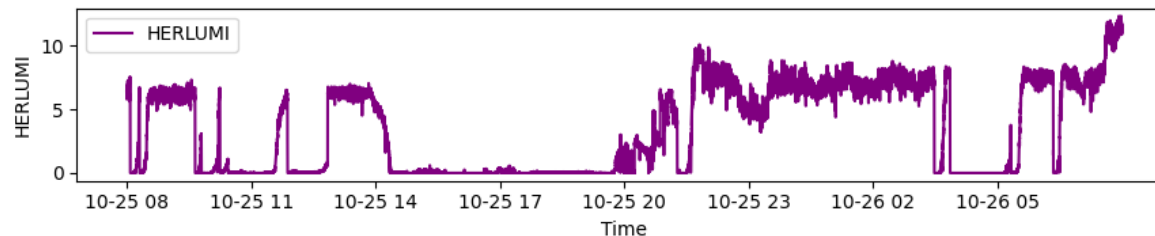
Belle II LumiBelle2 LER CH4



Belle II LumiBelle2 LER CH2



Belle II LumiBelle2 HER CH1+3



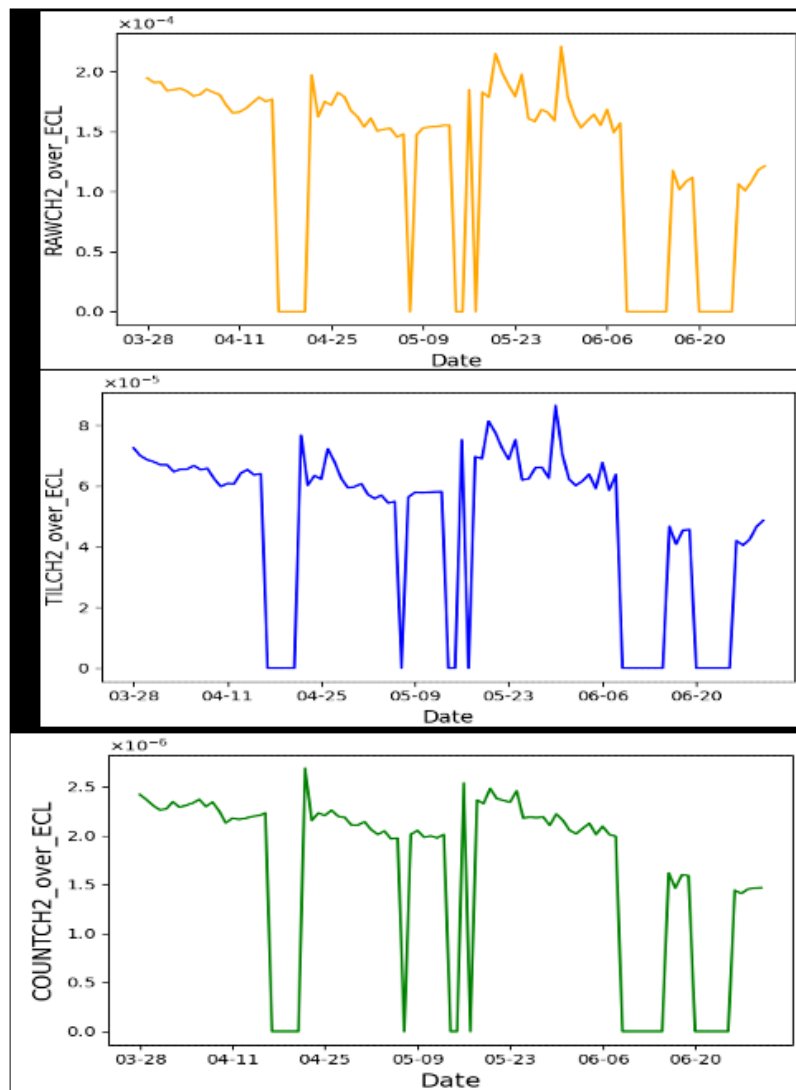
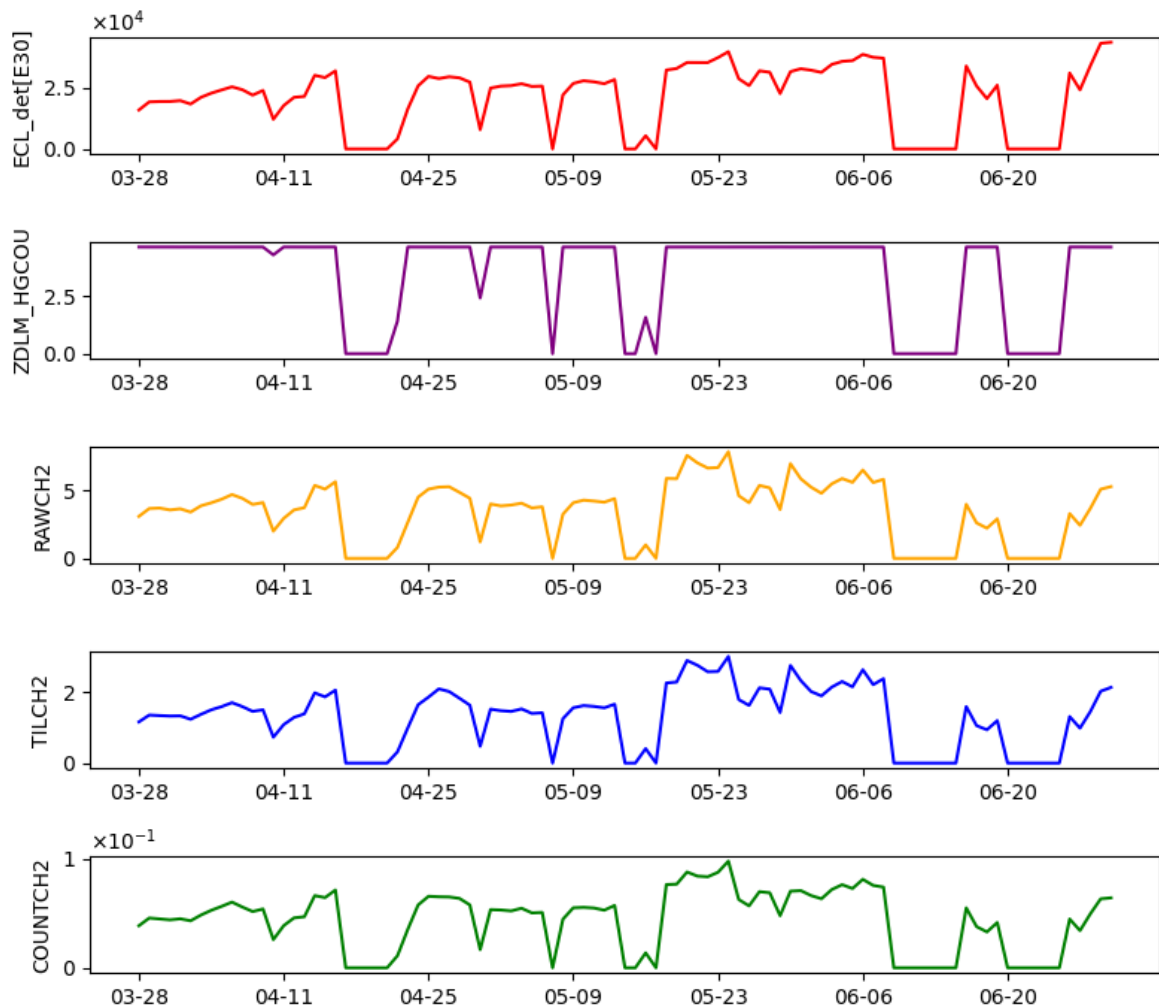
Luminosity sampled history from ECL, ZDLM and LumiBelle2 LER 140 μm channel

26/03/2024 \rightarrow 31/07/2024

Meng Li et al., "Status and performance of LumiBelle2 in the 2024 beam operation of SuperKEKB", IBIC2024 THP16

AI "forest method"

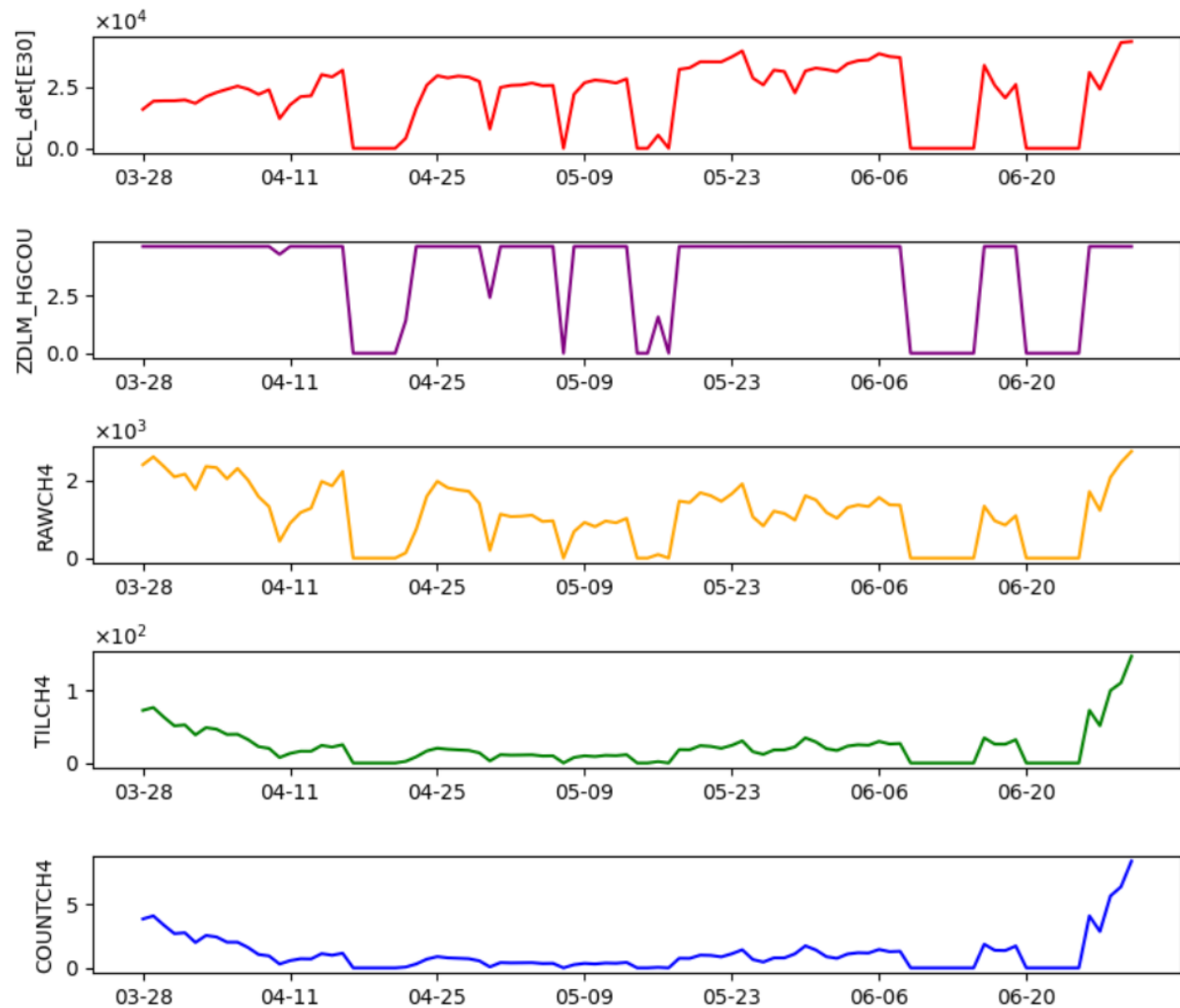
LumiBelle2 / ECL



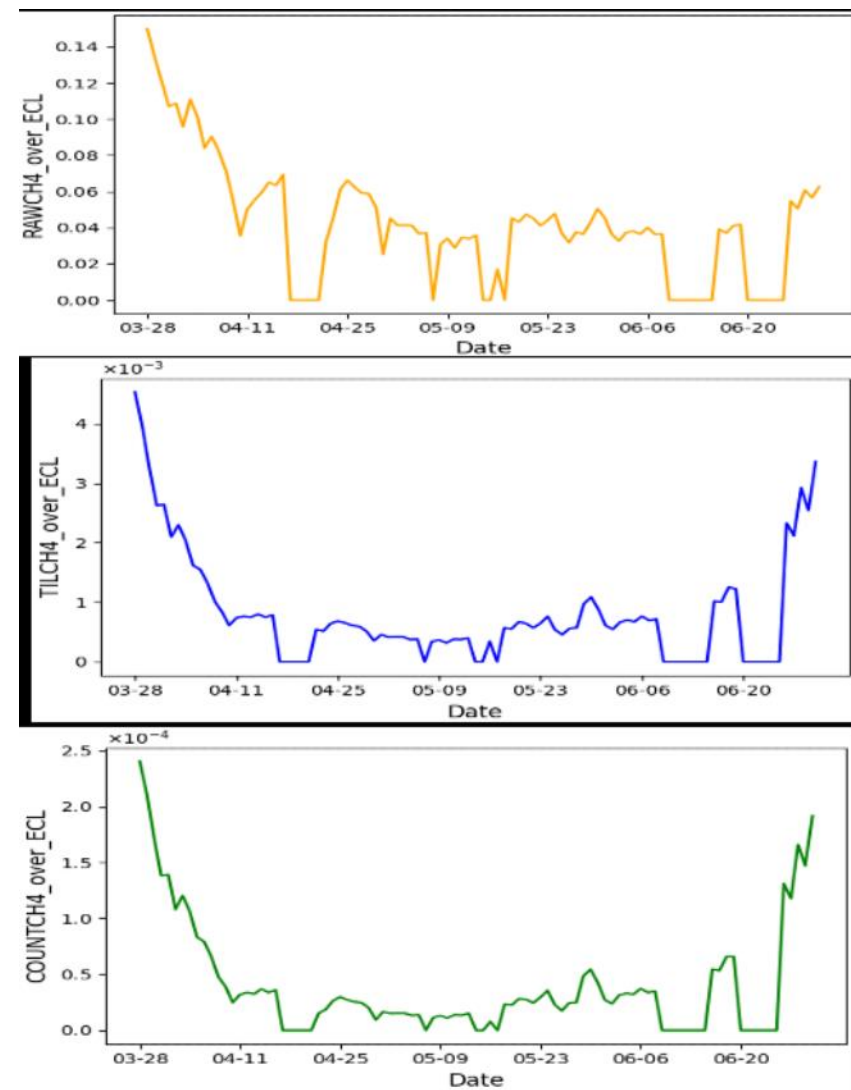
Luminosity sampled history from ECL, ZDLM and LumiBelle2 LER 500 μm channel

26/03/2024 \rightarrow 31/07/2024

AI "forest method"



LumiBelle2 / ECL



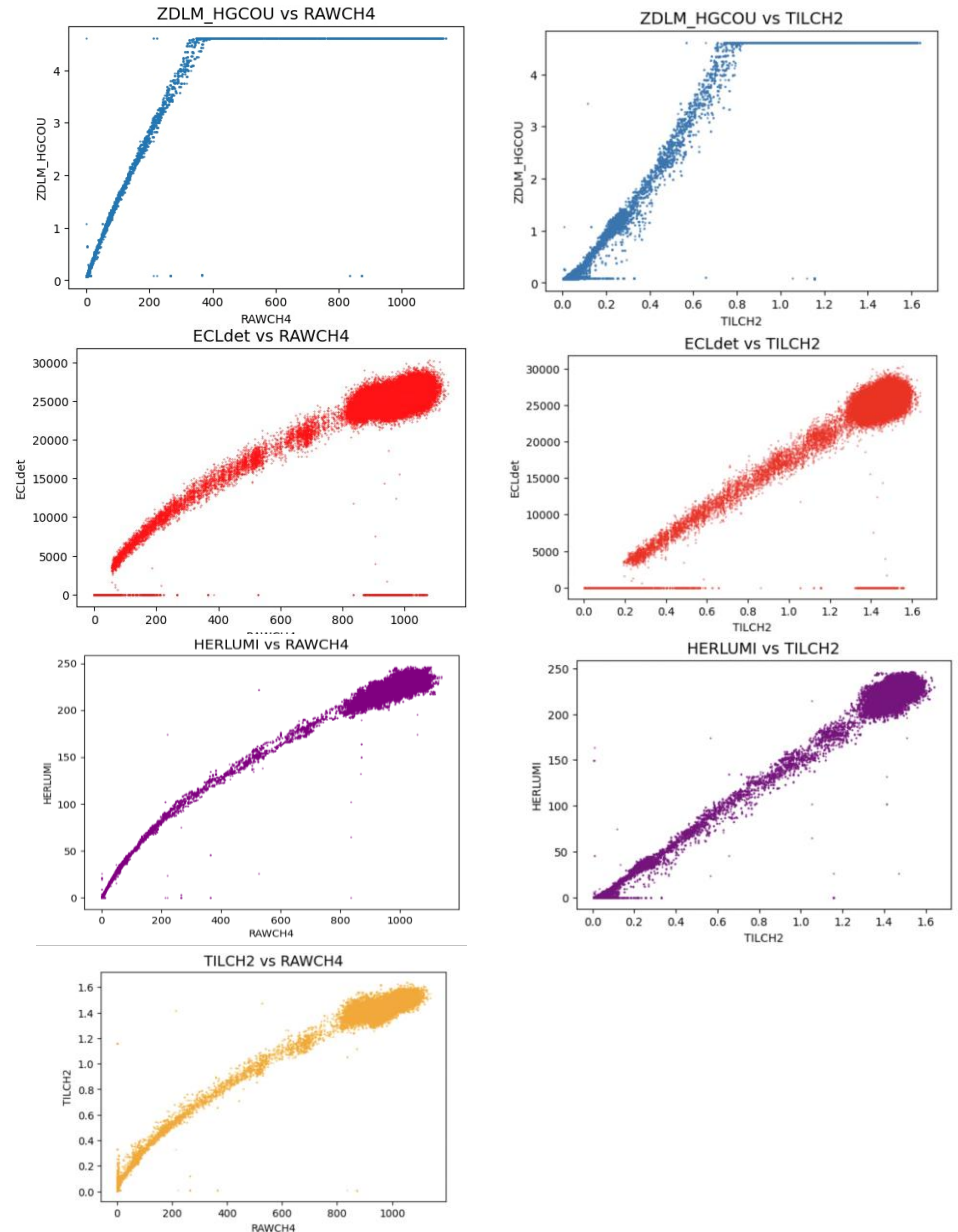
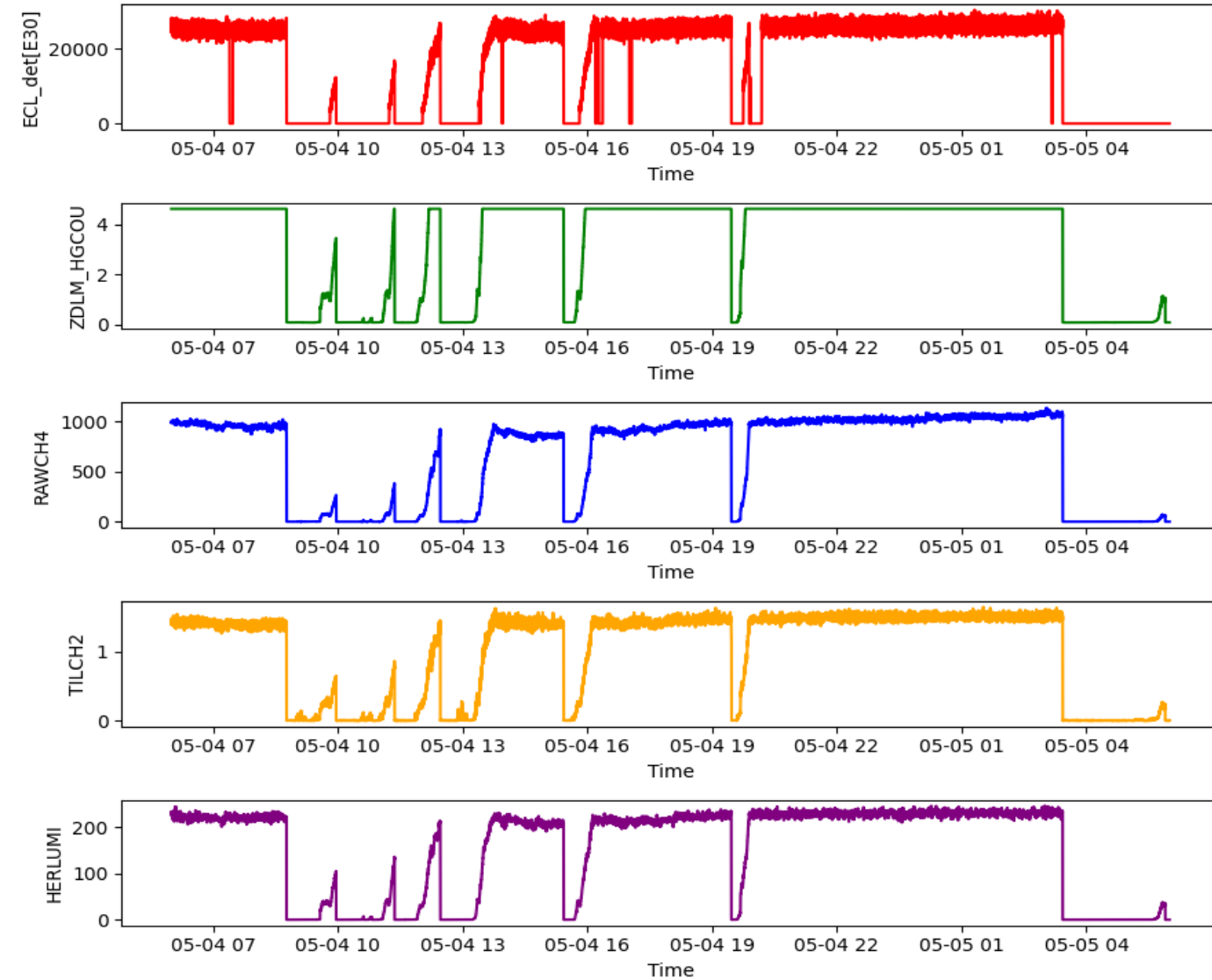
Further prospects

- LumiBelle2 provides useful input to the performance optimization of SuperKEKB
- Issue of radiation tolerance need further study
- Prospect of installing LGAD sensors in LumiBelle2 → radiation hardened version from IHEP-Beijing used in Atlas
- LumiBelle2 @ KEK operated by IJCLab partly remotely and with help from KEK, but very understaffed
 - ➔ collaboration & contributions from IFG PAN would be highly welcome

Extra slides

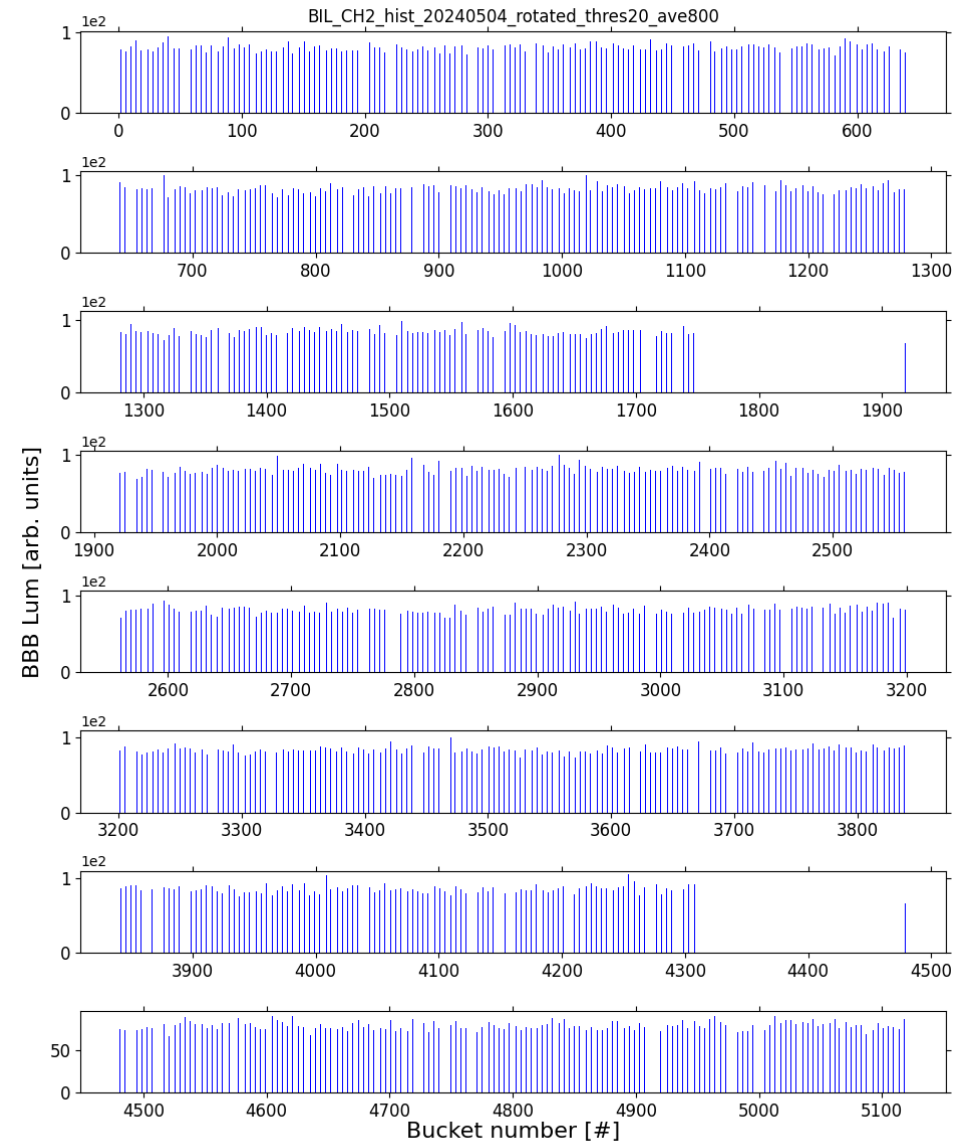
1Hz luminosity from ECL, ZDLM and LumiBelle2 LER 500/140 μm & HER 500 μm channels

04-05-2024



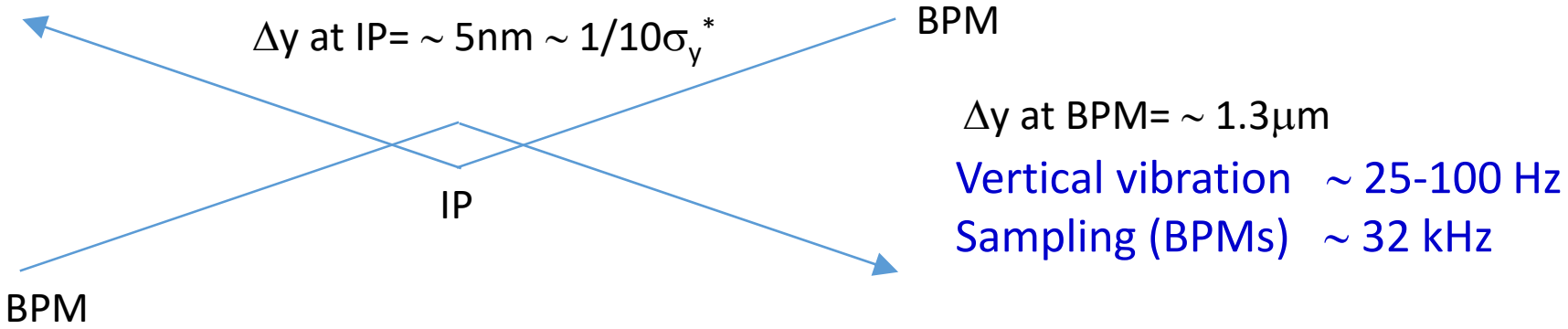
LumiBelle2 1Hz bunch-by-bunch luminosity

2346 bunches on 04-05-2024

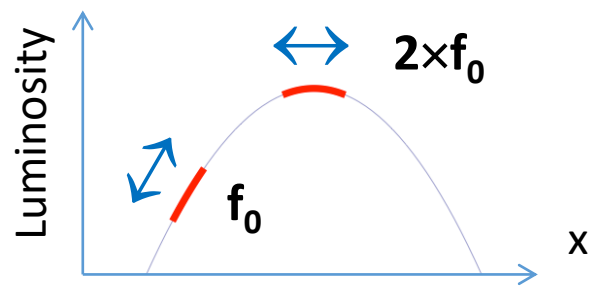


Fast & slow beam position variations at IP require feedback corrections

- **Beam-beam deflection** for fast vertical motion



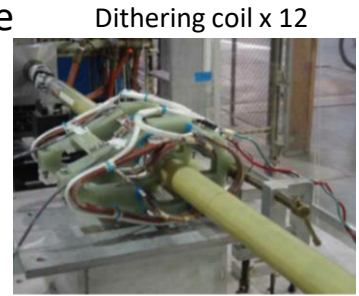
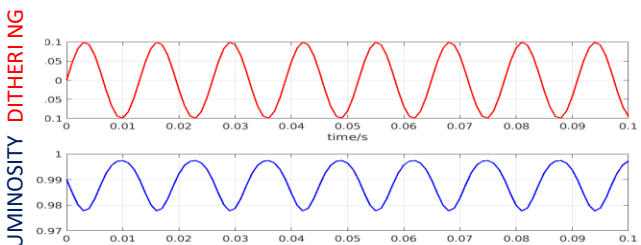
- **Luminosity feedback** by “dithering” for slower horizontal motion



- Horizontal motion** \sim few Hz
- Modulation freq. f_0** \sim 79 Hz
- Sampling (lumi. meas.)** \sim 1 kHz

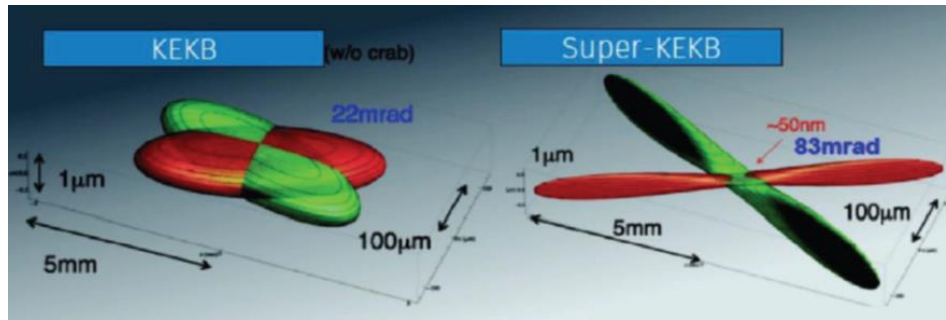
- minimize f_0 output component
- dithering \times lumi. signal \rightarrow phase

$$L(t) = \frac{f_{rev} N_1 N_2}{4\pi\sigma_x\sigma_y} e^{-\left(\frac{[q + p\sin(2\pi ft)]^2}{4}\right)}$$



Luminosity degradation with horizontal offset

nanobeam collision geometry



Sensitivity similar to head-on collisions for $\beta_y \rightarrow 0.3\text{ mm}$

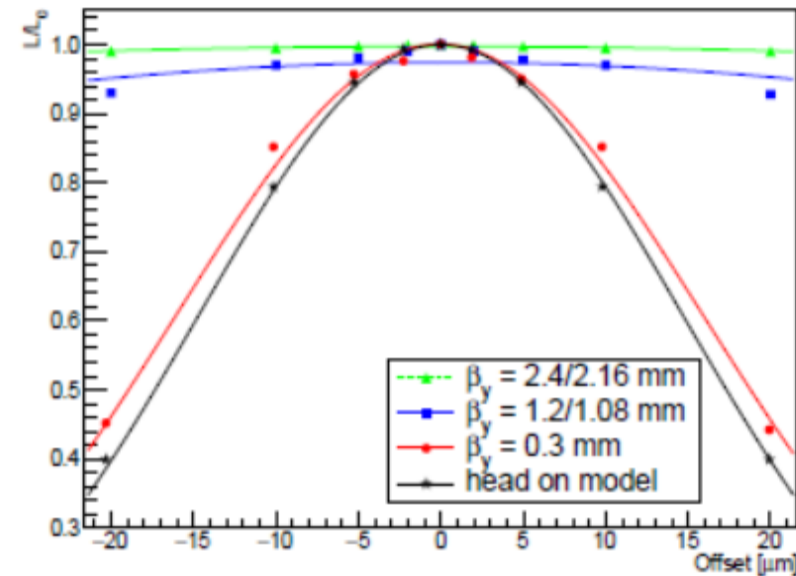
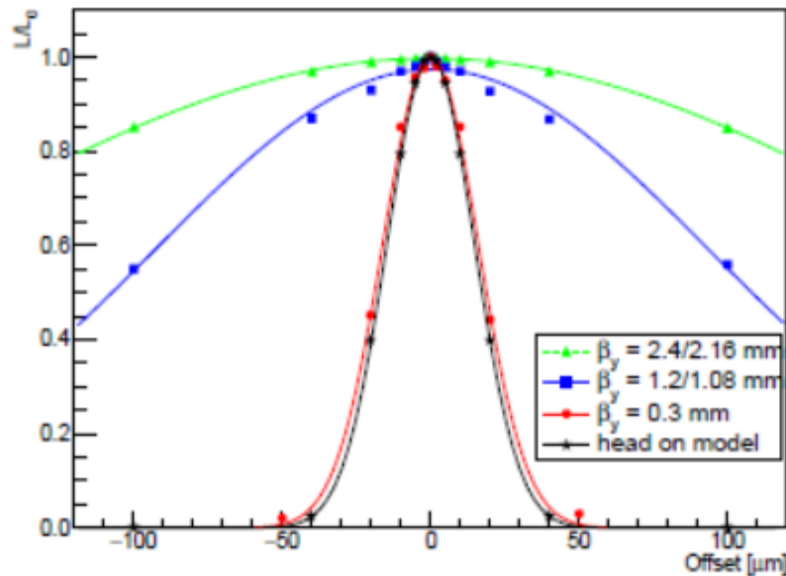


Figure 4.40: Luminosity degradation as function of beam-beam offset simulated with different β_y at the IP for the nano-beam collision geometry, and for the head-on model (with $\beta_y^* = 0.3\text{ mm}$).

Horizontal orbit dithering feedback simulation

basic ingredients & setup

Cheng Guo Pang, Doctoral thesis, <https://theses.hal.science/tel-03092297>

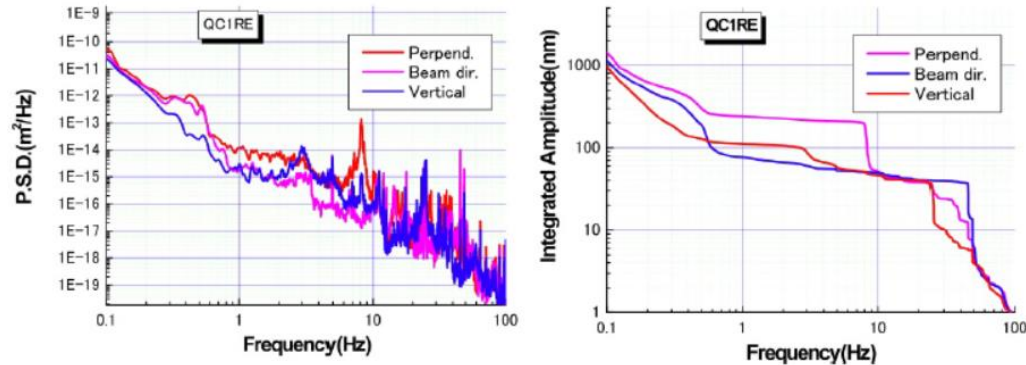


Figure 4.38: PSD (on l.h.s) and integrated amplitude (on r.h.s) of the QC1RE magnet vibration: the horizontal direction (labeled Perpend.) is shown in red on the l.h.s. plot and in pink on the r.h.s. plot.

Inverse FFT of measured GM spectra

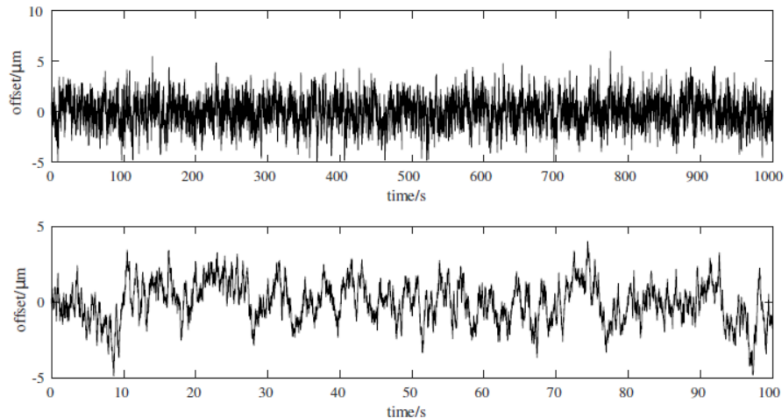


Figure 4.39: Example of ground motion induced vibration in the time domain obtained from the measured PSD spectrum (Figure 4.38) by application of iFFT.

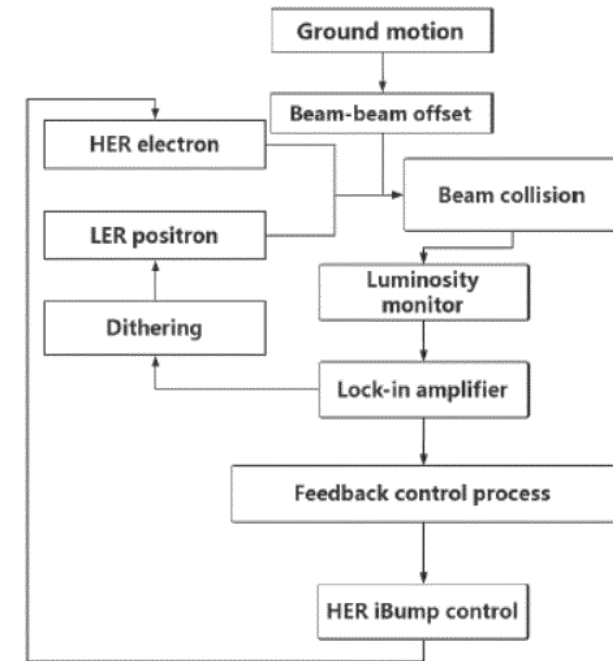


Figure 4.37: Flow-chart of the start-to-end simulation for the dithering orbit feedback system to maintain very high luminosity in the presence of mechanical vibration caused by ground motion.

$$\mathcal{L} = \mathcal{L}_0 \exp \left[-\frac{[x_0 + \Delta x \sin(2\pi ft)]^2}{2\Sigma_x^2} \right], \quad \Sigma_x^2 = \sigma_{x+}^2 + \sigma_{x-}^2$$

Horizontal dithering orbit feedback simulation

response to fixed offset

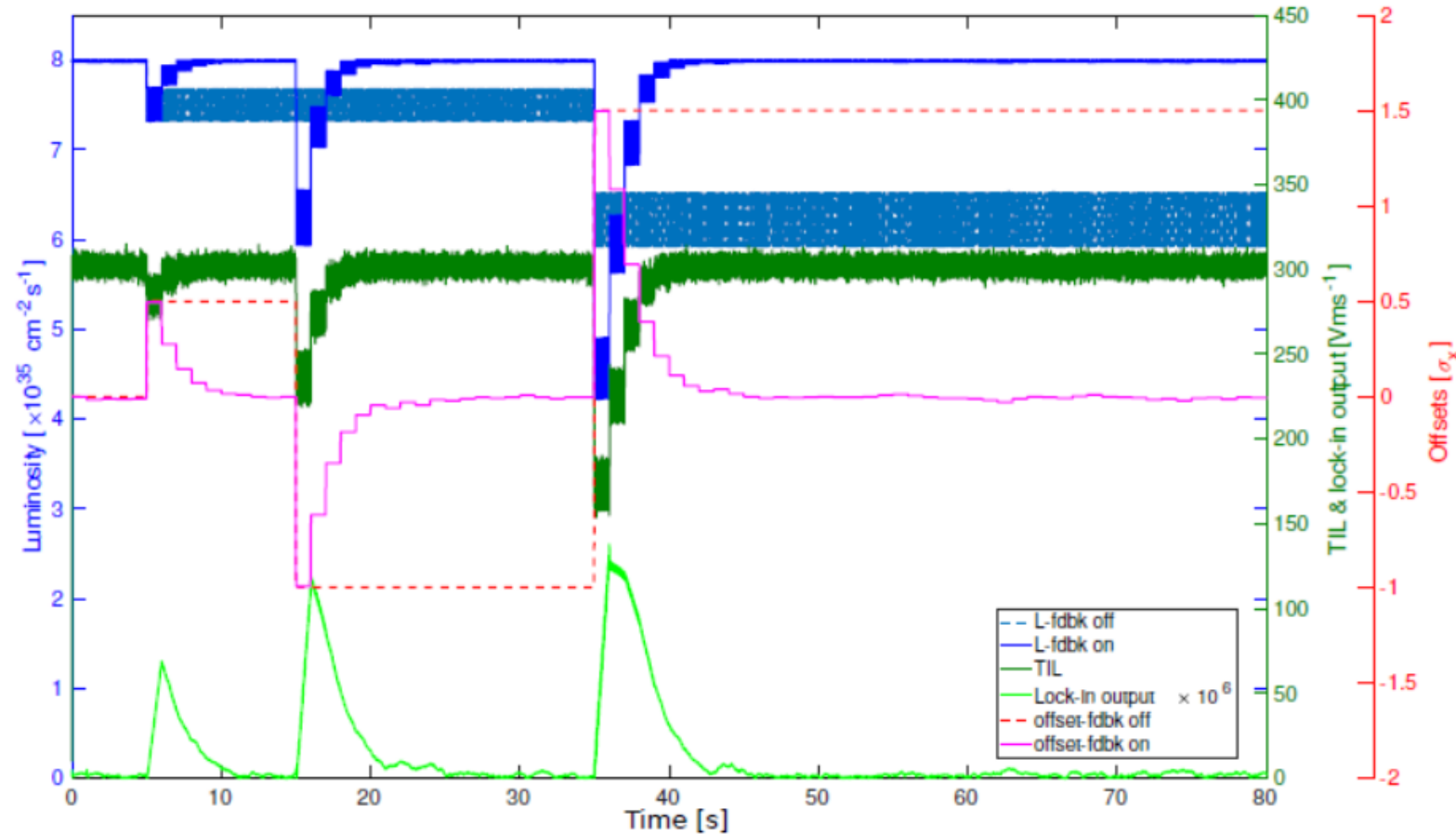
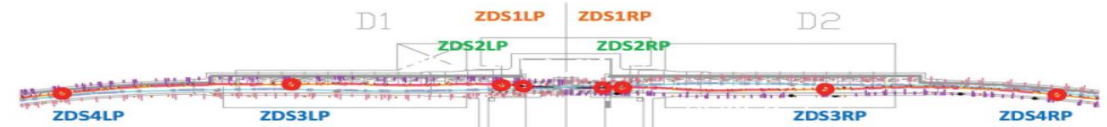
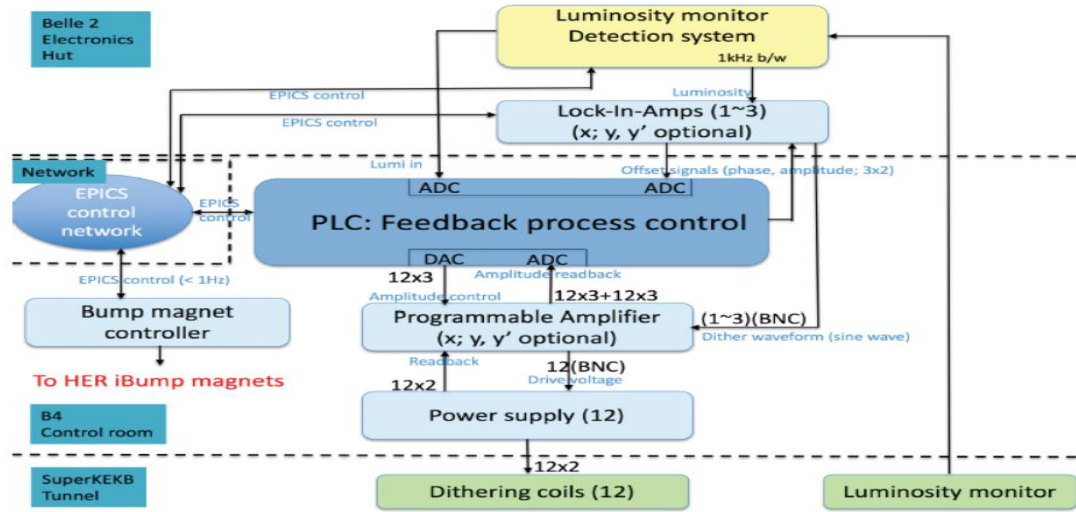


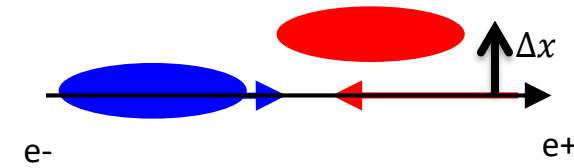
Figure 4.42: Simulated performance of feedback algorithm with several successive offsets. The luminosity is plotted in blue (with and without feedback), the simulated fast luminosity signal TIL in dark green, the magnitude of Fourier component at 79 Hz of the simulated fast luminosity signals in light green, and the offset between the two beams in red (without feedback) and pink (with feedback).

1st dithering feedback test in Phase 2

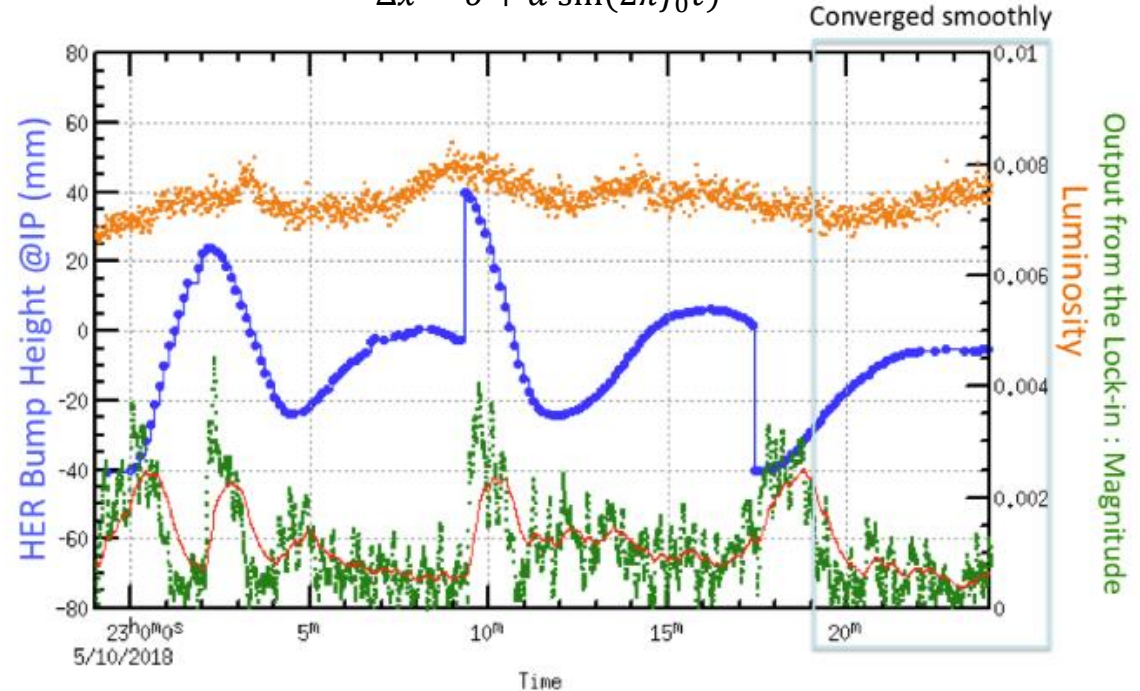
Mika Masuzawa et al., “Early Commissioning of the Luminosity Dither Feedback for SuperKEKB”, IBIC2018 MOPA13
 Yoshihiro Funakoshi et al., “Early Commissioning of the Luminosity Dither Feedback for SuperKEKB”, eeFACT2018 WEXBA04



4 dither coils on each side of IP



$$\Delta x = o + d \sin(2\pi f_0 t)$$



- e- beam artificially given an offset, while e+ beam was dithered
- Compute beam offset magnitude to cancel **magnitude [V]** of luminosity FFT component at dithering driving frequency f_0
- Beams brought back to optimal position (remove unwanted offset $o=0$) applying this offset with
 - sign set by relative phase of input dithering and induced luminosity variation
 - damping factor (depends on precision / noise levels)
- Corresponding bump parameters sent to magnet control system via EPICS
- After **first 2 attempts** + PI algorithm parameter optimization, the **3rd feedback test** could smoothly minimize the induced offset

Horizontal dithering orbit feedback simulation

response to ground motion

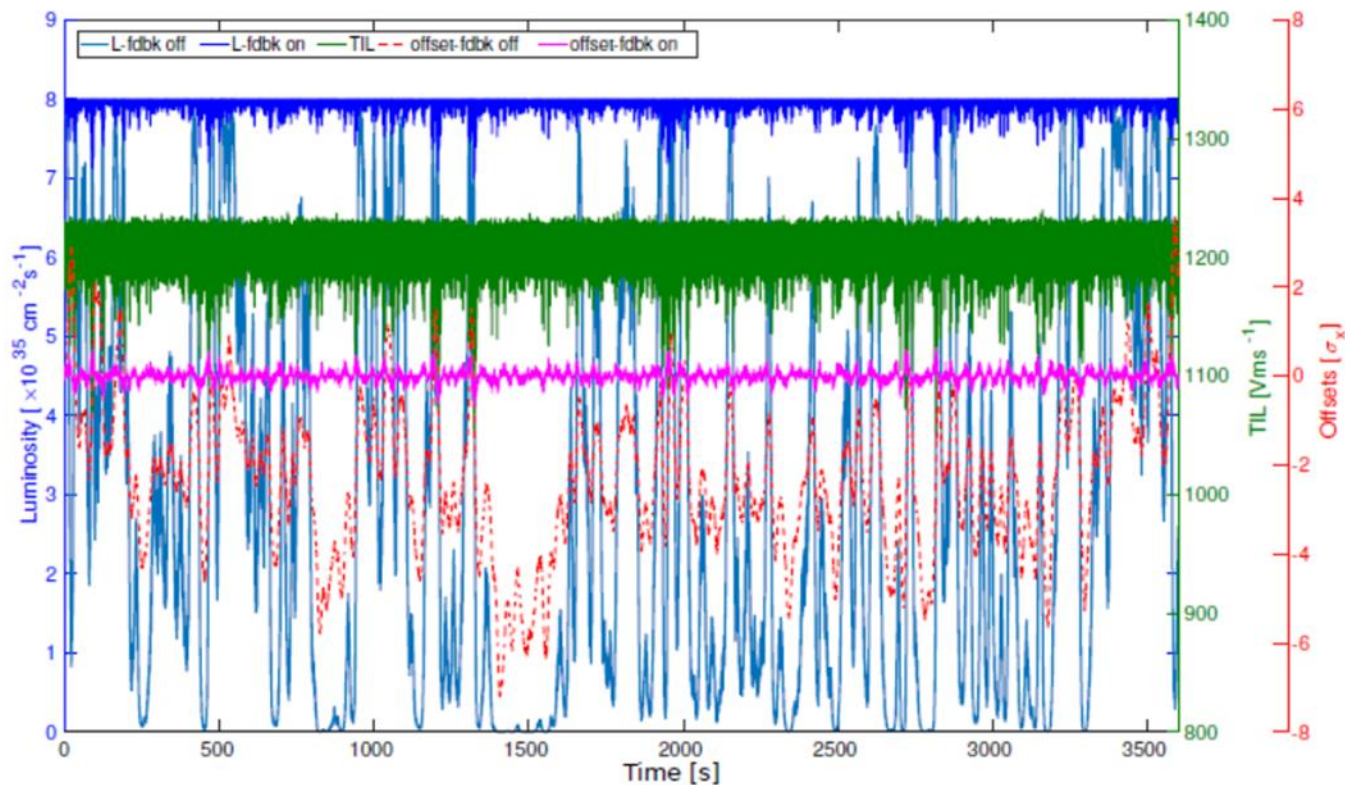


Figure 4.44: Luminosity, train integrated luminosity signal provided by diamond detector and the beam-beam offset with and without feedback for Phase-3 optics over a period of 3600 s.

Luminosity precision 2-3% @ 1 kHz
 → Luminosity loss < 1%

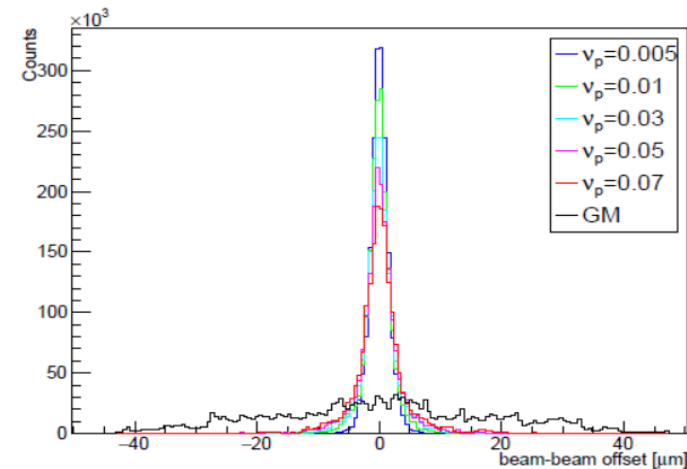


Figure 4.46: Residual beam-beam offset with feedback for different values of the relative luminosity precision.

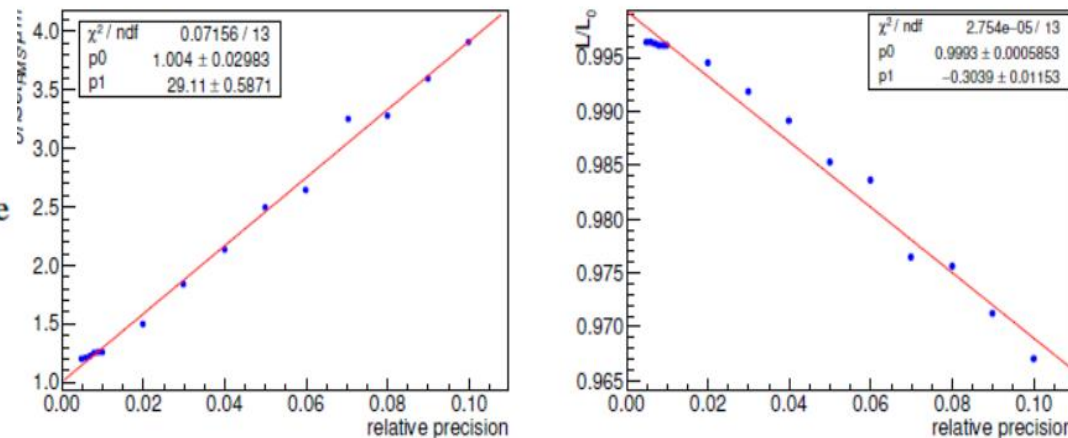


Figure 4.47: Residual RMS offset(l.h.s) and the ratio of luminosity with feedback with respect to the ideal luminosity as function of the train integrated luminosity signal's relative precision at 1 kHz.