

Tests of Lepton Flavour Universality in B decays at Belle II

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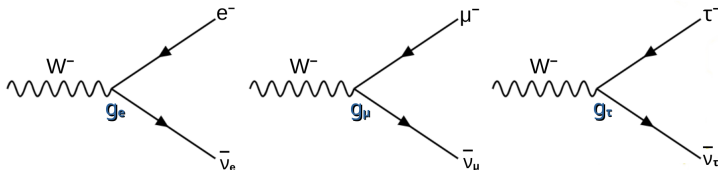
Joint IJCLAB-IFJ PAN Heavy Flavour meeting, Kraków,
12/11/2024

Outline

- I Introduction
 - LFU
 - Experimental techniques
- II First results from Belle II
 - $R(X_{\tau/\ell})$
 - $R(D^*)$
- III Ongoing analyses
 - $R(\pi)$
- IV Prospects and summary

Introduction

Lepton Flavor Universality



- in the SM all leptons share the same electroweak coupling, a symmetry known as Lepton Flavour Universality:

$$g_e = g_\mu = g_\tau$$

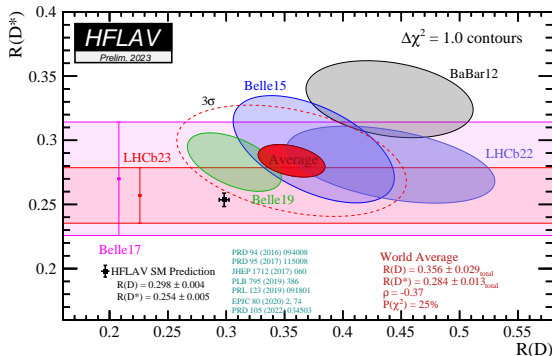
- difference in dynamic driven by differences in masses:

$$m_e < m_\mu < m_\tau$$

- Is this accidental (fundamental) symmetry of the Standard Model fully preserved?
- test "laboratories": on shell W decays in ATLAS/CMS; off shell in B & τ decays at Belle/Belle II; ...

LFU in B decays

tension with SM



$$R(D^{(*)}) = \frac{\mathcal{B}(B \rightarrow \bar{D}^{(*)} \tau^+ \nu_\tau)}{\mathcal{B}(B \rightarrow \bar{D}^{(*)} \ell^+ \nu_\ell)}$$

$\ell = e, \mu$

deviation from SM:

$\sim 1.98\sigma$ for $R(D)$

$\sim 2.15\sigma$ for $R(D^*)$

$\sim 3.2\sigma$ for $R(D) \& R(D^*)$

- ongoing updates on $R(D^{(*)})$ @ Belle II
- measure other inclusive ($R(X_{\tau/\ell})$) and exclusive ($R(\pi)$, $R(\rho)$) ratios
- utilize additional complementary observables sensitive to interaction structures
 \Rightarrow more in next talk by Mateusz Kaleta

Experimental techniques

Monte Carlo simulation samples at Belle/Belle II

MC generators

- $e^+e^- \rightarrow (\Upsilon(4S) \rightarrow B\bar{B})$ for measured B decays by EvtGen (ver. V00-10-07 / ver. R02-00-00)
 - $e^+e^- \rightarrow q\bar{q} (q = u, d, s, c)$ by KKMC
 - decay rates of B decays for which no measurements exist + hadronization of $e^+e^- \rightarrow q\bar{q}$ by PYTHIA (ver. 6 / ver. 8)
 - τ decays by TAUOLA
 - electromagnetic final-state radiation by PHOTOS
-
- detector response by GEANT (ver. 3 / ver. 4)
 - remark: independent `DECAY.DEC` files and (some) EvtGen models in basf and basf2 (Belle and Belle II frameworks)

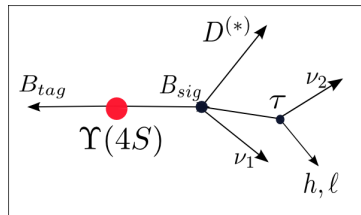
Experimental techniques

tagging in B decays

- efficiency ↑
purity ↓
- Inclusive
 $B \rightarrow \text{hadrons}$ (inclusive modes)
 $\epsilon \approx O(1\%)$
 - + large statistics
 - large background
 - Semileptonic
 $B \rightarrow D^{(*)} \ell \nu_\ell$
 $\epsilon \approx O(0.3\%)$
 - + efficient reconstruction
 - less information about B_{tag} due to ν_ℓ
 - Hadronic
 $B \rightarrow \text{hadrons}$ (exclusive modes)
 $\epsilon \approx O(0.1\%)$
 - + high purity
 - low tagging efficiency

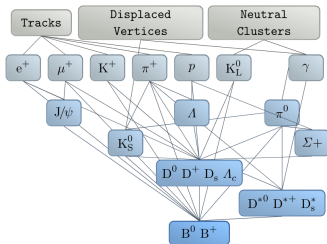
Modes with missing energy (i.e. multi ν) in final state:

- exclusive production of $B\bar{B}$ pairs at B factories
- kinematical constraints from beam energy
- B_{tag} kinematics, flavour/charge



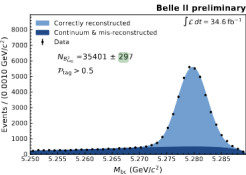
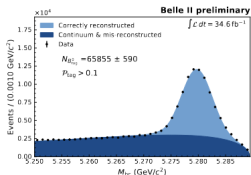
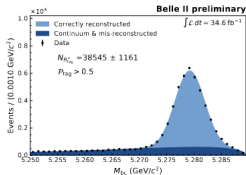
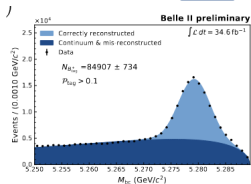
Experimental techniques

exclusive B_{tag} reconstruction algorithm



Full Event Interpretation (FEI)

- improved algorithm based on BDTs
- hierarchical approach to reconstruct $O(10^4)$ decay chains
- for hadronic tag: dominant tag-side decay mode categories: $D\pi$, $D^*\pi$, $Dn\pi$, $D^*n\pi$
- for semileptonic tag: $D^{(*)}l\nu$, $D^{(*)}\pi l\nu$
- $\epsilon_{SL} \approx 2\%$, $\epsilon_{had} \approx 0.5\%$

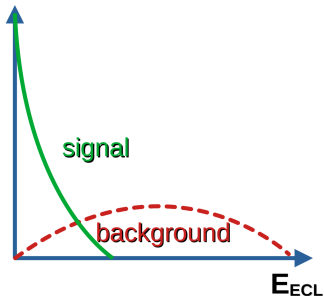


$$M_{bc} = \sqrt{E_{\text{beam}}^2 - (\vec{p}_{B_{\text{tag}}}^{\text{CM}})^2}$$

- E_{beam} is the beam energy in the CMS of $\Upsilon(4S)$
- \vec{p}_B is the momentum of the reconstructed B_{tag}

Experimental techniques

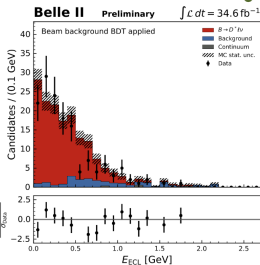
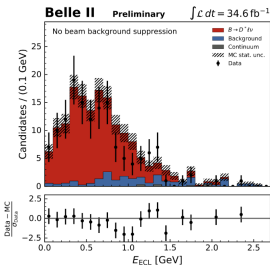
@ B-factories: key variable



ideal vs. reconstructed

E_{ECL} (called also E_{extra})

- hermetic, with large acceptance detector (Electromagnetic CaLorimeter)
- sum energy of all neutral clusters in the event after reconstruction of signal and B_{tag}
- $E_{ECL} \approx 0$ for correctly reconstructed signal
- $E_{ECL} > 0$ for bkg, extra energy due to additional energy deposition
- final shape depends on photons selection, which reduce beam bkg and hadronic split-off photons



$$R(X_{\tau/\ell})$$

the first test of LFU via **inclusive** B decays at Belle II

$R(X_{\tau/\ell})$: ratio explicitly or with B mesons only
PRL. **132**, 211804 (2024)

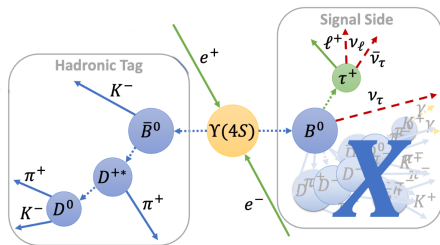
$$R(X) = \frac{\mathcal{B}(B \rightarrow X \tau^+ \nu_\tau)}{\mathcal{B}(B \rightarrow X \ell^+ \nu_\ell)}$$

Challenges

- large background from less constrained X (significant systematic uncertainties associated with background composition)
- difficult MC modeling of the $X = D, D^*, D^{**}$ (source of cross-feeds), non resonant hadronic decays ("gap") $\approx 1\%$
- \Rightarrow dedicated data driven templates reshaping

Selection

- hadronic FEI ($\epsilon_{had} \approx 0.1\%$) + ℓ
- optimized lepton ID requirements and quality of tracks+clusters from X
- continuum suppressed by BDT

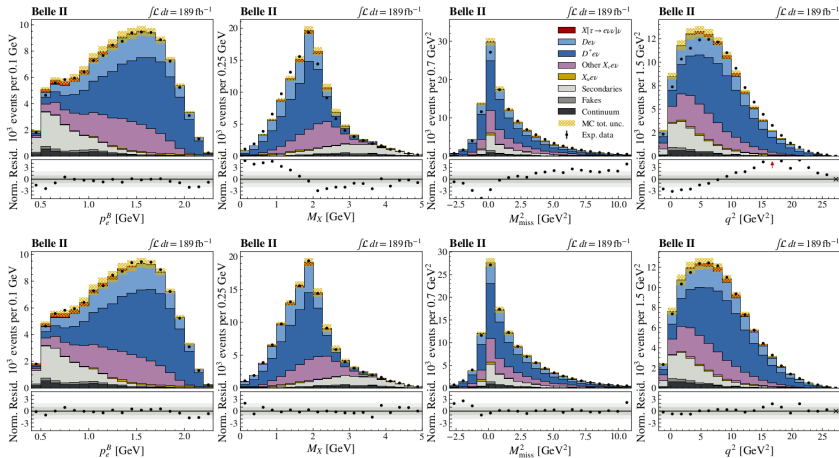


based on DATA sample: 189 fb^{-1}

Control samples

- "high- p_ℓ^B " ($p_\ell^B > 1.4 \text{ GeV}/c^2$) composed of 95% $B \rightarrow X \ell \nu$
- "same charge" enriched with fakes, secondaries, continuum, $B \rightarrow X \tau(\ell) \nu$ from neutral B meson oscillations

$R(X_{\tau}/\ell)$ simulation reweighting



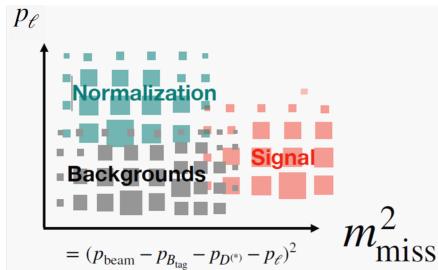
- four key kinematic quantities
- electron channel before (top) and after (bottom) template shape calibration
- mismodeling in M_X due to significant deficit/excess for low/high region due to relative abundance of D decays with K_L^0

$R(X_{\tau/\ell})$

Signal extraction

Strategy

- 2D binned likelihood template fit in the lepton momentum $p_{\ell}^{B_{\text{sig}}}$ in signal B rest frame and squared missing mass
- $$M_{\text{miss}}^2 = ((\sqrt{s}, \vec{0}) - P_{B_{\text{sig}}} - P_{B_{\text{tag}}})^2$$
- 4 components: signal, normalization, $B\bar{B}$ bkg, continuum
 - continuum with constraint on yield derived from off-resonance data

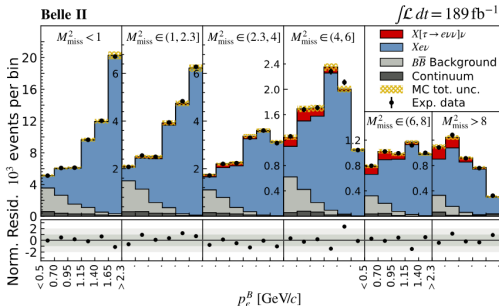


Signal yield

- $X_{\tau\nu}$: $N_e^{\text{meas}} = 2590 \pm 450$
 $N_{\mu}^{\text{meas}} = 1810 \pm 460$
- $X_{\ell\nu}$: $N_e^{\text{meas}} = 95690 \pm 770$
 $N_{\mu}^{\text{meas}} = 89970 \pm 810$
- $R(X_{\tau/\ell}) = \frac{N_{\tau}^{\text{meas}}}{N_{\ell}^{\text{meas}}} \times \frac{N_{\tau}^{\text{sel}}}{N_{\ell}^{\text{sel}}} \times \frac{N_{\tau}^{\text{gen}}}{N_{\ell}^{\text{gen}}}$
- **measured, selected, generated**

$R(X_{\tau/l})$

Fit results



- 1D template fit projections of lepton spectra in missing mass bins

- SM prediction:**

$$R(X_{\tau/l}) = 0.223 \pm 0.005$$

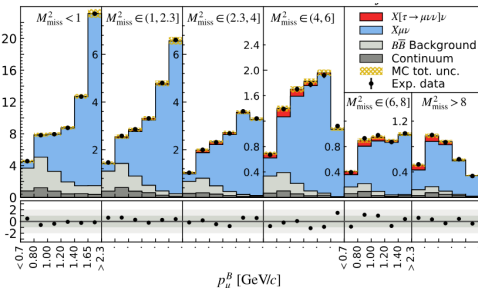
- specific modes:

$$R(X_{\tau/e}) = 0.232 \pm 0.020(\text{stat}) \pm 0.037(\text{syst})$$

$$R(X_{\tau/\mu}) = 0.222 \pm 0.027(\text{stat}) \pm 0.050(\text{syst})$$

- combined:

$$R(X_{\tau/l}) = 0.228 \pm 0.016 \pm 0.036$$



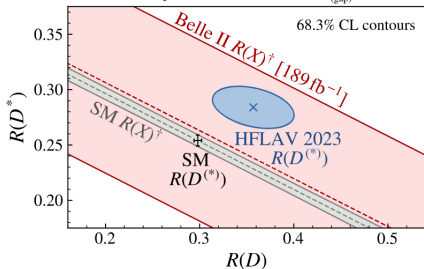
$$R(X_{\tau/l})$$

Systematics + reinterpretation

Source	Uncertainty [%]		
	e	μ	ℓ
Experimental sample size	8.8	12.0	7.1
Simulation sample size	6.7	10.6	5.7
Tracking efficiency	2.9	3.3	3.0
Lepton identification	2.8	5.2	2.4
$X_c \ell \nu$ reweighting	7.3	6.8	7.1
$B\bar{B}$ background reweighting	5.8	11.5	5.7
$X \ell \nu$ branching fractions	7.0	10.0	7.7
$X \tau \nu$ branching fractions	1.0	1.0	1.0
$X_c \tau(\ell) \nu$ form factors	7.4	8.9	7.8
Total	18.1	25.6	17.3

- dominant systematics for shape reweighting for bkg templates, $X \ell \nu$ composition and form factors

\dagger = with expected SM contributions of $D_{(\text{gap})}^{**}$, X_u removed



- result in agreement with SM prediction as well consistent with enhanced semitauonic BF

$$R(D^*)$$

the first test of LFU via **exclusive** B decays at Belle II

$R(D^*)$

PRD 110 072020 (2024)

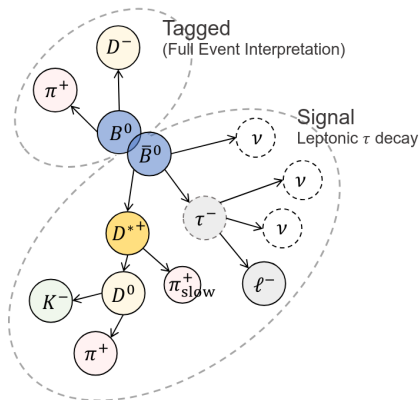
$$R(D^*) = \frac{\mathcal{B}(B \rightarrow D^* \tau^+ \nu_\tau)}{\mathcal{B}(B \rightarrow D^* \ell^+ \nu_\ell)}$$

Challenges

- multiple missing neutrinos in the final state \Rightarrow no clear peak in observables
- modeling of leading bkg: $B \rightarrow D^{**} \ell \nu$
- calibrations + corrections (fake D^* , efficiency of FEI, ...)

Reconstruction

- tag side by hadronic FEI
signal side by leptonic τ decays
- decay chains:
 $B^0 \rightarrow \overline{D}^* \ell^+ \nu, B^+ \rightarrow \overline{D}^{*0} \ell^+ \nu$
- three D^* decay channels:
 $D^{*+} \rightarrow D^0 \pi^+, D^+ \pi^0; D^{*0} \rightarrow D^0 \pi^0$



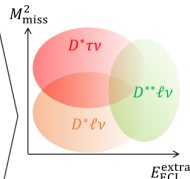
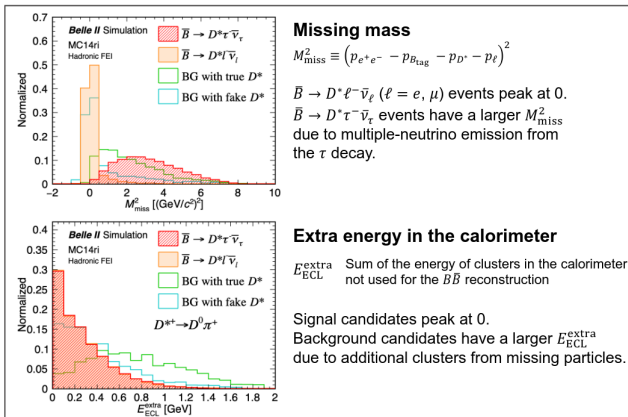
based on DATA sample: 189 fb^{-1}

$R(D^*)$

signal extraction

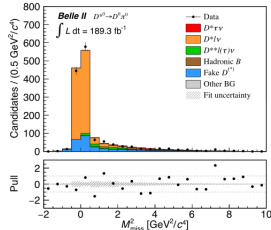
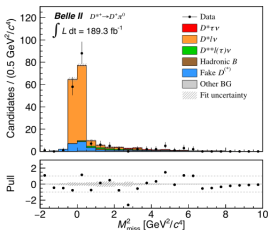
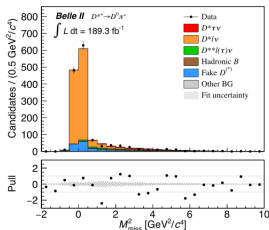
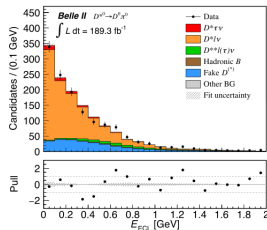
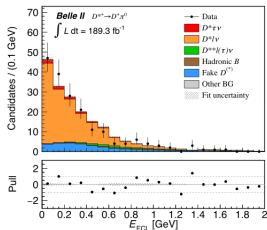
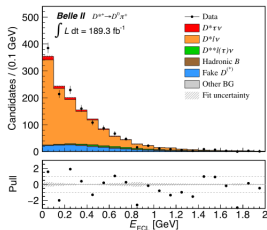
We determine $R(D^*)$ from a two-dimensional fit by extracting both $N_{\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau}$ and $N_{\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell}$.

$$R(D^*) = \frac{N_{\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau} \cdot \mathcal{E}_{\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell}}{N_{\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell} / 2 \cdot \mathcal{E}_{\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau}} \quad (\mathcal{E}: \text{reconstruction efficiency})$$



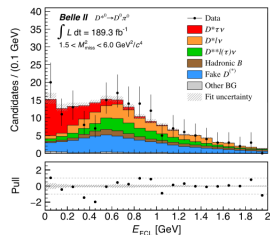
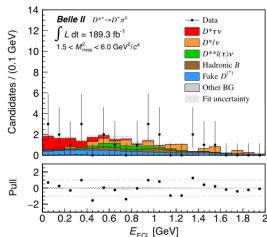
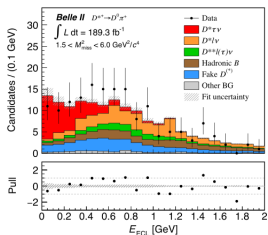
$R(D^*)$

Fit results



$R(D^*)$ Result + E_{ECL} in signal enriched region

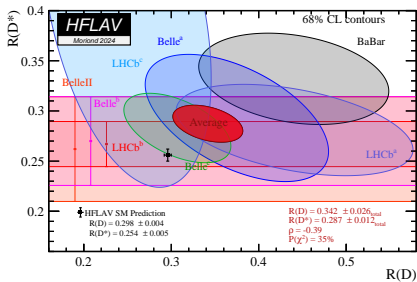
$$R(D^*) = 0.262^{+0.041}_{-0.039}(\text{stat})^{+0.035}_{-0.032}(\text{syst})$$



R(D*)

Systematics + update from HFLAV (Moriond 2024)

Source	Uncertainty
PDF shapes	+9.1%
	-8.3%
Simulation sample size	+7.5%
	-7.5%
$\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$ branching fractions	+4.8%
	-3.5%
Fixed backgrounds	+2.7%
	-2.3%
Hadronic B decay branching fractions	+2.1%
	-2.1%
Reconstruction efficiency	+2.0%
	-2.0%
Kernel density estimation	+2.0%
	-0.8%
Form factors	+0.5%
	-0.1%
Peaking background in ΔM_{D^*}	+0.4%
	-0.4%
$\tau^- \rightarrow \ell^- \nu_\tau \bar{\nu}_\ell$ branching fractions	+0.2%
	-0.2%
$R(D^*)$ fit method	+0.1%
	-0.1%
Total systematic uncertainty	+13.5%
	-12.3%



- **updated deviation from SM** with new Belle II and LHCb results:
 - $\sim 1.6\sigma$ for $R(D)$
 - $\sim 2.5\sigma$ for $R(D^*)$
 - $\sim 3.31\sigma$ for $R(D)$ & $R(D^*)$

LFU tests in $b \rightarrow ulv$

$R(\pi), R(\rho)$

test of LFU in rare semitauonic B decays

$$R(\pi) = \frac{\mathcal{B}(B \rightarrow \pi \tau \nu)}{\mathcal{B}(B \rightarrow \pi \ell \nu)},$$

$$R(\rho) = \frac{\mathcal{B}(B \rightarrow \rho \tau \nu)}{\mathcal{B}(B \rightarrow \rho \ell \nu)}, \ell = e, \mu$$

Motivation:

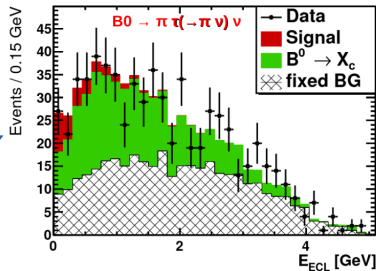
- $R(\pi)$ similar to $R(D) \rightarrow$ sensitive to scalar mediators
 - e.g. modification of q_2 in 2HDM type-II
- $R(\rho)$ similar to $R(D^*) \rightarrow$ sensitive to tensor mediators
 - larger set of angular observables that may probe NP effects

Challenges:

- **SM:** $\text{BF}(B^0 \rightarrow D^- \tau \nu) = 1.05 \pm 0.23 \times 10^{-2}$
- **SM:** $\text{BF}(B^+ \rightarrow D^{*0} \tau \nu) = 1.88 \pm 0.20 \times 10^{-2}$
- **SM:** $\text{BF}(B^0 \rightarrow \pi^- \tau \nu) = 0.94 \pm 0.04 \times 10^{-4}$
- **SM:** $\text{BF}(B^+ \rightarrow \rho^0 \tau \nu) = 0.85 \pm 0.04 \times 10^{-4}$

Experimental status:

- **UL:** $\text{BF}(B^0 \rightarrow \pi^- \tau \nu) < 2.5 \times 10^{-4}$; PRD 93, 032007 (2016)
- $\text{BF}(B^0 \rightarrow \pi^- \tau \nu) = (1.52 \pm 0.72 \pm 0.13) \times 10^{-4}$ @ 2.4 σ
- **SM:** $R(\pi) = 0.641 \pm 0.016$; PRD 92 (11), 115019 (2015)
 - exp test of LFU: **$R(\pi) = 1.05 \pm 0.51$**



$$R(\pi)$$

towards measurement

Modes:

- **signal**: $B^0 \rightarrow \pi^- \tau \nu$; $B^+ \rightarrow \rho^0 \tau \nu$
- **normalization**: $B^0 \rightarrow \pi^- l \nu$; $B^+ \rightarrow \rho^0 l \nu$; $l = e, \mu$

Reconstruction:

- B_{tag} : hadronic FEI
- B_{sig} : require 2 tracks: $\pi + e/\mu$
- cross check: hadronic τ decays ($\tau \rightarrow \pi/\rho \nu$)

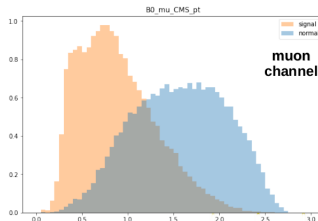
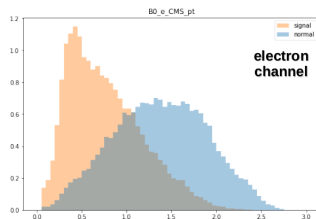
Bkg:

- dominated by $B \rightarrow X_c (e/\mu) \tau \nu$
- continuum ($c\bar{c}$, $s\bar{s}$, $u\bar{u}$, $d\bar{d}$)

Experimental challenges:

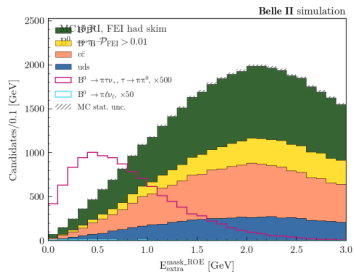
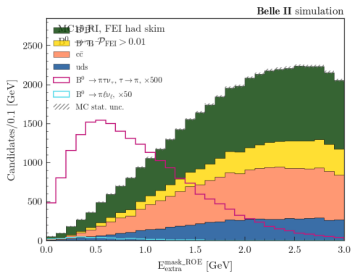
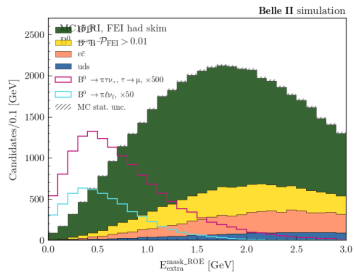
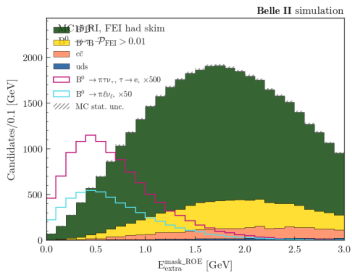
- low momentum leptons from $\tau \Rightarrow$ require improvement of PID, corrections of acceptance effects, better background suppression
- optimization purity of $E_{\text{ECL}} \Rightarrow$ higher S/N

reconstructed transverse momentum of leptons from **signal** and **normalization** modes



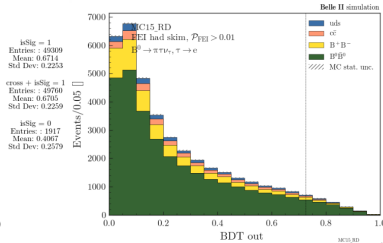
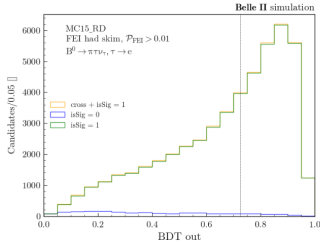
$R(\pi)$

signal extraction from E_{extra} (from AN)



$$R(\pi)$$

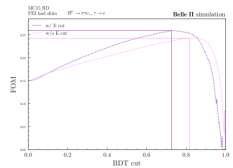
bkg suppressed by BDT in electron mode (from AN)



$$\text{FOM} = \frac{S}{\sqrt{S+B}}$$

S and B are scaled to data lumi
FOM is calculated with the cut on cut on $E_{\text{extra}} < 1.5$ GeV.

BDT out > 0.73	Signal efficiency [%]	Bkg retention [%]
BDT cut	51.27 ± 0.23	4.58 ± 0.05
All selection	0.1436 ± 0.0009	6.28 ± 0.04



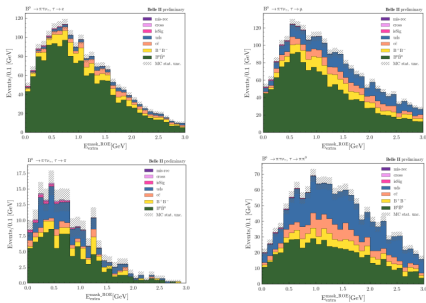
Signal efficiency also includes FEI reconstruction efficiency (#TM signal events/# generated MC events).

Comparing BDTs trained w/ and w/o cut on E_{extra}.

$R(\pi)$ and $R(\rho)$. AN

ISL WG Meeting, 22. 10. 2024

$R(\pi)$ sensitivity study (from AN)



		# signal events		# bkg events	
		isSig	isSig + cross	lisSig	lisSig + lcross
w/o E_{extra} cut	$\tau \rightarrow e$	10	10	1787	1787
	$\tau \rightarrow \mu$	8	9	2332	2329
	$\tau \rightarrow \pi$	3	5	165	164
	$\tau \rightarrow \pi\pi^0$	3	3	1347	1347
	All	24	27	5631	5627
w/ E_{extra} cut $E_{miss} < 1.5$ GeV	$\tau \rightarrow e$	9	9	1297	1297
	$\tau \rightarrow \mu$	8	9	1452	1448
	$\tau \rightarrow \pi$	3	4	149	144
	$\tau \rightarrow \pi\pi^0$	3	3	760	760
	All	23	25	3658	3649

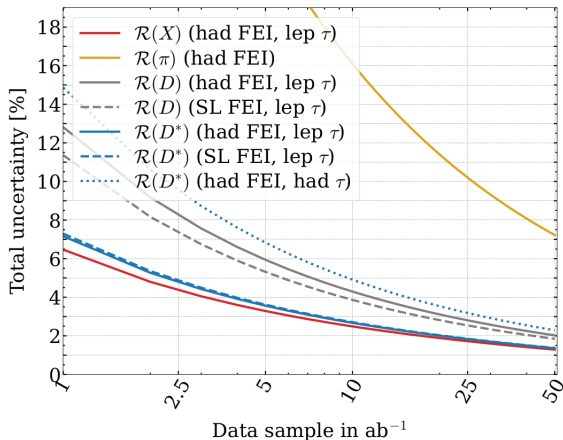
Further reduction of bkg is needed:

- Improve BDT
- Veto extra neutral particles from ROE - needs to be added to the reconstruction script

Expected number of events for signal and background for 365 fb^{-1} .
Number of signal events is estimated from signal MC samples.

Prospects

extrapolation from Snowmass report



$$R(X) = \frac{\mathcal{B}(B \rightarrow X \tau^+ \nu_\tau)}{\mathcal{B}(B \rightarrow X \ell^+ \nu_\ell)}$$

$X = \pi, D, D^*$; $\ell = e, \mu$

- expected Belle II sensitivity for various R measurements as a function of luminosity based on existing Belle and Belle II studies

Summary

+ prospects

- Belle II provide precise experimental information to resolve the puzzle with $R(D^{(*)})$ anomalies
 - the first measurement of $R(X_{\tau/\ell})$, test of LFU via **inclusive** B decays
 - the first measurement of $R(D^*)$ on Belle II dataset
 - ongoing study on $R(\pi)$
-
- important to carry out other complementary measurements in semitauonic B decays (differential distributions, angular observables, ...)
 - still untapped potential from combining the Belle and Belle II datasets
 - indication of possible violation of LFU, often accompanied by LFV \Rightarrow more in talk by Junaid Ur Rehman

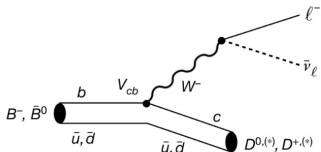
BACKUP BACKUP

Credits to :

Anja Novosel (IJS), Henrik J. (Bonn), Kazuki Kojima (Nagoya),
Florian Bernlochner (Bonn)
for plots, slides or figures

Semitauonic B decays

SM predictions + New Physics scenarios



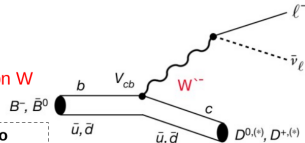
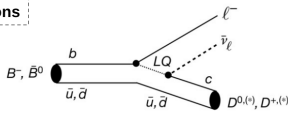
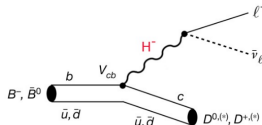
Charged Higgs

impact on R, q2,
angular distributions

Leptoquarks

RH vector boson W

modify only R, no
impact on kinematics



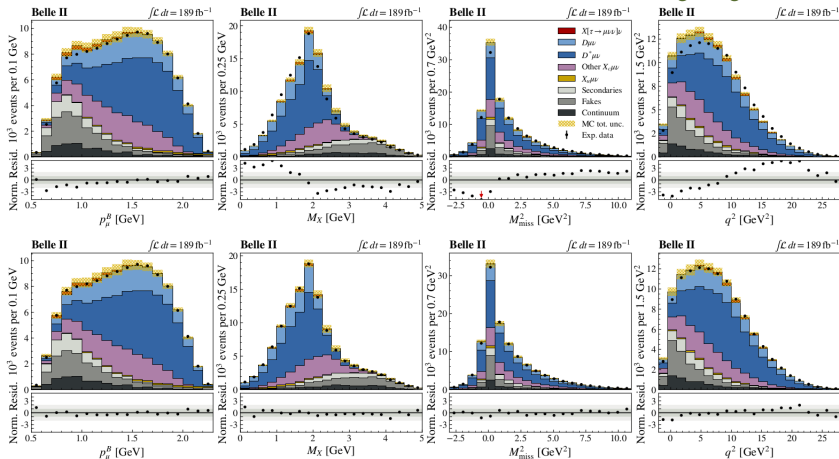
Arithmetic average of SM predictions from

HFLAV:

$$R(D^*)^{\text{SM}} = \frac{\mathcal{B}(B \rightarrow \bar{D}^* \tau^+ \nu_\tau)}{\mathcal{B}(B \rightarrow \bar{D}^* \ell^+ \nu_\ell)} = 0.258 \pm 0.005$$

$$R(D)^{\text{SM}} = \frac{\mathcal{B}(B \rightarrow \bar{D} \tau^+ \nu_\tau)}{\mathcal{B}(B \rightarrow \bar{D} \ell^+ \nu_\ell)} = 0.299 \pm 0.003$$

$R(X_{\tau}/\ell)$ simulation reweighting



- four key kinematic quantities
- muon channel before (top) and after (bottom) template shape calibration
- mismodeling in M_X due to significant deficit/excess for low/high region due to relative abundance of D decays with K_L^0

$R(D^*)$

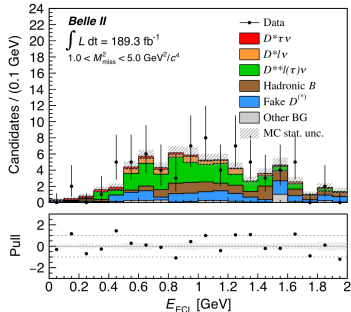
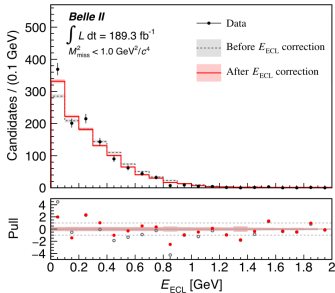


TABLE I. Simulated branching fractions of $\bar{B} \rightarrow D^{*} \ell \nu$ decays used for modeling the leading background. The branching fractions used for the evaluation of the systematic uncertainty due to nonresonant $\bar{B} \rightarrow D^{*} \ell \ell' \nu$ are shown in parenthesis.

Decay	Branching fraction [10^{-3}]	
	$B(B^*)$	$B(B^*)$
$\bar{B} \rightarrow D_s^* \ell \nu$	6.16 ± 1.01	6.63 ± 1.09
$\bar{B} \rightarrow D_s^* \ell' \nu$	3.90 ± 0.70	4.20 ± 0.75
$\bar{B} \rightarrow D_s^* \ell \nu$	3.90 ± 0.84	4.20 ± 0.90
$\bar{B} \rightarrow D_s^* \ell' \nu$	2.73 ± 0.30	2.93 ± 0.32
$\bar{B} \rightarrow D_s^* R^* \ell \nu$...	0.30 ± 0.14
$\bar{B} \rightarrow D_s^* R^* \ell' \nu$...	0.29 ± 0.19
$\bar{B} \rightarrow D_s^* \ell \nu$	$0.0(3.3 \pm 0.99)$	$0.0(3.3 \pm 0.99)$
$\bar{B} \rightarrow D^* \ell \ell' \nu$	$0(-1.1 \pm 1.1)$	$0(-1.1 \pm 1.1)$
$\bar{B} \rightarrow D^* \ell \ell' \nu$	0.58 ± 0.82	0.62 ± 0.89
$\bar{B} \rightarrow D^* \ell \ell' \nu$	2.01 ± 0.95	2.16 ± 1.02
$\bar{B} \rightarrow D^* \ell \ell' \nu$	4.09 ± 4.09	3.77 ± 3.77
$\bar{B} \rightarrow D^* \ell \ell' \nu$	4.09 ± 4.09	3.77 ± 3.77
$\bar{B} \rightarrow D^* \ell \nu$	0.52 ± 0.52	0.56 ± 0.56
$\bar{B} \rightarrow D^* \ell \nu$	0.33 ± 0.33	0.36 ± 0.36
$\bar{B} \rightarrow D^* \ell \nu$	0.33 ± 0.33	0.36 ± 0.36
$\bar{B} \rightarrow D^* \ell \nu$	0.23 ± 0.23	0.25 ± 0.25
$\bar{B} \rightarrow D^* \ell \nu$	0.05 ± 0.05	0.05 ± 0.05
$\bar{B} \rightarrow D^* \ell \ell' \nu$	0.17 ± 0.17	0.18 ± 0.18
$\bar{B} \rightarrow D^* \ell \nu$	0.35 ± 0.35	0.32 ± 0.32
$\bar{B} \rightarrow D^* \ell \nu$	0.35 ± 0.35	0.32 ± 0.32