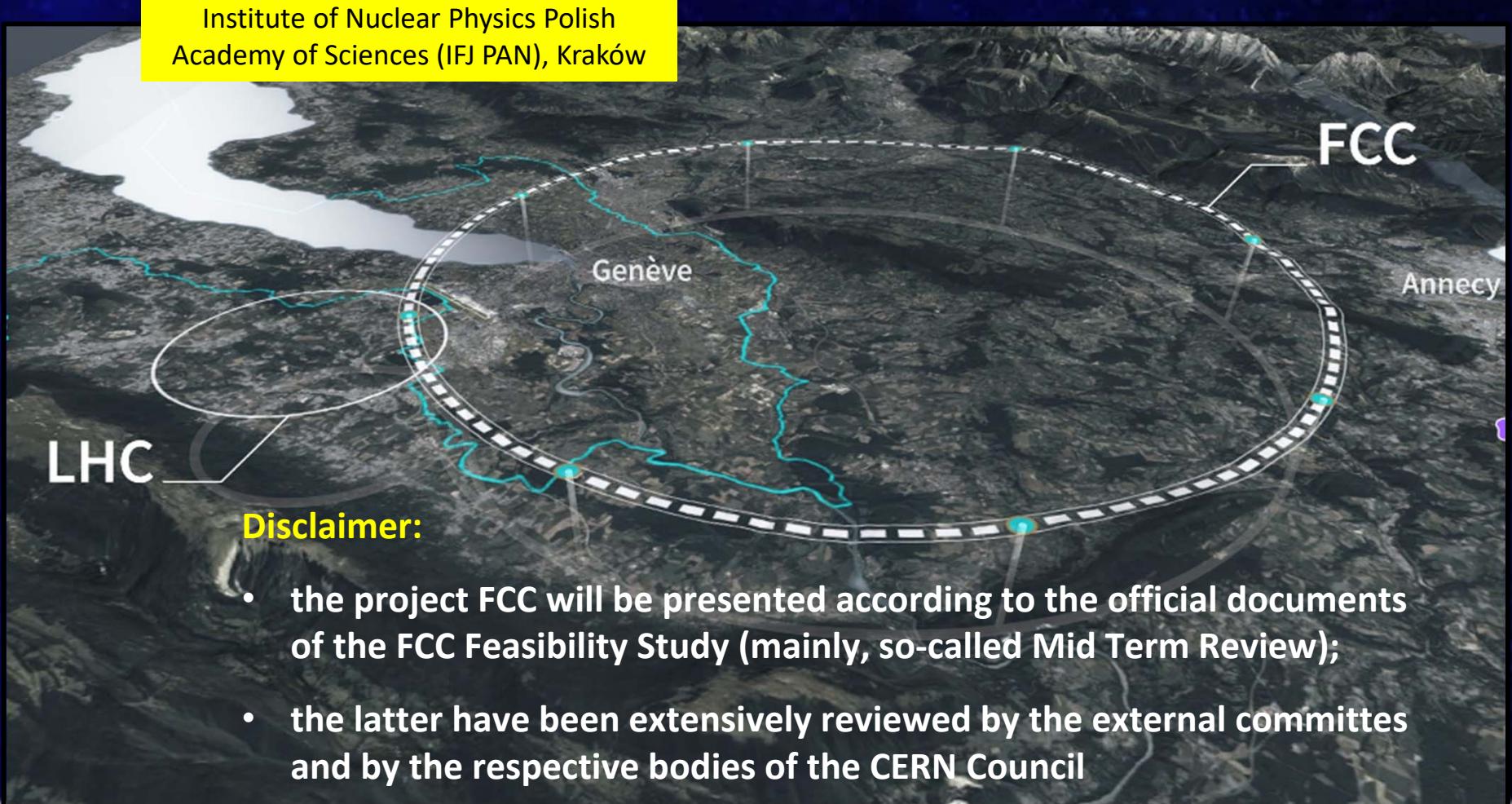


The Future Circular Collider Project: Plans and Physics Program

1. FCC project in a nutshell
2. FCC-ee Physics Programme
3. A few words about the FCC-hh

Tadeusz Lesiak

Institute of Nuclear Physics Polish
Academy of Sciences (IFJ PAN), Kraków



"An electron-positron Higgs factory is the highest-priority next collider.

For the longer term, the European particle physics community has
the ambition to operate a proton-proton collider at the highest achievable energy."

"Europe, together with its international partners, should investigate the technical and financial feasibility of a future hadron collider at CERN with a centre-of-mass energy of at least 100 TeV and with an electron-positron Higgs and electroweak factory as a possible first stage."

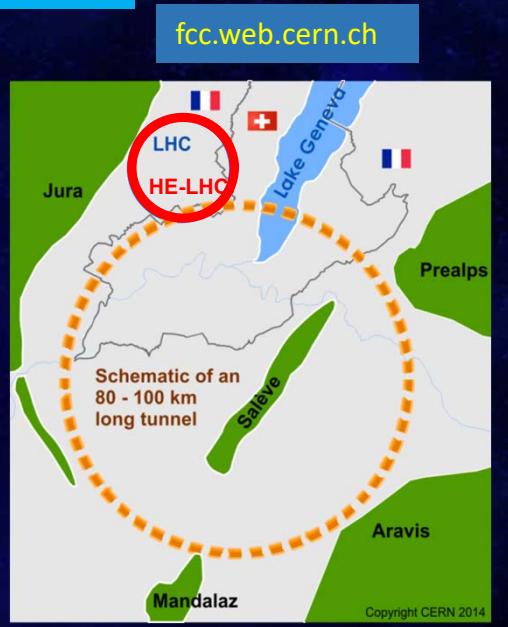
<https://cds.cern.ch/record/2721370/files/CERN-ESU-015-2020%20Update%20European%20Strategy.pdf>

CERN Council, June 2021:
approval of the FCC feasibility study (FCC-FS)
→ Mid term review by the end of 2023
→ Final report by the end 2025



FCC - global international collaboration hosted at CERN

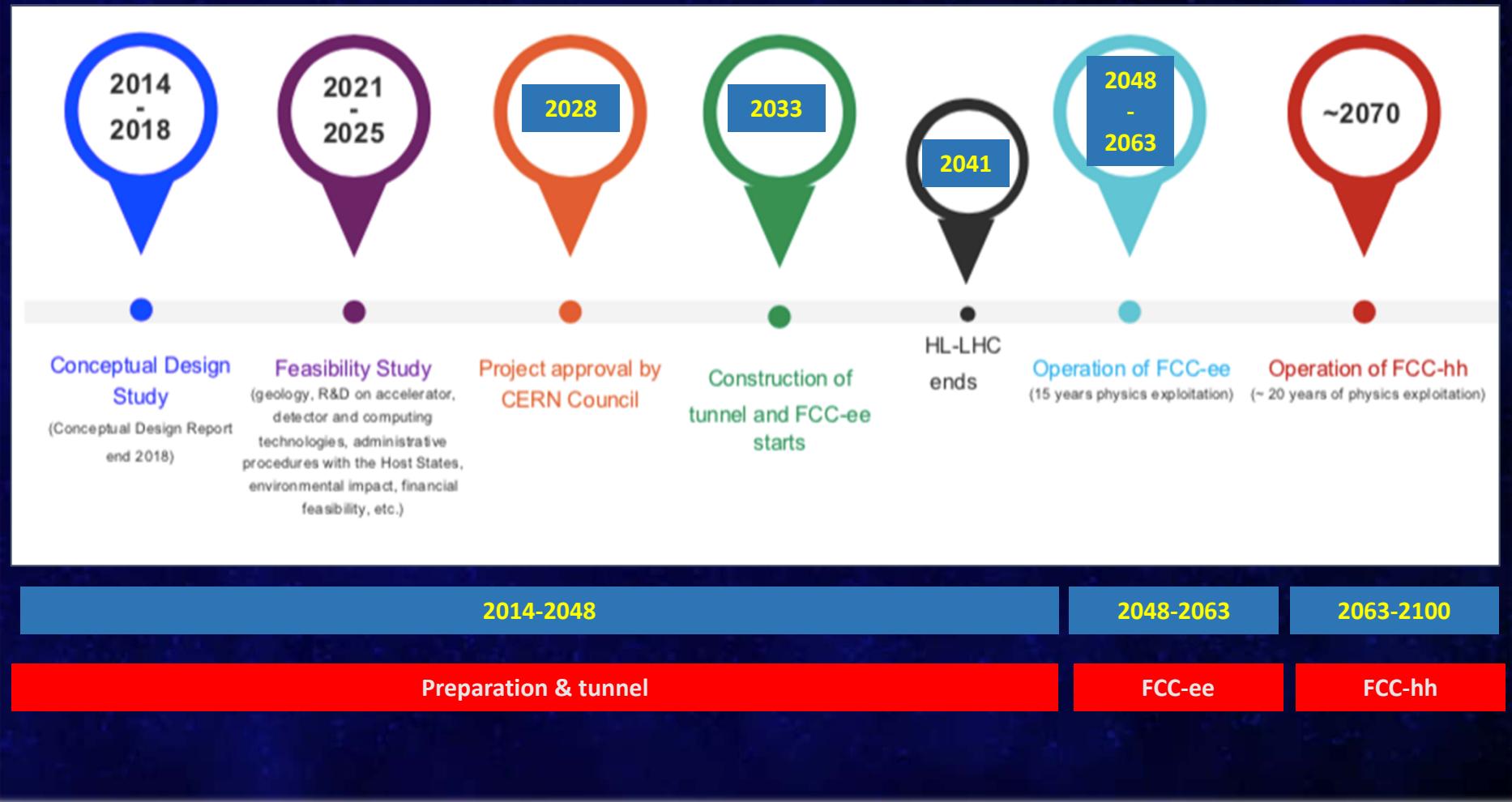
- ✓ **0th stage:** construction of ~91 km circumference tunnel infrastructure in Geveva area to host:
- ✓ **1st stage – FCC-ee:** electron positron collisions (90-360) GeV
- ✓ **2nd stage – FCC-hh:** proton-proton collisions at ~100 TeV
- ✓ Options of AA and eh also envisioned



FCC timeline



ANY future collider at CERN cannot start physics operation before ~2045-2048
 (but construction will proceed in parallel to HL-LHC operation)



Why FCC?

- **The motivation for FCC-ee: a circular e⁺e⁻ Higgs factory**
 - Opportunity for precise studies at four (five) energy thresholds - well motivated by physics:
 $\sqrt{s} = M_Z, M(WW), M(ZH), M(t\bar{t})$, (and m_H)?
 - Discovery of a light ($m= 125$ GeV) Higgs boson – accessible to a circular machine
 - Substantial progress in e⁺e⁻ circular collider technology (B factories et al.) → mature technology
 - Lack of BSM physics at the LHC → limits the physics case of the 1 TeV scale linear colliders
 - The best performance of all proposed Higgs and electroweak factories → see below
- **The motivation for proton-proton collider FCC-hh:**
 - Indirect exploration of the next energy frontier ($\sim 10x$ LHC)
 - Addressing the fundamental aspects of the SM; further significant improvement in its precision tests
 - Heavy-ion collisions and, possibly, ep/e-ion collisions
 - Excellent playground for the HFM/HTS technology
- **Optimization of overall investment: FCC-hh will reuse same civil engineering and large part of FCC-ee technical infrastructure**
- **It's the only facility commensurate to the size of the CERN community (at least 4 expts) which would guarantee the leading role of CERN in HEP for the next decades**

CIRCULAR, 20 years ago:
„LEP is the last circular e⁺e⁻ collider”



$$\Delta E_{SR} \propto \frac{(E/m)^4}{R}$$

\sqrt{s} (GeV)	ΔE_{SR} (GeV)
10	0.001
100	2.5
500	156

$$\mathcal{L} \propto R \frac{P_{SR}}{\beta_y^*}$$

$$\mathcal{L} \sim 10^{31} \text{ cm}^{-2}\text{s}^{-1}$$

$$\beta_y^* \sim 50 \text{ mm}$$



CIRCULAR, Now:
enormous progress



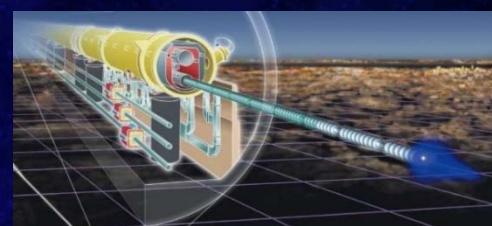
$$\mathcal{L} \leq 10^{36} \text{ cm}^{-2}\text{s}^{-1}$$

- $\beta_y^* \sim 0.8 \text{ mm} \times (50-250)$
- Continuous injection (x5)
- Increase beam power (x5)
- Increase radius (x4)

Maturing technology; usable up to t̄t threshold

LINEAR, Now:

enormous progress, mature(-ing) technology



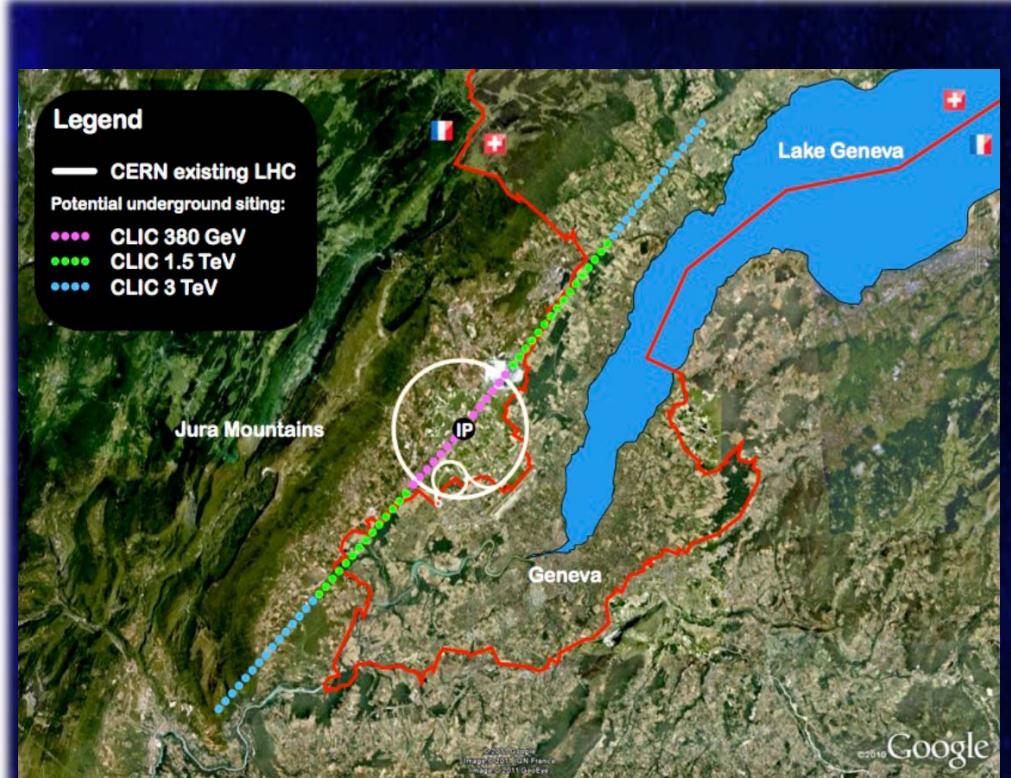
- The beams are accelerated and usable only once
- Longitudinal beam polarization
- The only option for $E > 400 \text{ GeV}$

Proposed Linear e^+e^- Colliders



ILC

International Linear Collider,
Kitakami, Japan



CLIC

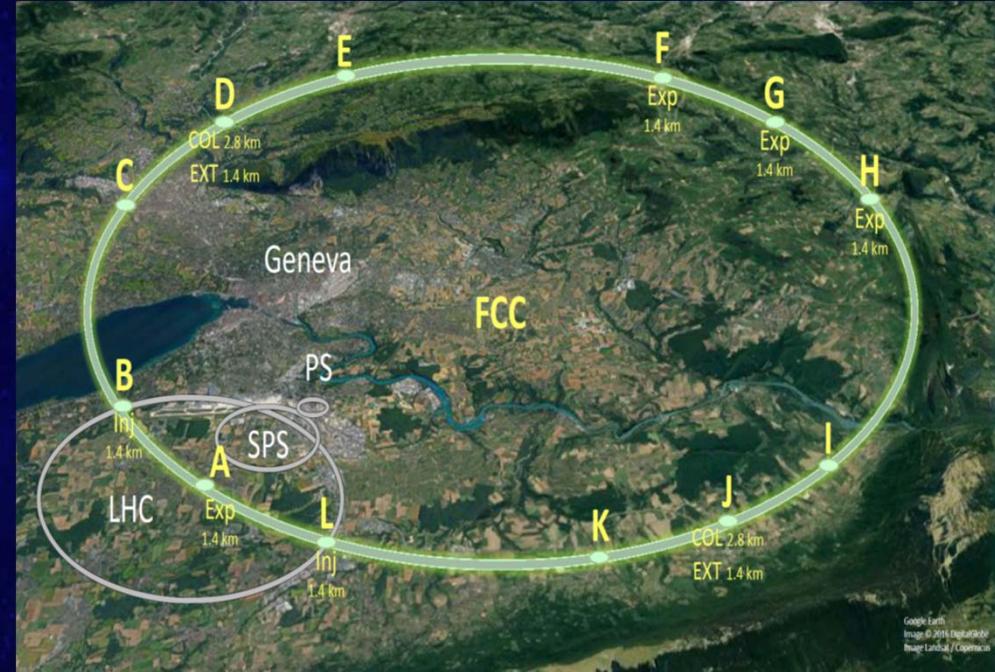
Compact Linear Collider,
CERN

Proposed Circular e^+e^- Colliders



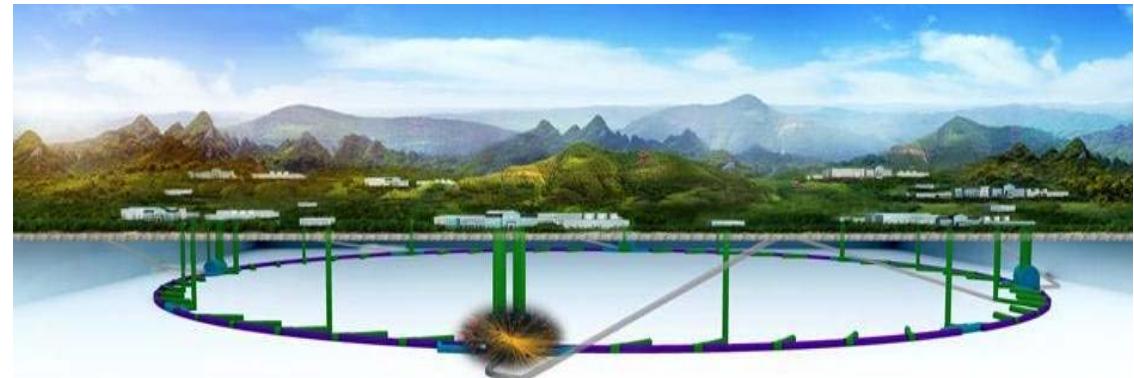
FCC – ee

Future Circular Collider,
CERN



CEPC

Circular Electron
Positron Collider,
China

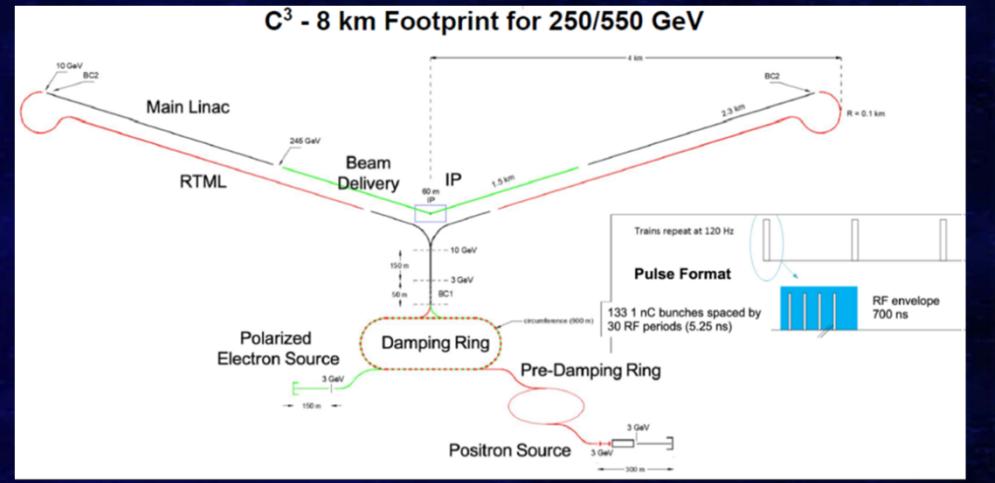


Recently Proposed e^+e^- Colliders



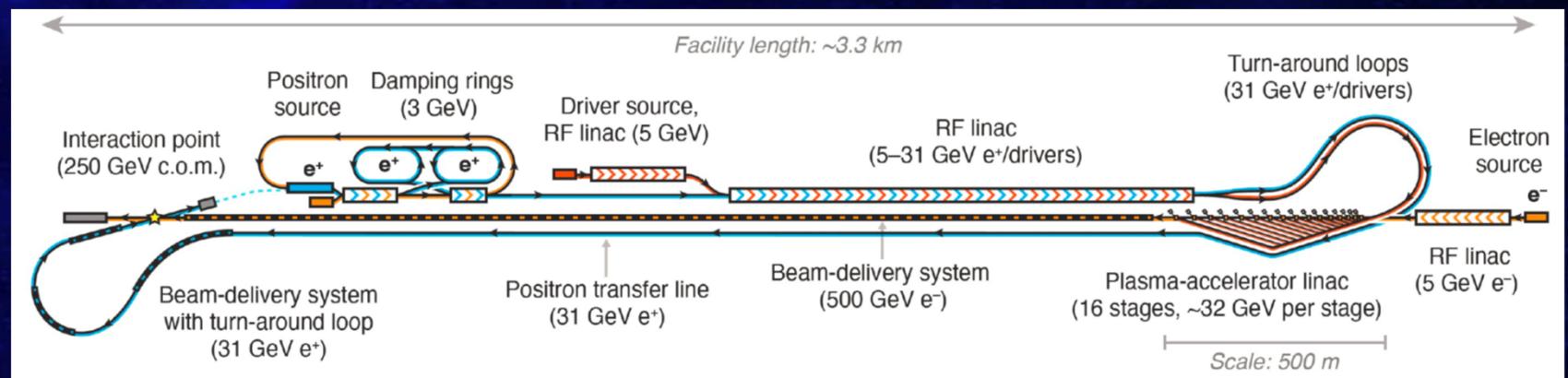
C³

Cool Copper Collider,
US
Normal conducting RF

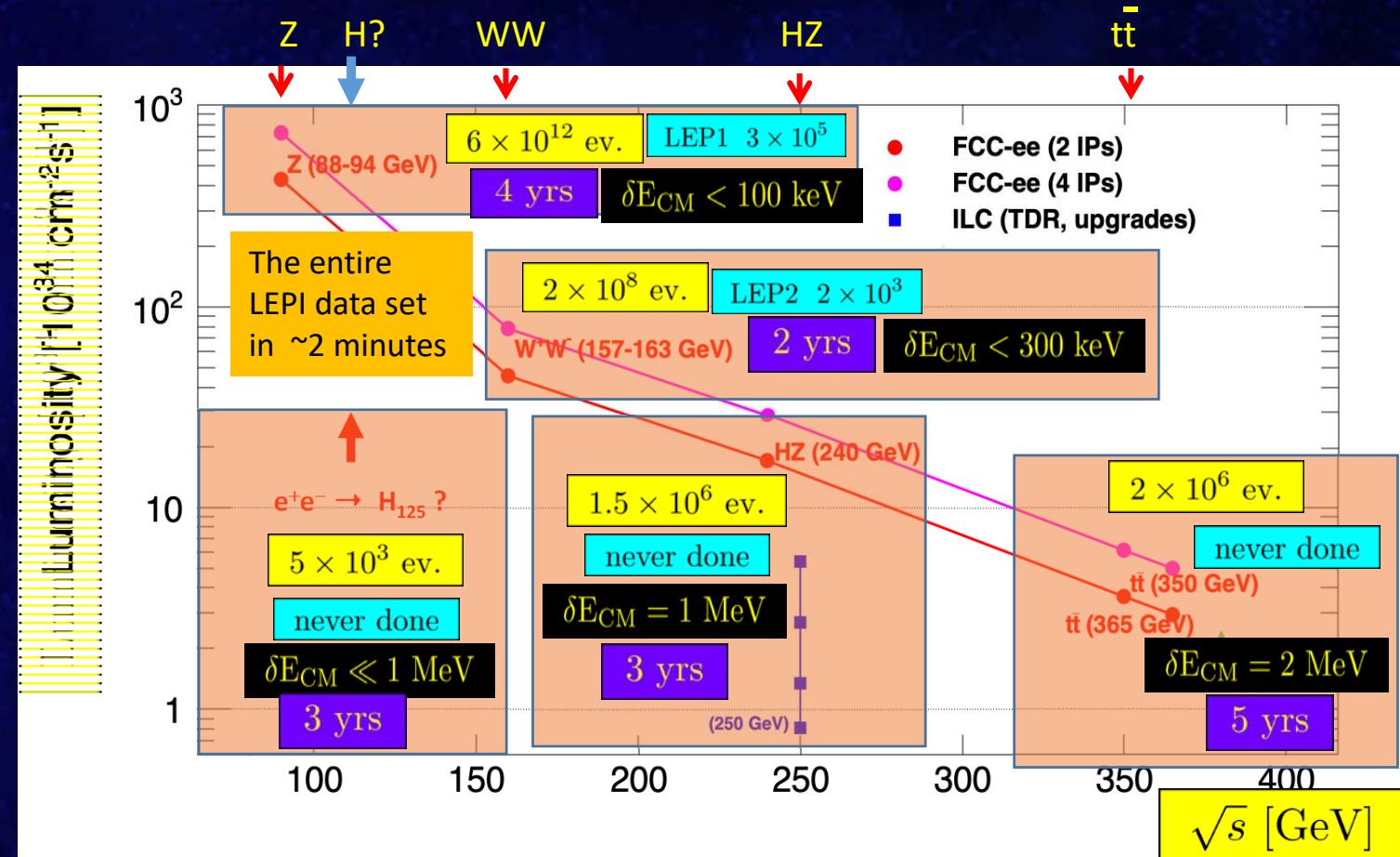


HALHF

Hybrid Asymmetric Linear Higgs Factory
B.Foster, R.D'Arcy, C.A. Lindstroem



FCC Working Points



- Optimal energy range for SM particles!
- HZ and ttbar thresholds never investigated at leptonic colliders !
- Circular colliders can serve up to 4 IPs → increase discovery potential and the community



The goal of the FCC FS mid-term review is to assess the progress of the Study towards the final report (to be submitted in 2025).

Deliverables (approved by Council in Sept 2022):

- D1 : Definition of the baseline scenario
- D2 : Civil engineering
- D3 : Processes and implementation studies with the Host States
- D4 : Technical infrastructure
- D5 : FCC-ee accelerator
- D6: FCC-hh accelerator
- D7: Project cost and financial feasibility
- D8: Physics, experiments and detectors

https://indico.cern.ch/event/1197445/contributions/5034859/attachments/2510649/4315140/spc-e-1183-Rev2-c-e-3654-Rev2_FCC_Mid_Term_Review.pdf

Many thanks to the Host States
for their strong support!



Documents:

- Mid-term report (all deliverables except D7; ~ 700 pages)
- Executive Summary of mid-term report (~ 50 pages)
- Updated cost assessment (D7)
- Funding model (D7)

**Extremely positive feedback so far.
The huge amount of work and great progress
appreciated by the committees.
No show-stopper found at this stage.**

Review steps:

- Oct 2023: FCC Scientific Advisory Committee (scientific and technical aspects) and Cost Review Panel (ad hoc committee; cost and financial aspects)
- Nov 2023: SPC and FC
- 2 Feb 2024: Council

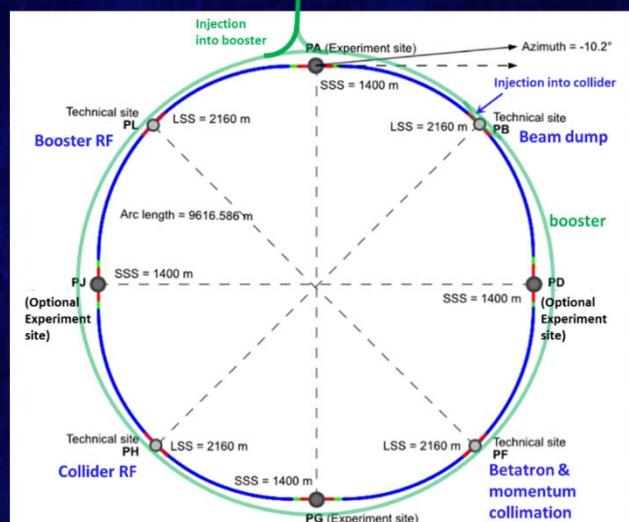
Financing:

**FCC IS: 100 MCHF (4yrs)
HFM : 20 MCHF (annually)**

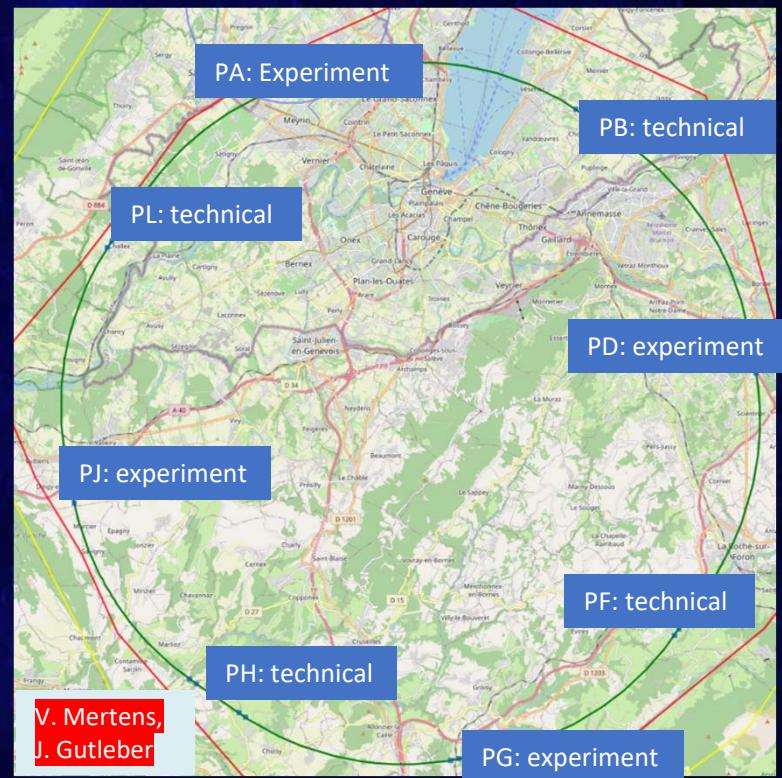
COST (tunnel & FCC-ee & 10% expts)

Domain	2 IP, without ttbar	4 IP, without ttbar	4 IP, incl ttbar
	MCHF	MCHF Additional	MCHF Additional
Total, Accelerators	3,847	60	1,144
Total, Injectors and transfer lines	585		
Total, Civil engineering	5,538	480	
Total, Technical infrastructures	2,490	28	321
Total, Experiments	150	142	
Total, Territorial Development	191		
FCC-ee TOTAL	12,801	710	1,465

- The double ring e^+e^- collider
- **Top-up injection scheme** (for HL) → requires booster synchrotron in the collider tunnel
- SR power of 50 MW/beam at all beam energies
- **Perfect 4-fold super-periodicity allowing 2 or 4 IPs** (robustness, statistics, option for specialised detectors, maximization of physics output)
- **Large horizontal crossing angle of 30 mrad**
- **Crab-waist collision optics**

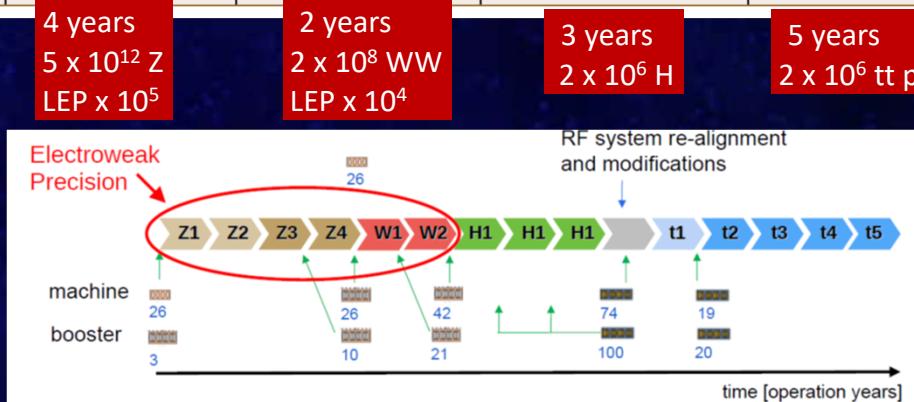


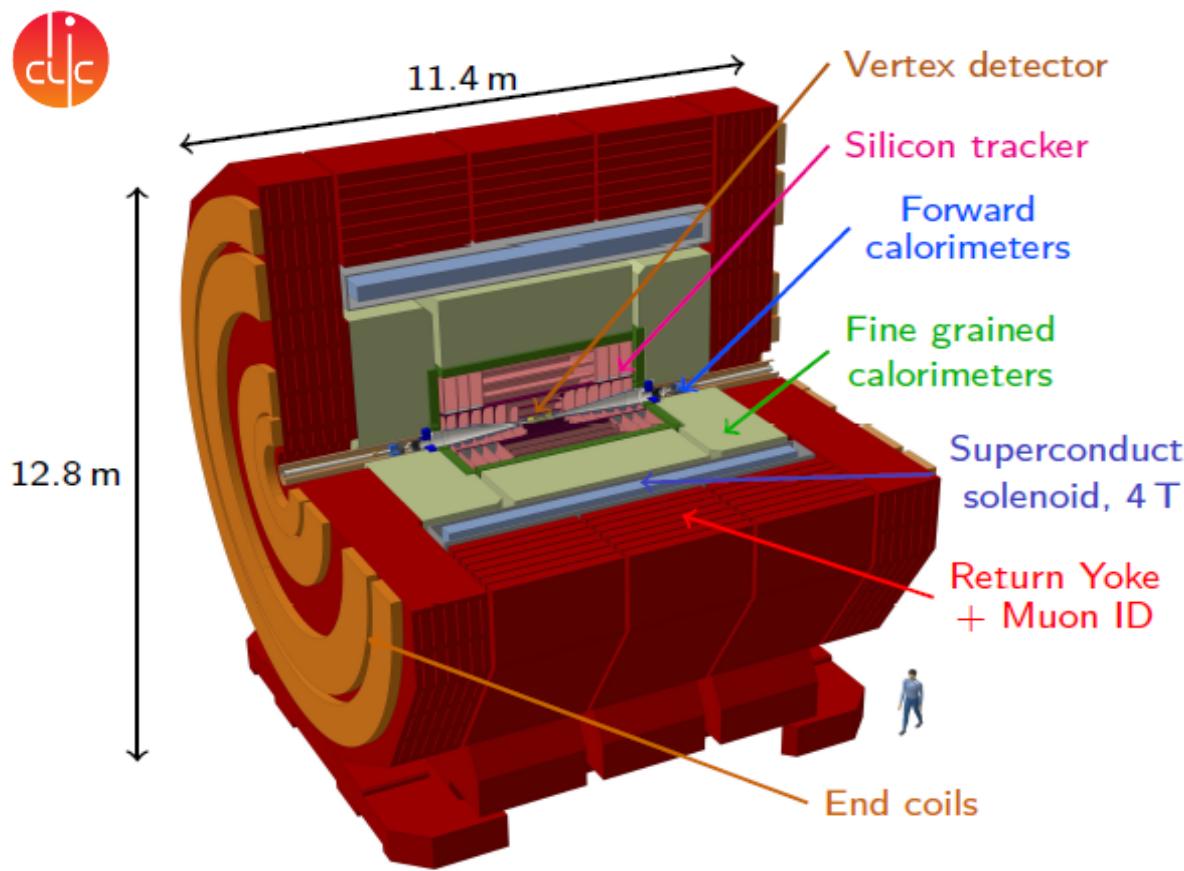
- **The optimized ring placement** chosen out of ~ 100 initial variants (based on geology, surface constraints, environment, infrastructure etc.)
- Total circumference 90.7 km
- Common footprint with FCC-hh (except around IPs)



Parameter	Z	WW	H (ZH)	ttbar
beam energy [GeV]	45	80	120	182.5
beam current [mA]	1280	135	26.7	5.0
number bunches/beam	10000	880	248	36
bunch intensity [10^{11}]	2.43	2.91	2.04	2.64
SR energy loss / turn [GeV]	0.0391	0.37	1.869	10.0
total RF voltage 400/800 MHz [GV]	0.120/0	1.0/0	2.08/0	4.0/7.25
long. damping time [turns]	1170	216	64.5	18.5
horizontal beta* [m]	0.1	0.2	0.3	1
vertical beta* [mm]	0.8	1	1	1.6
horizontal geometric emittance [nm]	0.71	2.17	0.64	1.49
vertical geom. emittance [pm]	1.42	4.34	1.29	2.98
horizontal rms IP spot size [μm]	8	21	14	39
vertical rms IP spot size [nm]	34	66	36	69
luminosity per IP [$10^{34} \text{ cm}^{-2}\text{s}^{-1}$]	182	19.4	7.3	1.33
total integrated luminosity / year [ab $^{-1}$ /yr] 4 IPs	87	9.3	3.5	0.65
beam lifetime (rad Bhabha + BS+lattice)	8	18	6	10

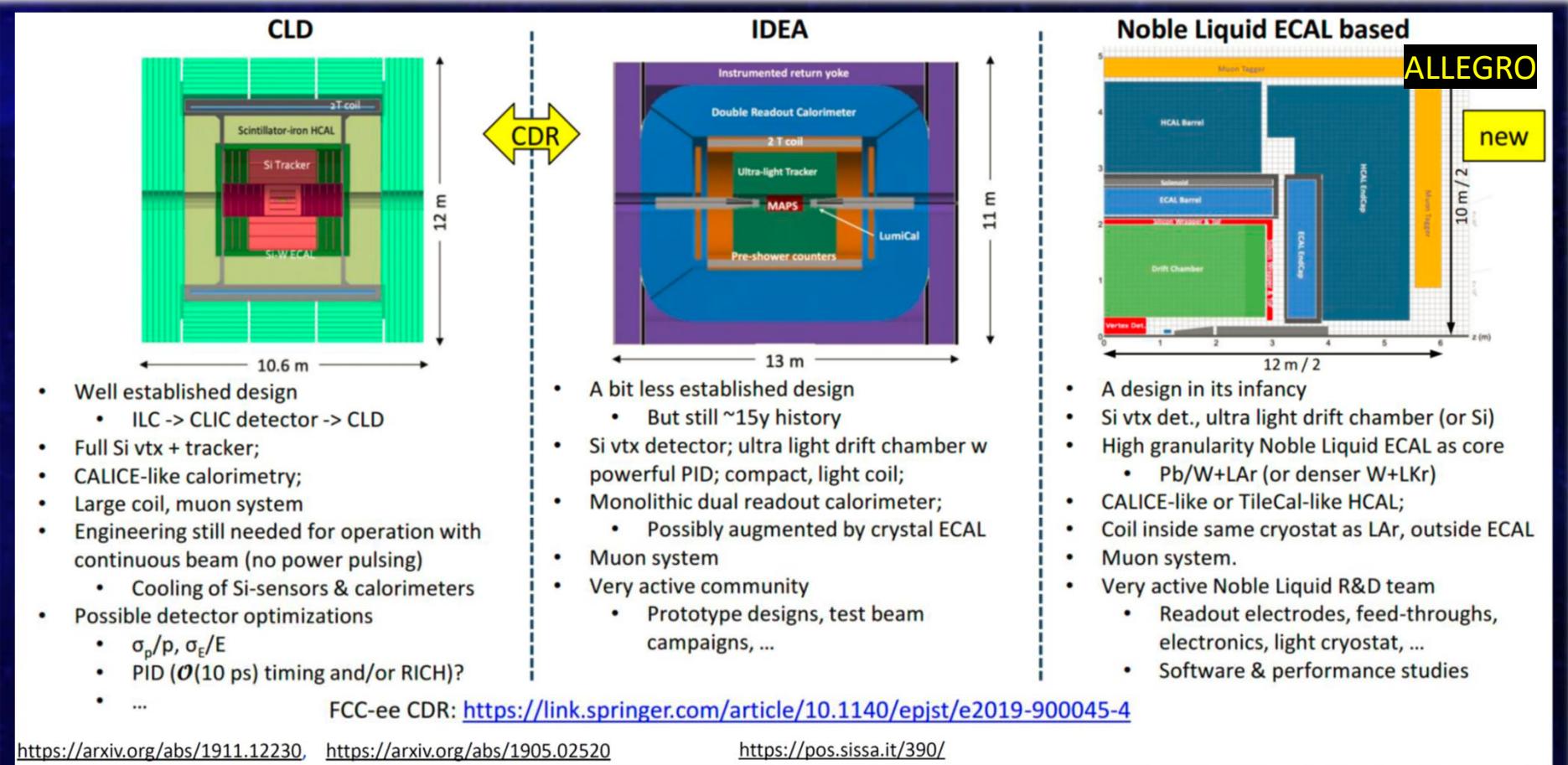
- Z run produces most events followed by the WW run
- Z run the most demanding a.s.a. accelerator and detector are concerned
- Accelerator upgrade in stages





- Number of electronic channels: $>10^9$
- Most of the machine induced limitations are imposed by the Z pole run (large collision rates (33MHz) and continuous beams, large event rates (100 kHz), beamstrahlung

- Low material budget
- Hermeticity (forward region)
- Precision vertex and tracking detectors
- High granularity calorimeters (Particle Flow Algorithm PFA)
- Cost 500-700 MEUR
- Technology fully mature



Full Si vtx

&

tracker

Si vtx

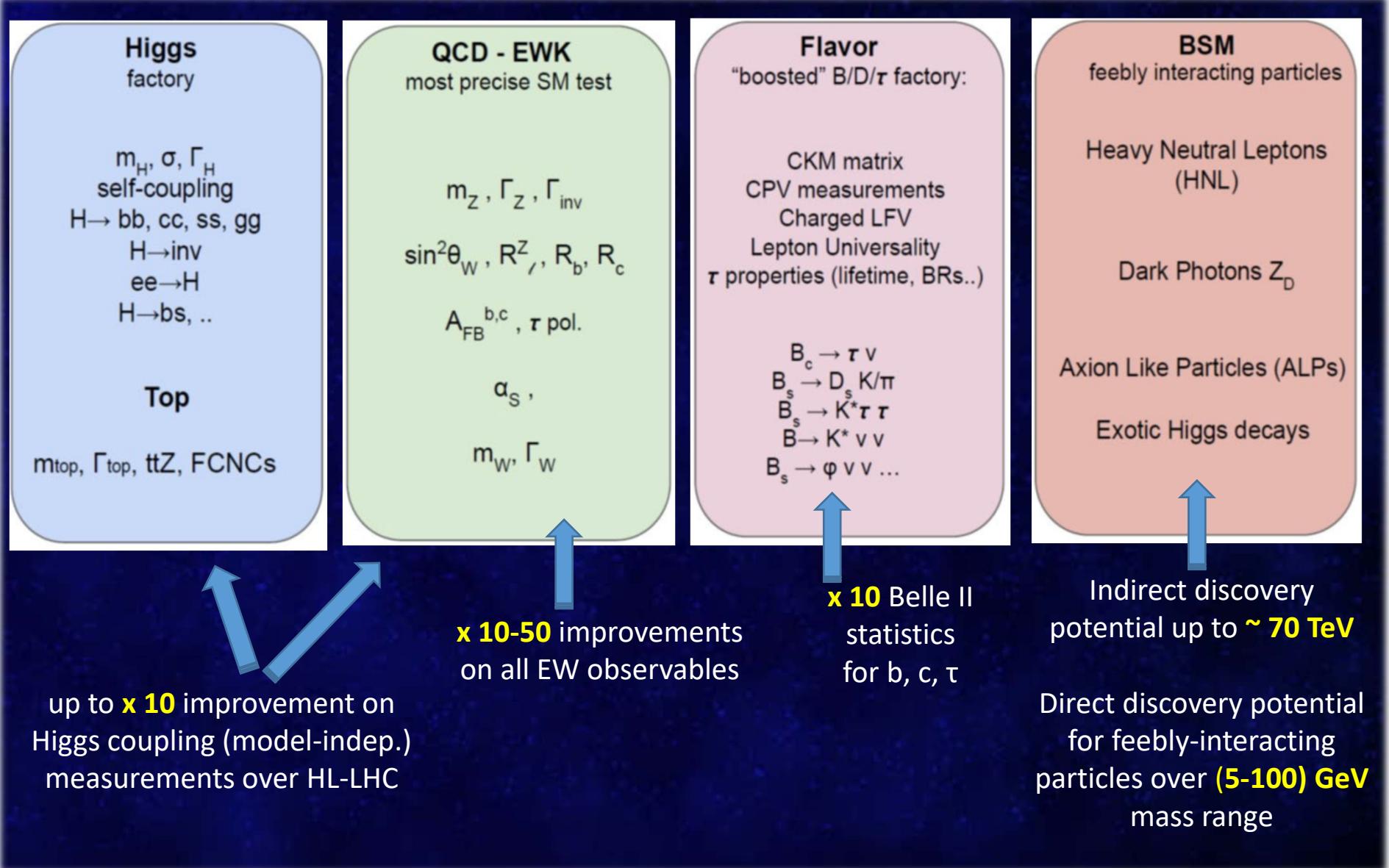
&

ultra light drift chamber

Si vtx &

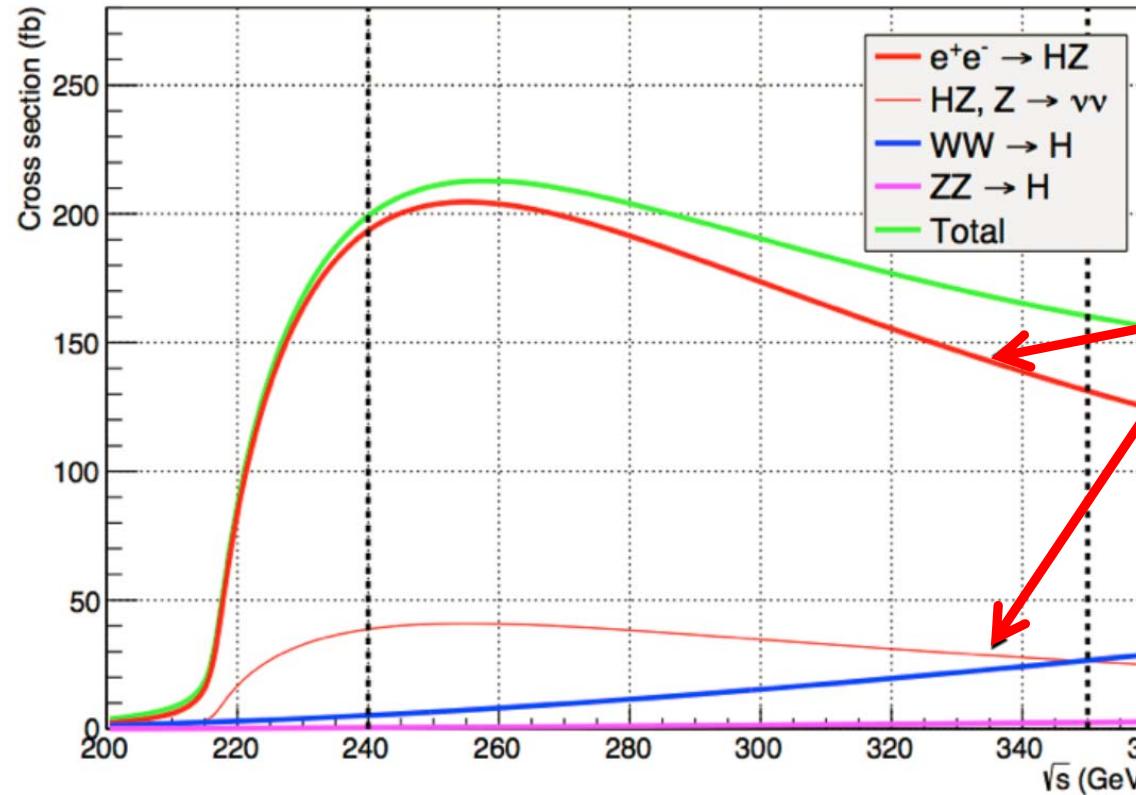
ultra light drift chamber (or Si)

High granularity noble Liquid ECAL

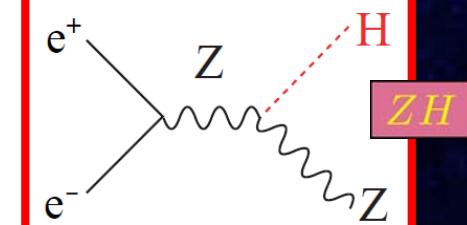


Unpolarized cross sections

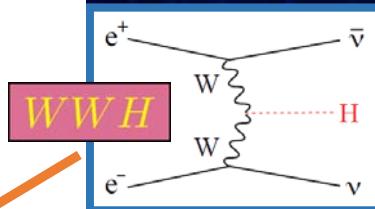
arXiv:1308.6176



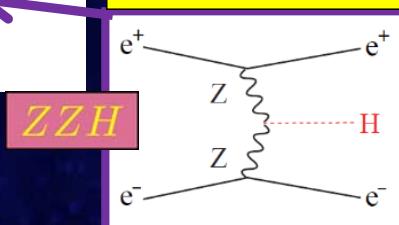
$e^+e^- \rightarrow ZH$



$e^+e^- \rightarrow \nu\bar{\nu}H$



$e^+e^- \rightarrow e^+e^-H$



With 2 IPs:

Phase / threshold	\sqrt{s} [GeV]	int. lumi. [ab^{-1}]	Run duration [years]	No. of Higgs bosons
ZH	240	5.0	3	10^6
$t\bar{t}$	345-365	1.5	5	2×10^5 ZH 5×10^4 VBF

$VBF = WWH + ZZH$

With 4 IPs:

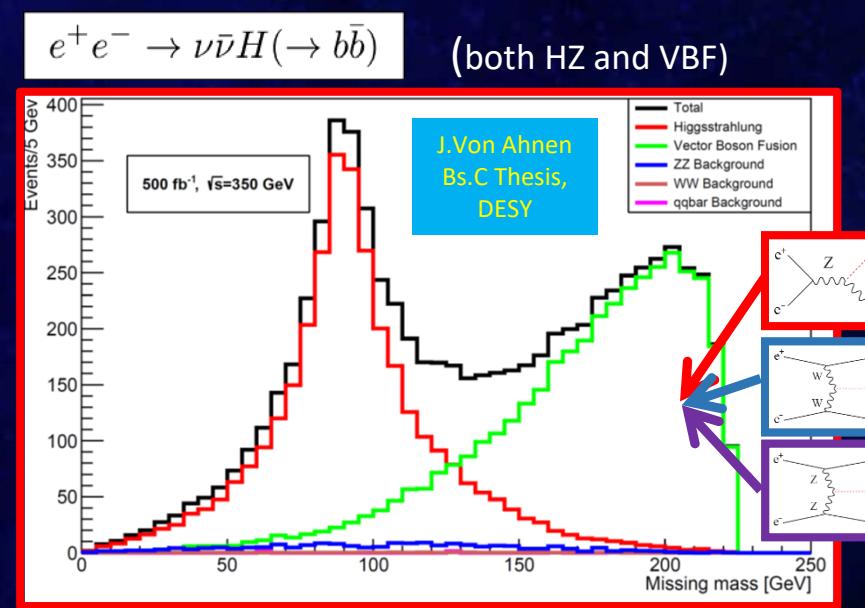
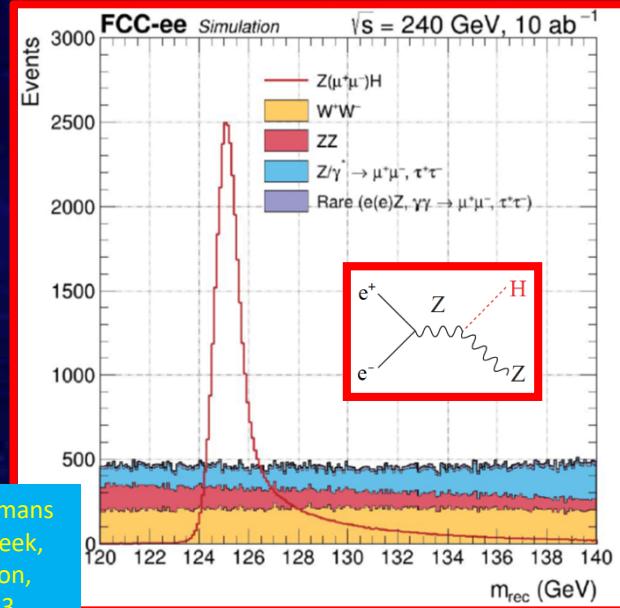
- **Total integrated luminosity $\times 1.7$**
- **Statistical precision increase $\times 1.3$**

Higgs Mass Determination



➤ The recoil technique in $e^+e^- \rightarrow ZH$ - unique for lepton colliders :

- Look just at the Z and reconstruct its decay products
- ZH events are tagged independently of Higgs decay mode (include invisible decay modes)
- Very clean Higgs mass determination: $m_{\text{recoil}}^2 = (\sqrt{s} - E_{\text{ll}})^2 - |\tilde{p}_{\text{ll}}|^2$ $\Delta m_H \sim 10 \text{ MeV}$
- Precise determination of the ZH cross-section: $\Delta\sigma(ZH)/\sigma(ZH) \sim 0.5\%$



$\sqrt{s} = 240 \text{ GeV}$

$$\sigma(HZ) \propto g_{HZZ}^2$$

**g_{HZZ}
measured
(0.1%)**

 $\sqrt{s} = 240 \text{ GeV}$
 $\sqrt{s} = 365 \text{ GeV}$

$$\frac{\sigma(e^+e^- \rightarrow H\nu_e\bar{\nu}_e) \times BR(H \rightarrow b\bar{b})}{\sigma(e^+e^- \rightarrow HZ) \times BR(H \rightarrow b\bar{b})} \propto \frac{g_{HWW}^2}{g_{HZZ}^2}$$

g_{HWW} measured

 $\sqrt{s} = 240 \text{ GeV}$

$$\sigma(e^+e^- \rightarrow HZ) \times BR(H \rightarrow ZZ^*) \propto \frac{g_{HZZ}^4}{\Gamma_H}$$

**Γ_H
measured
(1%)**

Higgs couplings normalized to the SM predictions:

$$k_f = \frac{g_{Hff}}{g_{Hff}^{SM}}, f = b, c, \tau, \mu \quad k_V = \frac{g_{HVV}}{g_{HVV}^{SM}}, V = W, Z, \gamma, g$$

Eur. Phys. J. Plus (2022) 137:92

Coupling	HL-LHC	+ FCC 240 GeV	+ FCC 265 GeV	+ FCC-hh
k_Z	1.5	0.18	0.17	0.16
k_W	1.7	0.44	0.41	0.19
k_b	5.1	0.69	0.64	0.48
k_c	SM	1.3	1.3	0.96
k_g	2.5	1.0	0.89	0.50
k_τ	1.9	0.74	0.66	0.46
k_μ	4.4	8.9	3.9	0.43
k_γ	1.8	3.9	1.2	0.32
$k_{Z\gamma}$	11	—	10	0.70
k_t	3.4	10	3.1	0.95
k_H	50	44	33	3-4

**Higgs couplings to $b\bar{b}$, $c\bar{c}$, $\tau^+\tau^-$, $\mu^+\mu^-$,
gg, $\gamma\gamma$...**

can be determined through the tagging
of the respective Higgs decay final states:

 $\sqrt{s} = 240 \text{ GeV}$

(X = b, c, τ , μ , g, γ , ...)

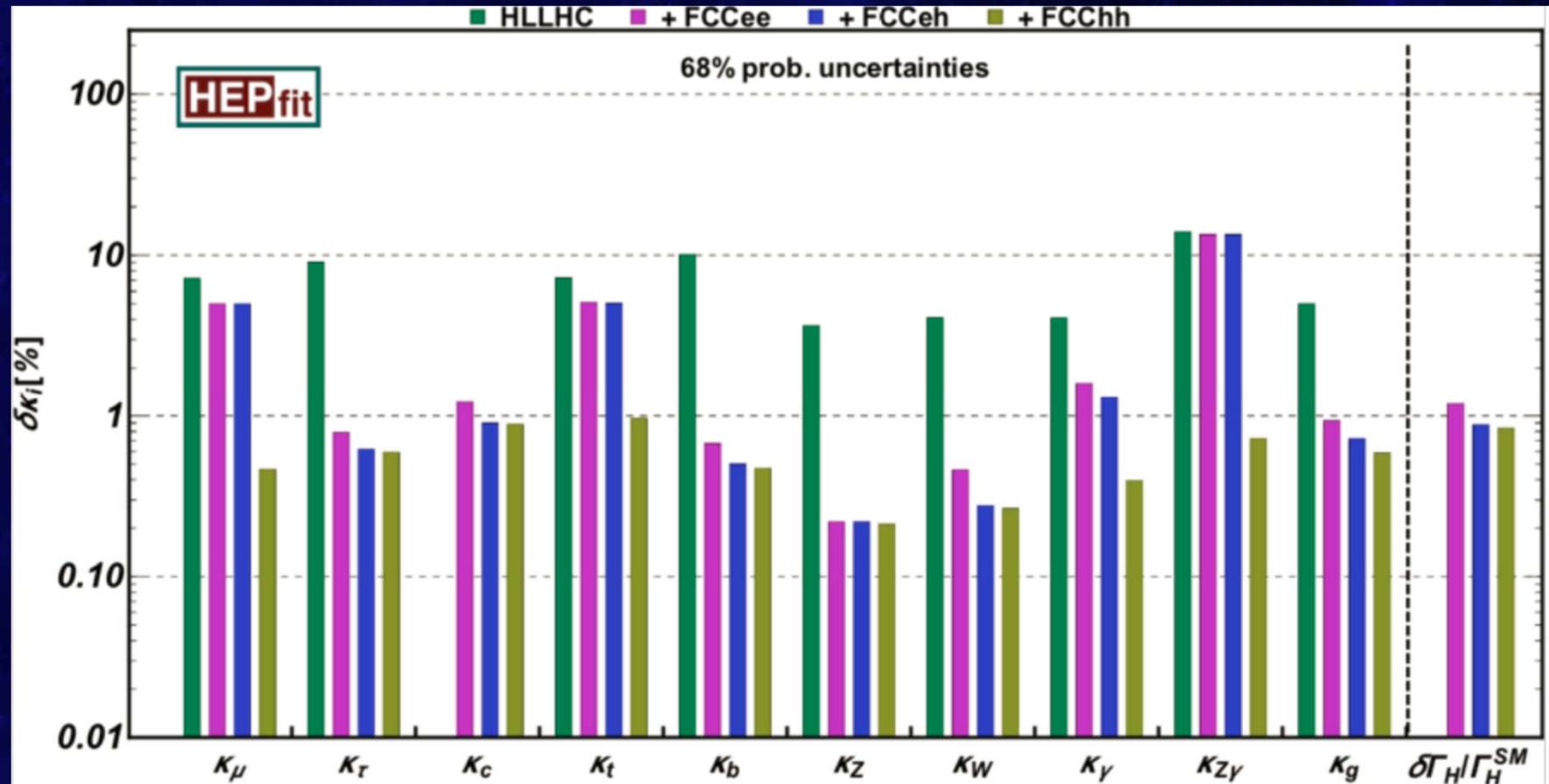
$$\sigma(e^+e^- \rightarrow HZ) \times BR(H \rightarrow X\bar{X}) \propto \frac{g_{HZZ}^2 g_{HXX}^2}{\Gamma_H}$$

 $\sqrt{s} = 365 \text{ GeV}$

$$\sigma(e^+e^- \rightarrow \nu\bar{\nu}H) \times BR(H \rightarrow X\bar{X}) \propto \frac{g_{HWW}^2 g_{HXX}^2}{\Gamma_H}$$



g_{HXX} measured

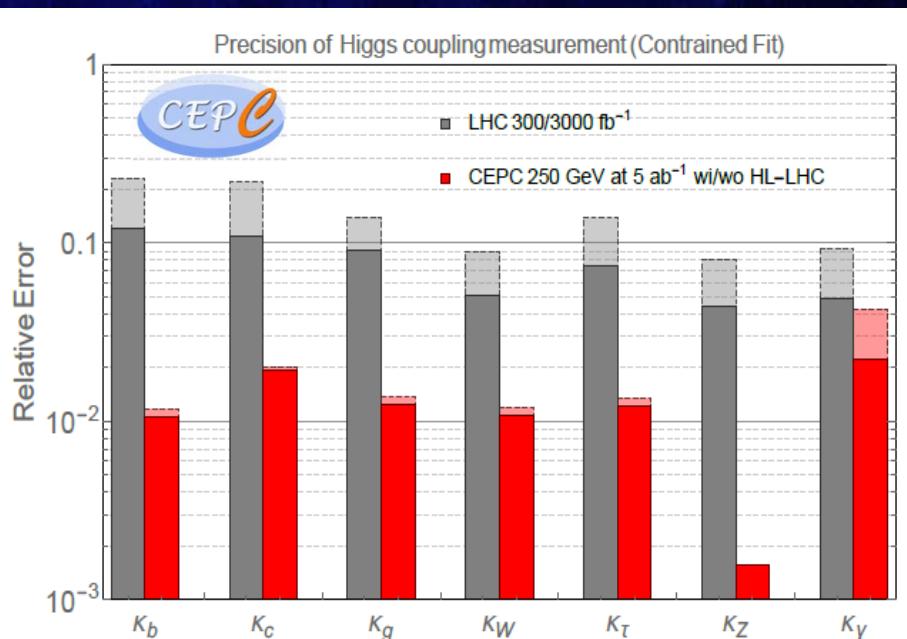


FCC: Factor of (4-10)x improvement for most couplings (w.r.t. HL-LHC)

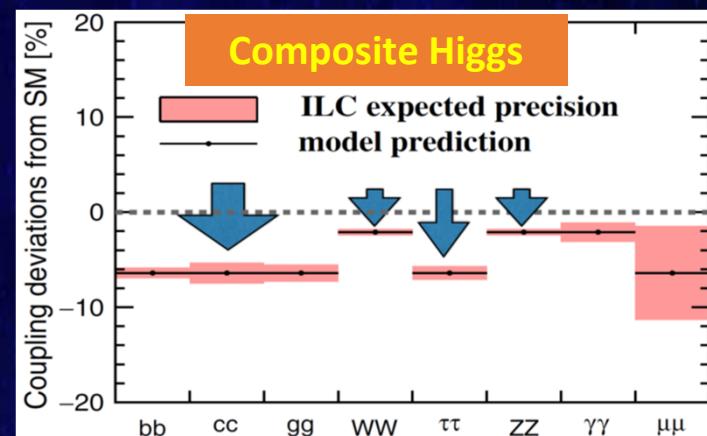
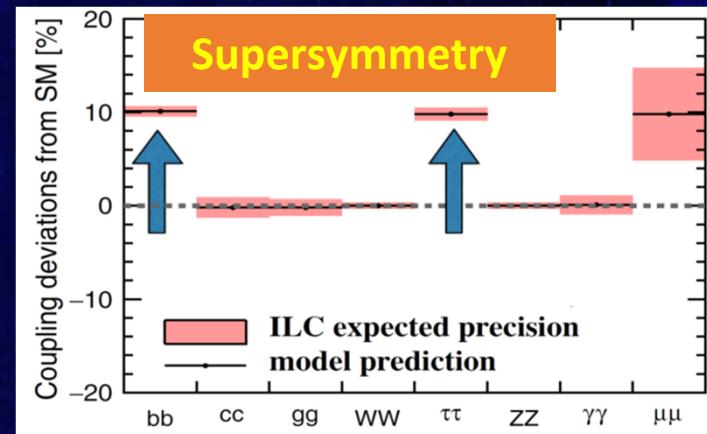
- Higgs couplings normalized to the Standard Model predictions:

$$k_f = \frac{g_{Hff}}{g_{Hff}^{SM}}, \quad f = b, c, \tau$$

$$k_V = \frac{g_{HVV}}{g_{HVV}^{SM}}, \quad V = W, Z, \gamma, g$$

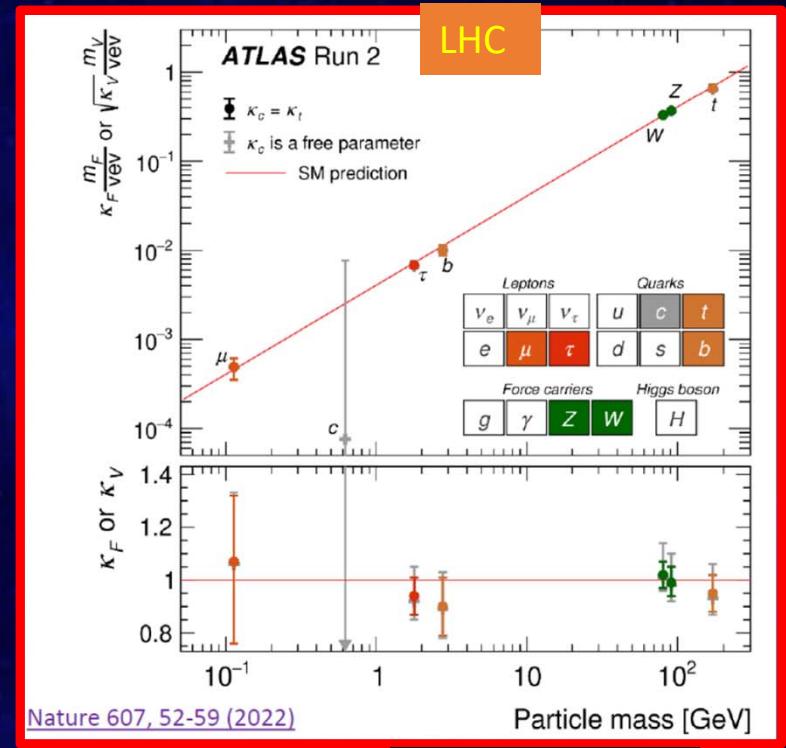


- Fingerprinting NP: different BSM models predict different pattern of deviations from the SM:



Phys Rev. D 97, 053003 (2018)

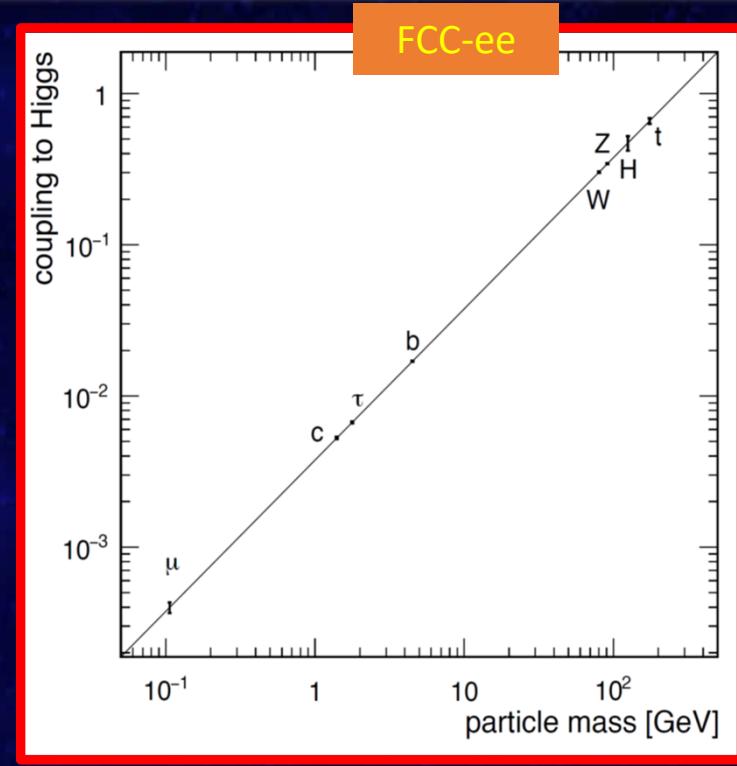
Higgs Couplings: Post FCC-ee



$$\Delta k_f \sim 15\%$$

3rd and 2nd fermion generations only (qualitative precision level for the latter)

Other Higgs topics: Higgs self-coupling



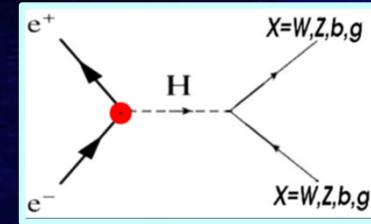
$$\Delta k_f \sim 1\%$$

3rd AND 2nd generations precise measurements

Direct Higgs Production in s-channel



- FCC-ee: potential for direct measurement of the H-e-e Yukawa coupling $BR(H \rightarrow e^+ e^-) \approx 5 \times 10^{-9}$
- $\sigma(e^+ e^- \rightarrow H) = 1.64 \text{ fb}$ - very small $(m_H = 125 \text{ GeV}, \Gamma_H = 4.2 \text{ MeV})$
(several (≈ 10) final states can be studied)
- Calls for a high-luminosity run precisely at $\sqrt{s} = M_H = 125 \text{ GeV}$
- Since $\Gamma_H = 4.1 \text{ MeV}$, it requires beam energy spread monochromatization from the natural spread of $\sim 46 \text{ MeV}$ down to $\sim 4.1 \text{ MeV}$ (and a prior knowledge of the Higgs mass to a few MeV)
- Other problems: ISR+FSR, big backgrounds



Currently reached monochromatization

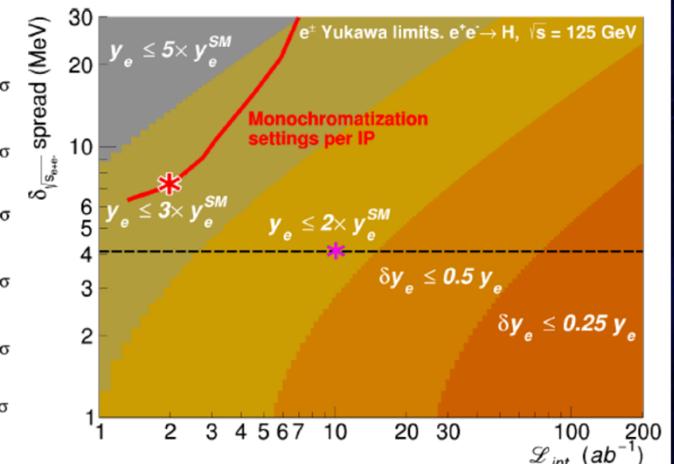
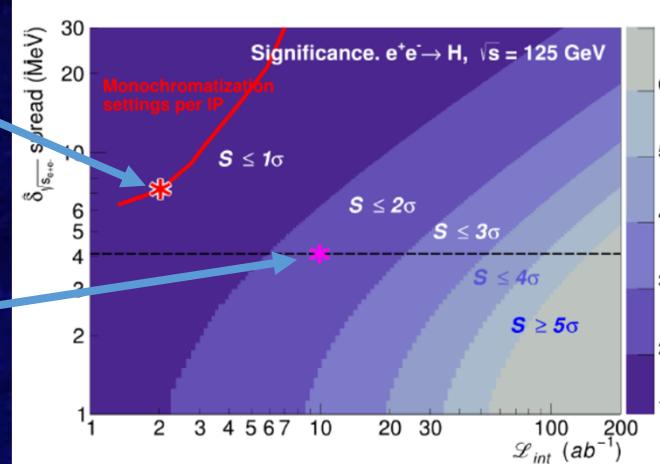
$$C = (\delta_{\sqrt{s}}, \mathcal{L}_{\text{int}}) = (7 \text{ MeV}, 2 \text{ ab}^{-1})$$

Best signal strength monochromatization

$$B = (\delta_{\sqrt{s}}, \mathcal{L}_{\text{int}}) = (4.1 \text{ MeV}, 10 \text{ ab}^{-1})$$

- The signal significance at C

$$S \approx 0.4\sigma/\text{year/IP}$$



- Assuming B and two years of running with 4 IPs ($\sim 12k$ eeH events) $\rightarrow |y_e| < 1.6|y_e^{\text{SM}}| (1.3\sigma)$

Not yet in the baseline

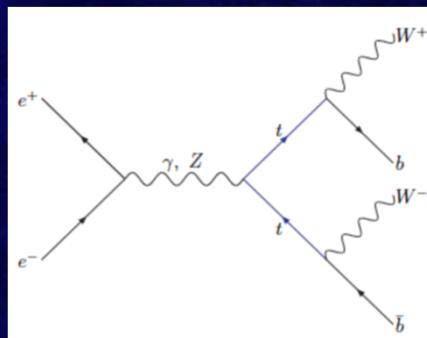
arXiv:2107.0268

$t\bar{t}$ Pair Production at Threshold



➤ Any next e^+e^- collider:

for the 1st time the top quark to be studied using a precisely defined leptonic initial state

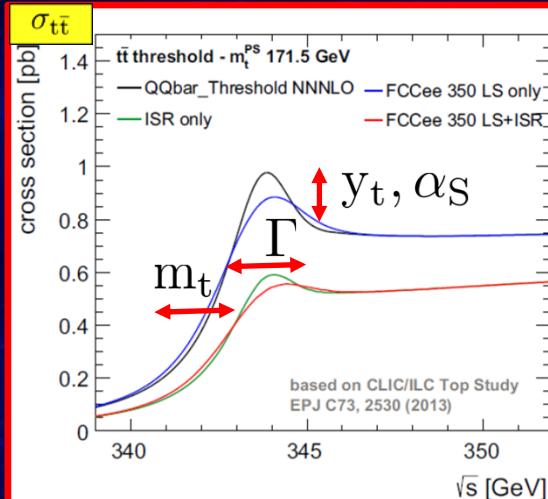
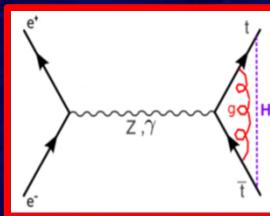


$$e^+e^- \rightarrow Z/\gamma \rightarrow t\bar{t} \rightarrow (bW^+)(\bar{b}W^-)$$

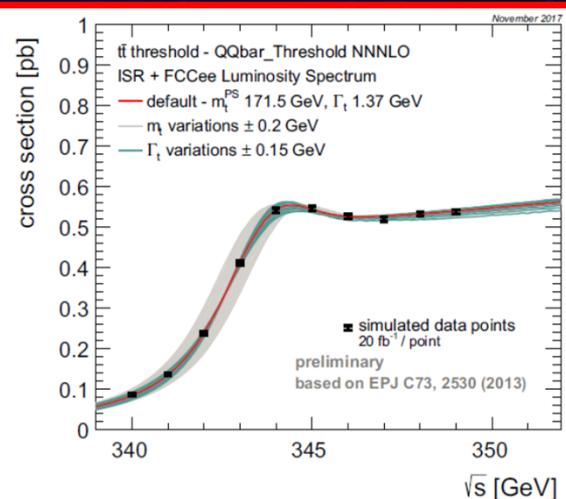
Final state	BR [%]	signature
Fully hadronic	46.2	6 jets
Semi leptonic	43.5	4 jets, 1 l^\pm , 1 ν
Fully leptonic	10.3	2 jets, 2 l^\pm , 2 ν

➤ The shape of the $t\bar{t}$ production cross-section at the threshold is computable to high precision and depends on m_t , Γ_t , α_s , y_t , (and luminosity spectrum)

Eur. Phys. J. C (2019) 79



PDG:



PDG : $m_t = (172.69 \pm 0.30) \text{ GeV}$



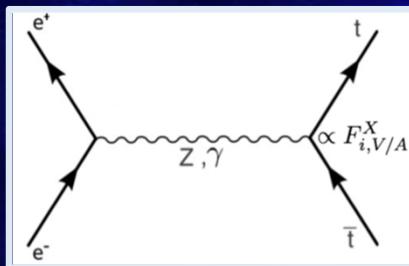
FCC-ee

$\Delta m_t \geq 10 \text{ MeV}$

➤ Other top topics:

Single top production,
 Top quark FCNC,
 $e^+e^- \rightarrow t\bar{t}\gamma$,
 Top-quark EW
 couplings
 ...

$$e^+ e^- \rightarrow \gamma^*/Z^* \rightarrow t\bar{t}$$



Clean EW proc.; parametrisation of the current at $t\bar{t}X, X = Z, \gamma$ vertex

$$\Gamma_\mu^{t\bar{t}X}(k^2, q, \bar{q}) = -ie \left\{ \begin{array}{lll} \text{Vector} & \text{Axial} & \text{Tensorial} \\ \gamma_\mu (F_{1V}^X(k^2) + \gamma_5 F_{1A}^X(k^2)) & + \frac{\sigma_{\mu\nu}}{2m_t} (q + \bar{q})^\nu (iF_{2V}^X(k^2) + \gamma_5 \cancel{F}_{2A}^X(k^2)) \end{array} \right\}$$

CPV

q (\bar{q}) - four-vector of the t (tbar) quark $k^2 = (q + \bar{q})^2$

Sensitivity of the V and A couplings to NP

Linear Collider: profit from the initial-state longitudinal polarisation of the incoming e^+, e^- beam

- Determination of the cross-section and the A_{FB} of two configurations:

$$\mathcal{P}_{e^-} = \pm 0.8$$

$$\mathcal{P}_{e^+} = \mp 0.3$$

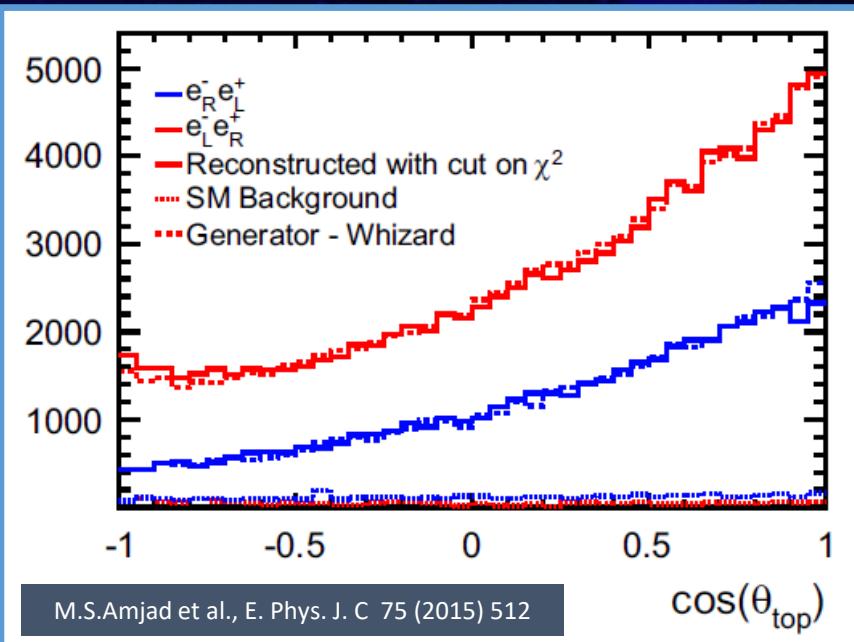
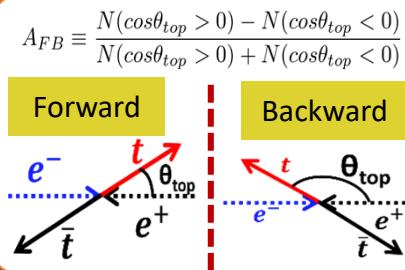
Measure: $\sigma^+, \sigma^-, A_{FB}^+, A_{FB}^-$

+	$= e_R^-$
-	$= e_L^-$

Extract:

$$F_{1V}^Z, F_{2V}^Z, F_A^Z$$

$$F_{1V}^\gamma \cdot F_{2V}^\gamma, F_A^\gamma \equiv 0$$

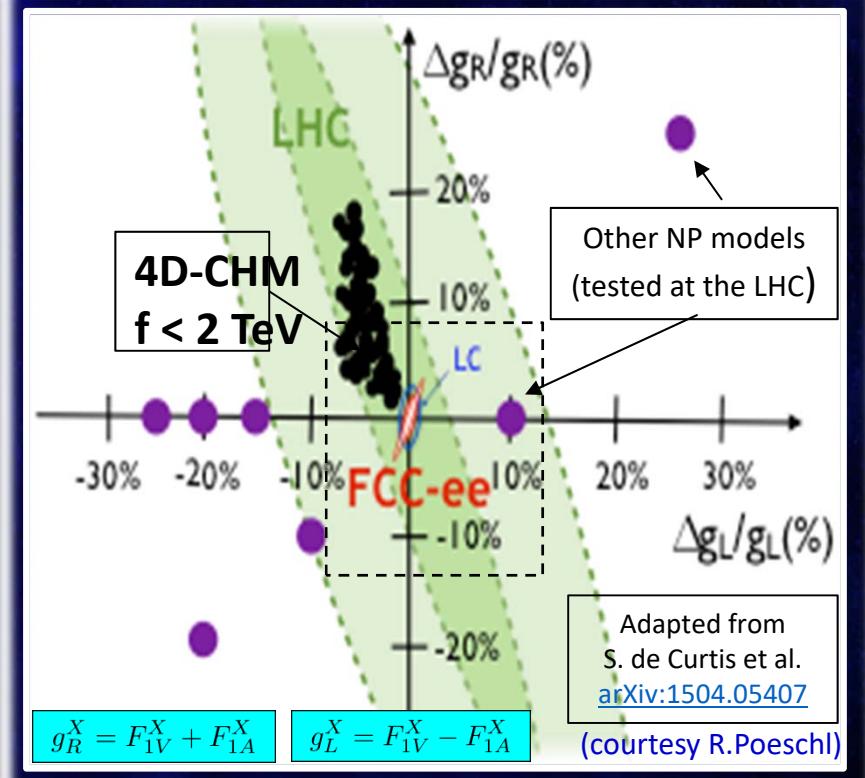
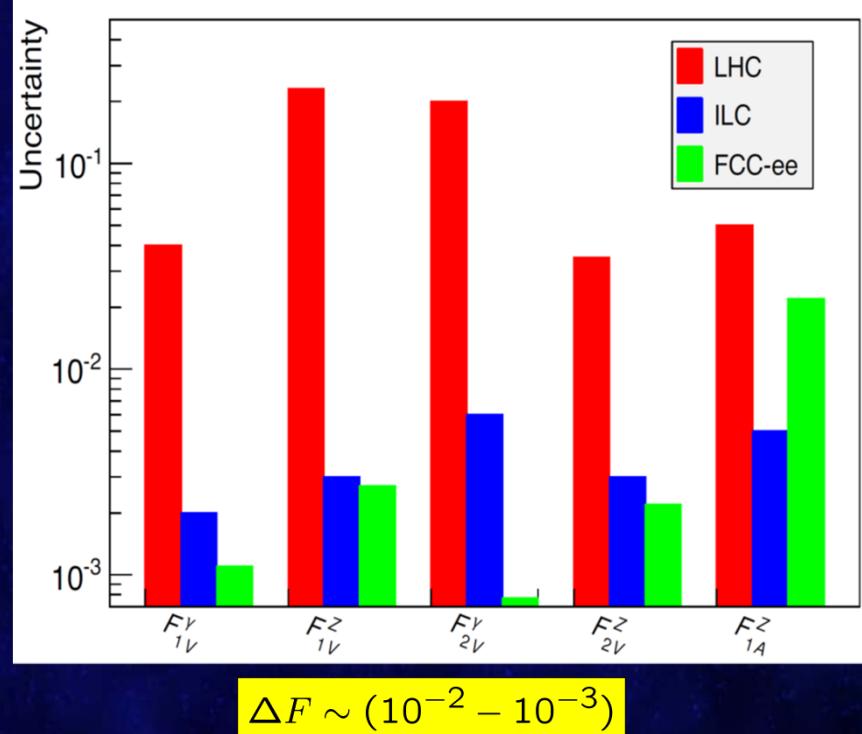


**Circular
Collider:**

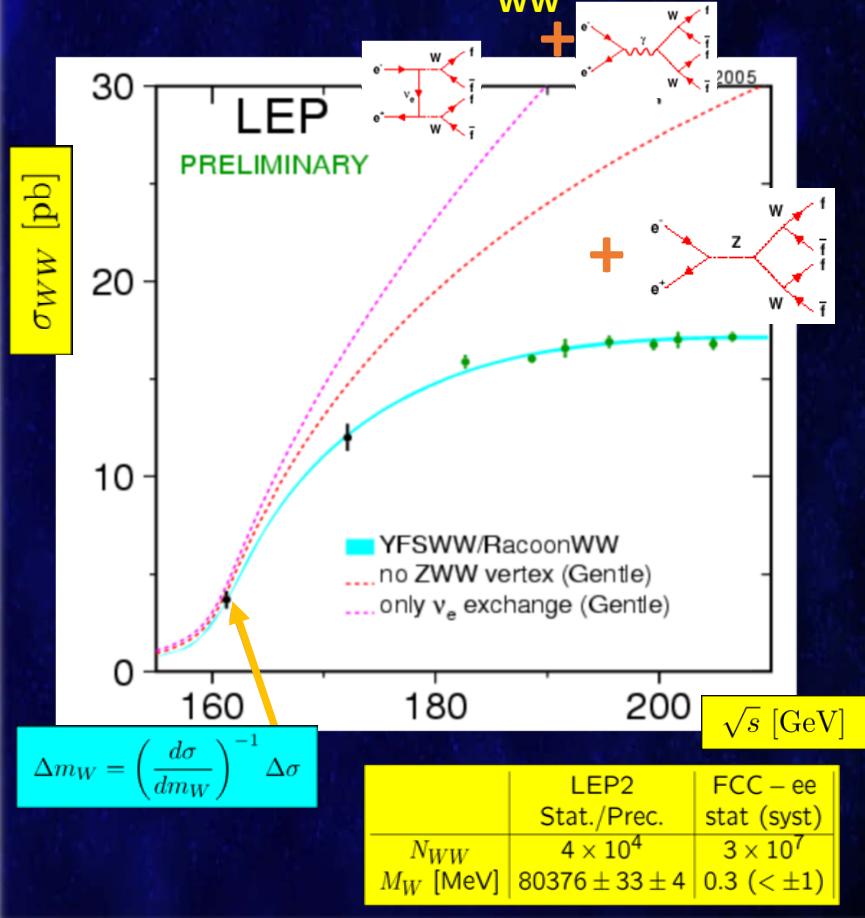
**lack of initial-state polarization → profit from the final-state polarisation,
which is maximally transferred to the top decay products ($t \rightarrow W b$)**

Any anomalous ttZ , $t\bar{t}\gamma$ coupling would lead to a **modification** of the final kinematics,
in particular **of the angular and energy distributions of the leptons from the W decays.**
(analogy to τ polarisation in $Z \rightarrow \tau \tau$ decays at LEP)

P. Janot JHEP 04 (2015) 182



➤ The W mass from σ_{WW} :

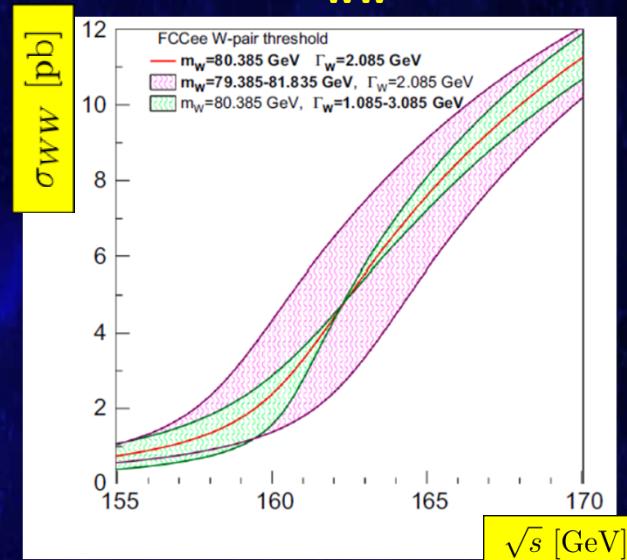


Other W topics:

W branching ratios (universality), TGCs, α_s ...

Eur. Phys. J. C (2019) 79

➤ The W width from σ_{WW} :



- Measure σ_{WW} in two energy points E_1 and E_2 , with the fractions of luminosity f and $(1-f)$
→ evaluation of both m_W and Γ_W
- Choose the parameters E_1 , E_2 , and f in order to minimize the errors: $\Delta\Gamma_W$ and Δm_W :

$$E_1 = 157.5 \text{ GeV} \quad E_1 = 162.5 \text{ GeV} \quad f = 0.4 \quad 12 \text{ ab}^{-1}$$

$$\Delta m_W = 0.5 \text{ MeV} \quad \Delta\Gamma_W = 1.2 \text{ MeV}$$

➤ **WW samples (FCC-ee)**

\sqrt{s} [GeV]	161	240	350
$N_{WW} [\times 10^6]$	30	80	15

➤ **W Branching ratios (%)**

LEP2

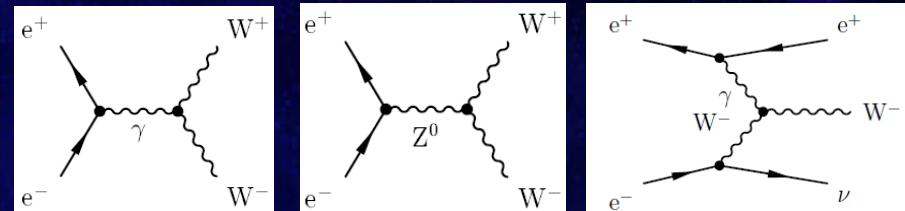
$BR(W \rightarrow e\nu)$	10.65 ± 0.17
$BR(W \rightarrow \mu\nu)$	10.59 ± 0.15
$BR(W \rightarrow \tau\nu)$	11.44 ± 0.22
$BR(W \rightarrow l\nu)$	10.84 ± 0.09
$BR(W \rightarrow \text{hadrons})$	67.48 ± 0.28

- Lepton universality tested at **2%** level (2.7 σ discrepancy between τ and μ/e)
- Quark-lepton universality tested at **0.6%**

FCC-ee

- Lepton universality test at **0.04%** level
- Quark-lepton universality test at **0.01%**
- Flavour tagging $\rightarrow V_{cs} V_{cb} \dots$

➤ **Triple Gauge Couplings**



- Selected LEP limits (95% C.L.)

Δk_γ	$[-9.9, 6.6] \times 10^{-2}$
λ_γ	$[-5.9, 1.7] \times 10^{-2}$
Δk_Z	$[-7.4, 5.1] \times 10^{-2}$
λ_z	$[-5.9, 1.7] \times 10^{-2}$
Δg_1^Z	$[-5.4, 2.1] \times 10^{-2}$

- FCC-ee: overall improvements by a factor of **50** to compare with LEP

➤ **The strong coupling constant:**

- FCC-ee: $\Delta_{\text{rel}}\alpha_S(m_W^2) = 3 \times 10^{-3}$ from hadronic W decays (Γ_W and $BR_{W,\text{had}}$)
- LEP2 precision: 37%

LEP
 $N_Z = 1.7 \times 10^7$

FCC-ee
 $N_Z \sim 5 \times 10^{12}$

**Extreme precision
of EW observables**

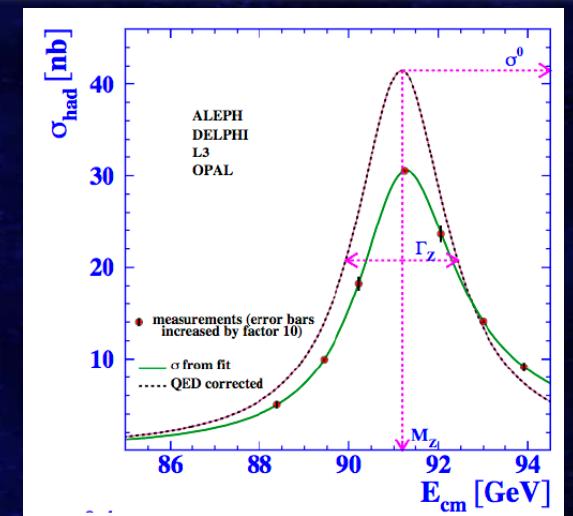
➤ **Z mass and width (from Z pole scan):**

The crucial factor: continuous E_{CM} calibration (resonant depolarization)

$$\Delta E_{CM} \approx (10 \text{ (stat)} + 100 \text{ (syst)}) \text{ keV}$$

	Δ_{rel} (LEP)	Improvement factor
Z mass	1×10^{-6}	~ 20
Z width	5×10^{-5}	~ 20

(~ 300 (stat) \oplus ~ 10 (syst))


 $2.1 \text{ MeV} \rightarrow 100 \text{ keV}$
 $2.3 \text{ MeV} \rightarrow 100 \text{ keV}$
Eur. Phys. J. C (2019) 79


➤ **Normalized partial widths:**

$$R_l = \frac{\Gamma_{had}}{\Gamma_{l\bar{l}}}, \quad l = e, \mu, \tau \quad \Gamma_{f\bar{f}} \propto (g_V^f)^2 + (g_A^f)^2$$

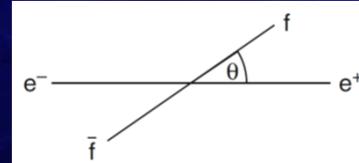
$$R_q = \frac{\Gamma_{q\bar{q}}}{\Gamma_{had}}, \quad q = b, c \quad f = l, q$$

	PDG (LEP) value	PDG (LEP) rel. precision	FCC – ee Improvement factor
R_e	20.804 ± 0.050	2.4×10^{-3}	~ 20
R_μ	20.785 ± 0.033	1.6×10^{-3}	~ 20
R_τ	20.764 ± 0.045	2.2×10^{-3}	~ 20
R_b	0.21629 ± 0.00066	3.1×10^{-3}	~ 10
R_c	0.1721 ± 0.0030	1.7×10^{-2}	~ 10

necessary input for a precise measurement of EW couplings (next slide)

and $\alpha_S(m_Z^2)$ (from hadronic Z decays). FCC-ee precision: $\Delta_{rel}\alpha_S(m_Z^2) = 2 \times 10^{-3}$ LEP: 2.5%

Z asymmetries:



$$\frac{d\sigma_{f\bar{f}}}{d\cos\theta} = \frac{3}{8}\sigma_{f\bar{f}}^{\text{tot}} [(1 - \mathcal{P}_e\mathcal{A}_e)(1 + \cos^2\theta) + 2(\mathcal{A}_e - \mathcal{P}_e)\mathcal{A}_f \cos\theta]$$

\mathcal{P}_e - polarization
of the initial state e^-

The forward-backward asymmetry:

$$A_{FB}^f = \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4}\mathcal{A}_e\mathcal{A}_f$$

The left-right asymmetry:

$$A_{LR}^f = \frac{\sigma_L - \sigma_R}{\sigma_L + \sigma_R} = \mathcal{A}_e$$

$$\mathcal{A}_f = \frac{2g_V^f g_A^f}{(g_V^f)^2 + (g_A^f)^2}$$

LEP & SLC: longstanding discrepancies between different asymmetry measurements; uncertainties dominated by statistics

tau lepton case:

the final state helicity can be measured

$$\mathcal{P}_\tau(\cos\theta) = \frac{\mathcal{A}_\tau(1 + \cos^2\theta) + 2\mathcal{A}_e \cos\theta}{(1 + \cos^2\theta) + \mathcal{A}_e\mathcal{A}_\tau \cos\theta}$$

$$\mathcal{P}_\tau(\cos\theta) = \frac{d(\sigma_r - \sigma_l)}{d\cos\theta} \cdot \left(\frac{d(\sigma_r + \sigma_l)}{d\cos\theta} \right)^{-1}$$

$$A_{FB}^\tau = \frac{(\sigma_r - \sigma_l)_F - (\sigma_r - \sigma_l)_B}{(\sigma_r + \sigma_l)_F + (\sigma_r + \sigma_l)_B}$$

Experimentally accessible observables:

$$\langle \mathcal{P}_\tau \rangle = -\mathcal{A}_\tau$$

$$A_{FB}^\tau = -\frac{3}{4}\mathcal{A}_e$$

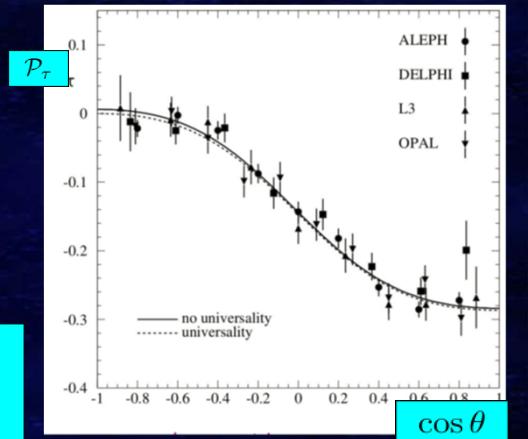
\mathcal{A}_f measured
($f = e, \mu, \tau, b, c$)



$g_V^f g_A^f$ extracted



$$\sin^2\theta_{W,\text{eff}}^f = \frac{1}{4} \left(1 - \frac{g_V^f}{g_A^f} \right)$$



Eur. Phys. J. C (2019) 79

Precision on vector and axial
couplings from R_f and A_f :

Improvement w.r.t. LEP: (10-100)x

	$\Delta_{\text{rel}}^{\text{stat}}$ (FCC - ee)	$\Delta_{\text{rel}}^{\text{syst}}$ (FCC - ee)	Improvement factor w.r.t. LEP
\mathcal{A}_e	5.0×10^{-5}	1.0×10^{-4}	~ 50
\mathcal{A}_μ	2.5×10^{-5}	1.5×10^{-4}	~ 30
\mathcal{A}_τ	4.0×10^{-5}	3.0×10^{-4}	~ 15
\mathcal{A}_b	2.0×10^{-4}	3.0×10^{-3}	~ 5
\mathcal{A}_c	3.0×10^{-4}	8.0×10^{-3}	~ 4

Systematic uncertainties dominate

fermion	Δg_V	Δg_A
e	2.5×10^{-4}	1.5×10^{-4}
μ	2.0×10^{-4}	2.5×10^{-5}
τ	3.5×10^{-4}	0.5×10^{-4}
b	1.0×10^{-2}	1.5×10^{-3}
c	1.0×10^{-2}	2.0×10^{-3}

→ $\sin^2 \theta_{W,\text{eff}}$ (absolute) uncertainties:

	stat	syst	Improvement w.r.t. LEP
from muon FB	10^{-7}	5.0×10^{-6}	~ 100
from tau pol	10^{-7}	6.6×10^{-6}	~ 75

➤ **Measurement of $\alpha_{\text{QED}}(m_Z^2)$ - better precision necessary for future precision SM tests !**

- **Current uncertainty:** $\Delta\alpha_{\text{QED}}(m_Z^2) = 10^{-4}$ from running coupling constant formula:
$$\alpha_{\text{QED}}(m_Z^2) = \frac{\alpha_{\text{QED}}(0)}{1 - \Delta\alpha_l(m_Z^2) - \Delta\alpha_{\text{had}}^{(5)}(m_Z^2)}$$
 dominated by the experimental determination of the hadronic vacuum polarization, obtained from dispersion integral with expt. input from low energies (KLOE, Belle, BaBar, CLEO, BES CMD-2...)

➤ **Alternative: the direct measurement of $\alpha_{\text{QED}}(m_Z^2)$ from the muon FB asymmetry just below and just above the Z pole (as part of Z resonance scan) – no need of extrapolation from $\alpha_{\text{QED}}(0)$**

- **The $A_{FB}^{\mu\mu}$ - self normalized quantity**
$$A_{FB}^{\mu\mu} = \frac{\sigma_{\mu\mu}^F - \sigma_{\mu\mu}^B}{\sigma_{\mu\mu}^F + \sigma_{\mu\mu}^B}$$
 (no need for measurement of L_{int} ;
most uncertainties (sel. efficiency, det. acceptance) cancel in the ratio

$$\frac{\Delta\alpha_{\text{QED}}}{\alpha_{\text{QED}}} \simeq \frac{\Delta A_{FB}^{\mu\mu}}{A_{FB}^{\mu\mu}} \times \frac{\mathcal{Z} + \mathcal{G}}{\mathcal{Z} - \mathcal{G}}$$

$\mathcal{Z}(\mathcal{G})$ - Z(photon)-exchange terms

Optimal CMS energies:

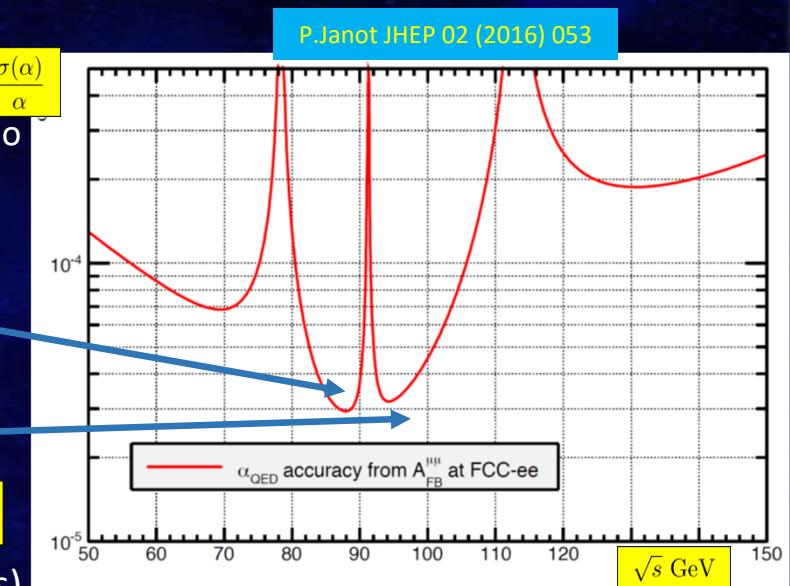
2x 6 months of FCC-ee running:

$$\sqrt{s_-} = 87.9 \text{ GeV}$$

$$\sqrt{s_+} = 94.3 \text{ GeV}$$

$$\frac{1}{\alpha_{\text{QED}}(m_Z^2)} = \frac{1}{\alpha_\pm} + \beta_{\text{QED}} \log \frac{s_\pm}{m_Z^2} \rightarrow \Delta\alpha_{\text{QED}}(m_Z^2) = 3 \times 10^{-5}$$

(adequate for future precision EW fits)



The Z Invisible Width – Number of Light Neutrino Species



1) N_ν determined at LEP1 from the Z line-shape scan:

$$N_\nu = 2.991 \pm 0.007$$

$$N_\nu \cdot \Gamma_\nu = \Gamma_Z - \Gamma_h - 3\Gamma_l$$

$$N_\nu = \left(\frac{\Gamma_l}{\Gamma_\nu} \right)_{\text{SM}} \cdot \left(\sqrt{\frac{12\pi R_l}{M_Z^2 \sigma_{\text{had}}^{\text{peak},0}}} - R_l - 3 \right)$$

theory

all measured at the peak

Only small room for improvements:

precision limited mainly by the theoretical uncertainty on luminosity determination

i.e. on small angle Bhabha cross section

(LEP1: $\Delta L/L = 0.00061$, $\Delta N_\nu^{\text{lumi}} = 0.0046 \rightarrow \Delta N_\nu^{\text{lumi}} = 0.0001$ @FCC-ee). $\Delta N_\nu^{\text{FCC-ee}} = 0.00008(\text{stat}) \pm 0.0001(\text{syst})$

Eur. Phys. J. C (2019) 79

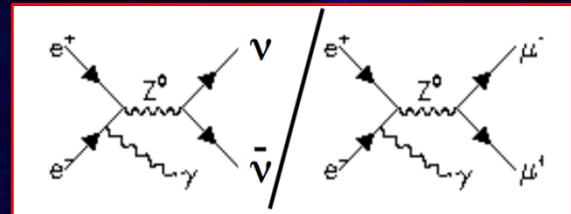
2) N_ν from the radiative return process

$$e^+ e^- \rightarrow Z\gamma, \quad Z \rightarrow \nu\bar{\nu}$$

from the higher masses than the Z resonance

Monophoton events (normalized to photon-lepton-lepton events):

$$N_\nu = \left[\frac{(e^+ e^- \rightarrow \gamma Z_{\text{inv}})^{\text{meas}}}{(e^+ e^- \rightarrow \gamma Z_{\text{lept}})} \right] \left(\frac{\Gamma_{\nu\bar{\nu}}}{\Gamma_{\text{lept}}} \right)^{\text{SM}}$$



- LEP1: $N_\nu = 2.92 \pm 0.05$ (statistics too scarce).
- Photon selection common for both final states \rightarrow cancellations of systematics.
- N_ν can be measured vs $\text{sqrt}(s)$ \rightarrow sensitivity to NP at high energy scales.
- FCC-ee sensitivity:

\sqrt{s} [GeV]	years of running	ΔN_ν (stat)
161	1	0.0011
240 & 340	5	0.0008
125	1	0.0004

$3 \times 10^7 \gamma Z(\text{inv})$ ev.
(running parasitically)
 $\Delta N_\nu \leq 4 \times 10^{-4}$



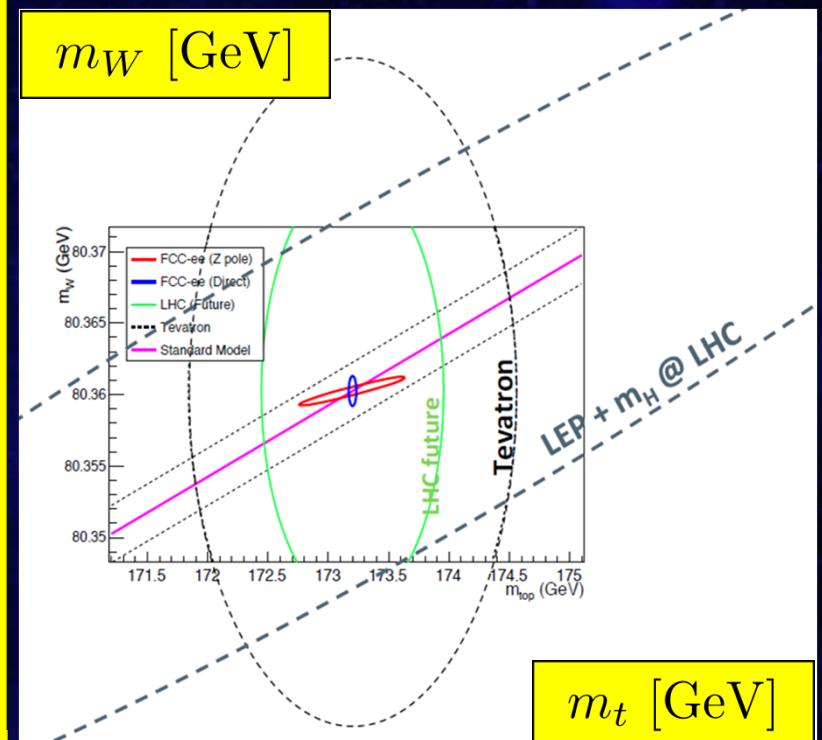
FUTURE
CIRCULAR
COLLIDER

Electroweak Observables: Instead of Summary



Eur. Phys. J. Plus (2022) 137

Observable	unit	Present value	\pm error	FCC-ee (stat.)	(syst.)
m_Z	[keV/c 2]	91 186 700	2 200	4	100
Γ_Z	[keV]	2 495 200	2 300	4	25
$\sin^2 \theta_W^{\text{eff}}$	[$\times 10^6$]	231 480	160	2	2.4
$1/\alpha_{\text{QED}}(m_Z^2)$	[$\times 10^3$]	128 952	14	3	small
R_t^Z	[$\times 10^3$]	20 767	25	0.06	0.2-1
$\alpha_S(m_Z^2)$	[$\times 10^4$]	1 196	30	0.1	0.4-1.6
σ_{had}^0	[$\times 10^3$ nb]	41 541	37	0.1	4
N_ν	[$\times 10^3$]	2 996	7	0.005	1
R_b	[$\times 10^6$]	216 290	660	0.3	< 60
$A_{\text{FB}}^{b,0}$	[$\times 10^4$]	992	16	0.02	1-3
$A_{\text{FB}}^{\text{pol},\tau}$	[$\times 10^4$]	1498	49	0.15	< 2
τ lifetime	[fs]	290.3	0.5	0.001	0.04
τ mass	[MeV/c 2]	1776.86	0.12	0.004	0.04
τ leptonic BR	[%]	17.38	0.04	0.0001	0.003
m_W	[MeV/c 2]	80 350	15	0.25	0.3
Γ_W	[MeV]	2 085	42	1.2	0.3



➤ **The sheer power of statistics:**

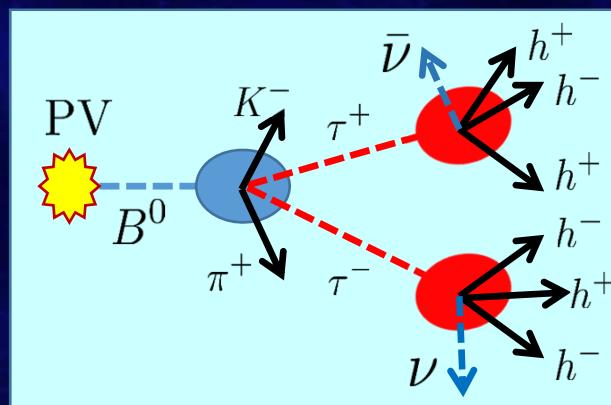
Particles	B^0/B^+	B_s^0	Λ_b	B_c	$Z \rightarrow \tau^+\tau^-$
Yields (FCC-ee 150 ab^{-1})	10^{12}	$2.5 \cdot 10^{11}$	$2.5 \cdot 10^{11}$	$2.5 \cdot 10^9$	$5 \cdot 10^{11}$
Yields (Belle II 50 ab^{-1})	10^{11}	10^{7-8}	—	—	$5 \cdot 10^{10}$

LEP : $\sim 6 \times 10^6$

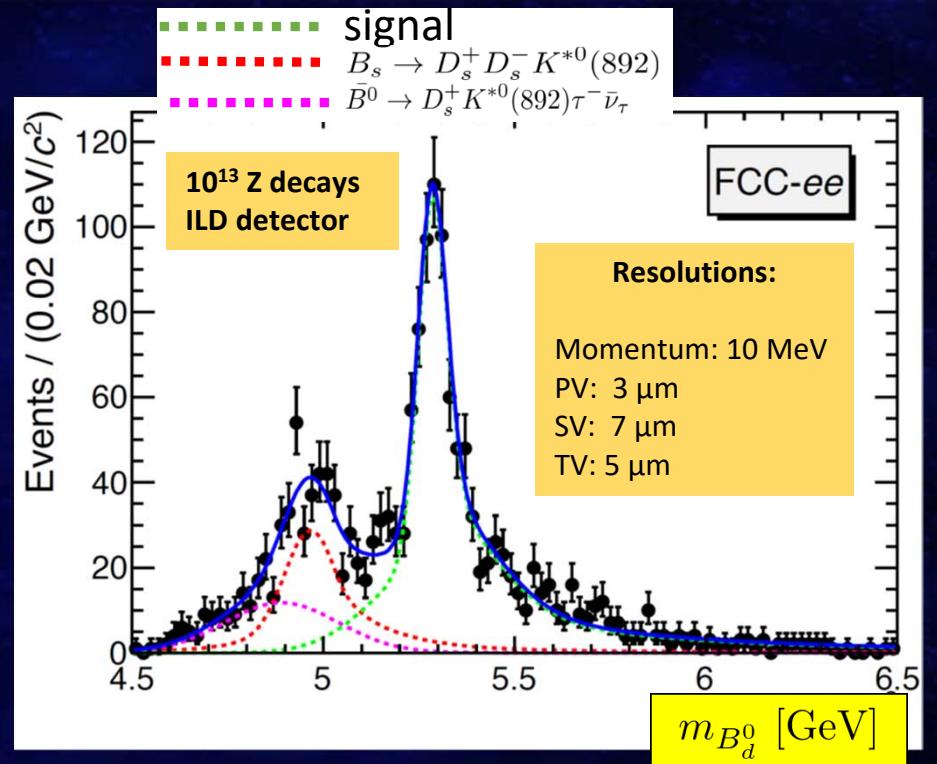
S.Monteil, 2nd FCC Physics Workshop

➤ **Example: $B \rightarrow K^*(892)\tau^+\tau^-$ decay**

- Excellent vtx reconstruction ($\tau \rightarrow 3$ prongs)



- FCC-ee: 1000 signal events expected, Belle2: 10 events expected
- The angular analysis feasible



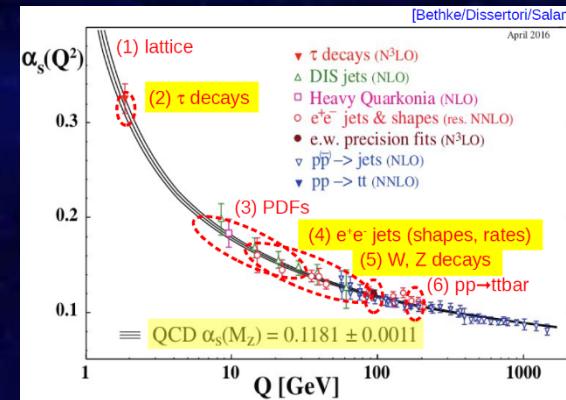
Other flavour topics: CKM parameters, UT angles, tau physics, lepton universality, heavy quark spectroscopy, rare decays...

QCD Measurements



➤ **High precision α_s determination**
 (with the accuracy at the ‰ level) from:

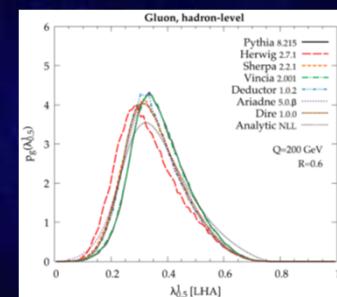
- hadronic τ decays
- Jet rates, event shapes
- hadronic Z decays
- hadronic W decays



Eur. Phys. J. Plus
 (2022) 137:92

➤ **High precision studies of perturbative parton radiation including:**

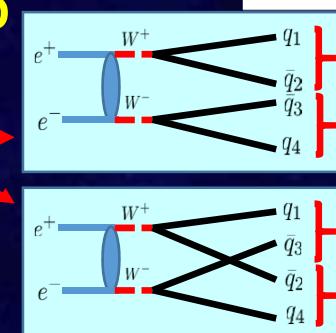
- jet rates and event shapes
- jet substructure
- quark/gluon/heavy-quark discrimination
- g,q,b,c parton-to-hadron fragmentation functions



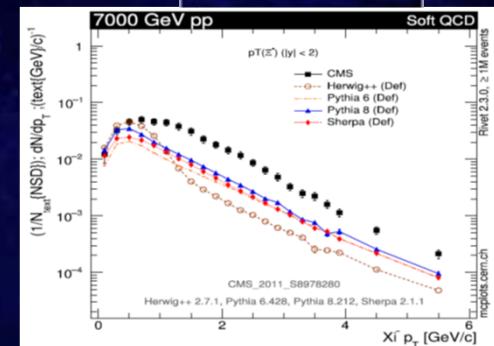
Gluon radiation
& fragmentation
poorly known

➤ **High precision non-perturbative QCD studies including:**

- colour reconnection (<1% control)
- final-state multiparticle correlations



Ξ^- spectrum

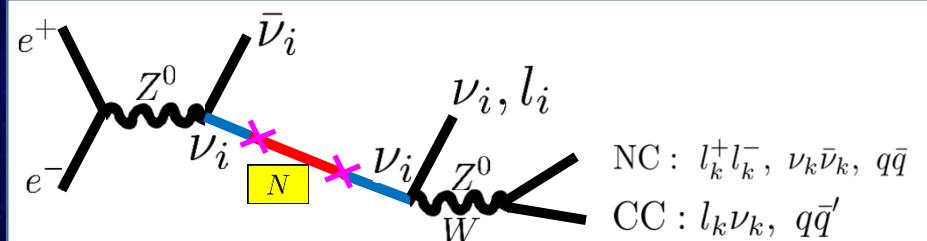


➤ **High precision hadronization studies**

- very rare hadron production and decays

- Sterile, right-handed neutrinos (N) are common in extensions of the SM; they couple to Higgs and SM ν
- Substantial part of them are HNLs: very massive and characterised by macroscopic decay length

- The HNL production and decay at the $\sqrt{s} = M_Z$



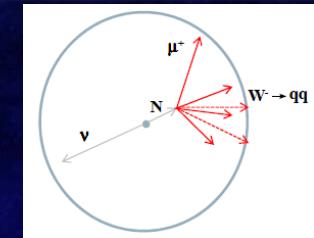
$$\nu_L = \nu \cos \theta + N \sin \theta$$

$$\theta \approx m_\nu / m_N$$

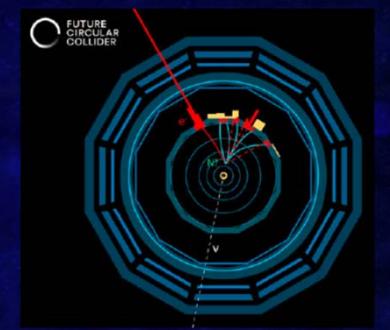
- Experimental signatures

NC: 2 leptons/jets + E_{miss}

CC: 2 jets + lepton/ E_{miss}

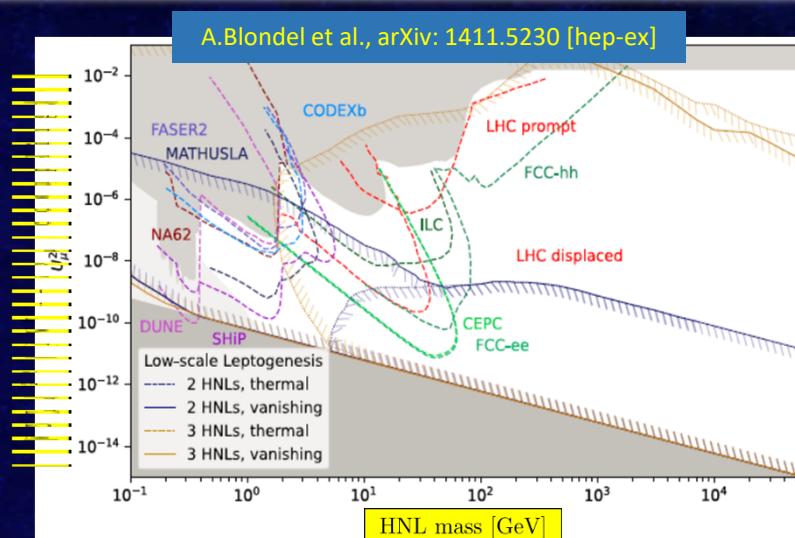


Search for (highly) displaced vertices;
 very clean events



- FCC-ee sensitivity to HNLs up to 10^{-11}

- Complementary to beam dump facilities
- The upper limits of LEP searches: 10^{-4}



Other topics:
 axion-like particles, exotic
 Higgs decays,...

Sensitivity to NP



➤ New Physics → new interactions of SM particles:

$$\mathcal{L}_{\text{rmEFT}} = \mathcal{L}_{\text{SM}} + \sum_i \frac{C_i^{(6)} O_i^{(6)}}{\Lambda^2} + o(\Lambda^{-4})$$

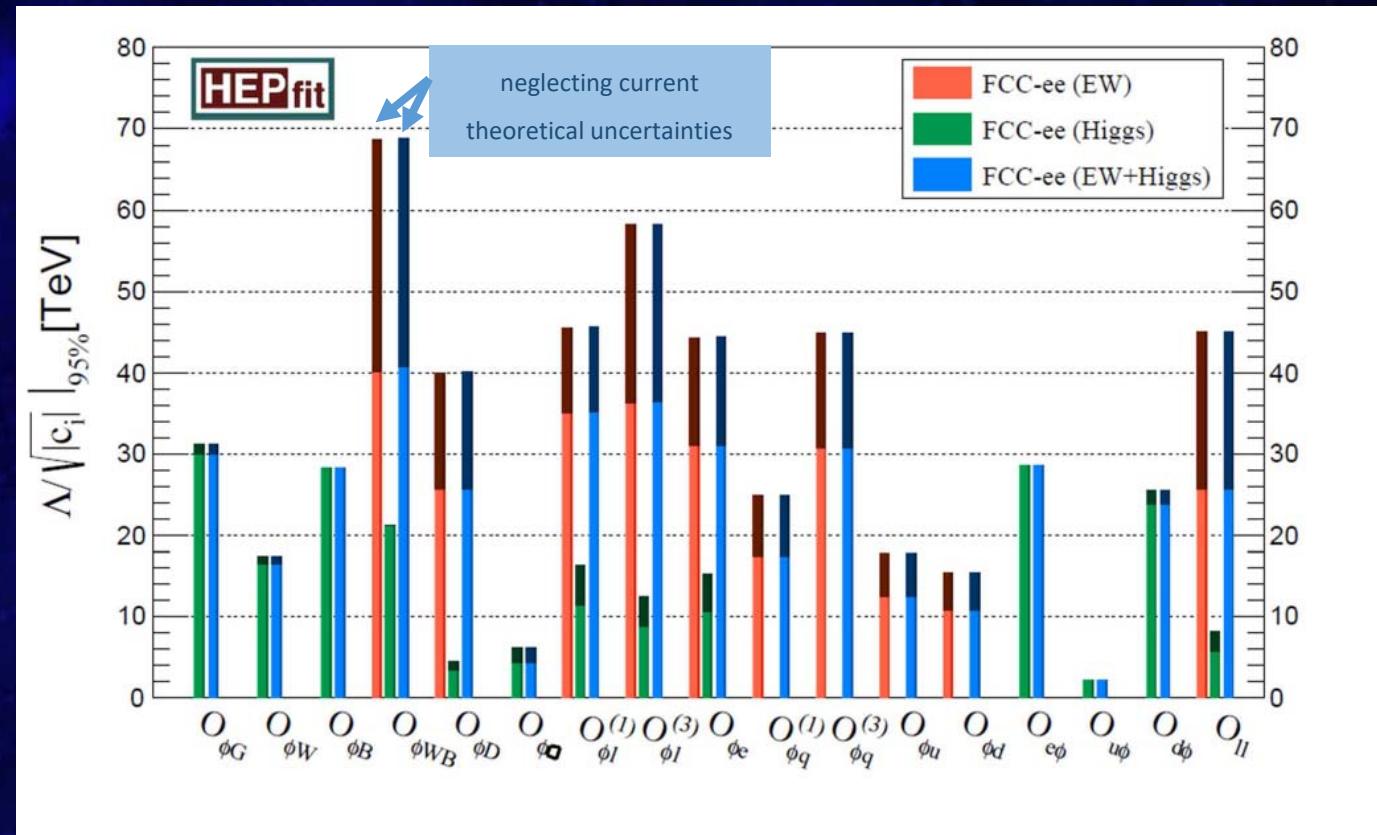
Λ - mass scale
 $C_i^{(6)}$ - dimensionless coefficients
 $O_i^{(6)}$ - operators of dimension d

95% probability
bounds on the
interaction scale
 $\Lambda/(c_i)^{1/2}$

Nucl. Phys. B268 (1986) 621

arXiv 1008.4884

Eur Phys. J. C. (2019) 79, 474



Sensitivity exceeding 50 TeV for several EFTs

Motivation for FCC-hh



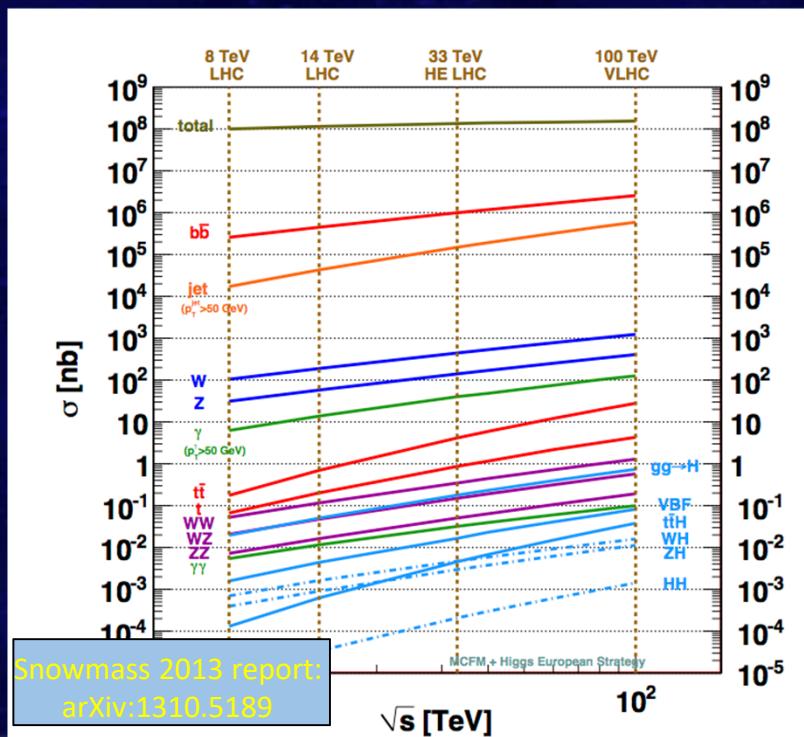
➤ **Opportunities of ~100 TeV pp collider:**

- Exploration of scenarios that could emerge from a FCC-ee
- The next qualitative leap in precision of crucial measurements, providing hope to answer nagging questions (shortages of SM, BSM...)

Eur. Phys. J. Special Topics (2019) 228; 755

➤ **Big gain (x10) in production cross sections of many relevant processes**

- Impressive precision of the SM measurements
- Reach of terra incognita in the energy frontier

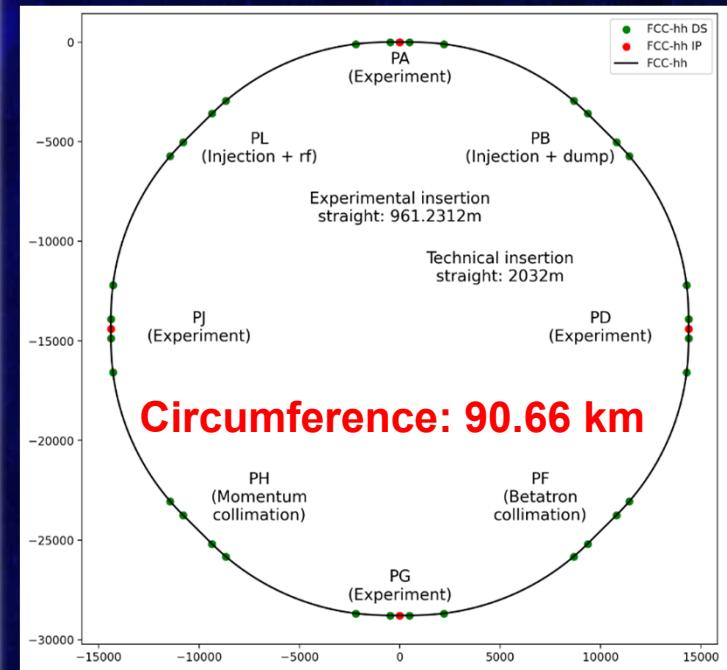


Process	σ (100 TeV) / σ (14 TeV)
Total pp cross-section	1.25
W, Z production	7
WW, ZZ production	10
t <bar>t</bar>	30
H	15
t <bar>t>H</bar>	60
HH	40
stop-stop production m=1 TeV	10 ³

With 20 ab⁻¹ at $\sqrt{s}=100$ TeV expect:

$\sim 10^{13}$ W	$\sim 10^9$ ttH
$\sim 10^{12}$ Z	$\sim 10^7$ HH
$\sim 10^{11}$ tt	$\sim 10^5$ gluino pairs m=8 TeV
$\sim 10^{10}$ H	

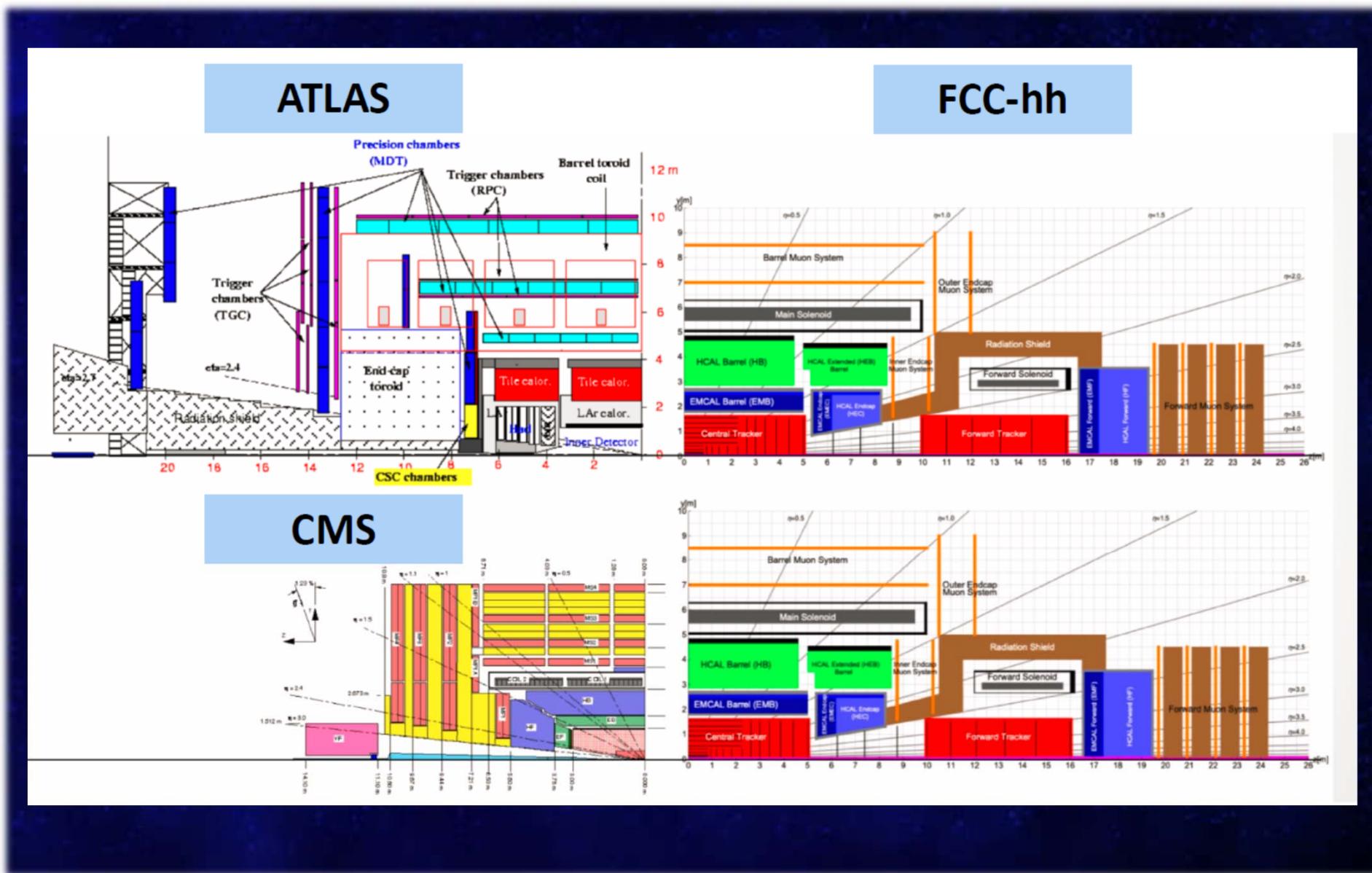
Parameter	FCC-hh	HL-LHC	LHC
collision energy cms [TeV]	80-116	14	14
dipole field [T]	14 (Nb ₃ Sn) – 20 (HTS/Hybrid)	8.33	8.33
circumference [km]	90.7	26.7	26.7
beam current [A]	0.5	1.1	0.58
bunch intensity [10 ¹¹]	1	1	2.2
bunch spacing [ns]	25	25	25
synchr. rad. power / ring [kW]	1020-4250	7.3	3.6
SR power / length [W/m/ap.]	13-54	0.33	0.17
long. emit. damping time [h]	0.77-0.26	12.9	12.9
beta* [m]	1.1	0.3	0.15 (min.)
normalized emittance [μm]	2.2	2.5	3.75
peak luminosity [10 ³⁴ cm ⁻² s ⁻¹]	5	30	5 (lev.)
events/bunch crossing	170	1000	132
stored energy/beam [GJ]	6.1-8.9	0.7	0.36
integrated luminosity [fb ⁻¹]	20000	3000	300



➤ Formidable challenges:

arXiv:2203.07804

- High-field SC magnets: (14 – 20) T; current setup with 16T dipoles → beam energy 48GeV
 - Power load in arcs from synchrotron radiation: 4 MW → cryogenics, vacuum
 - Stored beam energy: ~ 9 GJ → machine protection
 - Pile-up in the detectors: ~1000 events/crossing
 - Energy consumption: 4 TWh/year
 - ...
- R&D on cryogenics, HTS, beam current...

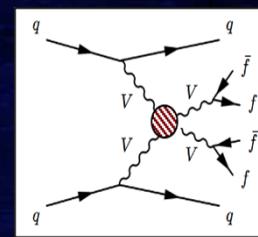


➤ Direct discovery potential up to ~ 40 TeV

➤ Conclusive elucidation of EWSB by probing SM in regime where EW symmetry is restored ($\sqrt{s} \gg v = 246$ GeV)

Without H: $V_L V_L$ scattering violates unitarity at $m_{VV} \sim$ TeV

- H regularizes the theory fully → a crucial “closure test” of the SM
- Else: new physics: anomalous quartic couplings ($VV\bar{V}\bar{V}$, $VVhh$) and/or new heavy resonances
- FCC-hh: direct discovery potential of new resonances in the $o(10)$ TeV range

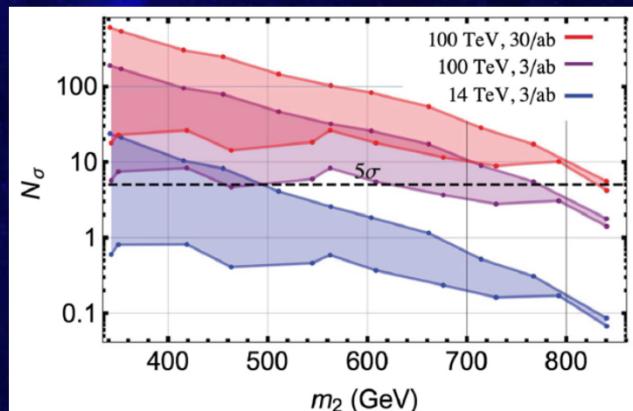


Eur. Phys. J. Special Topics (2019) 228; 755

Eur. Phys. J. C (2019) 79

➤ Determination of nature of EW phase transition

(is it 1st order transition, faster than in SM, as required for EW baryogenesis? → modification to Higgs potential)



Additional Higgs singlet with mass m_2 decaying into HH

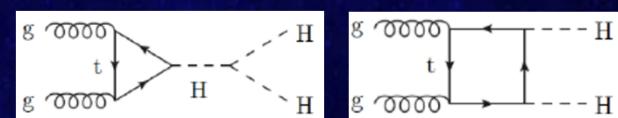
Constraints also from self-coupling (5% precision of FCC-hh, 50% @HL-LHC), and from HZZ at FCC-ee.

➤ Higgs Self Coupling (HSC λ_{3H})

$$V(h) = \frac{m_H^2}{2} h^2 + \lambda_{3H} \nu h^3 + \lambda_{4H} \nu h^4$$

$$\nu = 246 \text{ GeV}$$

- Issues of EWPT and HSC are tightly connected – their answer depends on the parameters of $V(h)$
- Di-Higgs production (destructive interference of the box and triangle diagrams):



$$\sigma_{HH}^{\text{LHC}} \approx 37 \text{ fb}$$

$$\sigma_{HH}^{\text{FCC}-\text{hh}} \approx 50 \times \sigma_{HH}^{\text{LHC}}$$

- Main decay channels: $b\bar{b}\gamma\gamma$, $b\bar{b}\tau\tau$, $b\bar{b}b\bar{b}$
- Expected precision:

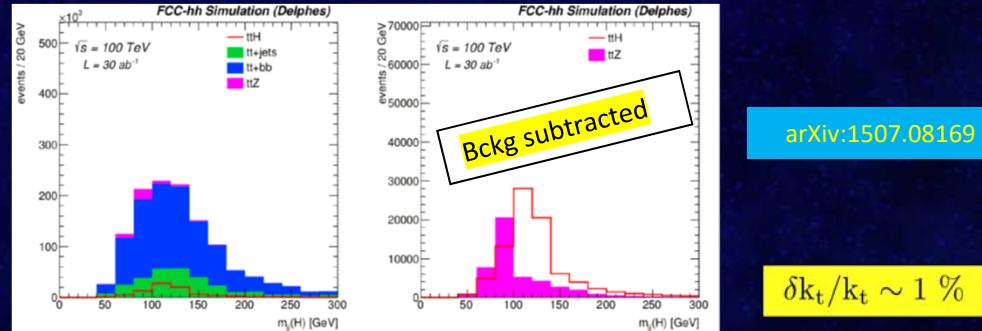
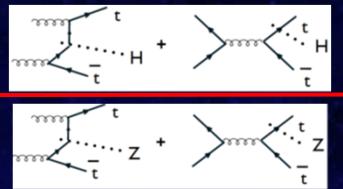
$$\delta\lambda_{3H}/\lambda_{3H} \sim 5 \%$$

arXiv:2203.08042

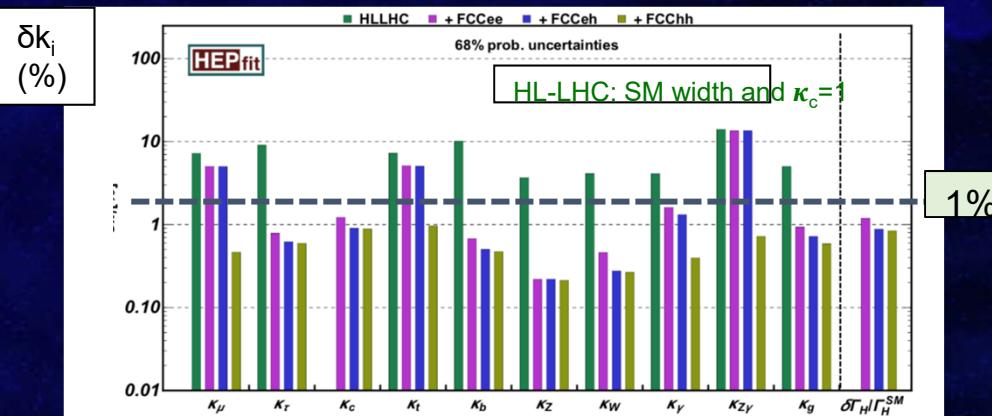


➤ Top - Higgs Yukawa Coupling (k_t)

- Measurement of $\sigma_{\text{ttH}}/\sigma_{\text{ttZ}}$
 - identical production dynamics
 - substantial reduction of theoretical uncertainties)

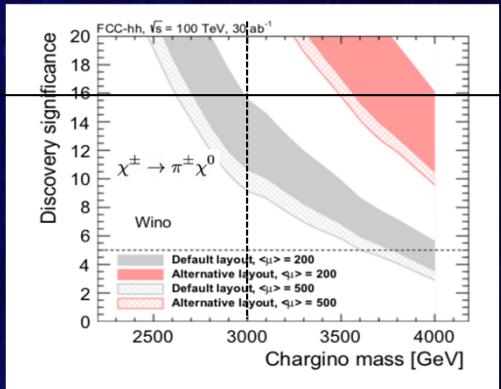


➤ Precise measurement of SM couplings with precision $\sim 1\%$



➤ Final word about thermal WIMP dark matter (DM)

- Thermal WIMP dark cannot be too heavy: (1- 3) TeV upper mass limit from observed relic abundance
- The conclusive affirmation/rejection of WIMPs by accelerator expts is of paramount importance
- LHC: can exclude only a fraction of the range (1-3) TeV
- FCC-hh is necessary and just sufficient with this respect



Eur. Phys. J. Special Topics (2019) 228; 755

- ✓ The FCC project offers a complete, coherent and exciting option for the particle physics for the next decades – in agreement with ESPP
- ✓ Both electron-positron and proton-proton machines have a complementary physics programme
- ✓ The exploitation of two (or more) subsequent colliders in the same tunnel maximizes the outcome
- ✓ The project is progressing well and gaining momentum