Towards a unitary Dalitz plot analysis of three-body hadronic B decays

In collaboration with :

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Recent publication:

CP violation and kaon-pion interactions in $B \rightarrow K\pi\pi$ decays, Phys.Rev. D 79 (2009) 094005, arXiv:0902.3645[hep-ph]



Motivation

- 1. search for CP violation,
- 2. studies of weak and strong interaction amplitudes,
- 3. tests of standard model and search for ``new physics'' effects,
- 4. determination of short and long-distance mechanisms in B-decays,
- 5. studies of Dalitz diagrams,
- 6. analysis of final state coupled channels.

Why unitarity is important?

Unitary model allows for:

- 1. a proper construction of B-decay amplitudes,
- 2. partial wave analyses of final states,
- 3. explanation of structures seen on Dalitz plots,
- adequate determination of branching fractions and asymmetries for different quasi-two body decay reactions,
- 5. extraction of standard model parameters or estimation of amplitudes of a "new physics",
- 6. application of B-decay results in hadron spectroscopy.

Theoretical constraints

- 1. Derivation of unitary three-body strong interaction amplitudes is difficult. It is easier to satisfy unitarity in quasi two-body subchannels of the decay process.
- 2. Cases discussed in this talk: $B \rightarrow (K\pi)\pi$ decays with <u>unitary K\pi strong interaction amplitudes</u> in the limited K\pi effective mass less than about 1.8 GeV.
- 3. Other theoretical tools: analyticity, chiral symmetry at low energies, QCD factorization approach.
- 4. Remark: amplitudes commonly used in the isobar model are not unitary neither in three-body decay channels nor in two-body subchannels.

Problems within the isobar model: determination of branching fractions in presence of wide scalar resonances

Example: $B \rightarrow K_0^*$ (1430) π decay.

1. S-wave resonances are often wide: width of K_0^* (1430) equals to 270 MeV, K_0^* (800) may have even 550 MeV width.

2. Important source of model errors in extraction of the branching ratio for this decay is a possible wrong attribution of a part of Dalitz plot density to a background amplitude and to its interference with other amplitudes, most probably with the S-wave.

Dalitz plot for $B^{\pm} \rightarrow K^{\pm} \pi^{+} \pi^{-}$ decays



Data from BaBar Collaboration: Phys. Rev. D 78 (2008) 012004

S-wave B⁻ \rightarrow K⁻ $\pi^+\pi^-$ decay amplitude

$$A_{S}^{-} = \frac{G_{F}}{\sqrt{2}} (M_{B}^{2} - m_{\pi}^{2}) \frac{m_{K}^{2} - m_{\pi}^{2}}{q^{2}} F_{0}^{B^{-} \to \pi^{-}} (q^{2})$$

$$\times \frac{f_{0}^{K^{-}\pi^{+}}(q^{2})}{\int_{0}^{K^{-}\pi^{+}}(q^{2})} \{\lambda_{u}(a_{4}^{u}(S) - \frac{a_{10}^{u}(S)}{2} + c_{4}^{u}) + \lambda_{c}(a_{4}^{c}(S) - \frac{a_{10}^{c}(S)}{2} + c_{4}^{c}) - \frac{2q^{2}}{(m_{b} - m_{d})(m_{s} - m_{d})} [\lambda_{u}(a_{6}^{u}(S) - \frac{a_{8}^{u}(S)}{2} + c_{6}^{u}) + \lambda_{c}(a_{6}^{c}(S) - \frac{a_{8}^{c}(S)}{2} + c_{6}^{c})]\}$$

$$\lambda_{u} = V_{ub}V_{us}^{*}, \quad \lambda_{c} = V_{cb}V_{cs}^{*}, \quad V_{ij} - CKM \text{ matrix elements}$$
$$f_{0}^{K^{-}\pi^{+}}(q^{2}) - \text{scalar form factor}, \quad q = m_{K\pi}$$
$$c_{4}^{u}, c_{4}^{c}, c_{6}^{u}, c_{6}^{c} - \text{complex parameters}$$

Scalar and vector form factors

- K₀^{*} (1430) resonance is essential in the scalar form factor;
 K^{*} (892) dominates the vector form factor.
- Form factors are connected to scattering amplitudes in the S- and P-waves via unitarity and analyticity relations.
- S-wave two coupled channel amplitudes: Kπ and Kη',
 P-wave three coupled channels: Kπ, K*π and Kρ.
- Scattering amplitudes are constrained by experimental data, especially by the LASS results from SLAC.
- Muskhelishvili- Omnès equations are used to calculate form factors (dispersion relations + unitarity).

Scalar kaon-pion form factor



Dependence on the ratio of the kaon to pion decay constants f_K/f_π

Measurable physical quantities:

- 1. Differential effective mass branching fractions,
- 2. Helicity angle distributions,
- 3. Integrated branching fractions,
- 4. Direct CP asymmetries,
- 5. Phase difference between the decay amplitudes (for example : $B^0 \rightarrow K^{*+}(892)\pi^-$ and $\overline{B}^0 \rightarrow K^{*-}(892)\pi^+$).

Some numerical results of fits to P-wave and predictions for S-wave

Branching ratios in units 10⁻⁶

decay	Belle	BaBar	our model
$B^{\scriptscriptstyle +}\! \longrightarrow (K^{\scriptscriptstyle +} \pi^{ -})_{P} \pi^{\scriptscriptstyle +}$	5.35±0.59	5.98±0.75	5.73±0.14
${ m B}^{0}$ $ ightarrow$ (K 0 π^{+}) $_{ m P}$ π^{-}	4.65±0.77	6.47±0.75	5.42±0.16
$B^+{\longrightarrow} (K^+\;\pi^-)_{S}\pi^+$	27.0±2.5	22.5±4.6	16.5±0.8
${ m B}^{0}$ $ ightarrow$ (K 0 π^{+}) _S π^{-}	26.0±3.4	17.3±4.6	15.8±0.7
			prediction

S-wave: 0.64 <m $_{K\pi}$ < 1.76 GeV, P-wave: 0.82 <m $_{K\pi}$ < 0.97 GeV

Effective K π mass distribution



Data from BaBar Collaboration: Phys. Rev. D 78 (2008) 012004

Helicity angle distributions in B[±] \rightarrow K[±] $\pi^+\pi^-$ decays



Data from Belle Colaboration: arXiv: hep-ex/0509001

Proposal for future experimental
parametrizations of the S-wave
amplitude in
$$B \rightarrow (K\pi)\pi$$
 decays

$$A_{S}(m_{K\pi}) = f_{0}^{K\pi}(m_{K\pi})(\frac{c_{0}}{m_{K\pi}^{2}} + c_{1})$$

 C_0 and C_1 are constant complex parameters to be fitted from data.

Scalar form factor is well constrained by unitarity and by data obtained from other experiments than B-decay studies.

Numerical values of the complex scalar form factor can be provided on request.

Summary

- 1. Analysis of the $B \rightarrow K\pi^{+}\pi^{-}$ decays has been performed with inclusion of the kaon-pion strong interactions.
- 2. Final state $K\pi$ interactions have been described using the scalar form factor for the S-wave and the vector $K\pi$ form factor for the P-wave.
- 3. Good agreement with data is obtained if four phenomenological parameters are incorporated into the decay amplitudes obtained from the QCD factorization approach.
- 4. The model describes well $K\pi$ effective mass distributions below 1.8 GeV, angular kaon or pion distributions and CP asymmetries.
- 5. A number of free parameters is smaller than that in the isobar model and in addition a **two-body unitarity is satisfied**.

Phenomenological parameters

$C_4^{\mu} = 0.402 \pm 0.244 + i (-3.641 \pm 0.054)$

- $C_4^c = 0.015 \pm 0.003 + i (0.033 \pm 0.004)$
- $C_6^u = -0.051 \pm 0.153 + i (-0.161 \pm 0.184)$
- $C_6^u = 0.075 \pm 0.009 + i (-0.033 \pm 0.007)$

P-wave $B^- \rightarrow K^- \pi^+ \pi^-$ decay amplitude

$$\begin{split} A_{P}^{-} &= 2\sqrt{2}G_{F}p_{\pi^{-}} \cdot p_{\pi^{+}}F_{1}^{B^{-} \to \pi^{-}}(q^{2})f_{1}^{K^{-}\pi^{+}}(q^{2}) \\ &\{\lambda_{u}(a_{4}^{u}(P) - \frac{a_{10}^{u}(P)}{2} + c_{4}^{u}) + \lambda_{c}(a_{4}^{c}(P) - \frac{a_{10}^{c}(P)}{2} + c_{4}^{c}) \\ &+ 2\frac{m_{K^{*}}}{m_{b}}\frac{f_{V}^{\perp}}{f_{V}}[\lambda_{u}(a_{6}^{u}(P) - \frac{a_{8}^{u}(P)}{2} + c_{6}^{u}) + \lambda_{c}(a_{6}^{c}(P) - \frac{a_{8}^{c}(P)}{2} + c_{6}^{c})]\} \end{split}$$

Vector kaon-pion form factor



Direct CP asymmetries in %

decay	Belle	BaBar	our model
$B^+ \rightarrow (K^+ \pi^-)_P \pi^+$	-14.9±6.8	3.2±5.4	-2.5±1.3
${ m B}^{0}$ $ ightarrow$ (K 0 π^{+}) $_{ m P}$ π^{-}	-	-14±12	-19.6±3.0
$B^{\scriptscriptstyle +}\! \longrightarrow (K^{\scriptscriptstyle +} \pi^{\scriptscriptstyle -})_{\rm S}^{\phantom {\scriptscriptstyle +}} \pi^{\scriptscriptstyle +}$	7.4±4.6	3.2±4.6	5.4±1.0
${ m B}^0 ightarrow$ (K ⁰ π^+) _S π^-	-	17±26	-0.2±1.3