



“QCD tests at NA48/2”

EPS 09

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On behalf of the NA48/2 collaboration:

Cambridge, CERN, Chicago, Dubna, Edimburgh, Ferrara, Florence,
Mainz, Northwestern, Perugia, Pisa, Saclay, Siegen,
Turin, Vienna

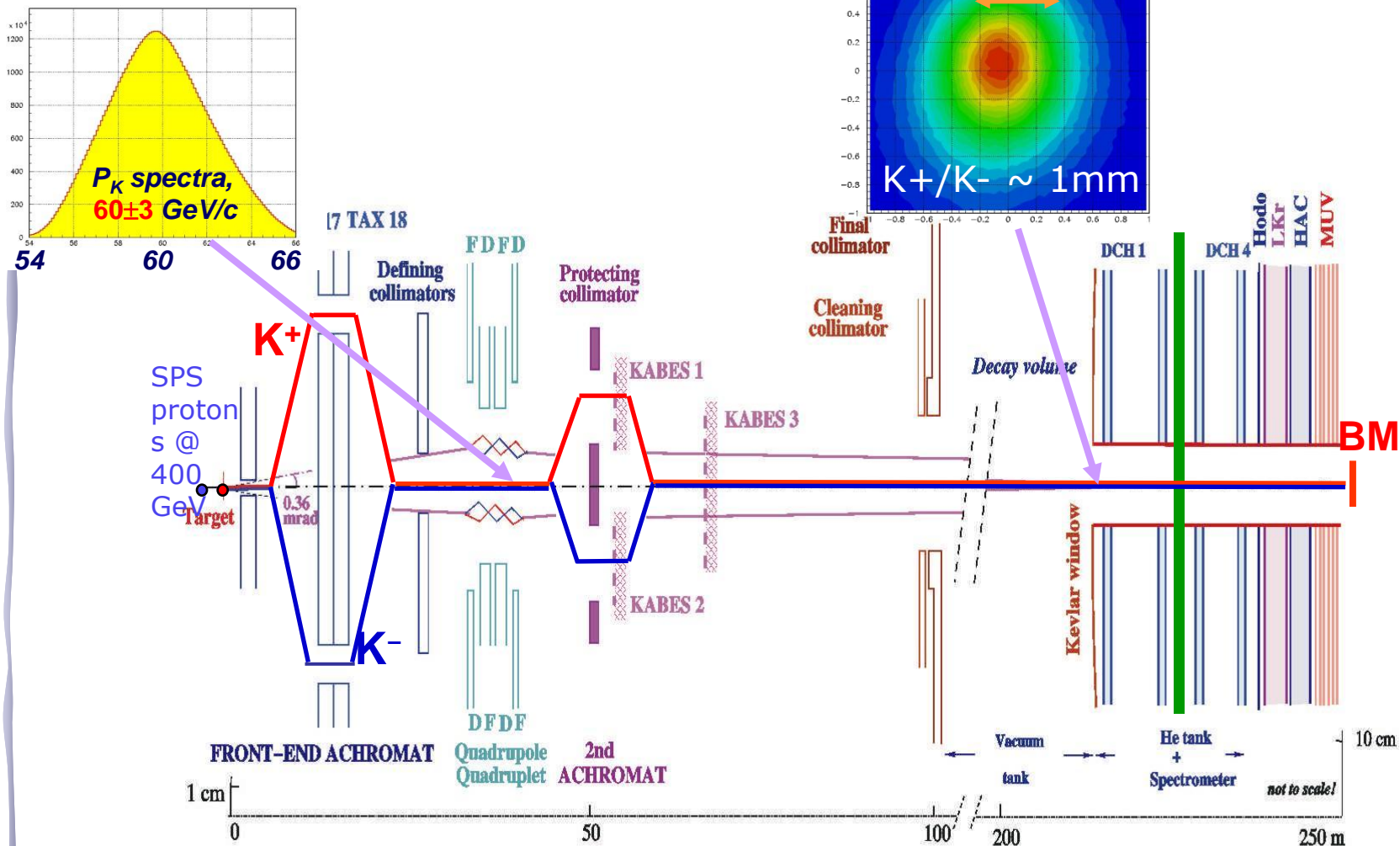
Outline

- NA48/2 experimental setup
- QCD tests
 - $\pi\pi$ scattering lengths (**Ke4 and Cusp**) (preliminary!)
 - $K^\pm \rightarrow \pi^\pm \gamma\gamma$: BR (preliminary!)
 - $K^\pm \rightarrow \pi^\pm \gamma e^+ e^-$: BR and Shape (final!)
- Conclusions



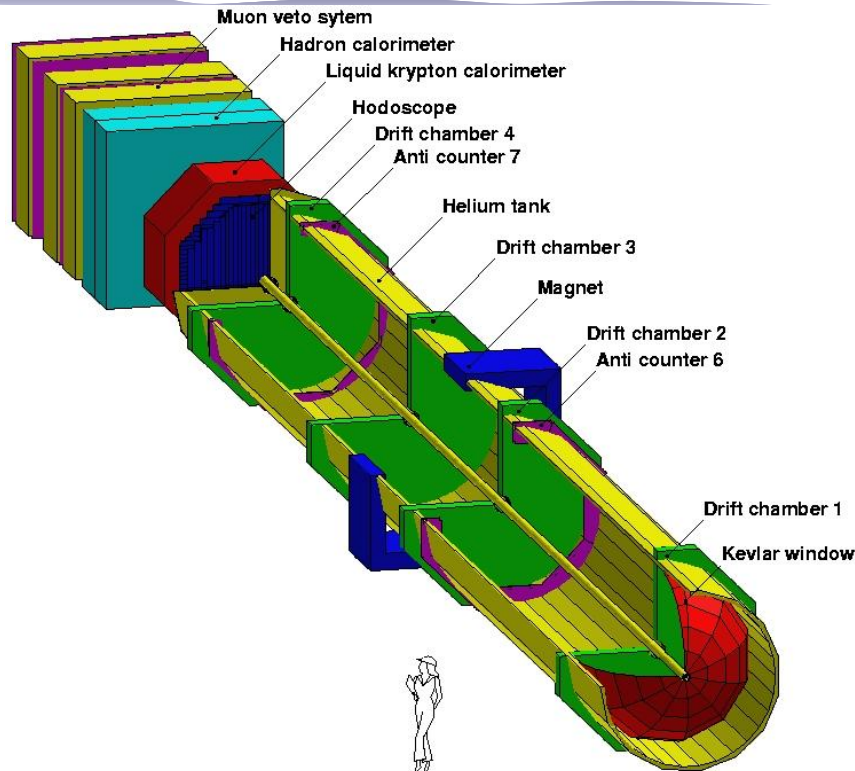
NA48	1997	e^+e^- run	$K_L + K_S$
	1998	e^+e^- run	$K_L + K_S$
	1999	e^+e^- run $K_L + K_S$	K_S Hi. Int.
	2000	K_L only	K_S High Intensity NO Spectrometer
	2001	e^+e^- run $K_L + K_S$	K_S High Int.
NA48/1	2002	K_S High Intensity	
NA48/2	2003	K^\pm High Intensity	
	2004	K^\pm High Intensity	
NA62	>2010	$K \rightarrow \pi \nu \nu$	

Beam Line



- fixed target experiment at CERN-SPS
- 60 ± 3 GeV/c kaon momentum ($\sim 7 \times 10^{11}$ ppp)
- 6.3×10^7 particles per pulse in decay region
- Simultaneous, unseparated, focused beams
- Similar acceptance for K^+ and K^- decays
- $K^+/K^- \sim 1.8$

Detector



- **~100 m** long decay region in vacuum
- Triggers based on LKr peaks, CHOD hits and DCH multiplicity
- Similar acceptance between **K+** and **K-** beams checked reversing magnetics fields
- Pion decay products, from the hadronic beam, remain into the beam pipe

Spectrometer:

$$\sigma_p/p = 1.0\% + 0.044\% p \quad [p \text{ in GeV}/c]$$

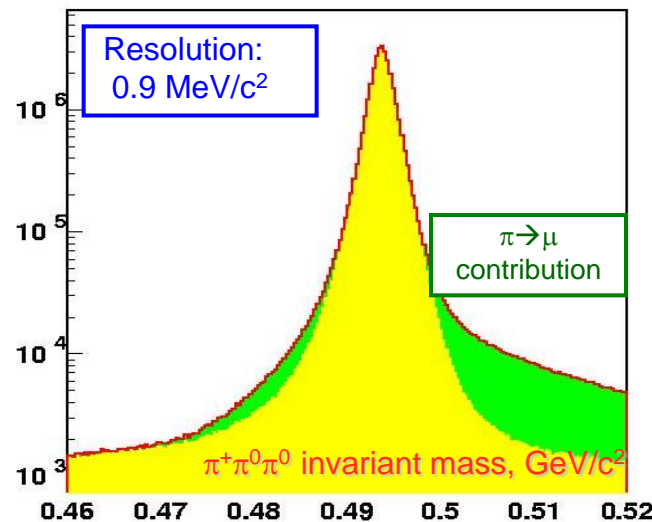
LKR calorimeter:

$$\sigma_E/E = 3.2\%/\sqrt{E} + 9\%/E + 0.42\% \quad [E \text{ in GeV}]$$

CHOD, **HAC**, **MUV**, **vetos**

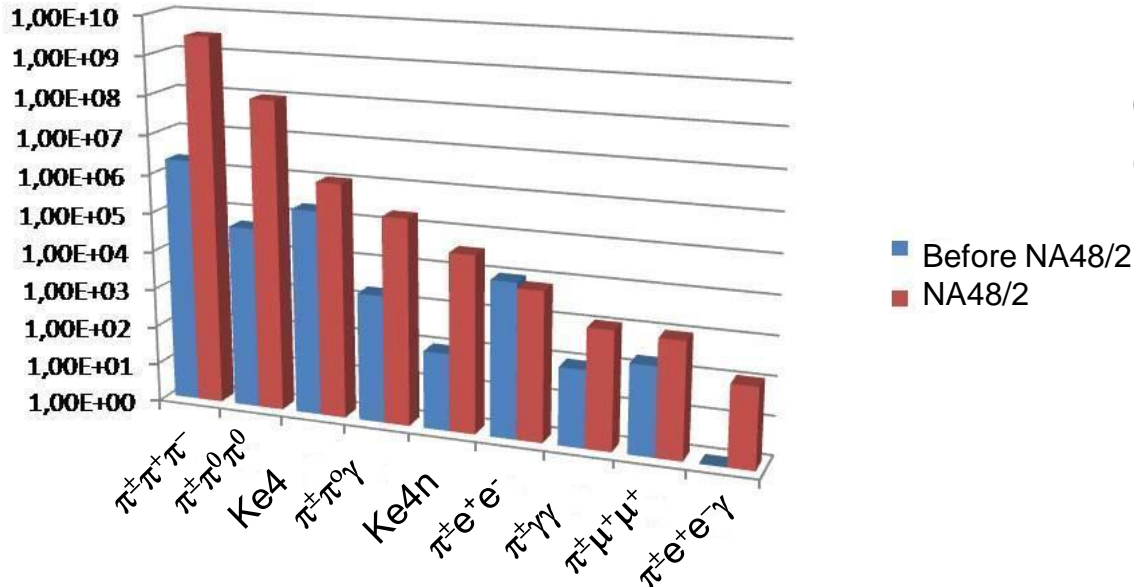
Kabes

Beam Monitor



Data Taking

G.Lamanna – EPS09 Krakow – 16.7.2009



Detector and trigger optimized to collect 3 pions events

$$K^\pm \rightarrow \pi^\pm \pi^0 \pi^0: \sim 1 \cdot 10^8$$

$$K^\pm \rightarrow \pi^\pm \pi^+ \pi^-: \sim 3 \cdot 10^9$$

- Unprecedented statistics in many channels
- Two years of data taking (2003+2004)
- Main purpose was to measure direct CP violation in charged Kaon decays, through asymmetry in Dalitz plot distribution.
- New limits on CP violation in charged kaon decays

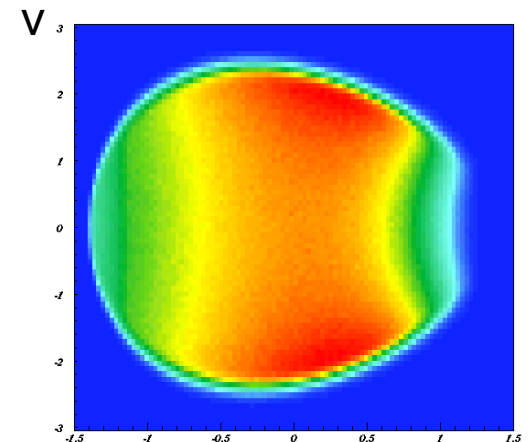
$$A_g = (-1.5 + 1.5_{\text{stat}} + 0.9_{\text{trig}} + 1.1_{\text{syst}}) \cdot 10^{-4}$$

$$A_g^0 = (1.8 + 1.7_{\text{stat}} + 0.5_{\text{syst}}) \cdot 10^{-4}$$

Phys.Lett.B 634:474-482,2006

Phys.Lett.B 638:22-29,2006

Eur.Phys.J C52:875-891,2007



Ke4: Formalism

- The Ke4 ($K^\pm \rightarrow \pi^+ \pi^- e^\pm \nu$) dynamics is fully described by 5 (*Cabibbo-Maksymovicz*) variables: $M_{\pi\pi}^2$, M_{ev}^2 , $\cos\theta_\pi$, $\cos\theta_e$ and ϕ

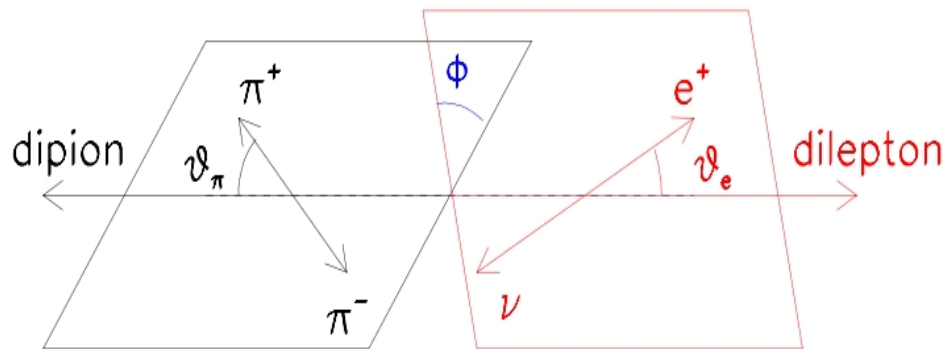
In the partial waves expansion the amplitude can be written using 2 axial and 1 vector form factors (the axial form factor R is suppressed in K_{e4} but accessible in $K_{\mu 4}$):

$$F = F_s e^{i\delta_s} + F_p e^{i\delta_p} \cos\theta_\pi$$

$$G = G_p e^{i\delta_p}$$

$$H = H_p e^{i\delta_p}$$

F (F_p, F_s), G , H and $\delta = \delta_p - \delta_s$ will be used as fit parameters



- The $q^2 = (M_{\pi\pi}^2/4m_\pi^2) - 1$ dependence can be studied expanding the fitted form factors assuming isospin symmetry:

$$F_s = f_s + f_s' q^2 + f_s'' q^4 + f_e'(M_{ev}^2/4m_\pi^2) + \dots$$

$$F_p = f_p + f_p' q^2 + \dots$$

$$G_p = g_p + g_p' q^2 + \dots$$

$$H_p = h_p + h_p' q^2 + \dots$$

Ke4: Selection

Signal selection:

- 3 tracks on spectrometer, total charge ± 1
- Missing energy and missing Pt, compatible with ν
- LKr/DCH used for electron PID
- 2 opposite sign pions

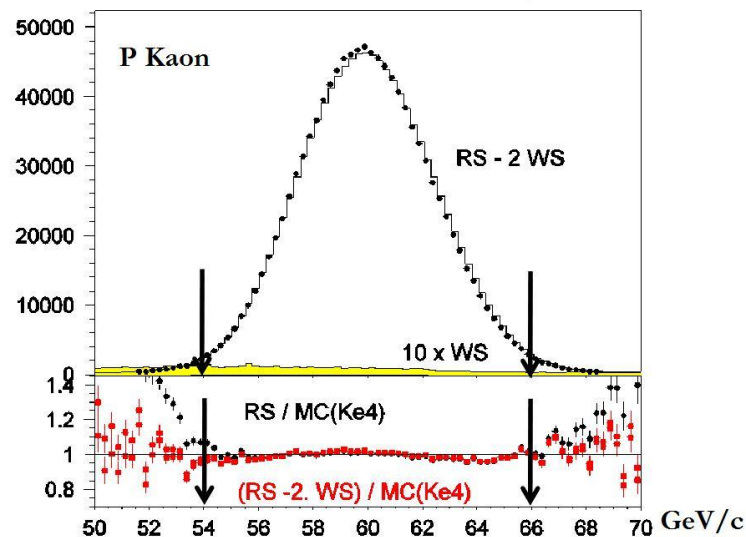
~1150000 decays

Main background sources:

$\pi\pi\pi + \pi \rightarrow e\nu$

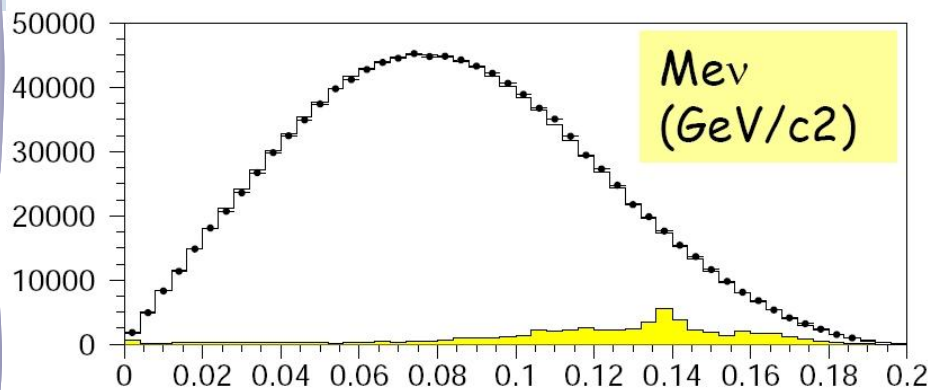
$\pi\pi\pi$ with π misidentified

$\pi\pi^0\pi^0$ or $\pi^0 + \pi^0$ (Dalitz) + e misidentified
and γ s outside the LKr



The background is studied using the electron “*wrong*” sign (WS) events (we assume $\Delta Q = \Delta S$ and total charge ± 1) and cross check with MC. The total bkg is at level of 0.5%.

Ke4: Fitting procedure



- Define $10(M\pi\pi) \times 5(M_{\pi\pi}) \times 5(\cos\theta_e) \times 5(\cos\theta_\pi) \times 12(\phi) = 15000$ iso-populated boxes
- In each $M\pi\pi$ bin the F, G, H and δ form factors are extracted minimizing a log-likelihood estimator over the 1500 boxes
- All the form factors are measured relatively to f_s (no overall BR measured)
- K^+ and K^- fitted separately, and then the fitted parameters are combined in each $M\pi\pi$ bin
- The form factors structure is studied in 10 bins of q^2 (or $M_{\pi\pi}^2$)
- Agreement with published results (based on 2003 data) [Batley et al. EPJC 54-3 (2008) 411]

(2003+2004)		Data	MC
K+	evts	726400	17.7×10^6
	evts/bin	48	1160
K-	evts	404400	9.8×10^6
	evts/bin	27	650

$$f'_s/f_s = 0.152 \pm 0.007 \pm 0.005$$

$$f''_s/f_s = -0.073 \pm 0.007 \pm 0.006$$

$$f'_e/f_s = 0.068 \pm 0.006 \pm 0.007$$

$$f_p/f_s = -0.048 \pm 0.003 \pm 0.004$$

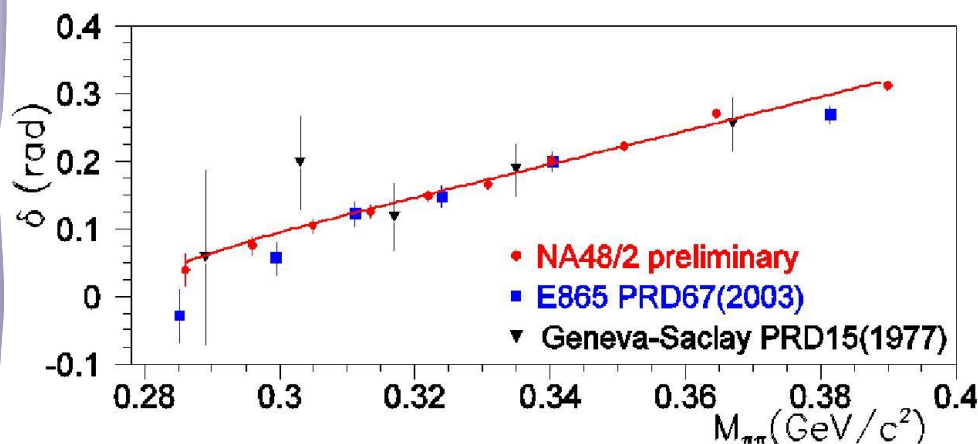
$$g_p/f_s = 0.868 \pm 0.010 \pm 0.010$$

$$g'_p/f_s = 0.089 \pm 0.017 \pm 0.013$$

$$h_p/f_s = -0.398 \pm 0.015 \pm 0.008$$

(stat+syst error quoted)

Ke4: Phase shift and $\pi\pi$ scattering length



- Each point in the plot has been corrected for isospin effect: 10-15 mrad
- The total error in each point is different for each experiment:

Geneva-Saclay: 40-50 mrad

E865: 15-20 mrad

NA48/2: 7-8 mrad

- The extraction of pion scattering lengths from the fitted $\delta = \delta_s - \delta_p$ phase shift needs external theoretical and experimental inputs:

- The *Roy equations* provide the relation between δ and a_0 and a_2 near threshold (1) (2) (3)
- Extrapolating the data from the $M_{\pi\pi} > 0.8$ GeV it's possible to fit the result in the threshold region (the uncertainty from the experimental data defines the *Universal Band*)

- Coulomb correction (Gamow factor) and real photons are included in simulation

- Isospin correction prescription given by Gasser (4) results in 11 to 15 mrad in the fitted $M_{\pi\pi}$ range

- The isospin correction is slightly greater than the error on each point: **can't be ignored!**

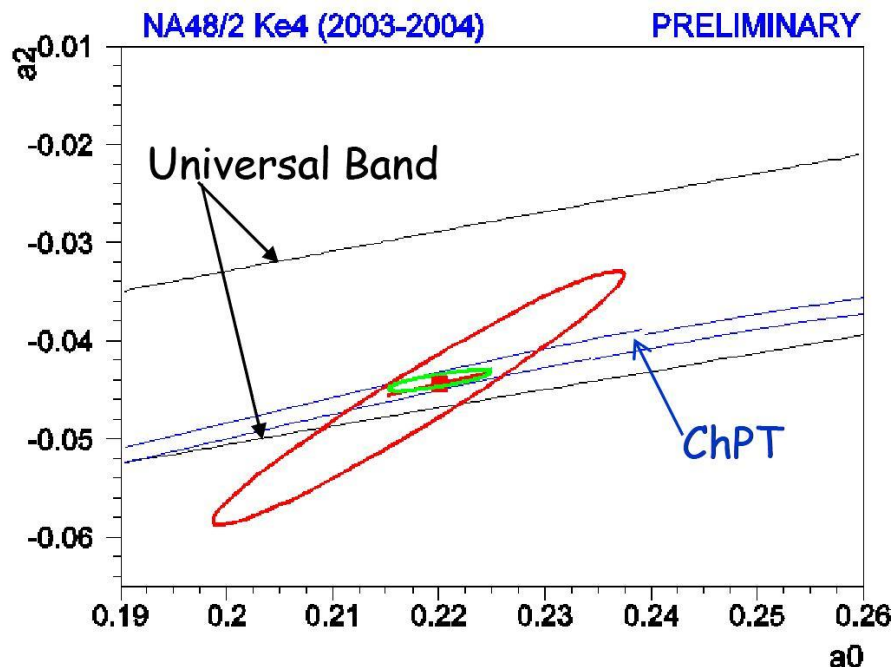
1)[Ananthanarayan, Colangelo, Gasser, Leutwyler Phys.Rept.353:207-279 (2001)]

2)[Descotes-Genon, Fuchs, Girlanda, Stern Eur.Phys.J.C24:469-483,2002]

3)[Kaminski, Pelaez, Yndurain Phys.Rev.D77 (2008)]

4)[Gasser et al. Eur.Phys.J. C59:777,2009]

Ke4: a0 and a2 results



- Theory prediction
Assuming ChPt and low energy constants
[Colangelo, Gasser, Leutwyler Nucl.Phys.B603,2001]
[Colangelo, Gasser, Leytwyler Phys.Rev.Lett.86,2001]:

$$a_0 = 0.220 \pm 0.005$$

$$a_2 = -0.0444 \pm 0.0008$$

$$1 \text{ par. Fit (ChPt)} : a_0 = 0.2206 \pm 0.0049_{\text{stat}} \pm 0.0018_{\text{syst}} \pm 0.0064_{\text{th}}$$

$$2 \text{ par. Fit} : a_0 = 0.2220 \pm 0.0128_{\text{stat}} \pm 0.0050_{\text{syst}} \pm 0.0037_{\text{th}}$$

$$a_2 = -0.0432 \pm 0.0086_{\text{stat}} \pm 0.0034_{\text{syst}} \pm 0.0028_{\text{th}}$$

Theoretical error computed from isospin corrections and Roy equation inputs [Gasser et al. Eur.Phys.J. C59:777,209]

Using data (21 points) from the three experiments (dominated by NA48/2)

$$a_0 = 0.2199 \pm 0.0125_{\text{exp}} \pm 0.0037_{\text{th}}$$

$$a_2 = -0.0430 \pm 0.0083_{\text{exp}} \pm 0.0028_{\text{th}}$$

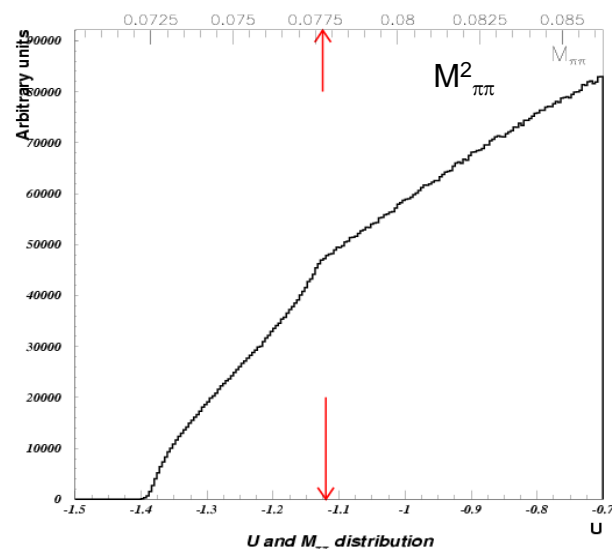
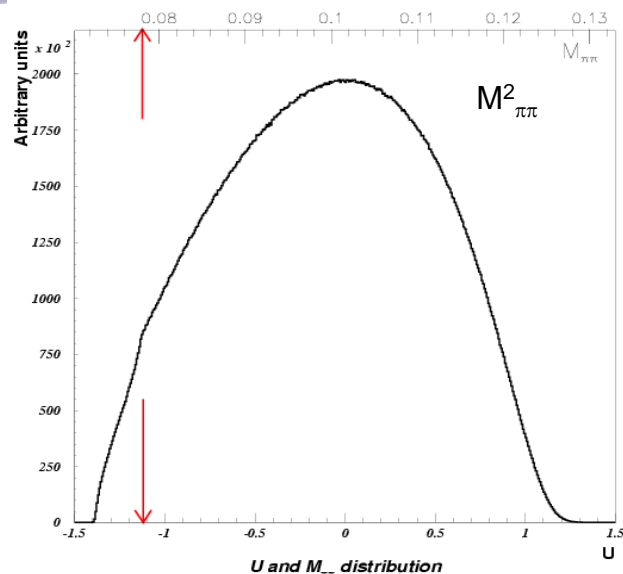
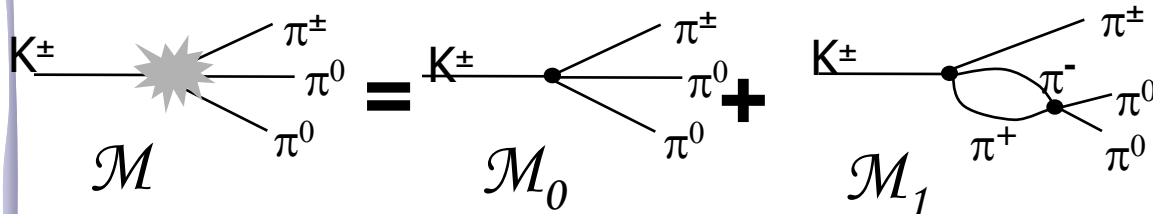
Cusp: Experimental evidence

- In $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ decay the matrix element is usually given as **polynomial expansion** as a function of the Dalitz variables U and V

$$|M(u,v)|^2 \sim 1 + g u + h u^2 + k v^2 + \dots$$

$$u = (s_3 - s_0)/m_\pi^2 \quad s_i = (P_K - P_{\pi,i})^2$$

- Thanks to the big statistics collected by NA48/2 and the good energy resolution, for the first time **a structure has been observed** at the $\pi\pi$ threshold value [Batley et al., Phys. Lett. B633:173-283, 2006]
- This structure has been interpreted by Cabibbo [Cabibbo Phys. Rev. Lett. 93, 121801 (2004)] as due to the **strong $\pi\pi$ rescattering** in the $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ final state



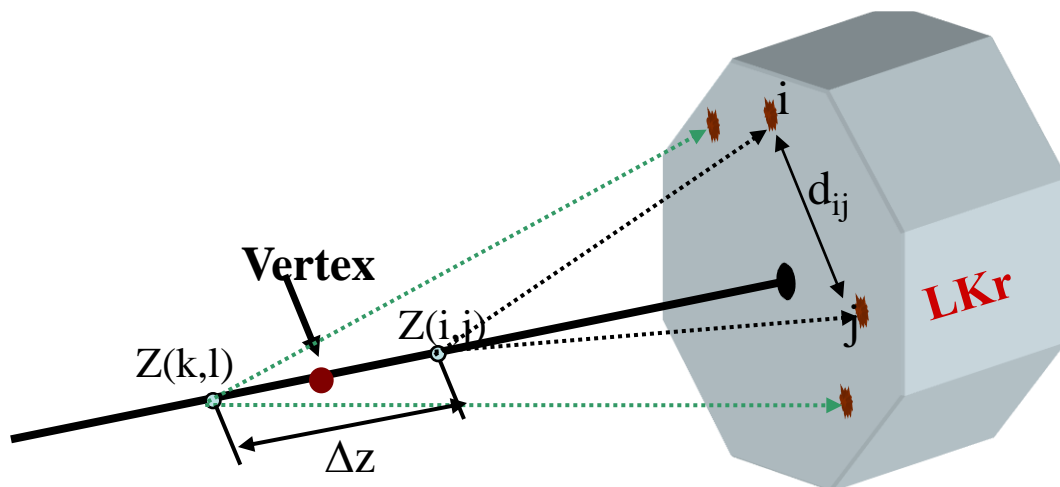
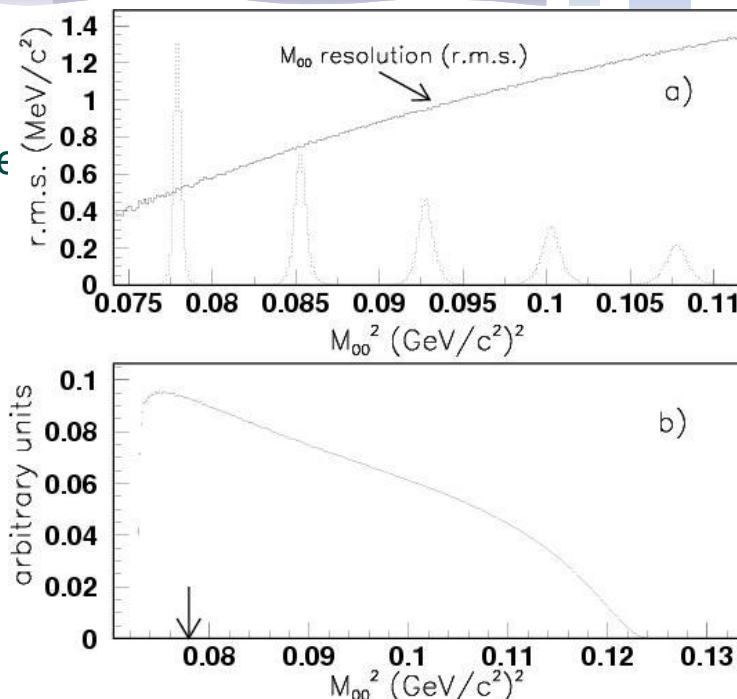
Cusp: $K \rightarrow 3\pi$ selection

- Online selection:

- (L1) one charged particle in CHOD and at least three peaks in at least one projection (x or y) of the LKr analog sum peak system.
- (L2) The opposite mass with respect to the charged tracks have to be far from one π^0 mass.

- Offline selection: among all the possible γ pairings, the couple for which χ^2 is smallest is selected

- the neutral vertex is obtained by imposing the π^0 mass. The final vertex is obtained as average between the 2 vertices.



- Very good **acceptance** and **resolution** in threshold region: high statistics and good opportunity to resolve tiny structures.

Cusp: Theoretical approach (Cabibbo-Isidori)

- Phenomenological approach
- The term M_0 (no rescattering) is given by the standard PDG expansion
- the first rescattering terms is **real** below threshold and **imaginary** above. Interference below threshold.

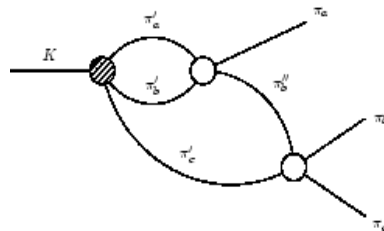
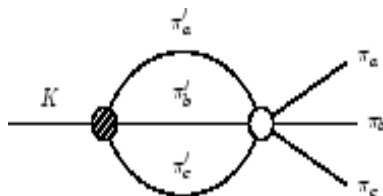
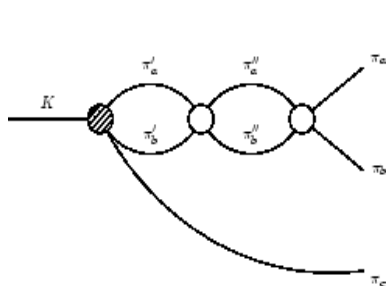
$$s_{\pi\pi} > (2m_{\pi^+})^2$$

$$M^2 = (M_0)^2 + |M_1|^2$$

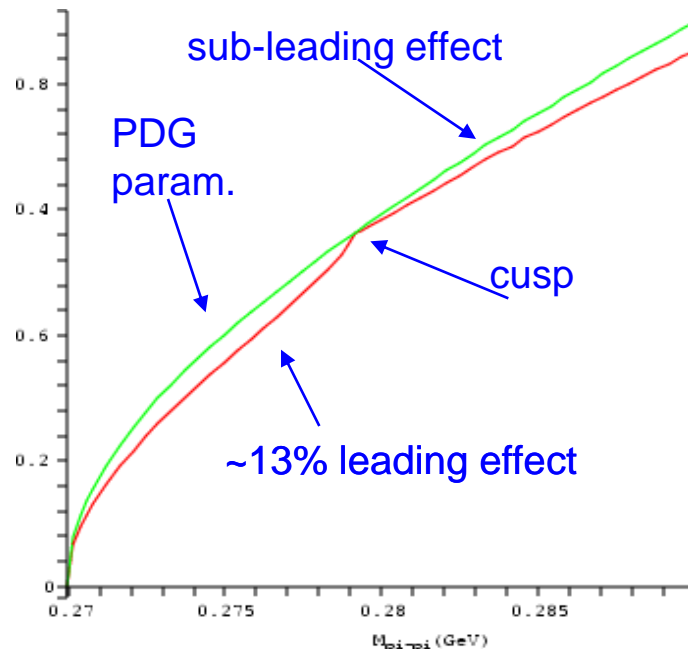
$$s_{\pi\pi} < (2m_{\pi^+})^2$$

$$M^2 = (M_0)^2 + (M_1)^2 + 2M_0M_1$$

$$\mathcal{M}_1 = -2/3(a_0 - a_2)m_+ \mathcal{M}_+ \sqrt{1 - \frac{(M_{00})^2}{2m_+}}$$



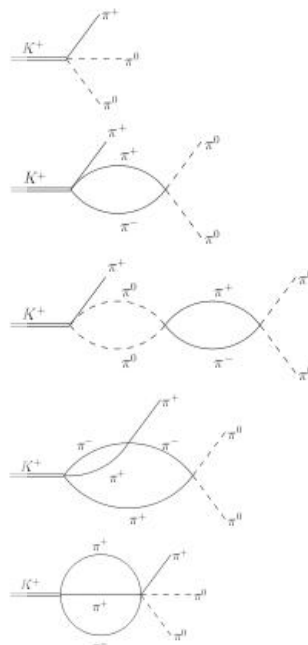
Cabibbo, Isidori JHEP 0503 (2005) 21



- The amplitude below threshold depends on $(a_0 - a_2)$
- Other 5 terms rise from two loops calculation (proportional to scattering lengths): effects below and above threshold
- Theoretical error evaluated from the next level expansion (work in progress...)

Cusp: theoretical approach (Bern-Bonn)

- Different approach based on **effective non-relativistic Lagrangian**
- The electromagnetic effects are **naturally included** in this approach (explicitly omitted in the CI work)
- **Different structure** of the expansion (different correlation between the terms wrt the Cabibbo-Isidori expansion): kinetic energy and threshold parameter.
- Simultaneous fitting of charged and neutral amplitude to extract M^+ slope parameters (modified with respect to the PDG parametrization)
- Radiative correction, outside the cusp point, included in the BB model



$$\mathcal{M}^{\text{tree}} = G_0 + G_1(p_3^0 - M_\pi) + \dots$$

$$\mathcal{M}^{1\text{-loop}} = B_1 J_{+-}(s_3) + B_2 J_{00}(s_3) + [B_3 J_{+0}(s_1) + (s_1 \leftrightarrow s_2)]$$

$$\mathcal{M}^{2\text{-loop}} = 2G_0 C_x^2 \underbrace{J_{+-}(s_3) J_{00}(s_3)}_{\text{double loops}} + \dots$$

$$+ 4H_0 C_x C_{+-} \underbrace{F_+(\dots; s_3)}_{\text{overlapping loops}}$$

$$+ \mathcal{O}(i\epsilon^4) \quad [\not\propto \text{scatt. lengths}]$$

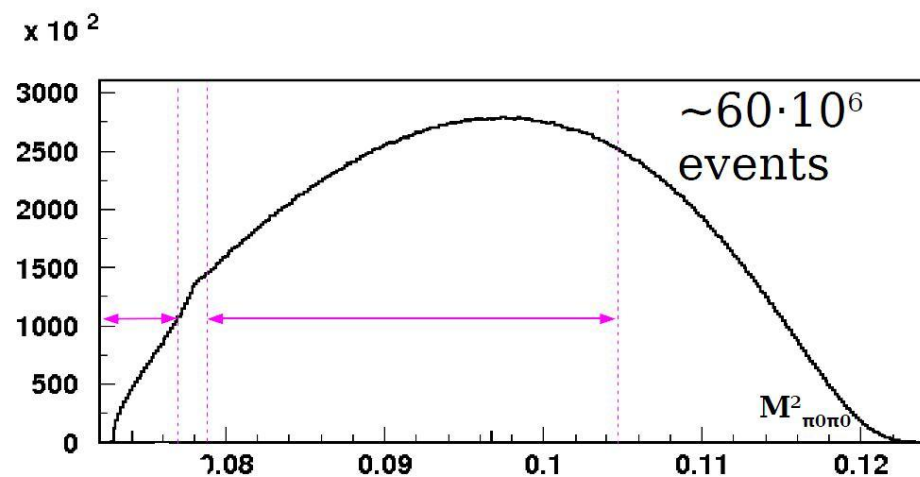
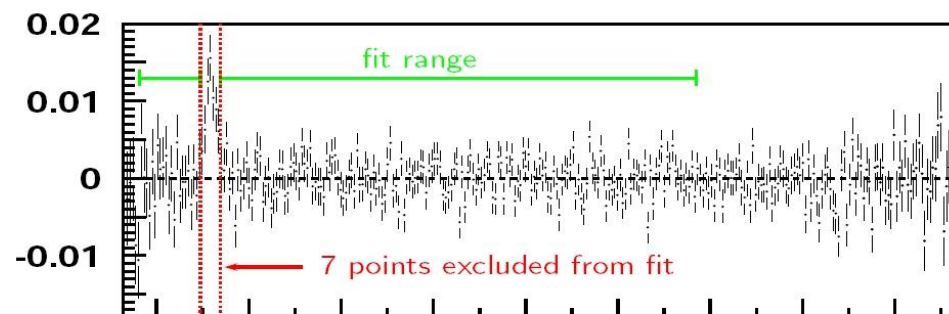
[Colangelo, Gasser, Kubis, Rusetsky in Phys.Lett.B638:187-194,2006]

[Bissenger, Fuhrer, Gasser, Kubis, Rusetsky in Phys.Lett.B659:576,2008]

[Bisseger, Fuhrer, Gasser, Kubis, Rusetsky in NPH B806:178, 2009]

Cusp: fitting procedure

- Resolution and detector response matrix obtained using accurate Geant3 based simulation
- Both theories can be fitted with the same procedure (fit parameters: g , h , a_0 - a_2 , a_2 , N)
- The M^+ terms appearing in the **CI** theory is fixed by the recent measured $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ slope parameters [Batley et al. Phys.Lett.B649:349-358,2007]
- In the **BB** the M^+ term is obtained simultaneously fitting $K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ and $K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ Dalitz plot
- Isospin effects included
- 7 bins around threshold excluded from the fit, upper limit to reduce the total error (226 bins)
- The **excess of events** in the cusp position, $R = (1.8 \pm 0.3) \cdot 10^{-5}$, can be explain by:
 - pionium $0.8 \cdot 10^{-5}$ [Silagadze, JETP Lett. 60 (1994) 689]
 - unbound state with resonant structure [Gevorkian, Tarasov, Voskeresenskaya, Phys.Lett.B649:159,2007]



- The numbers of “atoms” is used as free parameter in the fits

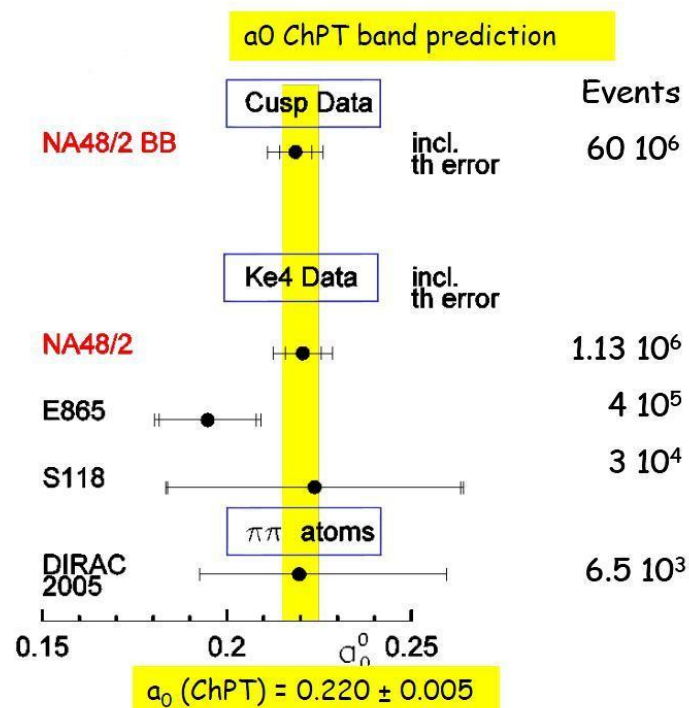
Cusp: Results

2 par. Fit :

$$(a_0 - a_2)m_+ = 0.2571 \pm 0.0048_{\text{stat.}} \pm 0.0025_{\text{syst.}} \pm 0.0014_{\text{ext.}}$$

$$a_2 m_+ = -0.024 \pm 0.013_{\text{stat.}} \pm 0.009_{\text{syst.}} \pm 0.002_{\text{ext.}}$$

1 par. Fit (ChPT): $(a_0 - a_2)m_+ = 0.2633 \pm 0.0024_{\text{stat.}} \pm 0.0014_{\text{syst.}} \pm 0.0019_{\text{ext.}}$



- Results based on **BB** model (better χ^2 , most complete theory)

- Very good agreement between the two approaches

- Good agreement with ChPT prediction [Colangelo, Gasser, Leutwyler PRL 86 (2001) 5008]:

$$(a_0 - a_2)m_+ = 0.265 \pm 0.004$$

- Similar theoretical and experimental precision

- Systematics error dominated by LKr non linearity and trigger efficiency

Cusp and Ke4: comparisons

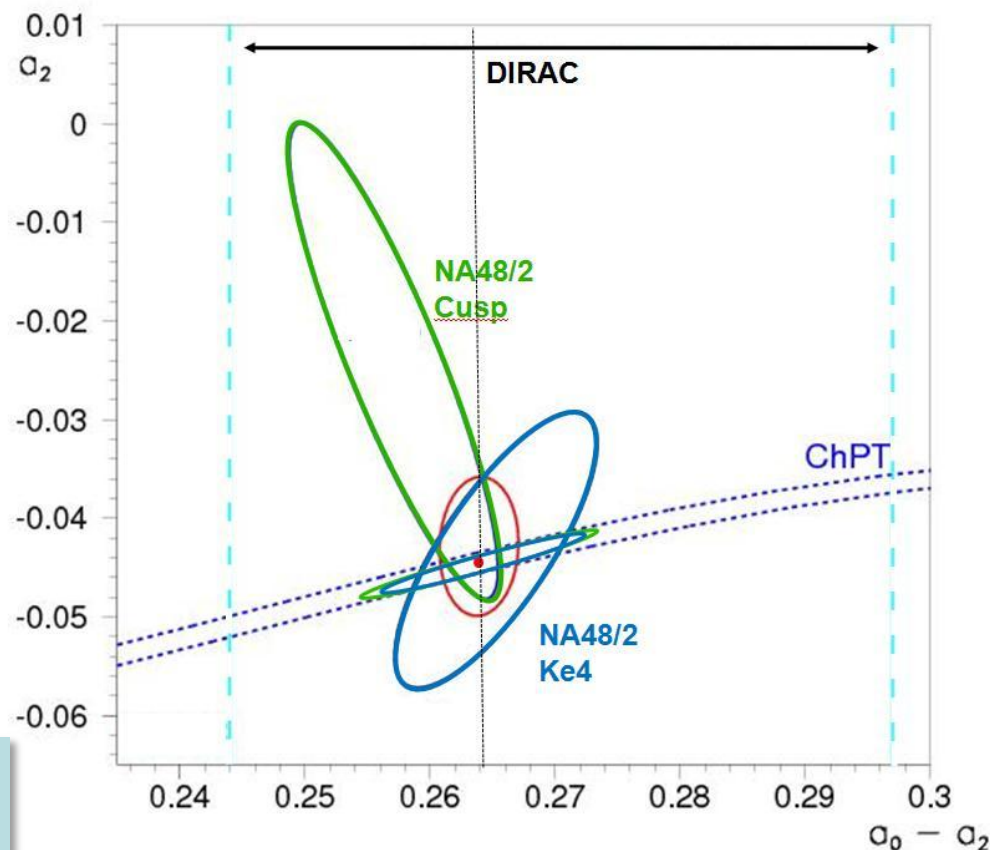
- Two independent measurements
 - 60 M K3p
 - 1.13 M Ke4
- Different systematics
 - Cusp: Calorimeter and trigger
 - Ke4: electron misID and Background
- Different theoretical inputs
 - Cusp: rescattering in final state and ChPT expansion
 - Ke4: Roy equation and isospin breaking correction

Combined results

$$(a_0 - a_2)m_+ = 0.2639 \pm 0.0020 \pm 0.0004 \pm 0.0021$$

Using ChPT constraints:

$$(a_0 - a_2)m_+ = 0.2640 \pm 0.0020 \pm 0.0017 \pm 0.0035$$



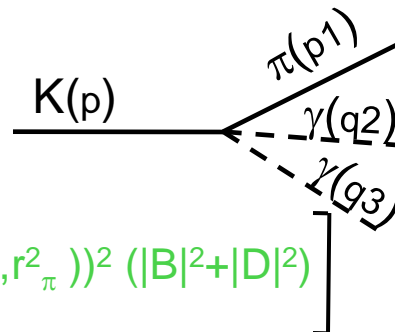
Very good agreement with ChPT prediction:

$$(a_0 - a_2)m_+ = 0.265 \pm 0.004$$

K → πγγ: Theory

- At leading order, in the framework of ChPT, the $K(p) \rightarrow \pi(p_1)\gamma(q_2)\gamma(q_3)$ differential rate is given by:

$$\frac{\partial^2 \Gamma}{\partial y \partial z} = \frac{m_K}{(8\pi)^3} \left[z^2 (|A+B|^2 + |C|^2) + (y^2 - 1/4\lambda(1, z, r_\pi^2))^2 (|B|^2 + |D|^2) \right]$$



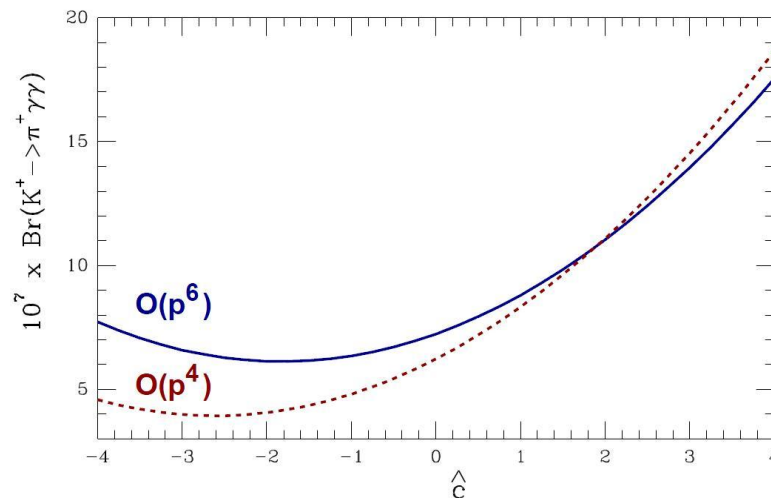
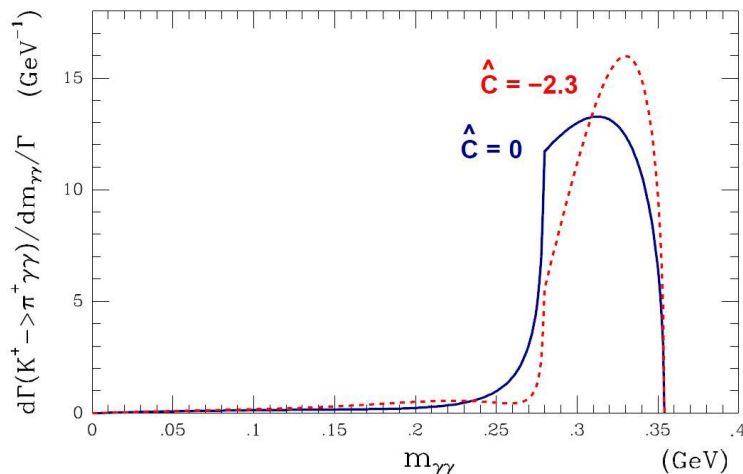
$$y = p(q_2 - q_3)/m_K^2$$

$$z = (q_2 + q_3)/m_K^2$$

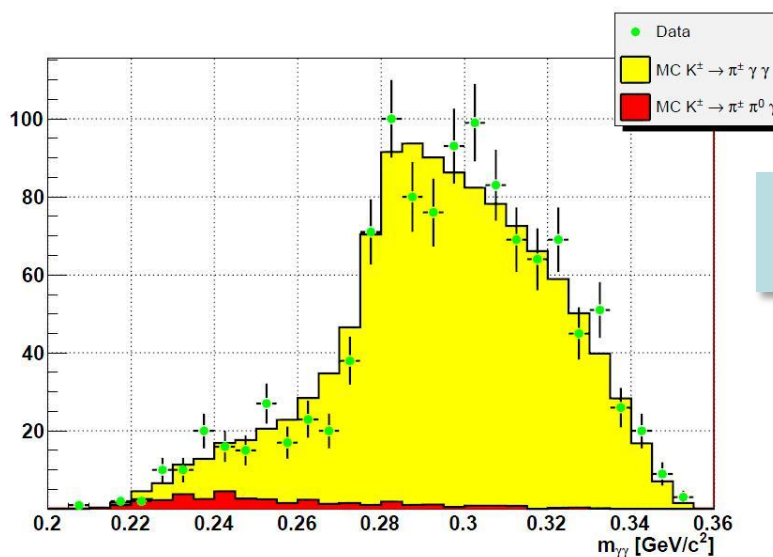
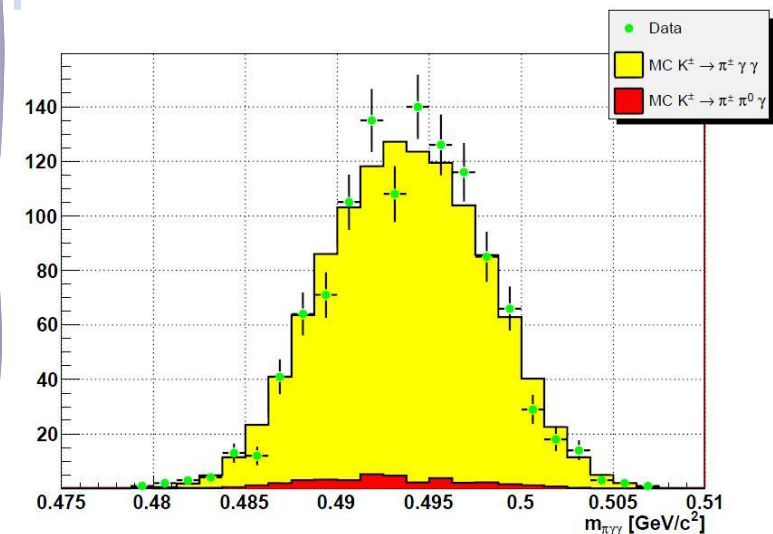
- At $O(p_4)$ the relevant contribution is given by $A(z, \hat{C})$ (loops) and $C(z)$ (poles); $B=D=0$ at $O(p_4)$ and relevant at leading order only at low $m_{\gamma\gamma}$ mass (1).
- \hat{C} is $O(1)$ and have to be extracted from data
- Order $O(p_6)$ can be relevant (30%-40% enhanced in BR) (2).

(1) [Ecker, Pich, De Rafael, in Nucl.Phys.B303:665,1988]

(2) [D'Ambrosio, Portoles, in Nucl.Phys.B386:403,1996]



K $\rightarrow\pi\gamma\gamma$: Results



- Analysis based on **40%** of whole data set
- **1164 events** found
- main background: $K^+ \rightarrow \pi^+ \pi^0 \gamma$ (3.3%)
- Main systematics from trigger efficiency determination
- Data shape ($m_{\gamma\gamma}$) follows ChPT description ($\hat{c}=2$ shown for qualitative comparison)
- Assuming **O(p6)** and $\hat{c}=2$ the preliminary result on *model dependent* BR determination is

$$\text{Br}(K^+ \rightarrow \pi^+ \gamma \gamma) = (1.07 \pm 0.04_{\text{stat}} \pm 0.08_{\text{syst}}) \cdot 10^{-6}$$

(model independent analysis on going)

- Overtaken the previous result from E787 with **31 events** candidates:

$$\text{Br}(K^+ \rightarrow \pi^+ \gamma \gamma) = (1.10 \pm 0.32) \cdot 10^{-6}$$

$K \rightarrow \pi \gamma e e$: Theory

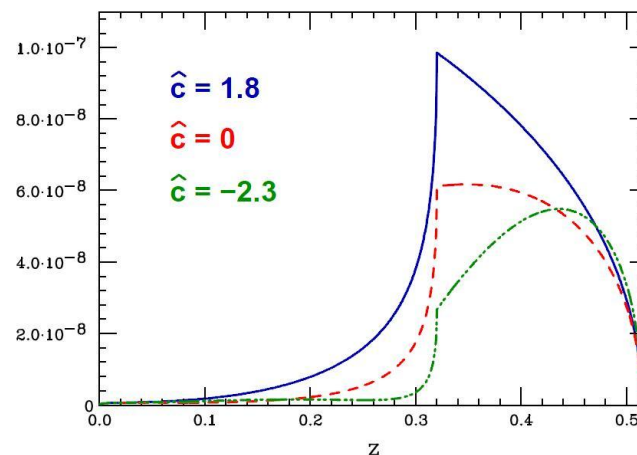
- Similar with respect to $K^+ \rightarrow \pi^+ \gamma \gamma$
- Br and $m_{ee\gamma}$ at order $O(p^4)$ determined by \hat{c}
- $O(p^6)$ could enhance the BR by 30%-40%
- Theoretical prediction at $O(p^6)$:

$$\text{Br}(K^+ \rightarrow \pi^+ \gamma e^+ e^-) = (0.9 \div 1.6) \cdot 10^{-8}$$

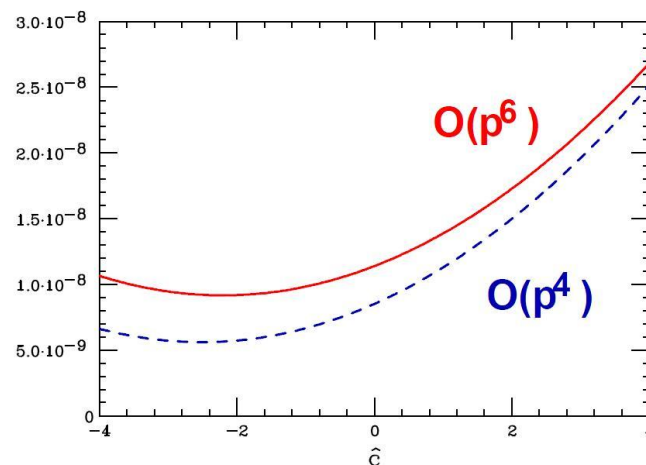
[Gabbiani, in Phys.Rev.Lett.D59,1999]

- Never observed before!

$d\text{BR}(K^+ \rightarrow \pi^+ \gamma e^+ e^-)/dz$

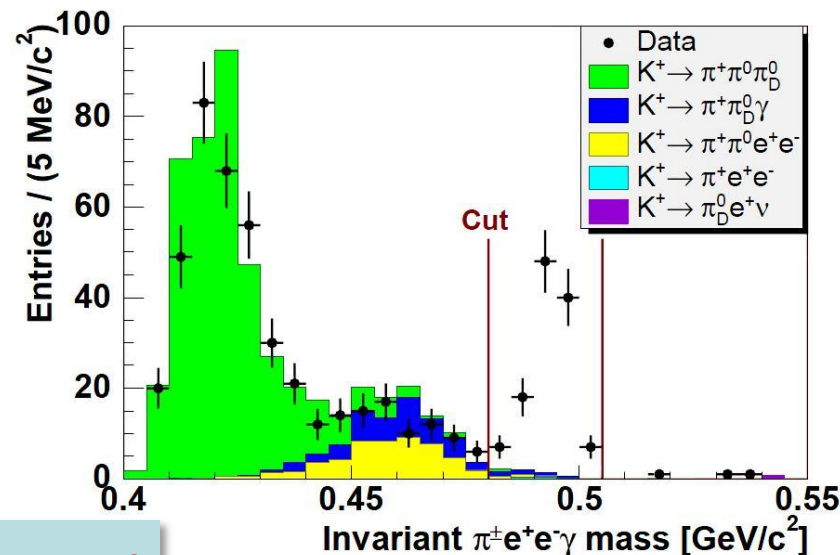


$\text{BR}(K^+ \rightarrow \pi^+ \gamma e^+ e^-)$



K → πγee : Results

- 120 events candidates
- Background from $K^+ \rightarrow \pi^+ \pi_D^0 \gamma$ (6.1%)
- BR computed in bins of $m_{ee\gamma}$
- no assumption on $m_{ee\gamma}$ (model independent measurement)
- Cut on $m_{ee\gamma} > 260 \text{ MeV}/c^2$



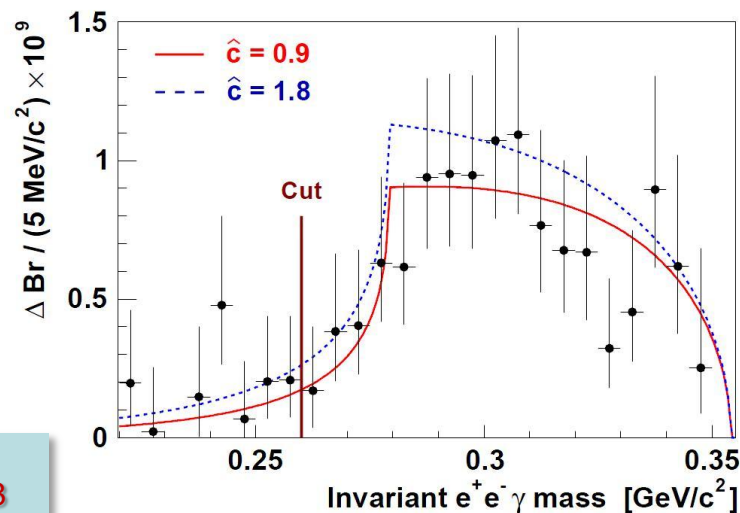
$$\text{BR}(K^\pm \rightarrow \pi^\pm e^+ e^- \gamma) = (1.19 \pm 0.12_{\text{stat}} \pm 0.04_{\text{syst}}) \cdot 10^{-8}$$

- Assuming ChPT $\mathcal{O}(p^6)$, the \hat{c} value is extracted from $m_{ee\gamma}$ distribution

$$\hat{c} = (0.90 \pm 0.45)$$

- From this the model dependent ChPT BR is:

$$\text{BR}(K^\pm \rightarrow \pi^\pm e^+ e^- \gamma) = (1.29 \pm 0.13_{\text{exp}} \pm 0.03_{\hat{c}}) \cdot 10^{-8}$$



[Batley et al. Phys.Lett.B659:493, 2008]

Conclusions

- The kaon decays give the possibility to study the low energy hadronic interaction with good precision
- Thanks to high statistics and high data quality, NA48/2 can check several ChPT predictions with **very high accuracy**
- Three significative “*examples*” have been presented in this talk:
 - $\pi\pi$ scattering lengths
 - $K^\pm \rightarrow \pi^\pm \gamma\gamma$
 - $K^\pm \rightarrow \pi^\pm \gamma e^+ e^-$
- The results obtained are compatible with the predictions
- In particular the measurement of the $\pi\pi$ scattering lengths obtained in two different ways, with an experimental error comparable with the theoretical uncertainty, is a very strong test of the theory.