

# Dijet Angular distributions at $\sqrt{s} = 14\text{TeV}$

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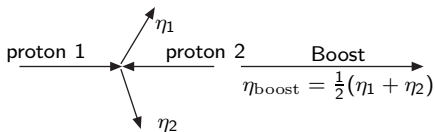
July 16, 2009

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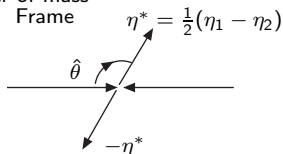
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# Introduction

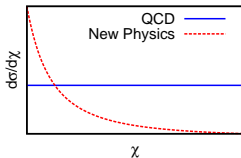
Lab Frame



Center-of-mass  
Frame



- Dijet final state, in pp-collisions through qq, qg and gg interactions.
- Variable of interest:  $\chi = \exp(|\eta_1 - \eta_2|) = \frac{1 + |\cos(\hat{\theta})|}{1 - |\cos(\hat{\theta})|}$
- Take bins in dijet invariant mass  $M_{jj}$ .  
At LO:  $M_{jj} = x_1 x_2 s = p_T (\sqrt{\chi} + 1/\sqrt{\chi})$
- Calculate dijet angular distribution:  $d\sigma/d\chi$  vs  $\chi$



- QCD curve is rather flat (Rutherford scattering)
- New physics usually more isotropic events  $\Rightarrow$  peak at small  $\chi$
- New physics? Gravitational effects from large extra dimensions, quark compositeness, ...

# Selection cuts

- 4 Mass ( $M_{jj}$ ) bins: [0.5, 1], [1, 2], [2, 3] and  $> 3\text{TeV}$
- Detector: can measure  $\eta$  up to  $\eta_{\text{max}}$ , in this study  $\eta_{\text{max}} = 3.1$  or  $4.0$
- Physics: 2 orthogonal selections cuts (see backup slides for more info):

$$|\eta_1 + \eta_2| < c \quad (1)$$

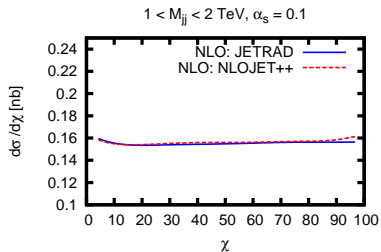
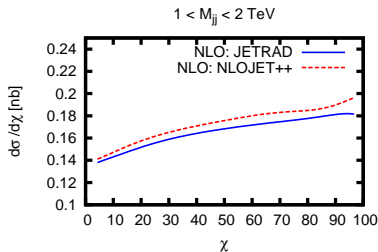
$$|\eta_1 - \eta_2| < 2\eta_{\text{max}} - c \iff \chi < \exp(2\eta_{\text{max}} - c), \quad (2)$$

with  $c = 1.5 \Rightarrow \chi_{\text{max}} \approx 100$  or  $600$ .

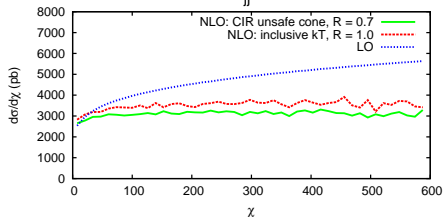
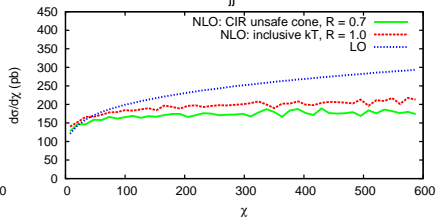
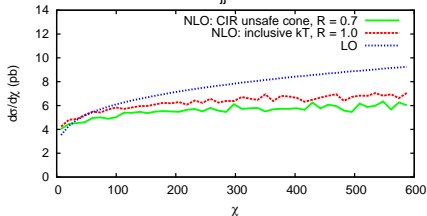
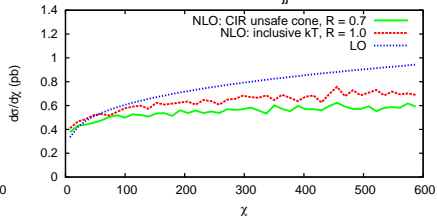
# QCD up to NLO: JETRAD and NLOJET++

2 programs for NLO calculations: JETRAD and NLOJET++

- JETRAD: phase space slicing
- NLOJET++: applies the Catani-Seymour dipole subtraction scheme with some modifications introduced because of computational reasons
- NLOJET++ uses different parametrization of  $\alpha_s$  than JETRAD (left plot), difference disappears when with fixed  $\alpha_s = 0.1$  (right plot)

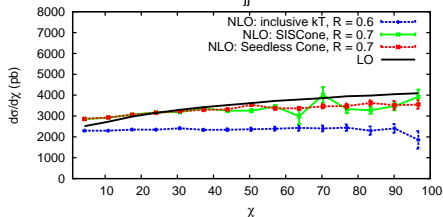
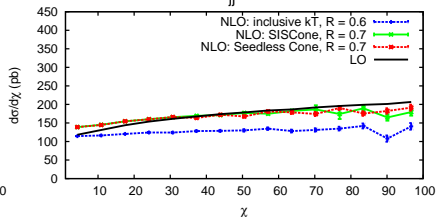
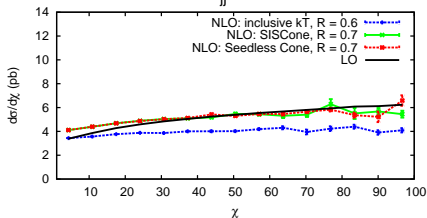
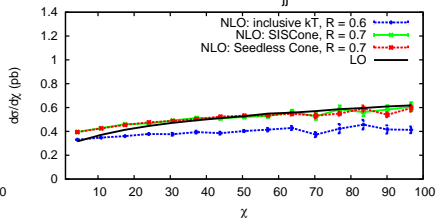


## NLO calculations with JETRAD

 $0.5 < M_{jj} < 1 \text{ TeV}$  $1 < M_{jj} < 2 \text{ TeV}$  $2 < M_{jj} < 3 \text{ TeV}$  $3 \text{ TeV} < M_{jj}$ 

- Calculations done with seeded cone 0.7 and inclusive  $k_T$  1.0
- 4 different mass bins,  $\chi < 600$
- At NLO, the different jet algorithm tends to give the same shape of the distributions, but a different normalization

## NLO calculations with NLOJET++

 $0.5 < M_{jj} < 1 \text{ TeV}$  $1 < M_{jj} < 2 \text{ TeV}$  $2 < M_{jj} < 3 \text{ TeV}$  $3 \text{ TeV} < M_{jj}$ 

- jet algorithms: seedless cone 0.7 with overlap 0.5 and SIScone 0.7 with overlap 0.75
- 4 different mass bins,  $\chi < 100$

# Systematic uncertainties

Uncertainties from theoretical calculations:

- renormalization ( $\mu_R$ ) and factorization scale ( $\mu_F$ )
- PDFs

Experimental uncertainties:

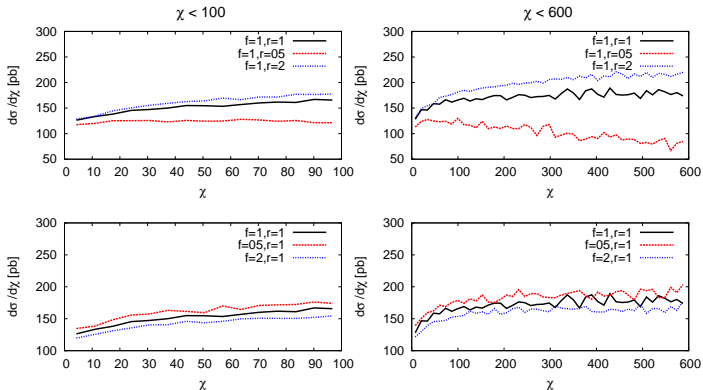
- Dominating uncertainty from jet energy calibration  $\Rightarrow$  normalize distributions to unit area to reduce the impact ( $(1/\sigma)d\sigma/d\chi$  vs  $\chi$ )



# Systematic uncertainty coming from $\mu_R$ and $\mu_F$

How to investigate?

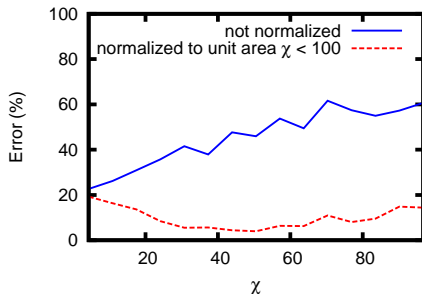
- Take  $\mu_{R,F} = 0.5, 1, 2 \times p_T$  highest jet  $\rightarrow$  9 possible combinations
- Figure: mass bin  $1 < M_{jj} < 2$  TeV,  $r$  and  $f$  are the fraction of the transverse momentum of the highest jet at which respectively  $\mu_R$  and  $\mu_F$  are evaluated. Left:  $\chi < 100$ , right:  $\chi < 600$ .



# Systematic uncertainty coming from $\mu_R$ and $\mu_F$

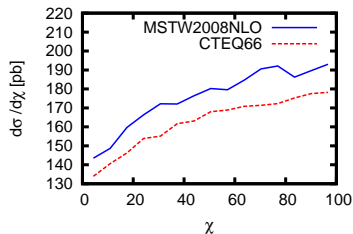
- Different  $\mu_F$  mainly influences the absolute normalization, while  $\mu_R$  influences both shape and normalization.

Error coming from choice of  $\mu_R$  and  $\mu_F$ :

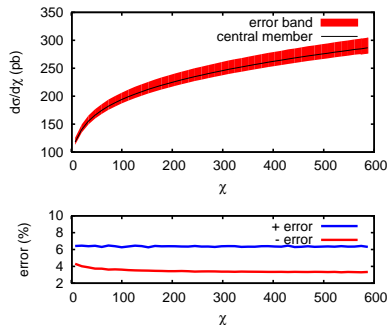


# Systematic uncertainty coming from PDFs

- Study 2 different PDF-sets: CTEQ66 and MSTW2008NLO in  $[1, 2]$ TeV mass bin:

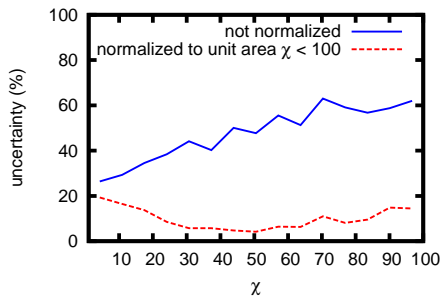


- For CTEQ66: study all  $2N = 44$  error members, use Master Equation (hep-ph/0611148v1) to calculate uncertainty:



# QCD Uncertainty

- Combining uncertainties from  $\mu_R$  and  $\mu_F$ , and intrinsic uncertainty from the CTEQ66 PDF in quadrature
- Uncertainty both on distributions normalized to unit area  $\chi < 100$  and not normalized
- Dominating uncertainty from  $\mu_R$



# Conclusions and outlook

## Dijet angular distributions

- $d\sigma/d\chi$  vs  $\chi$  in bins of dijet invariant mass
- allows to distinguish more isotropic scattering (new physics) from Rutherford scattering (QCD)

## QCD calculations up to NLO, using JETRAD and NLOJET++

- NLOJET++ and JETRAD agree reasonably well (difference in parametrization of  $\alpha_s$ )
- LO and NLO agree quite well at low  $\chi$ , but differ at large  $\chi$
- Different jet algorithms give different normalization
- Biggest uncertainty coming from the choice of  $\mu_R$
- Choice of  $\mu_F$  and the PDF-sets has mainly impact on absolute normalization, minimize the uncertainty by normalizing the distributions
- Biggest uncertainty at large  $\chi$ .

## Outlook

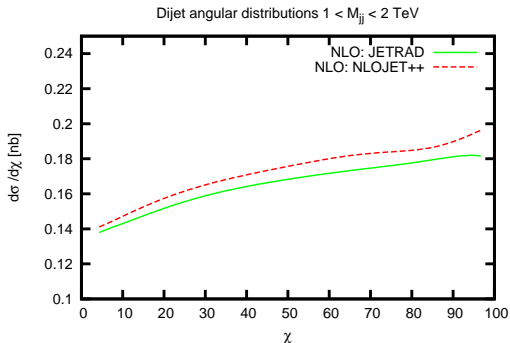
- ATLAS: early (2010) measurement ( $\chi < 30$ )

# NLOJET++ vs JETRAD

- NLOJET++ uses different parametrization of  $\alpha_s$  than JETRAD

- NLOJET++: 
$$\alpha_s(Q) = \frac{4\pi}{\beta_0 \ln(Q^2/\Lambda^2)} \left( \frac{1}{1 + \frac{2\beta_1}{\beta_0^2} \frac{\ln \ln(Q^2/\Lambda^2)}{\ln(Q^2/\Lambda^2)}} \right)$$

- JETRAD: 
$$\alpha_s(Q) = \frac{4\pi}{\beta_0 \ln(Q^2/\Lambda^2)} \left( 1 - \frac{2\beta_1}{\beta_0^2} \frac{\ln \ln(Q^2/\Lambda^2)}{\ln(Q^2/\Lambda^2)} \right)$$



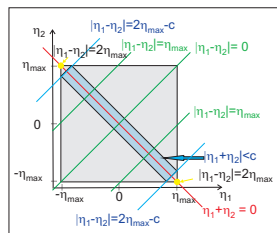
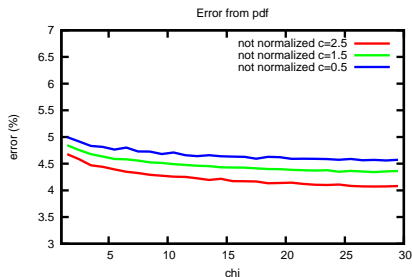
# Selection cuts

- Two orthogonal selection cuts:

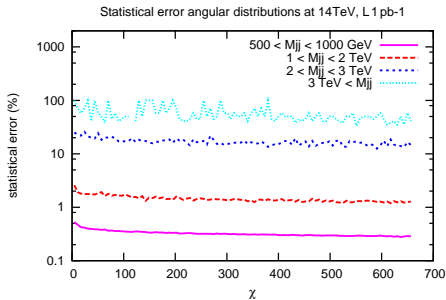
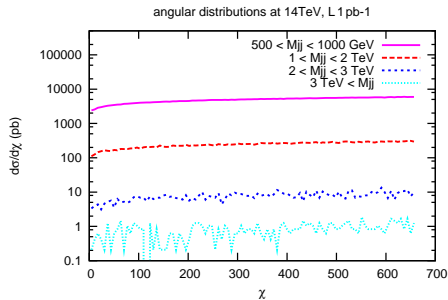
$$|\eta_1 + \eta_2| < c \quad (3)$$

$$|\eta_1 - \eta_2| < 2\eta_{\max} - c \iff \chi < \exp(2\eta_{\max} - c) \quad (4)$$

- Parameter  $c$ : trade-off between measurable  $\chi$ -range and error coming from statistics and PDFs



# Statistics at $1 \text{ pb}^{-1}$

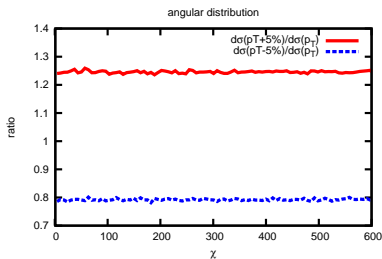




# Impact Jet Energy Scale (JES)

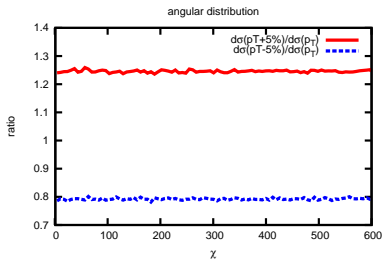
Simple test:

- 1 Generate events with pythia 6.4
- 2 Calculate  $d\sigma/d\chi$  vs  $\chi$  for  $1 < M_{jj} < 2$  TeV
- 3 For each event: increase jet  $p_T$  with +5%:  $p_T = p_T + 5\%$
- 4 Calculate  $d\sigma_{\text{increase}}/d\chi$  for  $1 < M_{jj} < 2$  TeV
- 5 Take ratio of differential cross-sections:  $(d\sigma_{\text{increase}}/d\chi)/(d\sigma/d\chi)$  (red curve)
- 6 Repeat steps 3.-4.-5. with  $p_T - 5\%$  (blue curve)



# Impact Jet Energy Scale (JES)

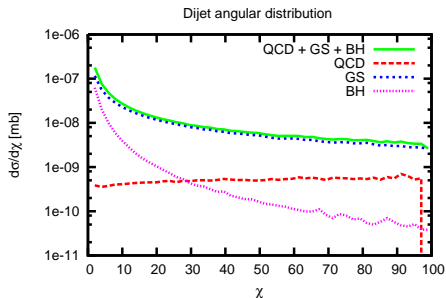
- Effect due to binning in  $\langle M_{jj} \rangle$
- Shape of distributions not effected by a global ( $\eta$  independent) error on JES  $\Rightarrow$  normalize distributions:  $(1/\sigma)d\sigma/d\chi$  vs  $\chi$
- Remaining  $\eta$  dependence of JES



# Gravitational scattering and black hole formation in large extra dimensions

- References: hep-ph/9811350, hep-ph/9811291, hep-ph/0608080, hep-ph/0608210
- ADD model including black hole formation (BH) and an effective field theory of gravity to describe gravitational scattering (GS)

Mass bin  $3 \text{ TeV} < M_{jj}$ , 6 extra dimensions and  $M_{\text{Planck}} \approx 1 \text{ TeV}$ :



# Large extra dimensions: the ADD model

- Large hierarchy found in nature: EW-scale  $\sim 10^2$  GeV, Planck Scale  $\sim 10^{19}$  GeV.
- Gravitational potential in world with  $n$  extra dimensions with compactification radius  $R$ :

$$V(r) \propto \begin{cases} \frac{1}{M_P^{n+2}} \frac{m}{r^{n+1}} & r \ll R \\ \frac{1}{M_P^{n+2} R^n} \frac{m}{r} & r \gg R \end{cases}$$

$M_P$  = fundamental Planck scale

- Compared with normal 4D-potential with 4D-Planck scale:  $V(r) = \frac{\hbar c}{M_{P4}^2} \frac{m}{r}$

$$M_{P4}^2 \sim M_P^{2+n} R^n$$

- $\rightarrow$  Fundamental Planck scale can be small, while observed 4D-Planck scale is large
- Arkani-Hamed Dimopoulos Dvali (ADD) model = existence of large extra spatial dimensions in which gravity is allowed to propagate, while the SM fields are confined to a 4D-membrane

# The ADD model

- Gravitational scattering through the exchange of virtual Kaluza-Klein (KK) modes
- Black Holes

