

# Study of CP violation in $B_s \rightarrow J/\psi\phi$ decays at CDF

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Search for New Physics in transitions

→ Measurement of the properties of oscillating particles:

 $K^0$  $B^0$  $D^0$  $B_s^0$

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→ Measurement of the properties of oscillating particles:

$K^0$

$B^0$

$D^0$

$B_S^0$

- ▶  $B^0$  and  $K^0$  are well explored by other experiments

Search for New Physics in transitions

→ Measurement of the properties of oscillating particles:

$$K^0 \quad B^0 \quad D^0 \quad B_s^0$$

- ▶ Evidence for  $D^0 - \bar{D}^0$  Mixing, also at CDF <sup>1</sup>

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<sup>1</sup>[http://www-cdf.fnal.gov/physics/new/bottom/070809.blessed-CharmMixing/dmix\\_pubnote.pdf](http://www-cdf.fnal.gov/physics/new/bottom/070809.blessed-CharmMixing/dmix_pubnote.pdf)

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- ▶ **Now: Measurement of the mixing phase**  $\beta_s$

Search for New Physics in transitions

→ Measurement of the properties of oscillating particles:

$K^0$

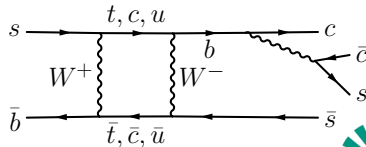
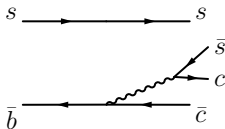
$B^0$

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- ▶  $B_s^0$  sector still partially unexplored.
- ▶ 2006: **Mixing frequency**  $\Delta m_s$  of the  $B_s^0$  measured by CDF and DØ
- ▶ **Now: Measurement of the mixing phase**  $\beta_s$
- ▶ Accessible through interference of decays with and without mixing

$$B_s \longrightarrow J/\Psi (\rightarrow \mu^+ \mu^-) \phi (\rightarrow K^+ K^-)$$





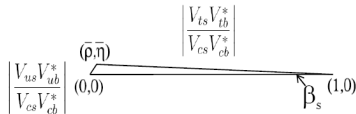
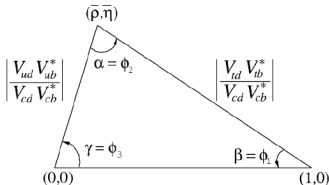
- ▶ The Cabibbo-Kobayashi-Maskawa matrix connects mass and weak quark eigenstates

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

- ▶ To conserve probability, CKM matrix must be unitary.
- ▶ Unitarity relations can be represented as unitarity triangles.

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$V_{us}V_{ub}^* + V_{cs}V_{cb}^* + V_{ts}V_{tb}^* = 0$$



- ▶ Subject of this measurement

$$\beta_s^{SM} = \arg\left(-\frac{V_{ts}V_{tb}^*}{V_{cs}V_{cb}^*}\right)$$

Flavor eigenstates of the  $B_s$  meson differ from mass eigenstates and mass eigenvalues are different.  $\rightarrow B_s$  oscillates with frequency

$$\Delta m_s = m_H - m_L = (17.77 \pm 0.12) ps^{-1}$$

Mass eigenstates have different decay widths:

$$\Delta\Gamma = \Gamma_L - \Gamma_H \approx 2|\Gamma_{12}|\cos(\phi_s) \text{ with } \phi_s = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right)$$

Standard Model expectation values:

$$\phi_s^{SM} = 4 \cdot 10^{-3} \quad \text{and} \quad \beta_s^{SM} = 0.02$$

New Physics affects both phases by **same** quantity <sup>1</sup>:

$$2\beta_s^{J/\Psi\phi} = 2\beta_s^{SM} - \phi_s^{NP} \quad \text{and} \quad \phi_s^{J/\Psi\phi} = \phi_s^{SM} + \phi_s^{NP}$$

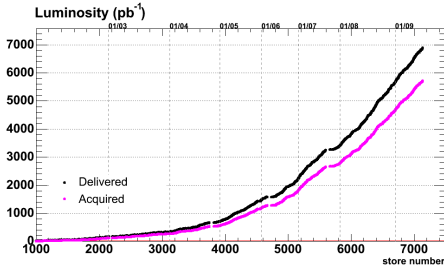
If the new physics phase  $\phi_s^{NP}$  dominates over the SM phases  $2\beta_s^{SM}$  and  $\phi_s^{SM}$   
 $\rightarrow$  neglect SM phases and obtain:

$$2\beta_s^{J/\Psi\phi} = -\phi_s^{NP} = -\phi_s^{J/\Psi\phi}$$

<sup>1</sup> arxiv:0705.3802v2

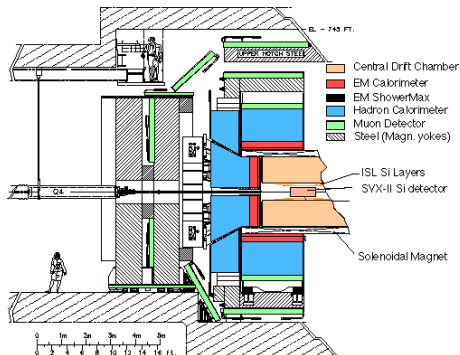
# The Tevatron

- ▶ Tevatron: circular particle accelerator at the Fermilab (near Chicago, Illinois)
- ▶ Proton-Antiproton collisions
- ▶  $\sqrt{s} = 1.96$  TeV
- ▶ Two detectors: CDF and DØ



Luminosity / Experiment:

Int. Lumi.	$fb^{-1}$
delivered	$\approx 7.0$
on tape	$\approx 5.8$
this analysis	$\approx 2.8$

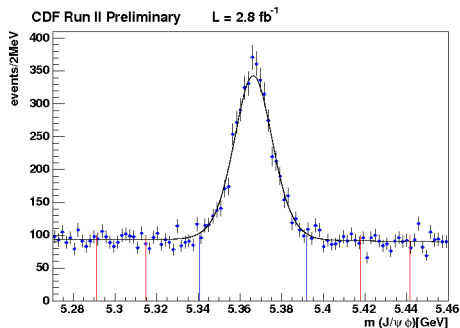


Multi purpose detector  
featuring . . .

- ▶ Tracking system contained inside a solenoid
- ▶ Electromagnetic and hadronic calorimeters
- ▶ Muon detectors ( $|\eta| < 2$ )
- ▶ Particle identification (dE/dx and TOF)

Mixing phase  $\beta_s$  and decay width difference  $\Delta\Gamma$  are extracted using an unbinned maximum likelihood fit in

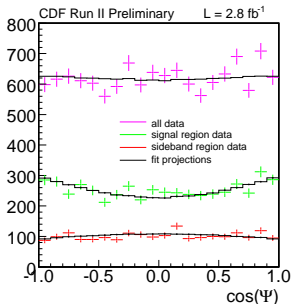
- ▶ **Mass**
- ▶ Transversity angles and Proper decay time
- ▶ Tagging information



$\approx 3200$  events

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An angular analysis is performed to disentangle **CP even** and **CP odd** components. → increase sensitivity on  $\beta_s$

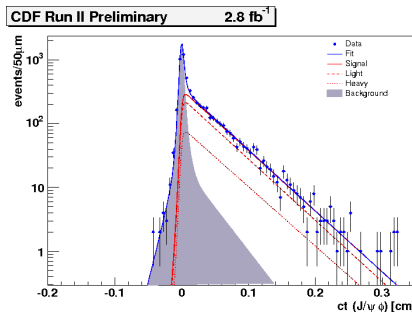
$\vec{\rho} = (\Psi_T, \theta_T, \phi_T)$  are angles given in the transversity basis<sup>a</sup>

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<sup>a</sup>hep-ph/9511363

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Mean lifetime assuming no CP violation ( $\beta_s^{J/\psi\phi} = 0$ ):

$$\tau(B_s) = (1.53 \pm 0.04(\text{stat.}) \pm 0.01(\text{syst.})) \text{ ps}$$

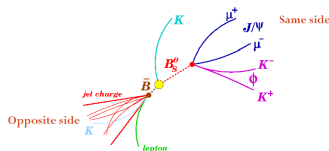
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- ▶ **Tagging information**

Tagging used to increase the sensitivity on the parameters.

## Approach:

- ▶ **OST**: exploits decay products of other b-hadron in the event ( $\epsilon D^2 \approx 1.2\%$ )
- ▶ **SST**: exploits the correlations with particles produced in fragmentation ( $\epsilon D^2 \approx 3.6\%$ , used in this analysis only in  $\mathcal{L}_{int} < 1.4 \text{ fb}^{-1}$ )



**Output:** Decision (b or  $\bar{b}$ ) and probability of being correct



Breaking News: First CDF amplitude scan after the 2006 observation paper!

Performance of the flavour tagger can be determined **on data** by measuring the **amplitude of the oscillation**.

**Decay channel:**

$$B_s^0 \rightarrow D_s^- (\rightarrow \phi (\rightarrow K^+ K^-) \pi^-) \pi^+$$

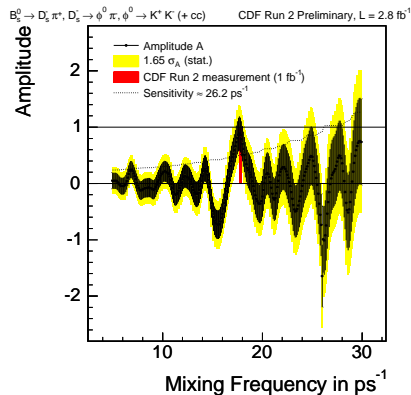
**Tagger:**

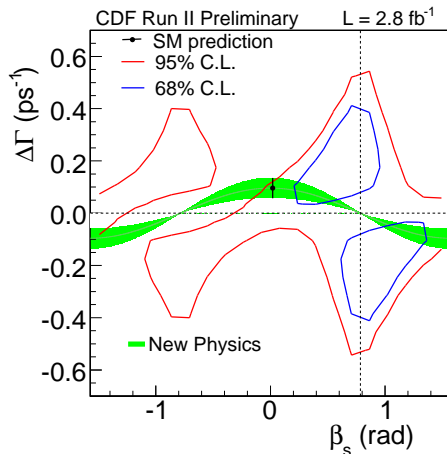
SSKT

**Amplitude Interpretation:**

$A < 1.0$ : tagger overestimates itself

$A > 1.0$ : tagger underestimates itself



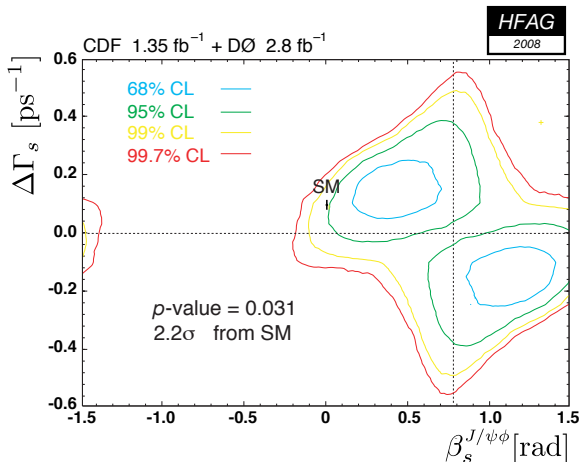


- Errors of  $\beta_s$  and  $\Delta\Gamma$  are not Gaussian  $\rightarrow$  study confidence region
- $p$  - value = 7%
- $1.8 \sigma$  from SM

<sup>2</sup> [http://www-cdf.fnal.gov/physics/new/bottom/080724.blessed-tagged-BsJpsiPhi\\_update\\_prelim/](http://www-cdf.fnal.gov/physics/new/bottom/080724.blessed-tagged-BsJpsiPhi_update_prelim/)

<sup>3</sup> arXiv:0712.2397v1 [hep-ex]

Combination of the up-to-date  $D\bar{D}$  measurement with the previous CDF measurement <sup>4</sup>:



$p\text{-value} = 3.1\%$   
2.2  $\sigma$  from SM

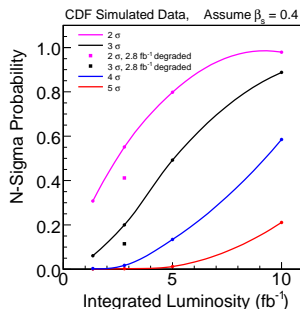
<sup>4</sup> arXiv:0808.1297v3 [hep-ex]

Evolution of the deviation from the SM:

Date	Analysis	Deviation
Dec 2007	CDF (1.35/fb)	$1.5 \sigma$
Mar 2008	DØ (2.8/fb)	$1.7 \sigma$
Jul 2008	CDF (2.8/fb)	$1.8 \sigma$
Jul 2008	Combination	$2.2 \sigma$

Fluctuations? Maybe! But the coherent pattern is interesting!

Probability to observe a non-SM  $\beta_s$  at CDF:



**Conclusions:**

**Future Plans:**

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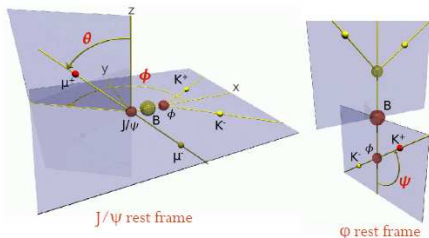
- ▶ Collect more data, perhaps even in 2011
- ▶ Inclusion of Two Track Trigger data
- ▶ Improvements in Tagging and PID
- ▶ Add other decay channels, e.g.  $B_s \rightarrow J/\psi f_0$

Thanks for your Attention  
and  
Stay tuned for Updates!

$$\begin{array}{ccc}
 B_s & \longrightarrow & J/\psi (\rightarrow \mu^+ \mu^-) \quad \phi (\rightarrow K^+ K^-) \\
 (\text{spin}=0) & & (\text{spin}=1) \quad (\text{spin}=1)
 \end{array}$$

Conservation of angular momentum lead to three different final states:

$$\begin{array}{lll}
 L = 0, 2 & (\text{s-wave}), (\text{d-wave}) & \text{CP even} \\
 L = 1 & (\text{p-wave}) & \text{CP odd}
 \end{array}$$



## Choice of basis:

Transversity basis<sup>a</sup> with corresponding decay amplitudes:

$$\begin{array}{ll}
 A_{\perp} & \text{CP odd} \\
 A_0 & \text{CP even} \\
 A_{\parallel} & \text{CP even}
 \end{array}$$

and angles

$$\vec{r} = (\Psi_T, \theta_T, \phi_T)$$

<sup>a</sup>hep-ph/9511363



Time evolution of  $B_s$  **flavor eigenstates** described by Schrödinger equation:

$$i \frac{\partial}{\partial t} \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix} = \left( \mathbf{M} - \frac{i}{2} \mathbf{\Gamma} \right) \begin{pmatrix} |B_s^0(t)\rangle \\ |\bar{B}_s^0(t)\rangle \end{pmatrix}$$

Diagonalize mass ( $M$ ) and decay matrices ( $\Gamma$ )  $\rightarrow$  **mass eigenstates**:

$$\begin{aligned} |B_s^H(t)\rangle &= p|B_s^0(t)\rangle - q|\bar{B}_s^0(t)\rangle \\ |B_s^L(t)\rangle &= p|B_s^0(t)\rangle + q|\bar{B}_s^0(t)\rangle \end{aligned}$$

Flavor eigenstates differ from mass eigenstates and mass eigenvalues are different.  $B_s$  oscillates with frequency  $\Delta m_s = m_H - m_L \approx 2|M_{12}|$

$$\Delta m_s = (17.77 \pm 0.12) ps^{-1}$$

Mass eigenstates have different decay widths:

$$\Delta\Gamma = \Gamma_L - \Gamma_H \approx 2|\Gamma_{12}|\cos(\phi_s) \text{ with } \phi_s = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right)$$

The different phases and their SM expectation value:

$$\phi_s^{SM} = \arg\left(-\frac{M_{12}}{\Gamma_{12}}\right) \approx 4 \cdot 10^{-3} \quad \text{and} \quad \beta_s^{SM} = \arg\left(-\frac{V_{ts} V_{tb}^*}{V_{cs} V_{cb}^*}\right) = 0.02$$

New Physics affects both phases by **same** quantity <sup>5</sup>:

$$\begin{aligned} 2\beta_s^{J/\Psi\phi} &= 2\beta_s^{SM} - \phi_s^{NP} \\ \phi_s^{J/\Psi\phi} &= \phi_s^{SM} + \phi_s^{NP} \end{aligned}$$

If the new physics phase  $\phi_s^{NP}$  dominates over the SM phases  $2\beta_s^{SM}$  and  $\phi_s^{SM}$   
→ neglect SM phases and obtain:

$$2\beta_s^{J/\Psi\phi} = -\phi_s^{NP} = -\phi_s^{J/\Psi\phi}$$

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<sup>5</sup> arxiv:0705.3802v2

Time and angular probability for  $B_s^0$ :

$$\begin{aligned} \frac{d^4 P(t, \vec{\rho})}{dt d\vec{\rho}} &\propto |A_0|^2 f_1(\vec{\rho}) \mathcal{T}_+(t) + |A_{||}|^2 f_2(\vec{\rho}) \mathcal{T}_+(t) \\ &+ |A_{\perp}|^2 f_3(\vec{\rho}) \mathcal{T}_-(t) + |A_0| |A_{||}| f_5(\vec{\rho}) \cos(\delta_{||}) \mathcal{T}_+(t) \\ &+ |A_{||}| |A_{\perp}| f_4(\vec{\rho}) \mathcal{U}(t) + |A_0| |A_{\perp}| f_6(\vec{\rho}) \mathcal{V}(t) \end{aligned}$$

$$\begin{aligned} \mathcal{T}_{\pm}(t) &= e^{-\Gamma t} [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &\mp \eta \sin(\Delta m_s t) \sin(2\beta_s)] \end{aligned}$$

$$\begin{aligned} \mathcal{U}(t) &= e^{-\Gamma t} [\cos(\delta_{\perp} - \delta_{||}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &+ \eta \cos(\Delta m_s t) \sin(\delta_{\perp} - \delta_{||}) \\ &- \eta \sin(\Delta m_s t) \cos(\delta_{\perp} - \delta_{||}) \cos(2\beta_s)] \end{aligned}$$

$$\begin{aligned} \mathcal{V}(t) &= e^{-\Gamma t} [\cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &+ \eta \cos(\Delta m_s t) \sin(\delta_{\perp}) \\ &- \eta \sin(\Delta m_s t) \cos(\delta_{\perp}) \cos(2\beta_s)] \end{aligned}$$

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Explanation

► Angular functions

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- ▶ Angular functions
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- ▶ Angular functions
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- ▶ Polarization amplitudes
- ▶ Time evolution
- ▶ Strong phases  
 $\delta_{\perp} = \arg(A_{\perp} A_0^*)$   
 $\delta_{||} = \arg(A_{||} A_0^*)$

$$\mathcal{T}_{\pm}(t) = e^{-\Gamma t} [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2) \mp \eta \sin(\Delta m_s t) \sin(2\beta_s)]$$

$$\begin{aligned} \mathcal{U}(t) = e^{-\Gamma t} &[\cos(\delta_{\perp} - \delta_{||}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &+ \eta \cos(\Delta m_s t) \sin(\delta_{\perp} - \delta_{||}) \\ &- \eta \sin(\Delta m_s t) \cos(\delta_{\perp} - \delta_{||}) \cos(2\beta_s)] \end{aligned}$$

$$\begin{aligned} \mathcal{V}(t) = e^{-\Gamma t} &[\cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &+ \eta \cos(\Delta m_s t) \sin(\delta_{\perp}) \\ &- \eta \sin(\Delta m_s t) \cos(\delta_{\perp}) \cos(2\beta_s)] \end{aligned}$$

Time and angular probability for  $B_s^0$ :

$$\begin{aligned} \frac{d^4 P(t, \vec{\rho})}{dt d\vec{\rho}} &\propto |A_0|^2 f_1(\vec{\rho}) \mathcal{T}_+(t) + |A_{||}|^2 f_2(\vec{\rho}) \mathcal{T}_+(t) \\ &+ |A_{\perp}|^2 f_3(\vec{\rho}) \mathcal{T}_-(t) + |A_0| |A_{||}| f_5(\vec{\rho}) \cos(\delta_{||}) \mathcal{T}_+(t) \\ &+ |A_{||}| |A_{\perp}| f_4(\vec{\rho}) \mathcal{U}(t) + |A_0| |A_{\perp}| f_6(\vec{\rho}) \mathcal{V}(t) \end{aligned}$$

Explanation

- ▶ Angular functions
- ▶ Polarization amplitudes
- ▶ Time evolution
- ▶ Strong phases  
 $\delta_{\perp} = \arg(A_{\perp} A_0^*)$   
 $\delta_{||} = \arg(A_{||} A_0^*)$
- ▶ Decay width difference

$$\mathcal{T}_{\pm}(t) = e^{-\Gamma t} [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2) \mp \eta \sin(\Delta m_s t) \sin(2\beta_s)]$$

$$\begin{aligned} \mathcal{U}(t) = e^{-\Gamma t} &[\cos(\delta_{\perp} - \delta_{||}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &+ \eta \cos(\Delta m_s t) \sin(\delta_{\perp} - \delta_{||}) \\ &- \eta \sin(\Delta m_s t) \cos(\delta_{\perp} - \delta_{||}) \cos(2\beta_s)] \end{aligned}$$

$$\begin{aligned} \mathcal{V}(t) = e^{-\Gamma t} &[\cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &+ \eta \cos(\Delta m_s t) \sin(\delta_{\perp}) \\ &- \eta \sin(\Delta m_s t) \cos(\delta_{\perp}) \cos(2\beta_s)] \end{aligned}$$



Time and angular probability for  $B_s^0$ :

$$\begin{aligned} \frac{d^4 P(t, \vec{\rho})}{dt d\vec{\rho}} &\propto |A_0|^2 f_1(\vec{\rho}) \mathcal{T}_+(t) + |A_{||}|^2 f_2(\vec{\rho}) \mathcal{T}_+(t) \\ &+ |A_{\perp}|^2 f_3(\vec{\rho}) \mathcal{T}_-(t) + |A_0| |A_{||}| f_5(\vec{\rho}) \cos(\delta_{||}) \mathcal{T}_+(t) \\ &+ |A_{||}| |A_{\perp}| f_4(\vec{\rho}) \mathcal{U}(t) + |A_0| |A_{\perp}| f_6(\vec{\rho}) \mathcal{V}(t) \end{aligned}$$

Explanation

- ▶ Angular functions
- ▶ Polarization amplitudes
- ▶ Time evolution
- ▶ Strong phases  
 $\delta_{\perp} = \arg(A_{\perp} A_0^*)$   
 $\delta_{||} = \arg(A_{||} A_0^*)$
- ▶ Decay width difference
- ▶ CPV Phase

$$\mathcal{T}_{\pm}(t) = e^{-\Gamma t} [\cosh(\Delta\Gamma t/2) \mp \cos(2\beta_s) \sinh(\Delta\Gamma t/2) \mp \eta \sin(\Delta m_s t) \sin(2\beta_s)]$$

$$\begin{aligned} \mathcal{U}(t) = e^{-\Gamma t} &[\cos(\delta_{\perp} - \delta_{||}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &+ \eta \cos(\Delta m_s t) \sin(\delta_{\perp} - \delta_{||}) \\ &- \eta \sin(\Delta m_s t) \cos(\delta_{\perp} - \delta_{||}) \cos(2\beta_s)] \end{aligned}$$

$$\begin{aligned} \mathcal{V}(t) = e^{-\Gamma t} &[\cos(\delta_{\perp}) \sin(2\beta_s) \sinh(\Delta\Gamma t/2) \\ &+ \eta \cos(\Delta m_s t) \sin(\delta_{\perp}) \\ &- \eta \sin(\Delta m_s t) \cos(\delta_{\perp}) \cos(2\beta_s)] \end{aligned}$$

$$f_1(\vec{\rho}) = 2\cos^2\Psi_T(1 - \sin^2\theta_T\cos^2\phi_T)$$

$$f_2(\vec{\rho}) = \sin^2\Psi_T(1 - \sin^2\theta_T\sin^2\phi_T)$$

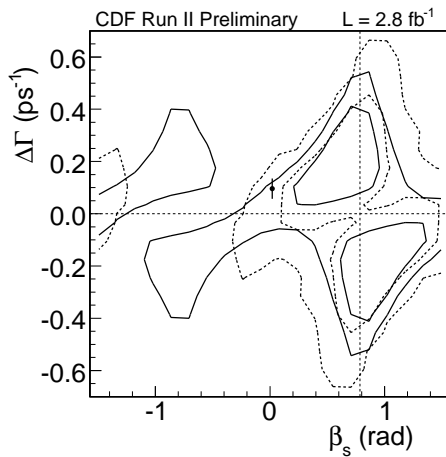
$$f_3(\vec{\rho}) = \sin^2\Psi_T\sin^2\theta_T$$

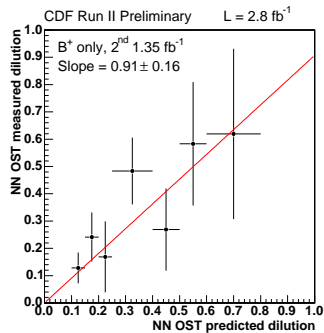
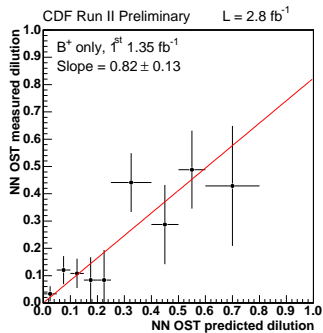
$$f_4(\vec{\rho}) = -\sin^2\Psi_T\sin 2\theta_T\sin\phi_T$$

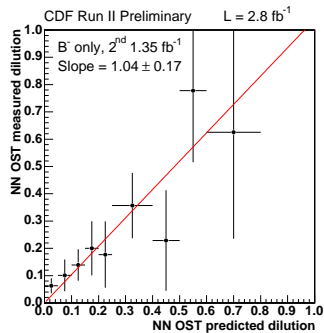
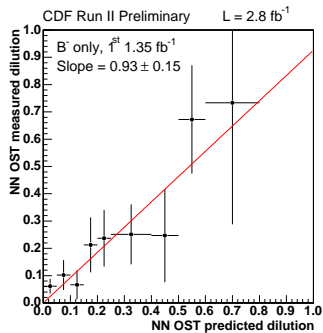
$$f_5(\vec{\rho}) = 1/\sqrt{2}\sin 2\Psi_T\sin^2\theta_T\sin 2\phi_T$$

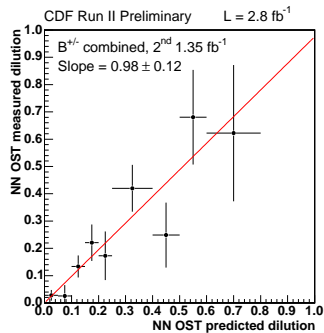
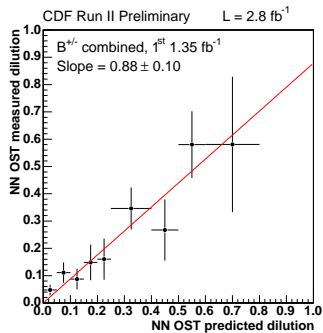
$$f_6(\vec{\rho}) = 1/\sqrt{2}\sin 2\Psi_T\sin 2\theta_T\cos\phi_T$$

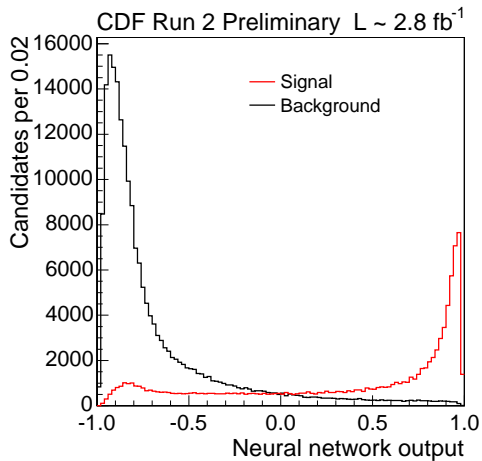
## 2D likelihood profile comparison with published result

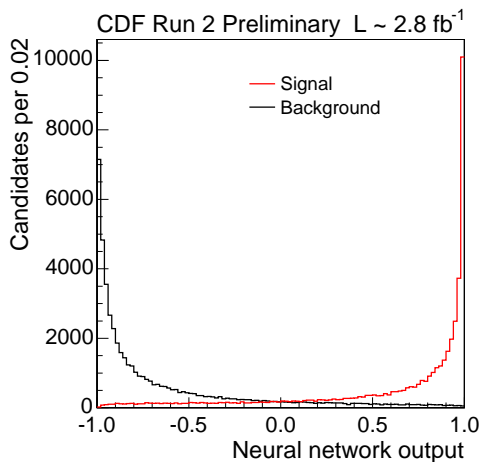














# Invariant Mass of $B^+$

