

Flavour Theory (EPS 2009)

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Good Afternoon !

Overture

(A Novel Look at Short Distance Scales)

**Frontiers of
Elementary Particle
Physics**



**Search for Physics Laws
at very short distance scales**

**Heisenberg
Principle**

**To test 10^{-18} m
we need $E \cong 200$ GeV**

Frontiers of Elementary Particle Physics

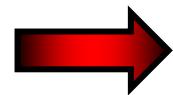


Search for Physics Laws
at very short distance scales

Heisenberg
Principle

: To test 10^{-18} m
we need $E \cong 200$ GeV

LHC
 $E \approx 4$ TeV



Tests at
 $5 \cdot 10^{-20}$ m
possible

Frontiers of Elementary Particle Physics



Search for Physics Laws
at very short distance scales

Heisenberg
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 $5 \cdot 10^{-20}$ m
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Unlikely that we can do better
before 2046 through high
energy collider experiments.

Frontiers of Elementary Particle Physics



Search for Physics Laws at very short distance scales

Heisenberg Principle

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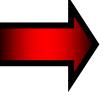
Tests at $5 \cdot 10^{-20}$ m possible

Unlikely that we can do better before 2046 through high energy collider experiments.

Flavour Physics governed by Quantum Fluctuations is sensitive to $E \approx 200$ TeV and even higher energy scales



Tests at 10^{-21} m and shorter scales possible



Frontiers in testing very very short distance scales belong to Flavour Physics

but

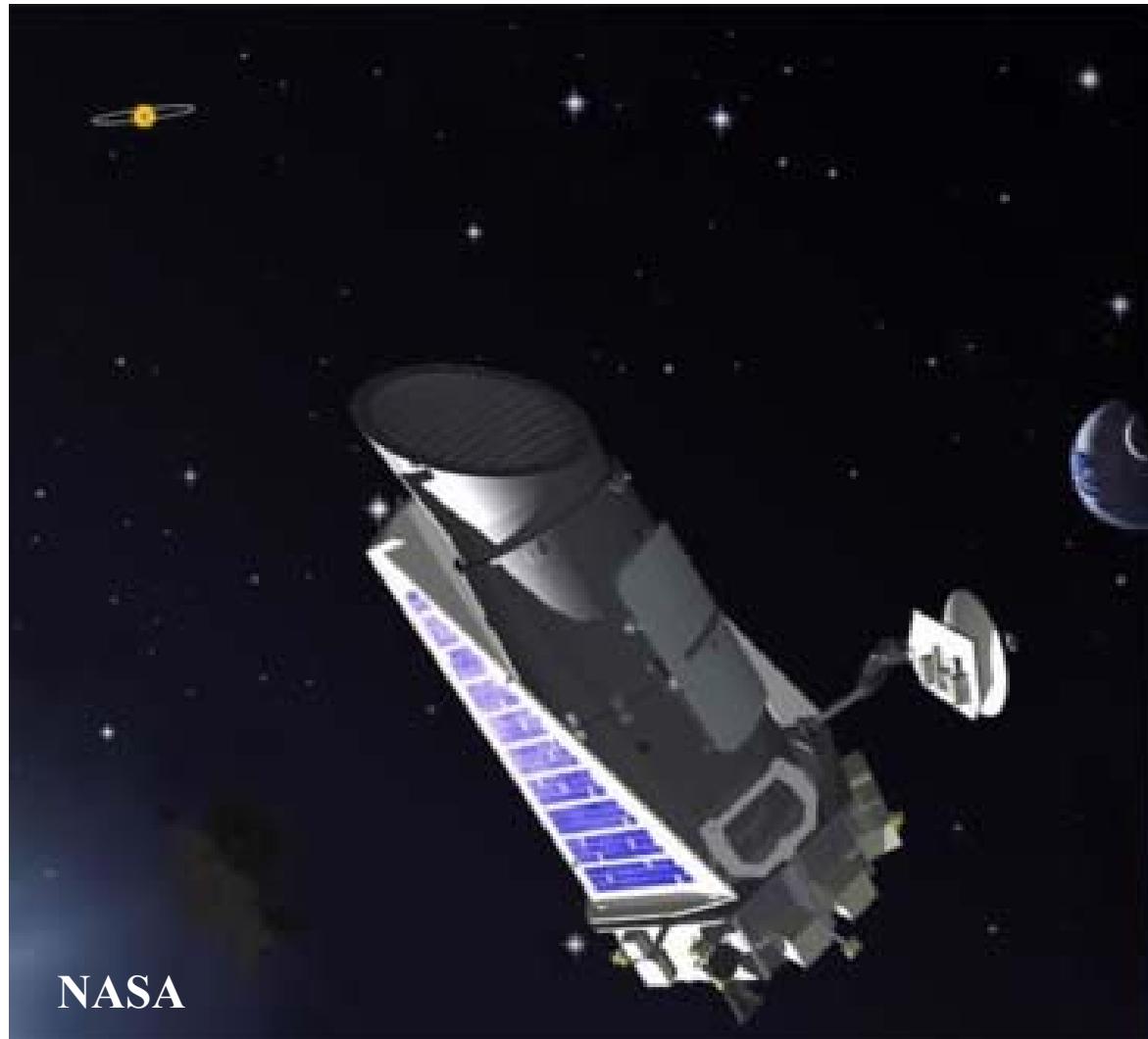
Very high precision required !!

Usual Picture of the Month

(CERN Courier)



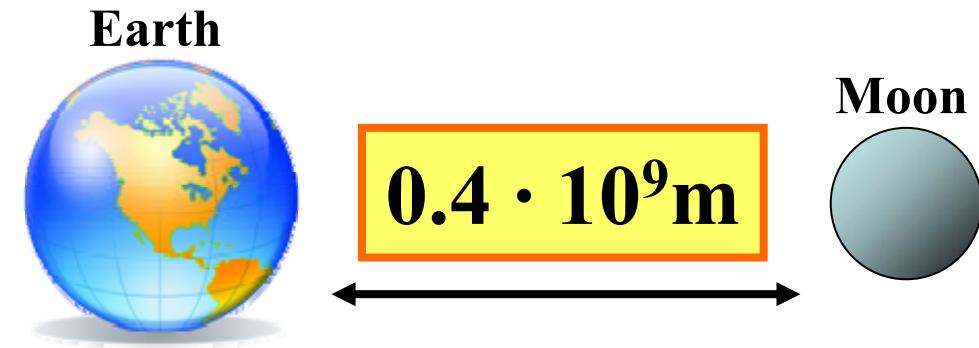
Kepler Searching for new Planetary Systems and New Lifes



March 2009

Dual Picture of Short Distances

10^9m



3 light seconds

Dual Picture of Short Distances

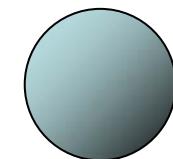
10^9m



Earth

3 light seconds

Moon



$0.4 \cdot 10^9\text{m}$

10^{18}m

105 light years

Dual Picture of Short Distances

10^9m



3 light seconds

$0.4 \cdot 10^9\text{m}$

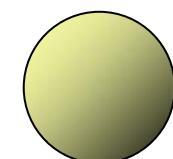


10^{18}m



105 light years

Beta Ceti



(in the constellation
Cetus)

92 light years



Cetus



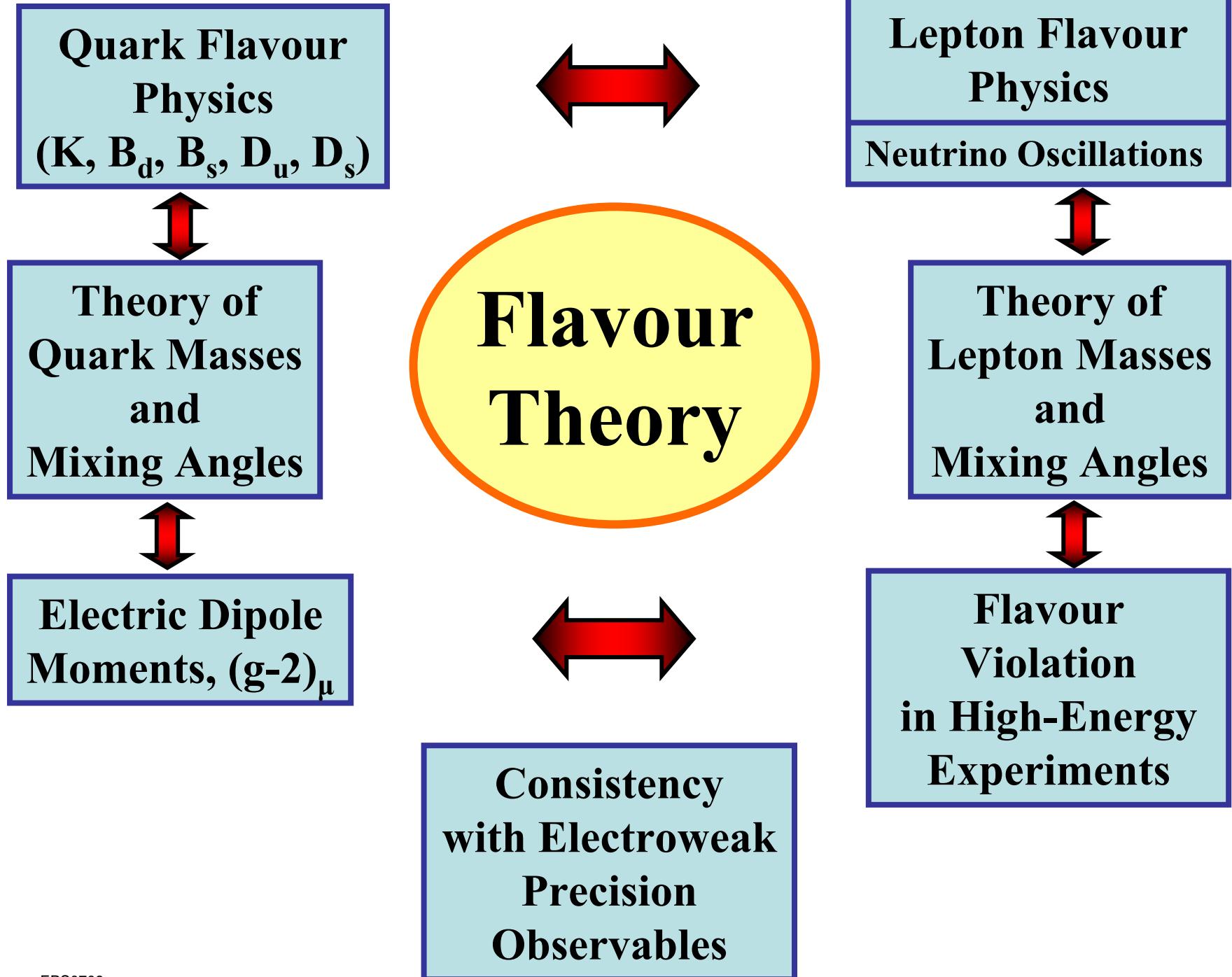
Mira

© AlltheSky.com

Beta Ceti



NASA/CXC 2004



Yet

Impressive Success of the CKM Picture of Flavour Changing Interactions

(GIM)

- 1.** Several tensions between the flavour data and the SM exist.
- 2.** Hierarchies in Fermion Masses and Mixing Angles have to be understood with the help of some New Physics (NP).
- 3.** There is still a lot of room for NP contributions, in particular in rare decays of mesons and leptons, in \mathcal{CP} flavour violating transitions and EDM's.

Are **1.** - **3.** somehow related ?

Will we see any footprints of this NP in 2010's ?

Strategy for the Next 36 Min ± Possible Tensions

1.

Theoretical Framework (~ 9 min)

2.

20 Goals in Flavour Physics for the Next Decade (~ 5 min)

3.

Waiting for Signals of New Physics in FCNC Processes (~ 20 min)

4.

Final Messages (~ 2 min)

See also talks by G. Punzi, A. Bevian and A. Golutvin and parallel session talks

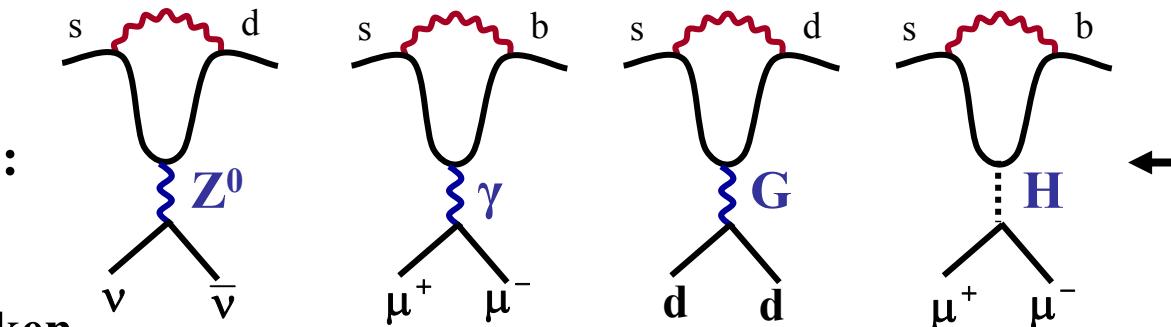
1.

Theoretical Framework

Basic Diagrams in FCNC Processes

Penguin Family

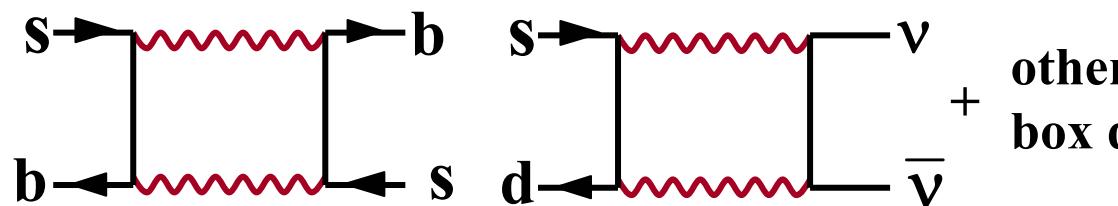
↑
(GIM broken
at one loop)



New Physics
enters here

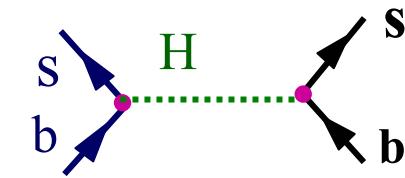
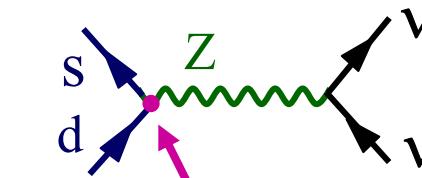
Similar
diagrams
in LFV
and EDM's

Box
Diagrams



Tree
Diagrams

(GIM broken
at tree level)

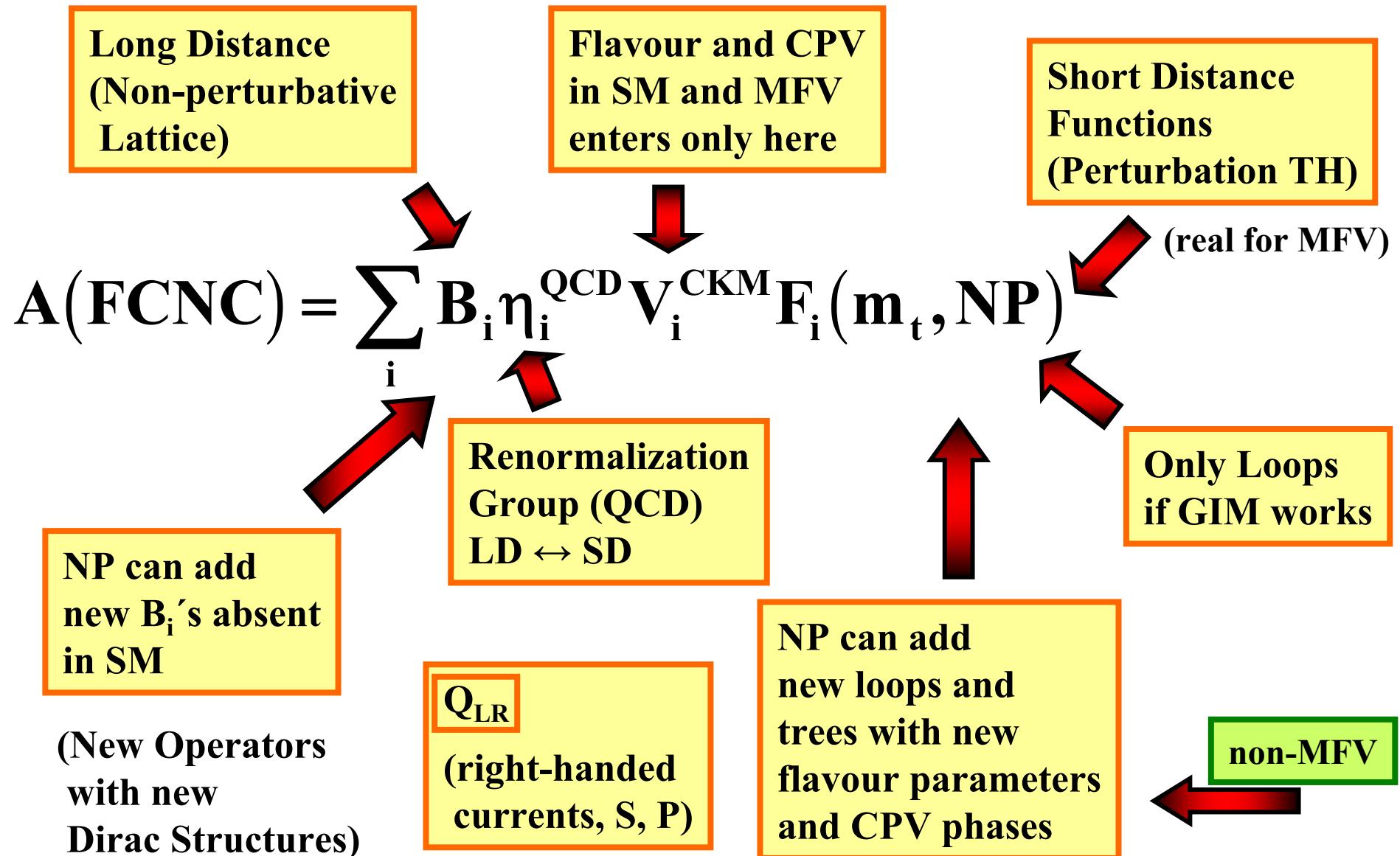


RS

Generated
through
mixing with
New Gauge
Bosons

Double Higgs Penguin
in SUSY

Master Formula for FCNC Amplitudes



Most popular BSM Directions

CMFV

(constrained MFV)

MFV

(NMFV)
(GMFV)

LHT

(Littlest Higgs
with T-parity)

SUSY

(flavour models)

Z'

(Langacker...)

RS

(Randall-Sundrum)
(Warped Extra Dimensions)

4th G

(Hou..., Soni..., Lenz...)

**Vector-Like
Quarks**

(Branco...,
del Aguila)

Non-Decoupling



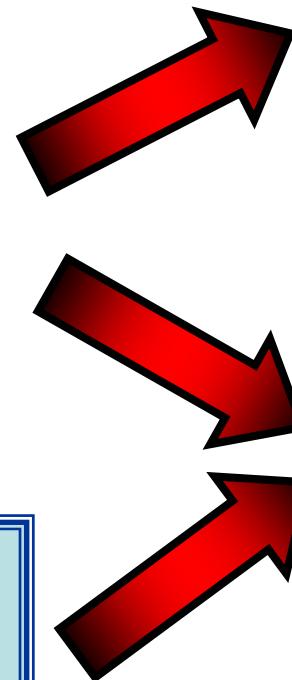
**New gauge bosons, fermions, scalars in loops
and even trees with often non-CKM interactions.**

Little Hierarchy Problem

Electroweak Precision Tests

+

Agreement of the CKM Picture of Flavour and CP Violation with existing Data (FCNC)



(generic)

$\Lambda_{\text{NP}} \approx 5 \text{ TeV}$

Very strong Constraints on Physics beyond SM with scales $O(1 \text{ TeV})$

Necessary to solve the hierarchy problem



$\Lambda_{\text{NP}} \approx 1000 \text{ TeV}$

(generic)

$(M_{\text{PLANCK}} \gg \Lambda_{\text{EW}})$

Message 1

: **New Physics at TeV-Scale must have a non-Generic Flavour Structure**

Message 2

: **Protection Mechanisms to suppress FCNCs generated by TeV-Scale New Physics required**

Ciuchini et al
Isidori et al
Agashe et al
+50



MFV

GIM

RS-GIM

T-Parity

R-Parity

Alignment

Degeneracy

Flavour Symmetries
(abelian, non-abelian)

Custodial Symmetries

(continuous, discrete)

Minimal Flavour Violation (MFV)

MFV

SM Yukawa Couplings are the only breaking sources of the $SU(3)^5$ flavour symmetry of the low-energy effective theory

(Y_t, Y_b)

D'Ambrosio, Guidice, Isidori, Strumia (02) Chivukula, Georgi (87)



CKM the only source of Flavour Violation
but for $Y_t \approx Y_b$ new operators could enter

CP
SM-like

CMFV

Operator structure of
SM remains



AJB, Gambino, Gorbahn, Jäger, Silvestrini (00)
Ali, London

VERY STRONG
RELATIONS
BETWEEN
K and B Physics
and generally
 $\Delta F=2$ and $\Delta F=1$
FCNC Processes

Related Studies : Ratz et al (08)
Smith et al (08)
Zupan et al (09)

Spurion Technology

Nir et al.
AGIS
Feldmann, Mannel

also beyond
MFV

Dominant New Flavour and CP Violating Interactions at 0(μ_{NP})

SUSY:

GIM

LHT:

RS:

RS-GIM

- a) Misalignment of quark- and squark mass matrices, similarly for lepton sector
- b) Effects enhanced at large $\tan\beta$: δ_{ij}^{AB}

Typical scales(200-1000 GeV)

New flavour and CP violating mixing matrices in the interactions of SM fermions with mirror fermions mediated by W_H, Z_H, A_H

Typical scales (500-1000 GeV)

New Heavy Gauge Bosons (KK)
New Heavy Vector-like Fermions (KK)

Tree Level FCNC's mediated by KK Gluon ($\Delta F=2$) and Z($\Delta F=1$)

(Typical scales $M_{KK} \approx 2-3$ TeV)

Related to the explanation of hierarchies in masses and mixings

Battle in the Bulk to save RS with $M_{KK} \sim 2\text{-}3 \text{ TeV}$

“Warped Flavour”

Some
fine tuning
required

Blanke et al

Custodial Symmetries, Flavour Symmetries, etc.

(some related to EWPT, some related to FCNC's)

Ghergetta, Pomarol; Huber, Shafi (03)

Agashe, Delgado, May, Sundrum (03)

Csaki, Grojean, Pilo, Terning (03)

Agashe, Contino, Da Rold, Pomarol (06)

Agashe, Perez, Soni (06)

Cacciapaglia, Csaki, Weiler et al. (07)

Csaki, Falkowski, Weiler (08)

Fitzpatrick, Perez, Randall (07)

Santiago (08)

Casagrande, Goertz, Haisch, Neubert (08)

Blanke, AJB, Duling, Gori, Weiler (08)

Albrecht, Blanke, AJB, Duling, Gemmeler (09)

AJB, Duling, Gori (09)

Csaki, Grossman, Perez, Surujon, Weiler (09)

Agashe, Azatov, Zhu (08)

Azatov, Toharia, Zhu (09)

Agashe, Contino (09)

Gedalia, Isidori, Perez (09)

Csaki, Curtin (09)

Q_{LR} and dipole operators
most problematic

ε_K , $B \rightarrow X_s \gamma, \mu \rightarrow e \gamma$, d_n
 ε'/ε



Quark flavor in RS:
Overtime

Ulrich Haisch

2 x 2 Flavour Matrix of Basic NP Scenarios

(AJB, hep-ph/0101336, Erice)

	SM Operators	+ Additional Operators
CKM	A CMFV (Y_t) SM, 2 HDM at low $\tan\beta$ LH without T-parity Universal flat ED	B MFV (Y_t, Y_b) MSSM with MFV 2 HDM at large $\tan\beta$
New Flavour (CP) Violating Interactions	C beyond CMFV LH with T-parity Some Z'-models 4 th generation	D beyond MFV MSSM with $(\delta_{ij})_{AB} \neq 0$ RS, Other Z'-models, LR Models, NMfv

2.

20 Goals in Flavour Physics for the Next Decade

1.

**Determination
of $|V_{us}|$, $|V_{cb}|$,
 $|V_{ub}|$ and γ
from
Tree Level Decays**

2.

**Improved Lattice
Calculations
of
 $F_{B_{s,d}}$, B_i -parameters**

3.

**Is ε_K (1964)
consistent with
 $S_{\psi K_S} = \sin 2\beta$
(2001)
within the SM?**

4.

**Is $S_{\psi\phi}$
much larger
than
 $(S_{\psi\phi})_{SM} \approx 0.035$?**

(CP in $B_s \rightarrow \psi\phi$) (A_{SL}^s)

5.

**Clarification of
few puzzles in
Non-Leptonic
Decays
 $(S_{\phi K_S}, S_{\pi^0 K_S}, \pi K, \dots)$**

6.

**Discovery of
 $B_s \rightarrow \mu^+ \mu^-$
and
 $B_d \rightarrow \mu^+ \mu^-$**

**(Fleischer,..Buchalla,
Gronau, London, ...)**

7.**Improved TH+EXP**

$$B \rightarrow X_{s,d} \gamma$$

$$B \rightarrow K^*(\rho) \gamma$$

$$A_{CP}^{\text{dir}}(B \rightarrow X_s \gamma)$$

(Misiak,...)

8.

$B \rightarrow X_s l^+ l^-$
 $B \rightarrow K^* l^+ l^-$
 in particular
 various angular
 observables
 (sensitive to NP)

(Hurth; Straub)

9.

$B^+ \rightarrow \tau^+ \nu$
 $B^+ \rightarrow D^0 \tau^+ \nu$
 H^\pm effects in
Tree Level Decays

(Hou..., Recksiegel,...
 Isidori, ... Westhoff,...)**10.****Rare K Decays**

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

$$K^0 \rightarrow \pi^0 \nu \bar{\nu}$$

$$K_L \rightarrow \pi^0 \mu^+ \mu^-$$

$$K_L \rightarrow \pi^0 e^+ e^-$$

(TH very clean,
 sensitive to NP)**11.****Rare B Decays**

$$B \rightarrow X_s \nu \bar{\nu}$$

$$B \rightarrow K^* \nu \bar{\nu}$$

$$B \rightarrow K \nu \bar{\nu}$$

(Straub) (sensitive to
 right-handed currents)**12.**

Lattice
Calculations of
Penguin hadronic
matrix elements
 for ϵ'/ϵ
 (NA31, NA48, KTeV)

(Very sensitive to
 NP in the EW-Penguins)

13.

\mathcal{CP} in Charm
Decays and

$$\begin{aligned} D^+ &\rightarrow l^+ \nu, D_s^+ \rightarrow l^+ \nu \\ D^0 &\rightarrow \mu^+ \mu^- \end{aligned}$$

(Bigi; Grossman,..Golowich..
Kronfeld)

14.

Search for \mathcal{CP}
in the Lepton
Sector and
 θ_{13}

(Feruglio,...Antusch,...
Branco,...Hagedorn)

15.

Tests of
 $\mu\text{-}e$, $\mu\text{-}\tau$
universalities
in
 $K^+ \rightarrow l^+ \nu, B^+ \rightarrow l^+ \nu$

(Isidori,...Paradisi, ...)

16.

Lepton Flavour
Violation

$$\begin{aligned} \mu &\rightarrow e\gamma, \tau \rightarrow \mu\gamma, \\ \tau &\rightarrow e\gamma \\ \mu &\rightarrow 3e, \tau \rightarrow 3e \\ \tau &\rightarrow 3\mu \end{aligned}$$

(Hisano,...Raidal,...)

17.

Electric Dipole
Moments
of
neutron, leptons
(d_n, d_e)

(Nagai, ...Paradisi,...)

18.

Clarification
of
($g\text{-}2$) $_\mu$
Anomaly

(Passera,...Jegerlehner,
Czarnecki,...de Rafael)

19.

**Tests of Flavour
Violation in
High Energy
Processes**

(Hiller, Nir,...)

19.

Tests of Flavour Violation in High Energy Processes

(Hiller, Nir,...)

20.

Construction of a New SM

19.

**Tests of Flavour
Violation in
High Energy
Processes**

(Hiller, Nir,...)

20.

**Construction
of
a New SM**

21.

22.

23.

24.

3.

Waiting for Signals of New Physics in FCNC Processes

3.

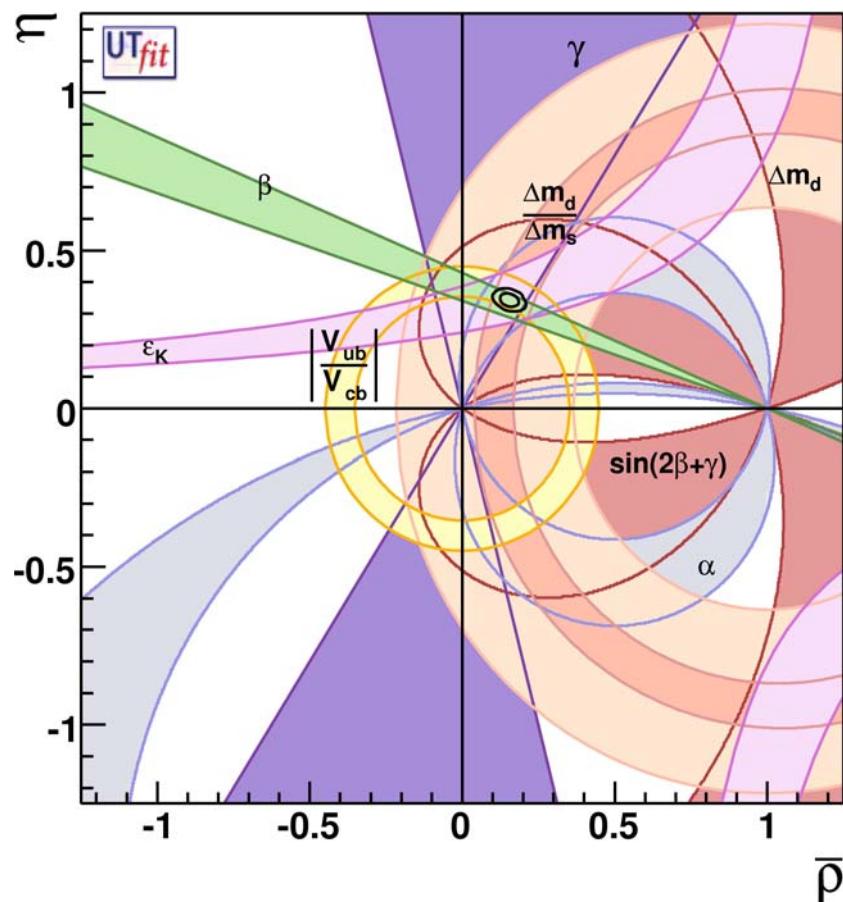
Waiting for Signals of New Physics in FCNC Processes

**Many Thanks for inviting me to give
this Talk !!**

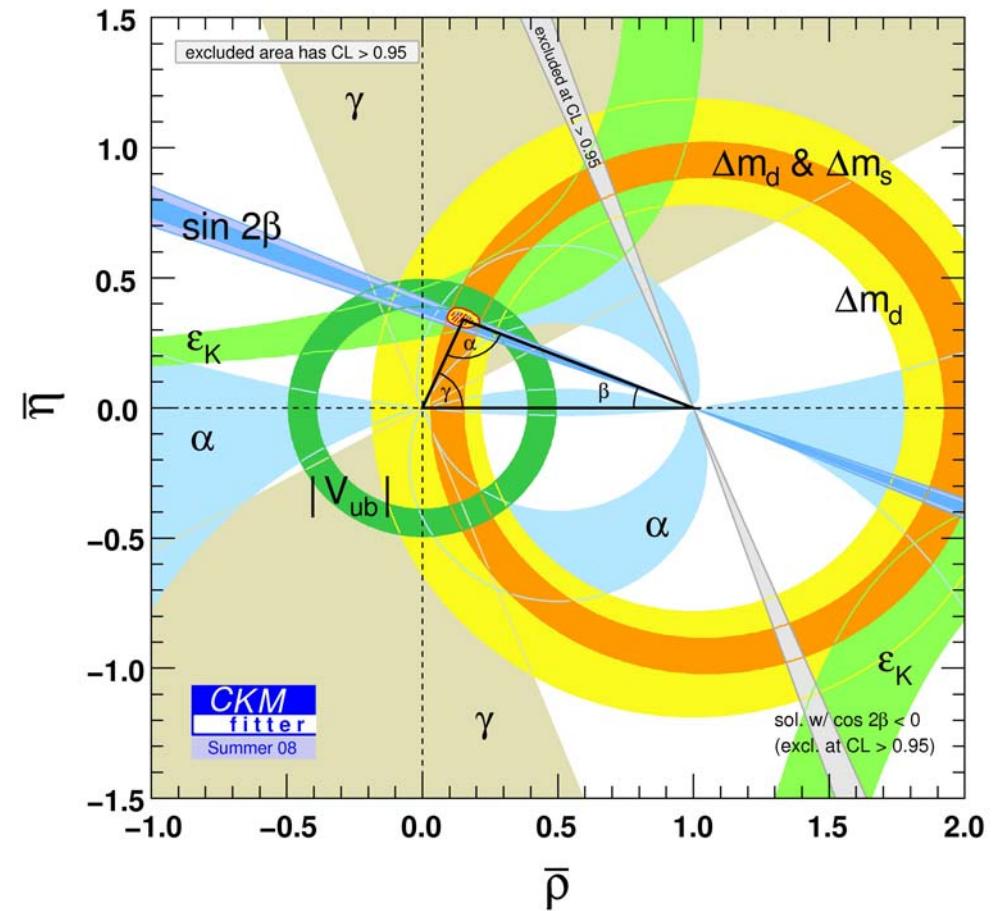
Unitarity Triangle Fits

(Icons of Flavour Physics)

UT fit



CKM fitter



(R_b, γ)
Reference UT
(Goto et al)

(coming
decade)

Unitarity Triangle

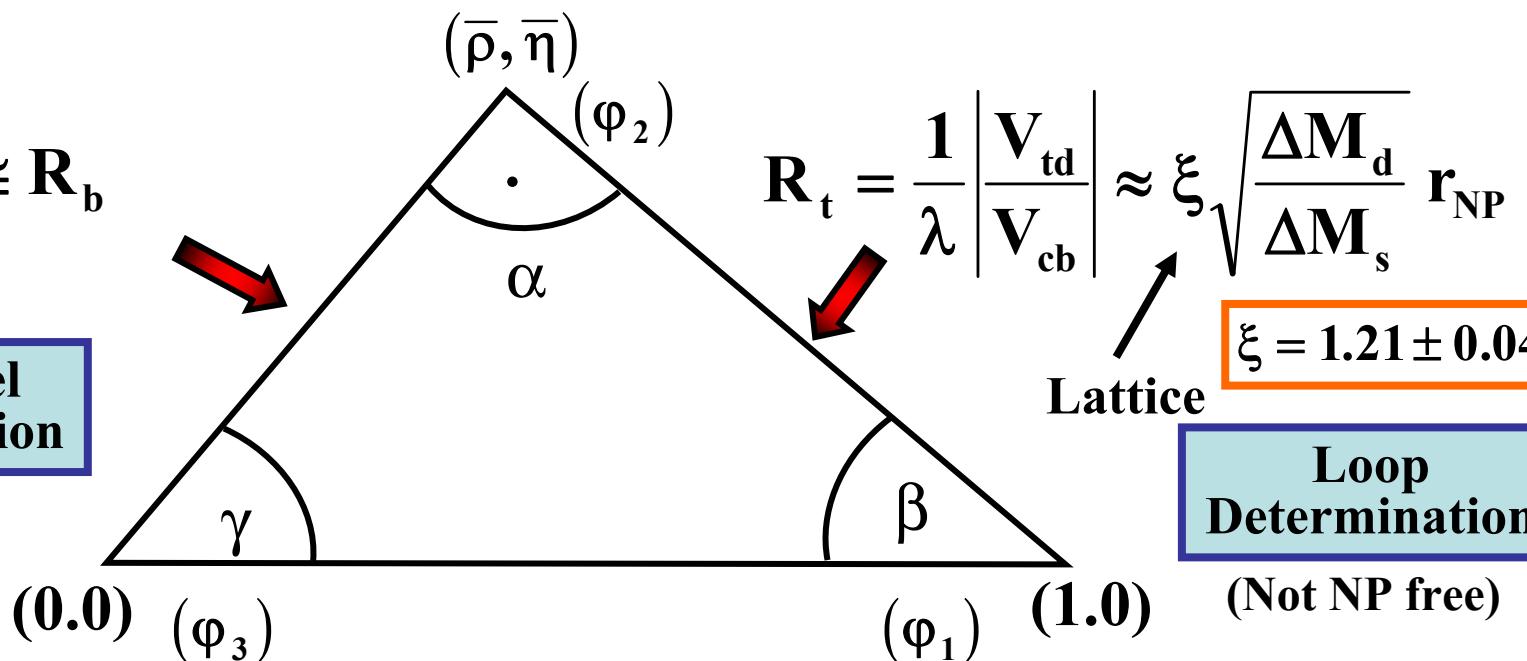
$$\alpha ? = 90^\circ$$

(this
decade)

R_t, β
Universal UT
of CMFV
(BGGJS, BBGT)
 $(\phi_{NP}=0, r_{NP}=1)$

$$\frac{1}{\lambda} \left| \frac{V_{ub}}{V_{cb}} \right| \approx R_b$$

Tree Level
Determination
(NP free)



$$R_t = \frac{1}{\lambda} \left| \frac{V_{td}}{V_{cb}} \right| \approx \xi \sqrt{\frac{\Delta M_d}{\Delta M_s}} r_{NP}$$

$$\xi = 1.21 \pm 0.04$$

Lattice

Loop
Determination
(Not NP free)

Flavour
Matrix

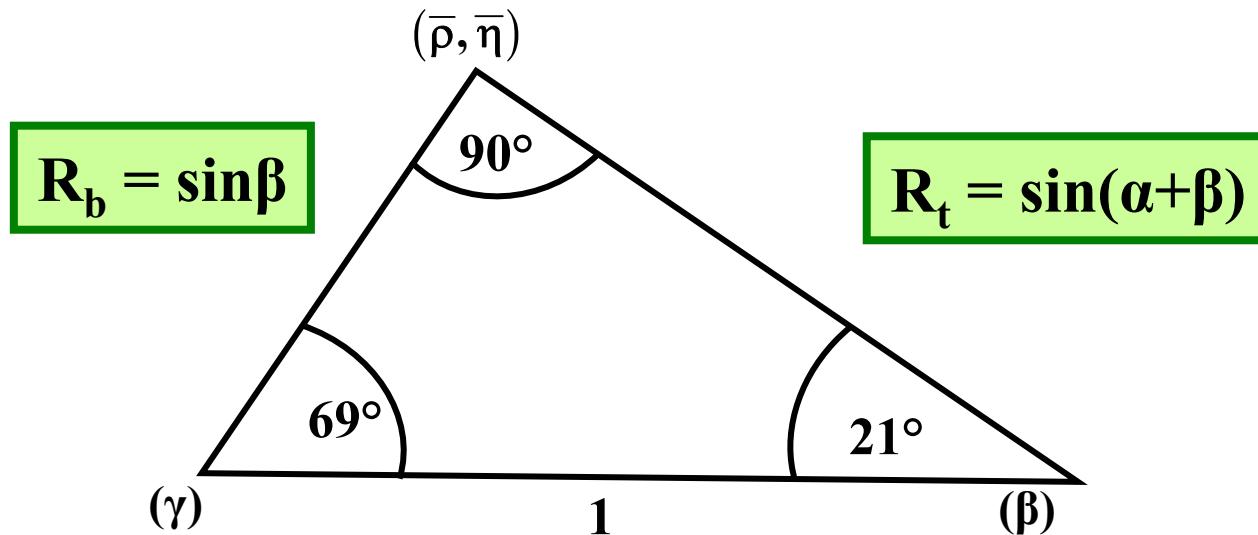
$\phi_{NP} = 0$	$\phi_{NP} = 0$
$r_{NP} = 1$	$r_{NP} \neq 1$
$\phi_{NP} \neq 0$	$\phi_{NP} \neq 0$
$r_{NP} \neq 1$	$r_{NP} \neq 1$

$$S_{\psi K_s} = \sin(2\beta + 2\phi_{NP})$$

Unitarity Triangle in LO Approximation

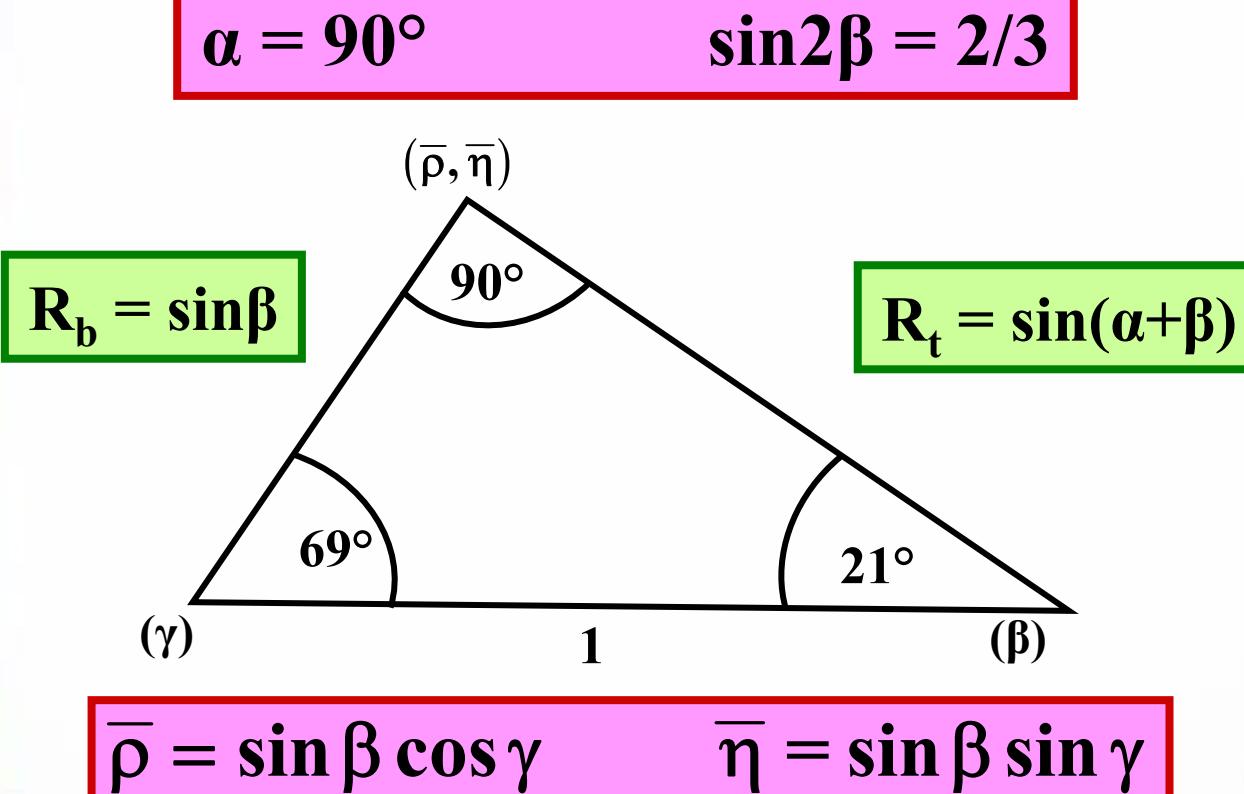
$$\alpha = 90^\circ$$

$$\sin 2\beta = 2/3$$



$$\bar{\rho} = \sin \beta \cos \gamma \quad \bar{\eta} = \sin \beta \sin \gamma$$

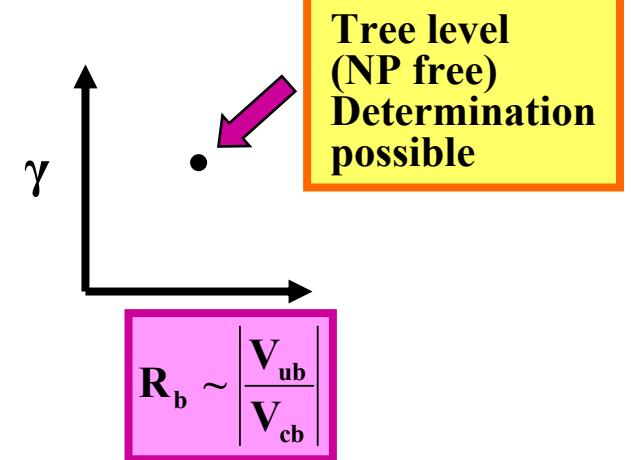
Unitarity Triangle in LO Approximation



Search for New Physics in 2010's

★ To study transparently possible tensions between ε_K , $\sin 2\beta$, V_{ub} , γ , $\Delta M_d / \Delta M_s$

Leave
 $(\bar{\rho}, \bar{\eta})$ plane
 Go to



★ To search for NP in rare K, B, B_s , D decays,
 \not{CP} in B_s , D decays,
 Lepton Flavour Violations

Go to

Specific Plots (Correlations)

- $Br(K_L \rightarrow \pi^0 \bar{v}v)$ vs $Br(K^+ \rightarrow \pi^+ \bar{v}v)$
- $Br(B_s \rightarrow \mu^+ \mu^-)$ vs $S_{\psi\phi}$
- $Br(B_s \rightarrow \mu^+ \mu^-)$ vs $Br(B_d \rightarrow \mu^+ \mu^-)$
- $Br(K^+ \rightarrow \pi^+ \bar{v}v)$ vs $S_{\psi\phi}$
- d_n vs $S_{\phi K_s}$
- $A_{CP}(B \rightarrow X_S \gamma)$ vs $S_{\phi K_s}$
- $Br(\tau \rightarrow \mu \gamma)$ vs $\Delta(g-2)_\mu$
- $Br(\tau \rightarrow \mu \mu \mu)$ vs $Br(\tau \rightarrow \mu \gamma)$
- $Br(\mu \rightarrow 3e)$ vs $Br(\mu \rightarrow e \gamma)$

★ Correlations will be crucial to distinguish various NP scenarios

Can SM describe simultaneously \mathcal{CP} in K and B_d Systems?

$$|\varepsilon_K|^{\text{SM}} \sim \kappa_\varepsilon \hat{B}_K |V_{cb}|^2 \left(\frac{1}{2} |V_{cb}|^2 R_t^2 \underbrace{\sin 2\beta}_{\text{(NLO)}} \eta_{tt}^{\text{QCD}} S_0(x_t) + F \underbrace{(\eta_{ct}^{\text{QCD}}, \eta_{cc}^{\text{QCD}}, m_c, \dots)}_{\text{(NLO)}} \right)$$

BJW (90)

HN (94)

2009
News

★ $\hat{B}_K \cong 0.72 \pm 0.03$

(precise and lower by
~10% vs 2007)

RBC-UKQCD
Aubin et al.
ETMC

★ $\kappa_\varepsilon \cong 0.92 \pm 0.02$

(correction neglected
in the past)

AJB + Guadagnoli (08)
(Nierste; Vysotsky)

Large N
 $\hat{B}_K = 0.75$

BBG (87)

★ NNLO QCD
calculation of η_{cc}, η_{ct}

Brod + Gorbahn (09)

(BG)

$$|\varepsilon_K^{\text{SM}}| = (1.80 \pm 0.22) \cdot 10^{-3}$$

$$|\varepsilon_{\text{exp}}| = (2.223 \pm 0.012) \cdot 10^{-3}$$

(BaBar
Belle)

using $(\sin 2\beta)_{\psi K_s} = 0.672 \pm 0.023$

(NA48, KLOE, KTeV)

Possible Solutions to ε_K - Anomaly

$$|\varepsilon_K|^{\text{SM}} \sim \kappa_\varepsilon \hat{B}_K |V_{cb}|^2 \left(\frac{1}{2} |V_{cb}|^2 R_t^2 \sin 2\beta \eta_{tt}^{\text{QCD}} S_0(x_t) + F(\eta_{ct}^{\text{QCD}}, \eta_{cc}^{\text{QCD}}, m_c, \dots) \right)$$

1.

Add New Physics to ε_K

$$\text{CMFV } S_0(x_t) \rightarrow S_0(x_t) + \Delta S_0^{\text{NP}}$$

or simply $\Delta\varepsilon_k$ (Non-MFV)

AJB
Guadagnoli

2.

$$\text{Increase } \sin 2\beta \cong 0.67 \Rightarrow 0.85$$

$$S_{\psi K_s} = \sin(2\beta + 2\phi_{\text{NP}})$$

(Ulfit; BBGT; Ball, Fleischer;
Branco et al)

$$\phi_{\text{NP}} \cong -8.1^\circ$$

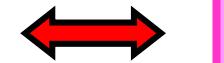
$$\text{Large } |V_{ub}|$$

Lunghi
Soni

Super-B

3.

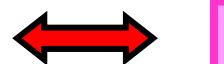
$$\text{Increase } R_t \rightarrow \gamma = \delta_{\text{CKM}} \approx 67^\circ \Rightarrow 82^\circ$$



LHC

4.

$$\text{Increase } |V_{cb}| \approx (41.2 \cdot 10^{-3}) \Rightarrow (43.5 \cdot 10^{-3})$$



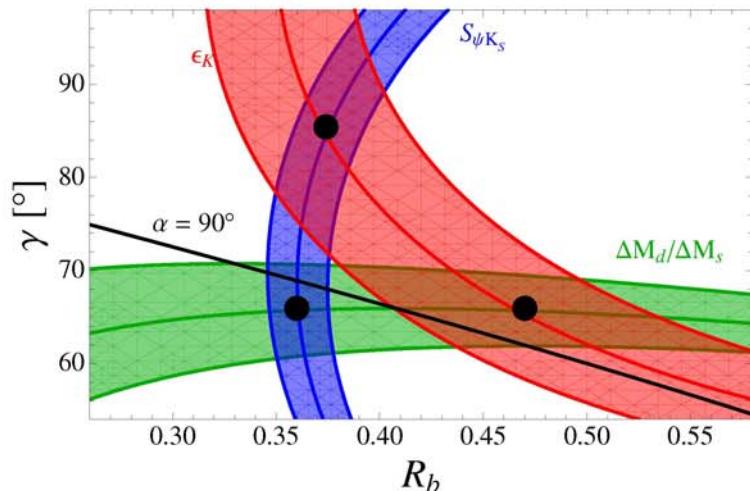
Super-B

AJB, Parodi, Stocchi (2002)
 Altmannshofer, AJB,
 Guadagnoli (2007)

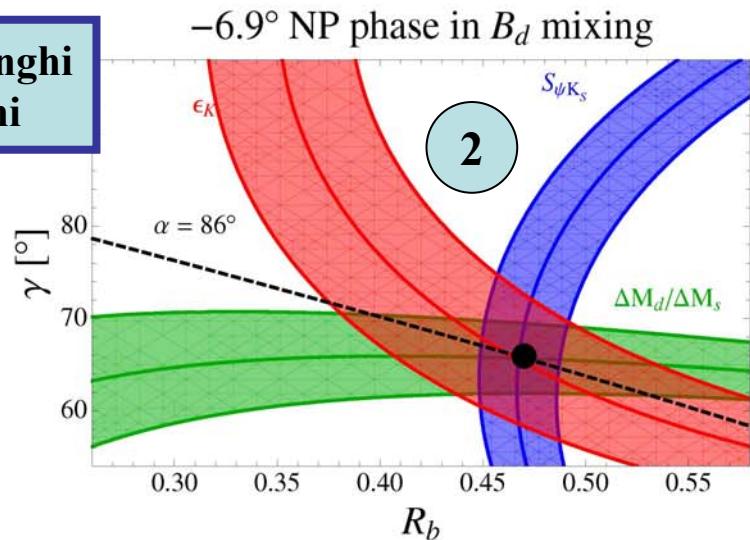
The R_b - γ Plane

Altmannshofer, AJB, Gori,
 Paradisi, Straub (2009)

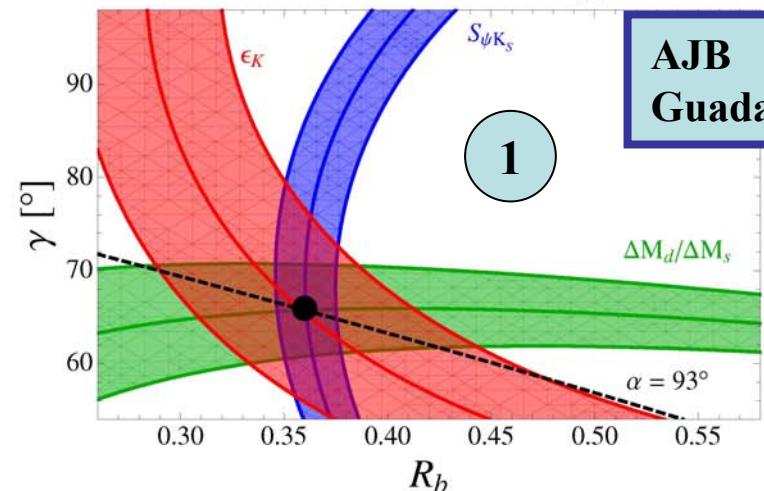
Situation in the SM



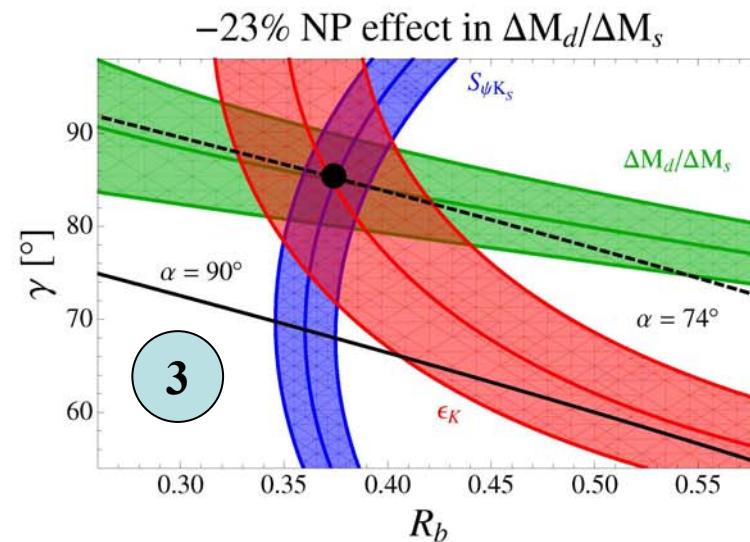
Lunghi
 Soni



+25% NP effect in ϵ_K



AJB
 Guadagnoli



$$K^+ \rightarrow \pi^+ \nu\bar{\nu} \text{ and } K_L \rightarrow \pi^0 \nu\bar{\nu} \text{ (Z°-penguins)}$$

(TH cleanest FCNC decays in Quark Sector)

Extensive
TH efforts
over
20 years

: Buchalla, AJB; Misiak, Urban (NLO QCD)
AJB, Gorbahn, Haisch, Nierste (NNLO QCD)
Brod, Gorbahn (QED, EW two loop)
Isidori, Mescia, Smith (several LD analyses)
Buchalla, Isidori (LD in $K_L \rightarrow \pi^0 \nu\bar{\nu}$)

$$\frac{\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu})}{\text{Br}(K_L \rightarrow \pi^0 \nu\bar{\nu})} = 3.2 \pm 0.2$$

SM : $\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu}) = (8.4 \pm 0.7) \cdot 10^{-11}$

$$\text{Br}(K_L \rightarrow \pi^0 \nu\bar{\nu}) = (2.6 \pm 0.4) \cdot 10^{-11}$$

Exp : $\text{Br}(K^+ \rightarrow \pi^+ \nu\bar{\nu}) = \left(17^{+11}_{-10} \right) \cdot 10^{-11}$

$$\text{Br}(K_L \rightarrow \pi^0 \nu\bar{\nu}) \leq 6.8 \cdot 10^{-8}$$

(E787, E949 Brookhaven)

(E391a, KEK)

Future :

NA62
Project X (FNAL)

Both very
sensitive to
New Physics

CP-conserving
TH uncertainty 2-3%

J-PARC KOTO

CP-Violation in Decay
TH uncertainty 1-2%

Maximal Enhancements of $K_L \rightarrow \pi^0 \nu \bar{\nu}$ and $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

Model independent bound

$$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu}) \leq 4.4 \text{ Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$$

Grossman
Nir

Model	$\text{Br}(K^+ \rightarrow \pi^+ \nu \bar{\nu})$	$\text{Br}(K_L \rightarrow \pi^0 \nu \bar{\nu})$
CMFV	20%	20%
MFV	30%	30%
LHT	200%	300%
RS	100%	200%
GMSSM	300%	500%
AC	2%	2%
RVV	10%	10%

SUSY
with
flavour
symmetries

↓
(abelian)

(non-abelian)

Large
RH Currents

(Bobeth et al
Haisch, Weiler
Isidori et al)

(Blanke et al)

(Duling et al)

(ABGPS)

$\text{RC} = \text{RC with custodial protections}$

AC = Agashe, Carone

RVV = Ross, Velaso-Sevilla, Vives (04)

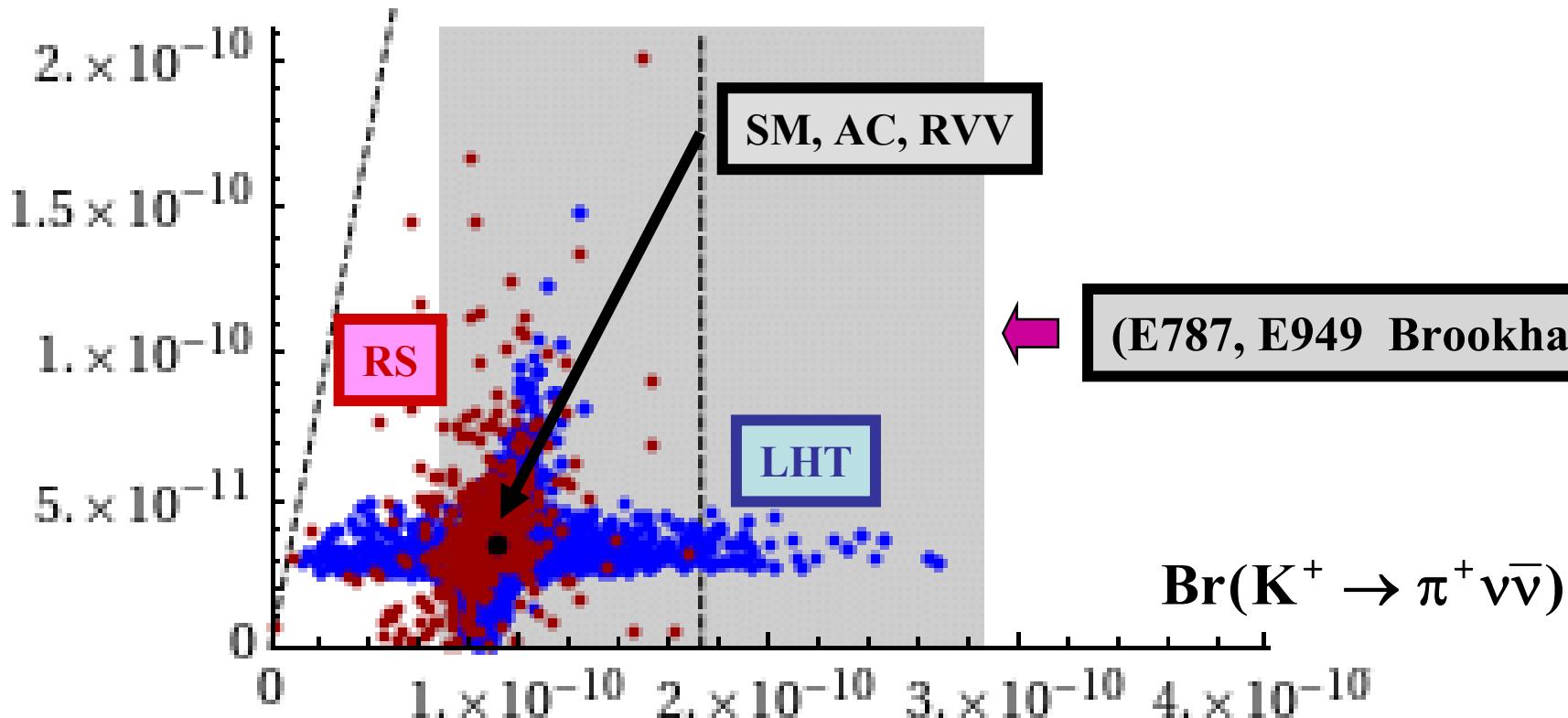
$U(1)_F$
 $SU(3)_F$



$K_L \rightarrow \pi^0 \bar{\nu}\bar{\nu}$ vs. $K^+ \rightarrow \pi^+ \bar{\nu}\bar{\nu}$

$\text{Br}(K_L \rightarrow \pi^0 \bar{\nu}\bar{\nu})$

Blanke et al (08)
Goto et al (08)
Recksiegel et al (09)





$$B_s \rightarrow \mu^+ \mu^- \text{ and } B_d \rightarrow \mu^+ \mu^-$$

Z-Penguin (SM
+ Boxes CMV)

SM

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) = (3.6 \pm 0.4) \cdot 10^{-9}$$

$$\text{Br}(B_d \rightarrow \mu^+ \mu^-) = (1.1 \pm 0.1) \cdot 10^{-10}$$

Error dominated by $\hat{B}_{d,s}$

AJB (03)

CMFV
“Golden Relation”

$$\frac{\text{Br}(B_s \rightarrow \mu^+ \mu^-)}{\text{Br}(B_d \rightarrow \mu^+ \mu^-)} = \frac{\hat{B}_d}{\hat{B}_s} \frac{\tau(B_s)}{\tau(B_d)} \frac{\Delta M_s}{\Delta M_d}$$

(ΔB = 1) (1.00 ± 0.03)
 Lattice (ΔB = 2)

Valid in all CMFV models

Can be strongly violated in SUSY, LHT, RS

95% CL

$$\text{Br}(B_s \rightarrow \mu^+ \mu^-) \leq \begin{cases} 3.3 \cdot 10^{-8} & (\text{CDF}) \\ 5.3 \cdot 10^{-8} & (\text{D0}) \end{cases}$$

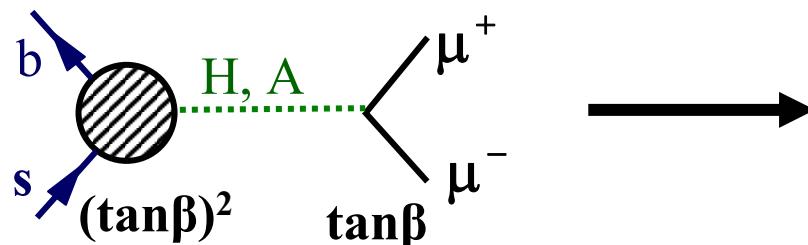
$$\text{Br}(B_d \rightarrow \mu^+ \mu^-) \leq 1 \cdot 10^{-8} \text{ (CDF)}$$

LHC should be able to discover $B_s \rightarrow \mu^+ \mu^-$ even at the SM level

$B_{s,d} \rightarrow \mu^+ \mu^-$ in SUSY and Higgs Penguins

(Helicity suppression lifted)

Babu, Kolda (99), ... + 100



$$\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-) \sim \frac{(\tan \beta)^6}{M_A^4}$$

Can reach CDF and DØ bounds

Very important for the distinction of SUSY from LHT and RS !!!



$$\frac{\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)_{\text{LHT}}}{\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)_{\text{SM}}} \leq 1.3$$

(Z-penguin)
(Blanke et al) (09)

$$\frac{\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)_{\text{RS}}}{\text{Br}(B_{s,d} \rightarrow \mu^+ \mu^-)_{\text{SM}}} \leq 1.1$$

(Z-penguin + Z-tree with
r.h. couplings)
(Custodial protection at work)
(Gori et al) (08)

Mixing Induced CP Asymmetry in $B_s \rightarrow \psi\varphi$ ($S_{\psi\varphi}$)

(TH very clean; Analog of $S_{\psi K_s}$ *)

$$S_{\psi\varphi} = \sin(2|\beta_s| - 2\phi_s^{\text{new}}) \stackrel{\text{SM}}{\cong} 0.035$$

$$V_{ts} = -|V_{ts}| e^{-\beta_s}$$

$$(\beta_s = -1^\circ)$$

$0.53^{+0.23}_{-0.21}$

New Phase in $B_s^0 - \bar{B}_s^0$ mixing



CDF
D0

$$0.20 \leq (S_{\psi\varphi})_{\text{exp}} \leq 0.98$$

90% C.L. (HFAG)

See also
Perez et al

Model Expectations

$$S_{\psi\varphi} \leq \begin{cases} 0.75 & (\text{AC}) \text{ (abelian flavour, SUSY)} \text{ (Higgs penguin)} \\ 0.50 & (\text{RVV}) \text{ (non-abelian flavour, SUSY)} \text{ (Higgs penguin)} \\ 0.75 & (\text{RS}) \text{ (Heavy KK Gauge Bosons)} \text{ (Duling et al (08))} \\ 0.30 & (\text{LHT}) \text{ (Mirror Fermions at work)} \text{ (Tarantino et al (09))} \end{cases}$$

ABGPS

*) See however Faller, Fleischer, Mannel (08)

Maximal Enhancements of $S_{\psi\phi}$, $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ and $K^+ \rightarrow \pi^+ \bar{v}v$

(without taking correlation between them)

Model	Upper Bound on ($S_{\psi\phi}$)	Enhancement of $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$	Enhancement of $\text{Br}(K^+ \rightarrow \pi^+ \bar{v}v)$
CMFV	0.04	20%	20%
MFV	0.04	1000%	30%
LHT	0.30	30%	200%
RS	0.75	10%	100%
GMSSM	0.75	1000%	300%
AC	0.75	1000%	2%
RVV	0.50	1000%	10%

Correlations between $K^+ \rightarrow \pi^+ \nu\bar{\nu}$, $K_L \rightarrow \pi^0 \nu\bar{\nu}$, $S_{\psi\phi}$, $B_s \rightarrow \mu^+ \mu^-$



Impact of a future $S_{\psi\phi} \approx 0.3$

LHT
RS

Sizable Enhancements in $K^+ \rightarrow \pi^+ \nu\bar{\nu}$
and $K_L \rightarrow \pi^0 \nu\bar{\nu}$ excluded in RS and
unlikely in LHT

(Blanke et al)

$B_{s,d} \rightarrow \mu^+ \mu^-$ SM - like

(abelian)
AC
RVV
(non-abelian)

$\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ forced to be
 $3 \cdot \text{Br}(B_s \rightarrow \mu^+ \mu^-)_{\text{SM}} \sim 10^{-8}$

SUSY
Flavour
Models

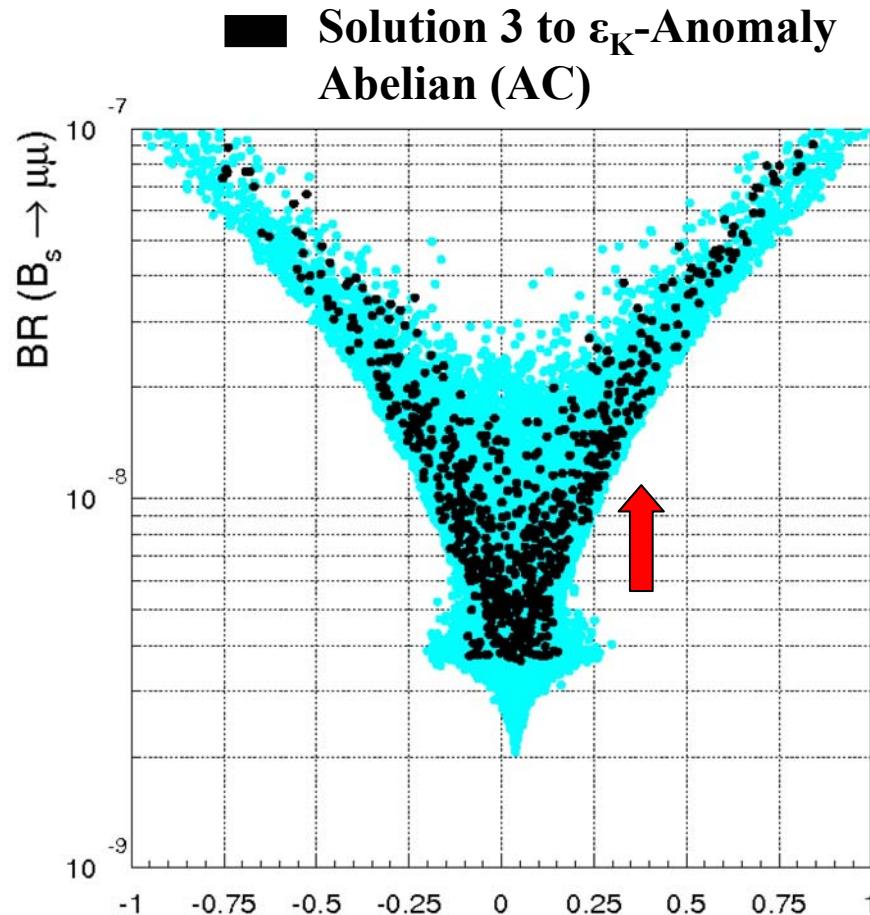
Altmannshofer, AJB, Gori, Paradisi, Straub (09)

ABGPS

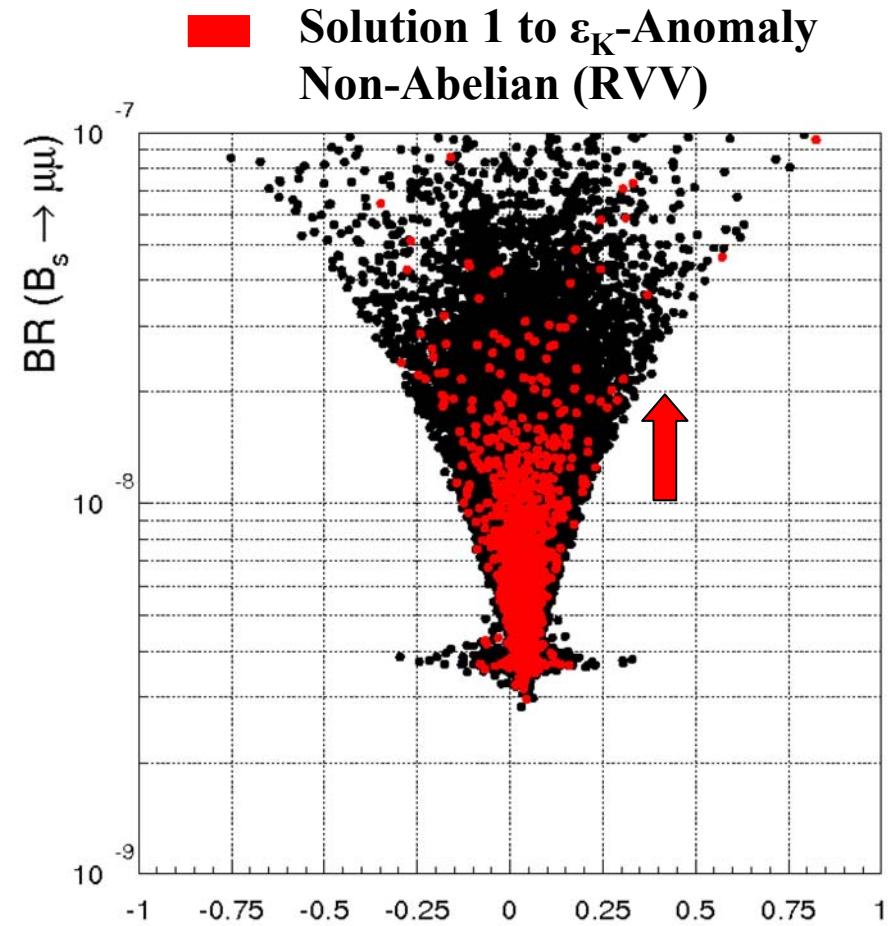
CDF, D0
LHCb

$\text{Br}(\text{B}_s \rightarrow \mu^+ \mu^-) \text{vs } S_{\psi\phi}$

ABGPS



(Large Effects in $D^0-\bar{D}^0$)



(Small Effects in $D^0-\bar{D}^0$)

Lepton Flavour Violation, $\Delta(g - 2)_\mu$ and EDM's

(MEGA) $\text{Br}(\mu \rightarrow e\gamma) < 1.2 \cdot 10^{-11}$ \rightarrow 10^{-13} (MEG) SM: 10^{-54}

$$\left(a_\mu\right)_{\text{SM}} < \left(a_\mu\right)_{\text{exp}} \quad (3.6\sigma)$$

(Brookhaven) 1.9σ

$$a_\mu = \frac{1}{2} (g - 2)_\mu$$

(Regan et al) $d_e < 1.6 \cdot 10^{-27}$ \rightarrow 10^{-31} $(d_e)_{\text{SM}} \approx 10^{-38}$

[e cm]

(Baker et al) $d_n < 2.9 \cdot 10^{-26}$ \rightarrow 10^{-28} $(d_n)_{\text{SM}} \approx 10^{-32}$

Clear Distinction between MSSM and LHT

MSSM

$$\frac{\text{Br}(\mu^- \rightarrow e^- e^+ e^-)}{\text{Br}(\mu^- \rightarrow e^- \gamma)} \approx \frac{1}{161}$$

LHT

$$0.02 - 1$$

Both
can
reach
MEGA's
 $\mu \rightarrow e\gamma$
bound

$$\frac{\text{Br}(\tau^- \rightarrow \mu^- \mu^+ \mu^-)}{\text{Br}(\tau^- \rightarrow \mu^- \gamma)} \approx \frac{1}{435}$$

$$0.04 - 0.4$$

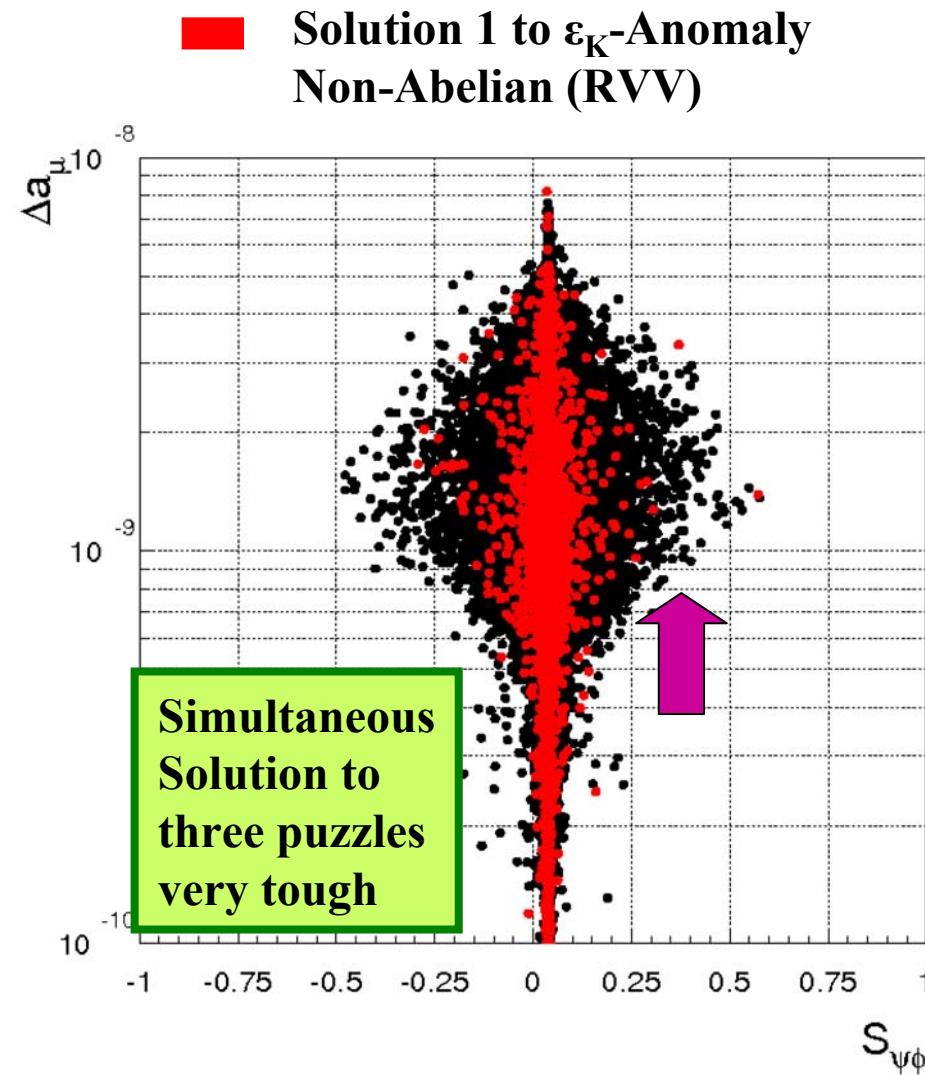
MSSM

: (Ellis, Hisano, Raidal, Shimizu; Arganda, Herrero; Paradisi)
(Brignole, Rossi)

LHT

: (Blanke, AJB, Duling, Poschenrieder, Tarantino) (2007)
del Aguila, Illana, Jenkins (2008), Goto, Okada, Yamamoto (2009)

More Correlations in Flavour SUSY Models



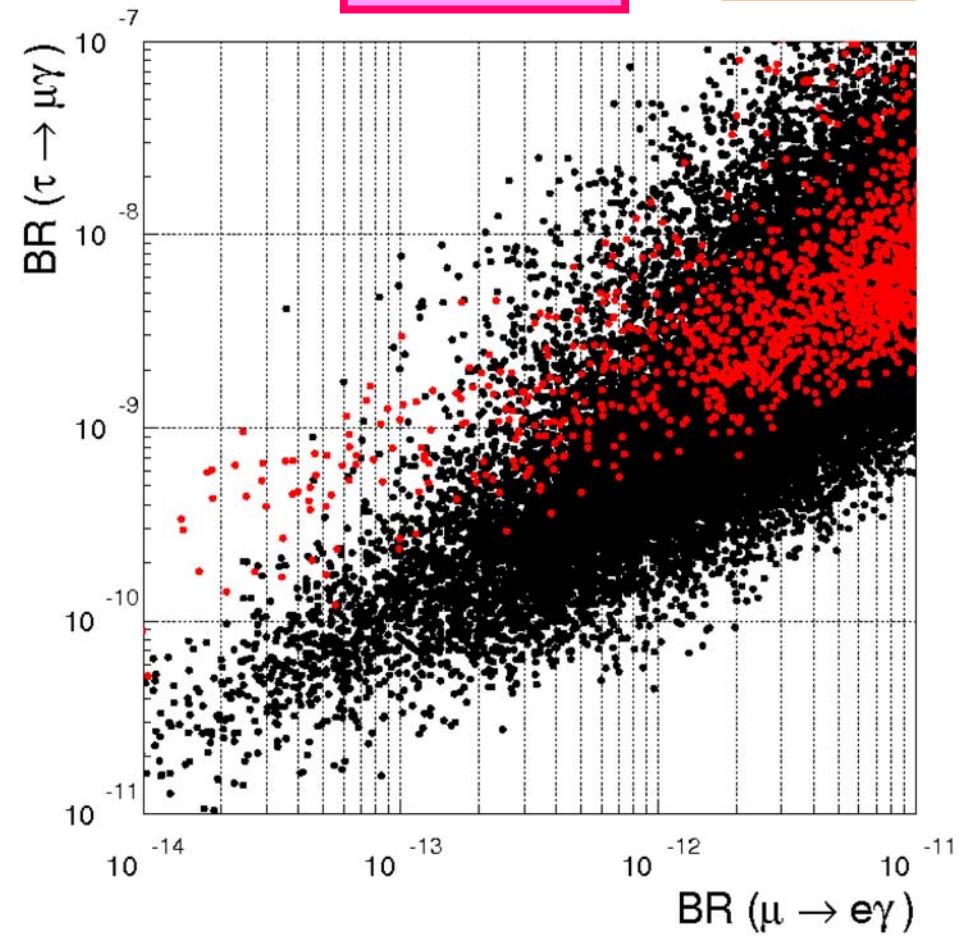
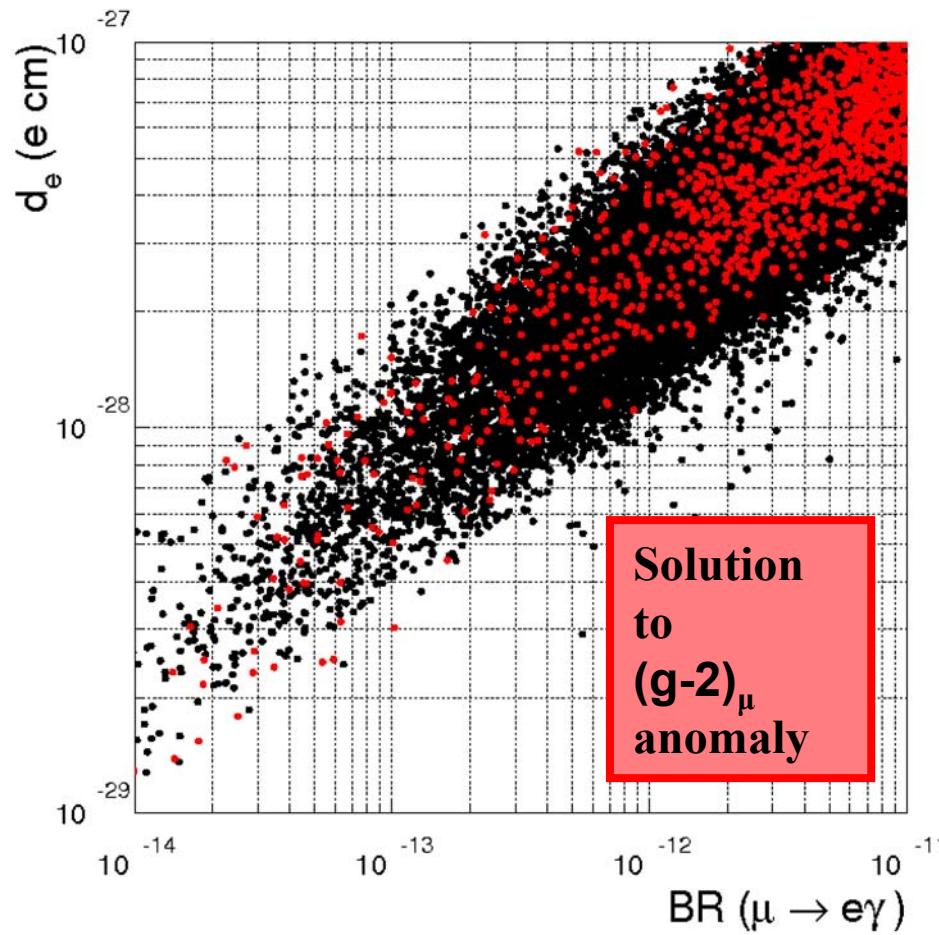
(See also Perez et al)

Testing SUSY through d_e , $(g-2)_\mu$, Br ($l_i \rightarrow l_j \gamma$)

Hisano, Nagai, Paradisi, Shimizu (09)
Isidori et al (08) ABGPS (09)

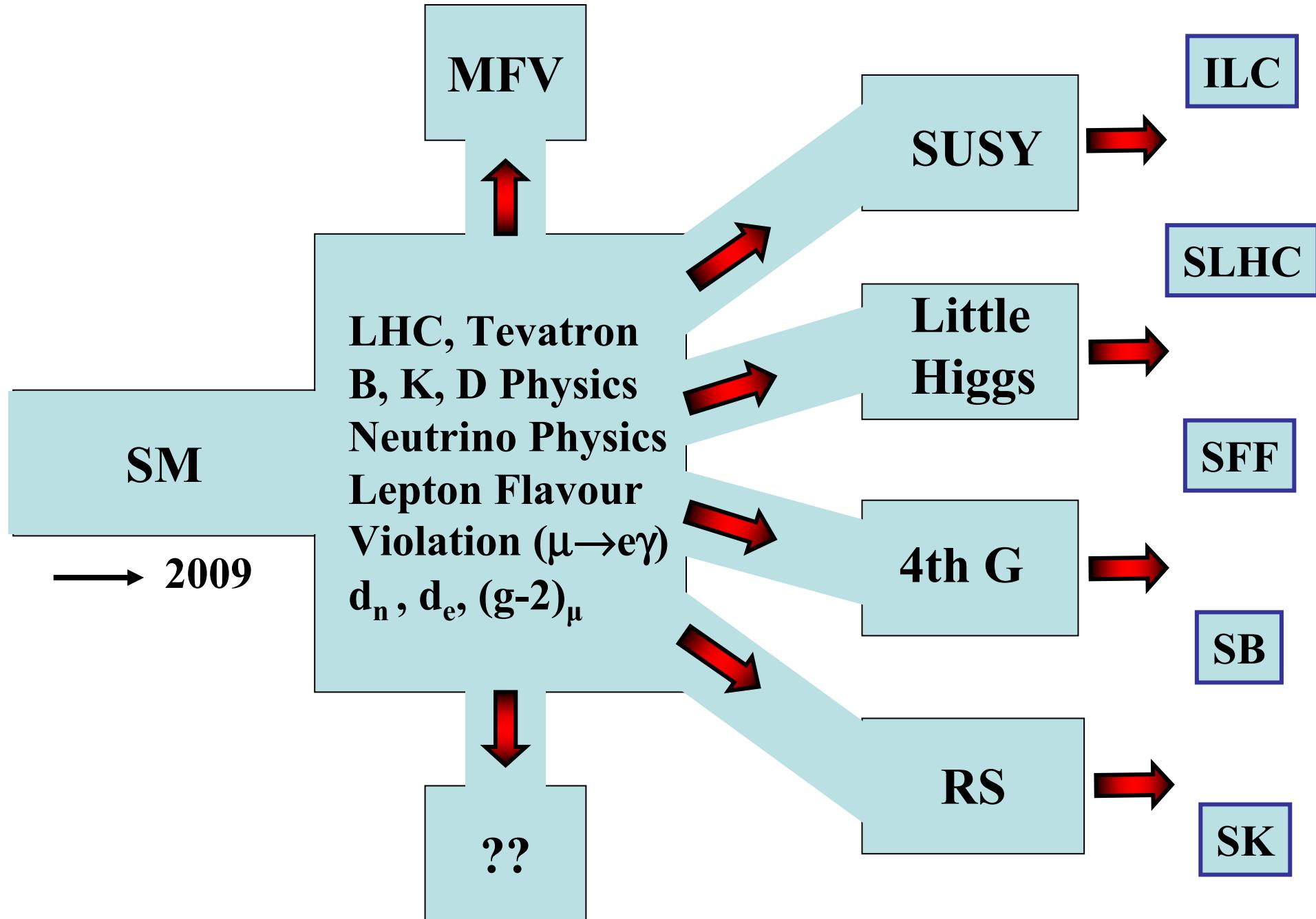
Dipole
Transitions

RVV



4.

Final Messages



Flavour Physics (Quarks and Leptons)

Final Messages of this Talk

:

Many observables (decays) not measured yet or measured poorly. Flavour Physics only now enters the precision era.



Spectacular deviations from SM still possible

Interplay



Direct searches at Tevatron, LHC, ILC

Flavour Physics (Quarks and Leptons)

DNA Flavour Test of NP models

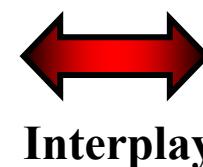
Final Messages of this Talk

:

Many observables (decays) not measured yet or measured poorly. Flavour Physics only now enters the precision era.



Spectacular deviations from SM still possible



Direct searches at Tevatron, LHC, ILC

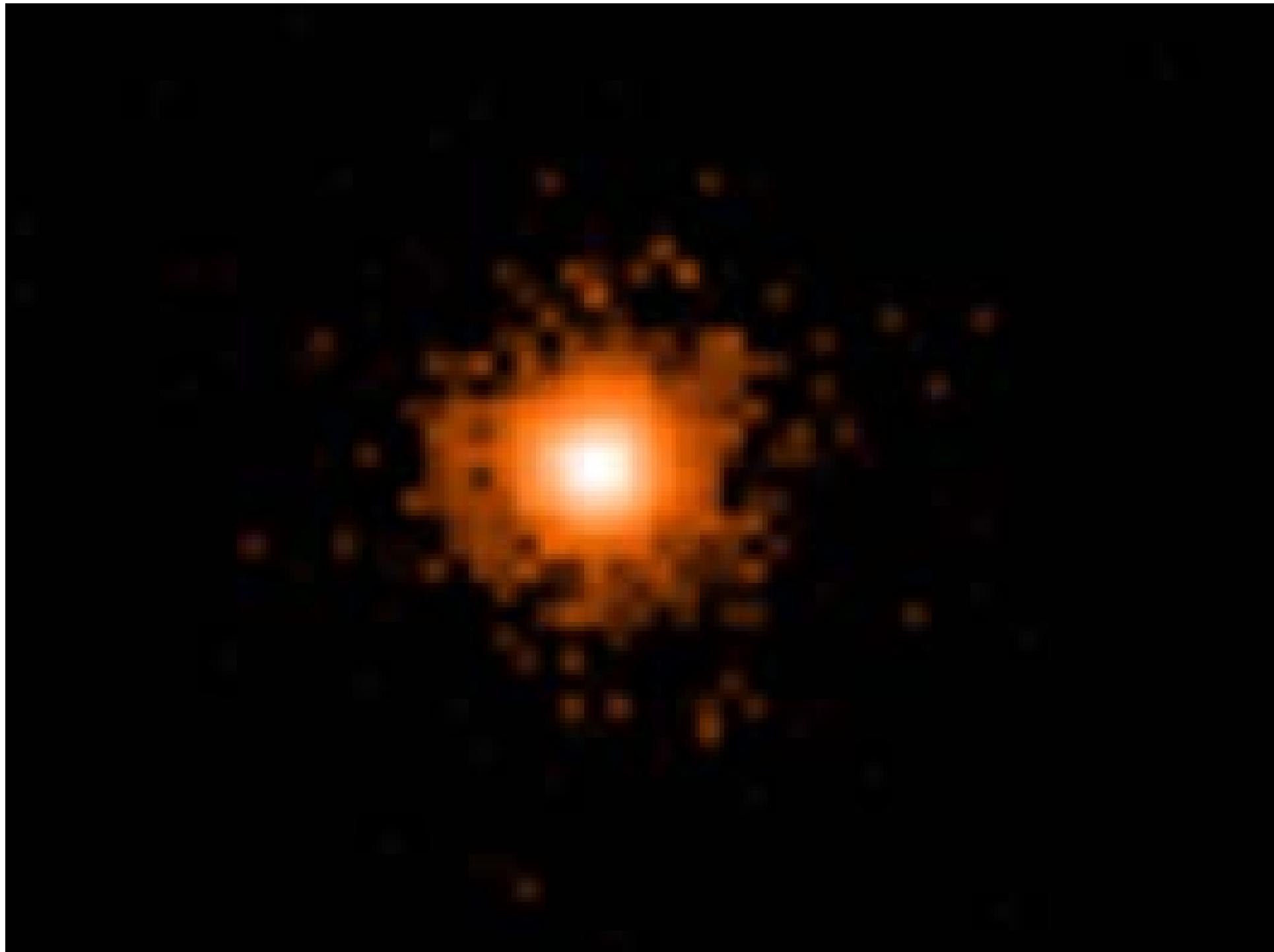
Correlations between various observables can distinguish NP scenarios easier than LHC !

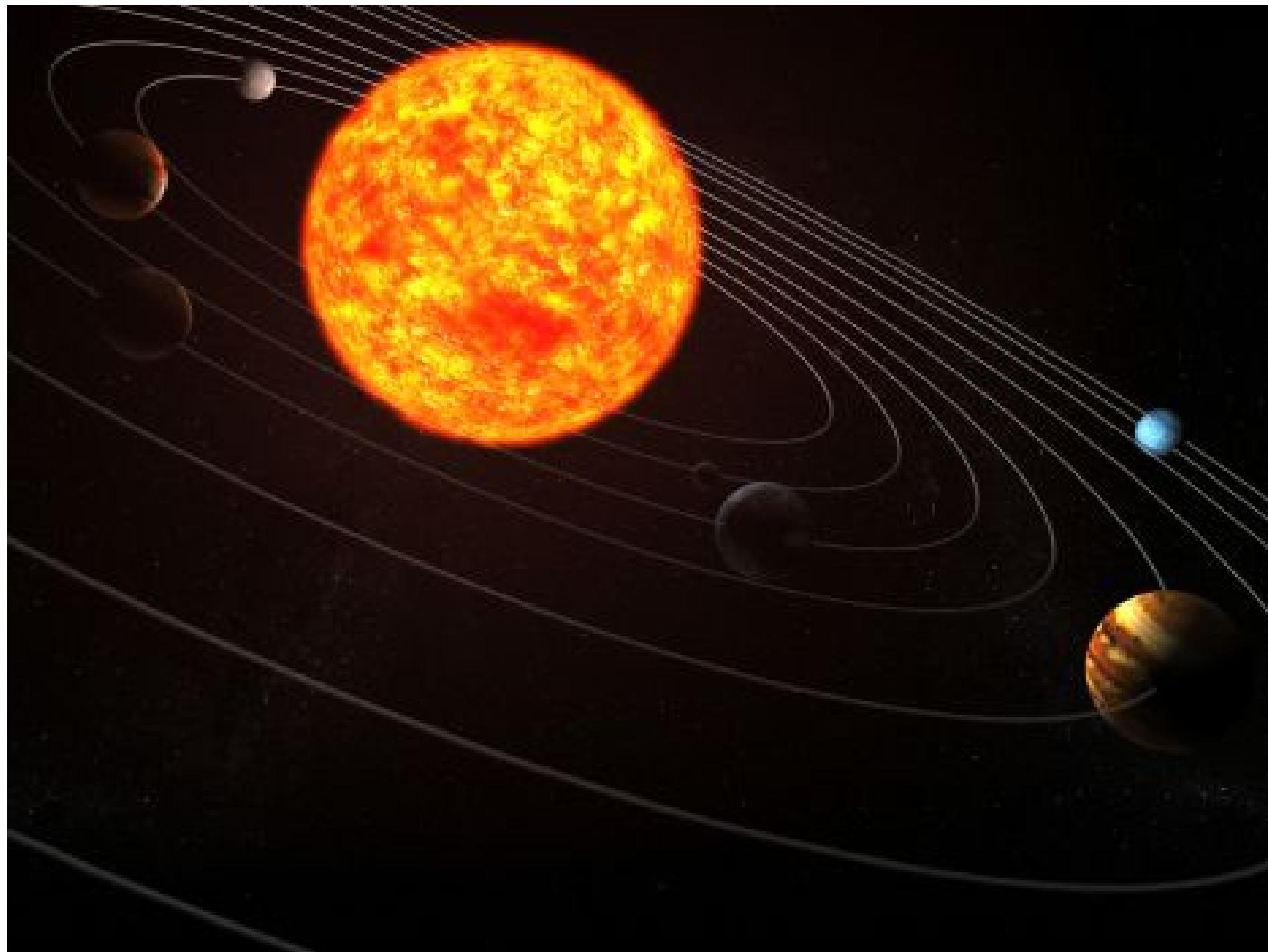


Great discoveries are just ahead of us !

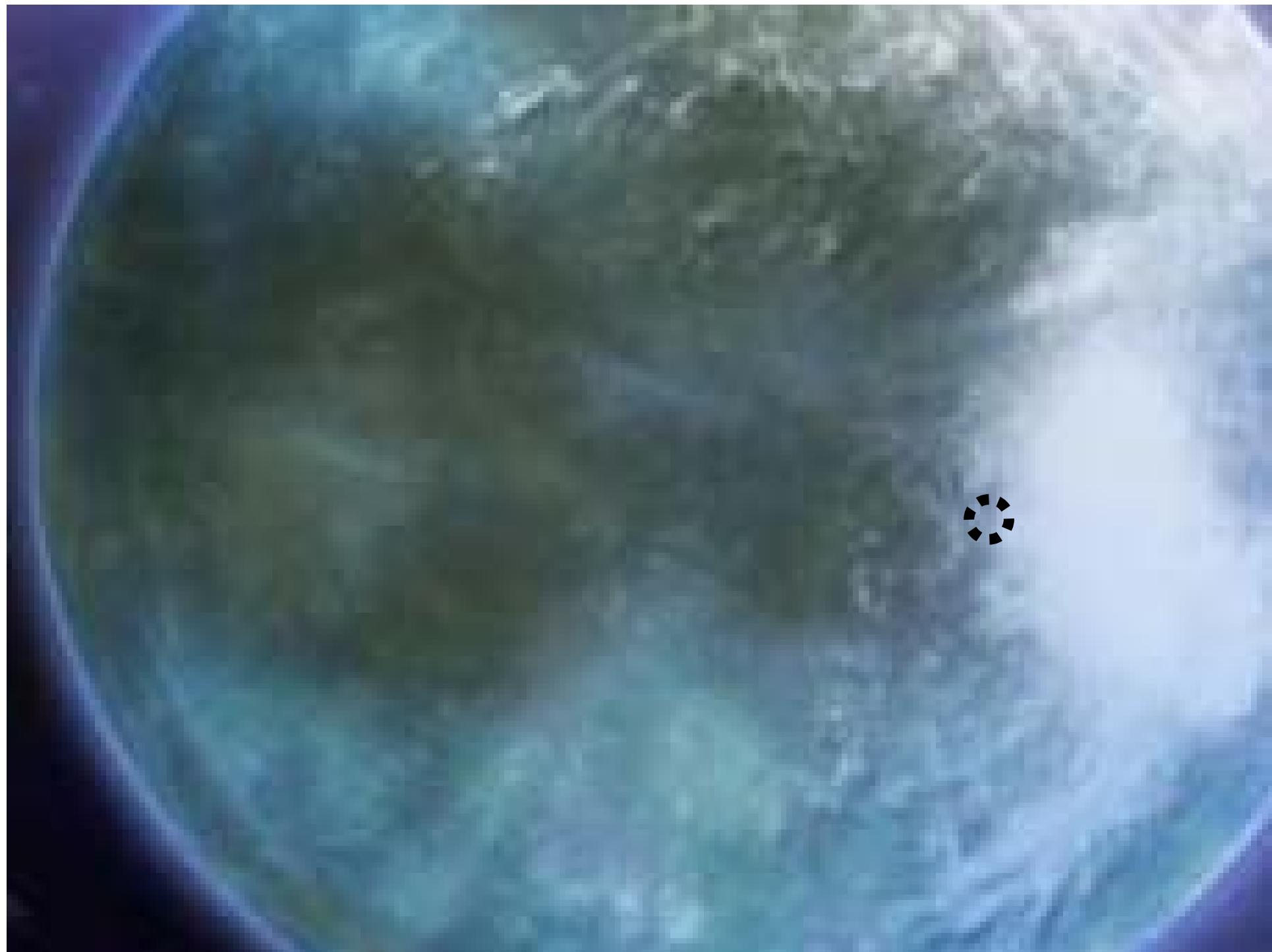


NASA/CXC 2004











25th Beta Ceti Conference on High Energy Physics (1917)



25th Beta Ceti Conference on High Energy Physics (1917)



Backup

SUSY



W. Altmannshofer

S. Gori

P. Paradisi

D. Straub

LHT



M. Blanke

B. Duling

S. Recksiegel

C. Tarantino

RS



M. Albrecht

M. Blanke

B. Duling

K. Gemmeler

S. Gori

A. Weiler

U(2) Custodial Flavour Symmetry

SUSY



W. Altmannshofer

S. Gori

P. Paradisi

D. Straub

LHT



M. Blanke

B. Duling

S. Recksiegel

C. Tarantino

RS



M. Albrecht

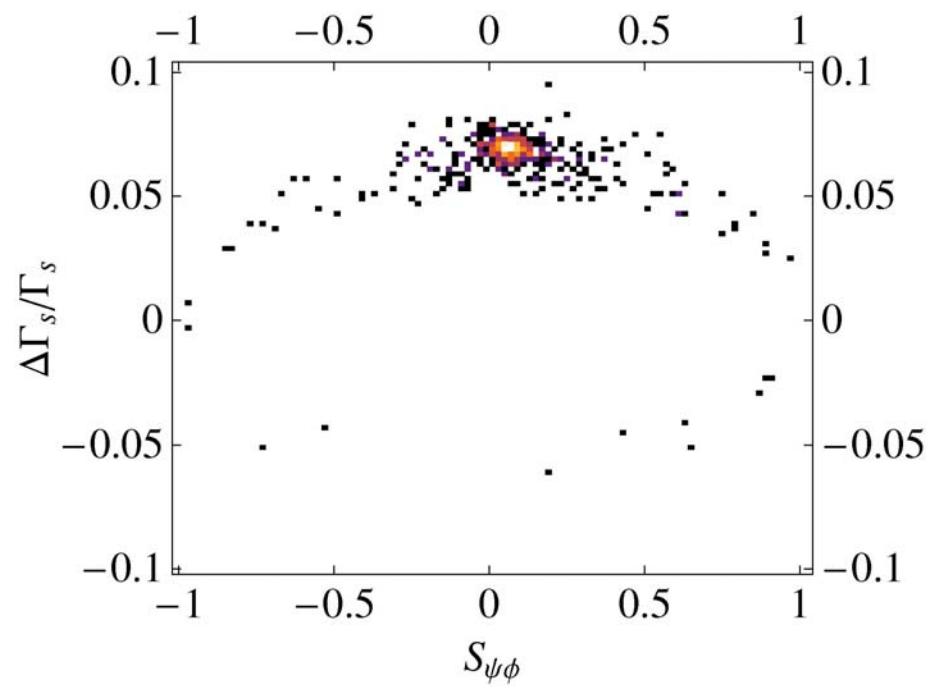
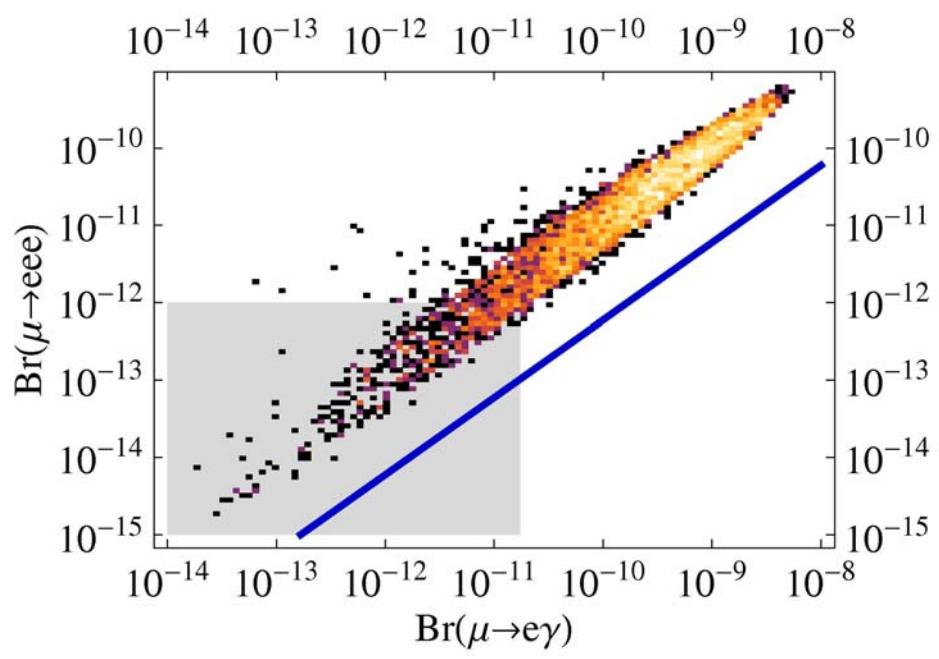
M. Blanke

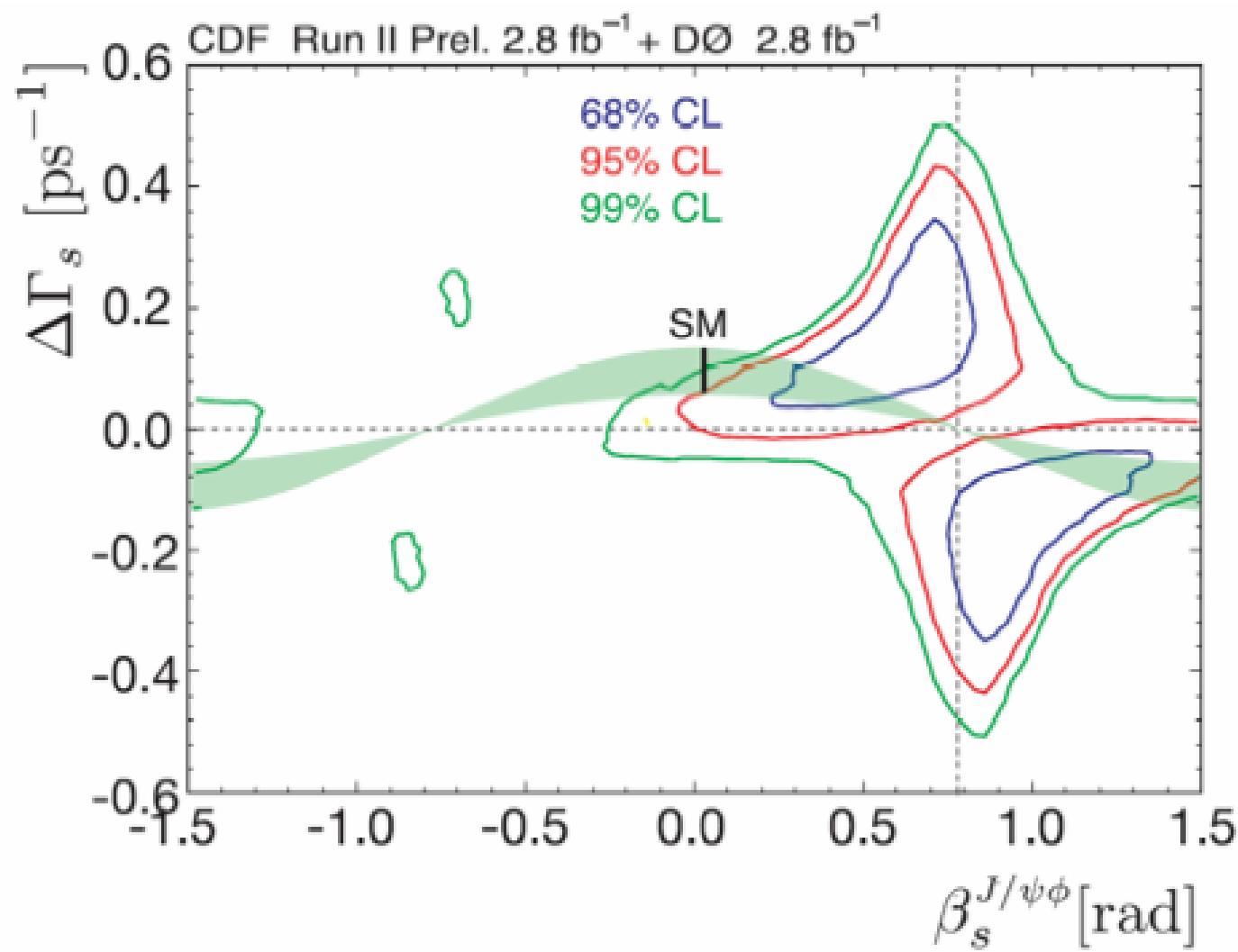
B. Duling

K. Gemmeler

S. Gori

A. Weiler





DNA Flavour Test of New Physics Models

	GMSSM	AC	RVV	δ_{LL} only	FBMSSM
$D^0 - \bar{D}^0$ mixing	★★★	★★★	★	★	★
ϵ_K	★★★	★	★★★	★	★
$S_{\psi\phi}$	★★★	★★★	★★★	★	★
$S_{\phi K_S}, S_{\eta' K_S}$	★★★	★★★	★★	★★★	★★★
$A_{CP}^{bs\gamma}$	★★★	★	★	★★★	★★★
$\langle A_{7,8} \rangle (B \rightarrow K^* \mu^+ \mu^-)$	★★★	★	★★	★★★	★★★
$\langle A_9 \rangle (B \rightarrow K^* \mu^+ \mu^-)$	★★★	★	★★	★	★
$B_s \rightarrow \mu^+ \mu^-$	★★★	★★★	★★★	★★★	★★★
$B \rightarrow K^{(*)} \nu \bar{\nu}$	★★	★	★	★	★
$K \rightarrow \pi \nu \bar{\nu}$	★★★	★	★★	★	★
d_e, d_n	★★★	★★★	★★	★★	★★★

★★★: large effects, ★★: medium effects, ★: small effects

Return of ε'/ε ?

Final
Result
(NA48, KTeV)

$$\text{Re}(\varepsilon'/\varepsilon) = (16.8 \pm 1.4) \cdot 10^{-4}$$

(2009)

$$\text{Re}(\varepsilon'/\varepsilon)_{\text{SM}} \approx \left\{ \begin{array}{l} \text{QCD} \\ \text{Penguins} \end{array} \right\}_{(B_6)} - \left\{ \begin{array}{l} \text{Electroweak} \\ \text{Penguins} \end{array} \right\}_{(B_8)}$$

Very sensitive
to New Physics

Wilson
Coefficients
of Penguins
known at
NLO (1990's)
Munich (92,93)
Rome (93)

Large N calculations of
hadronic Matrix Elements

Bardeen, AJB, Gerard (85)
Pich et al
De Rafael et al.
Bijnens + Prades } (1990's)

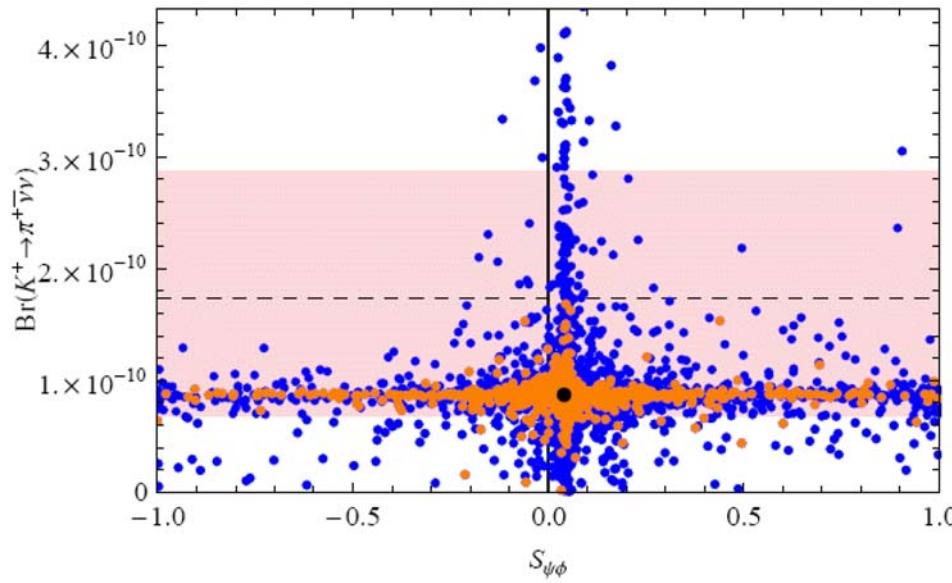
New Efforts
on the Lattice

(Norman Christ
et al.)

20015 ?

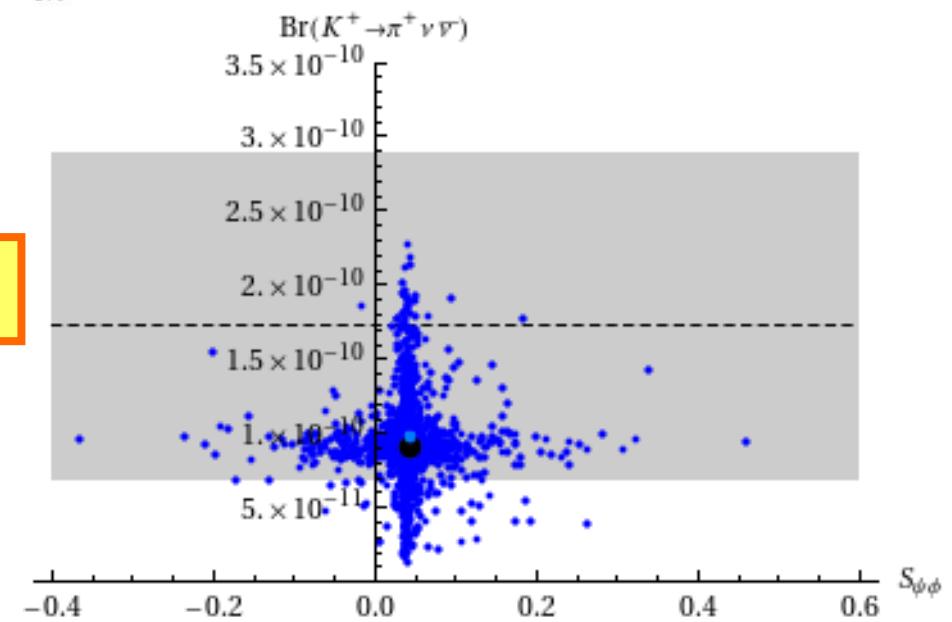
$$K^+ \rightarrow \pi^+ \nu\bar{\nu} \text{ vs. } S_{\psi\phi}$$

(Simultaneous Large Enhancements unlikely)



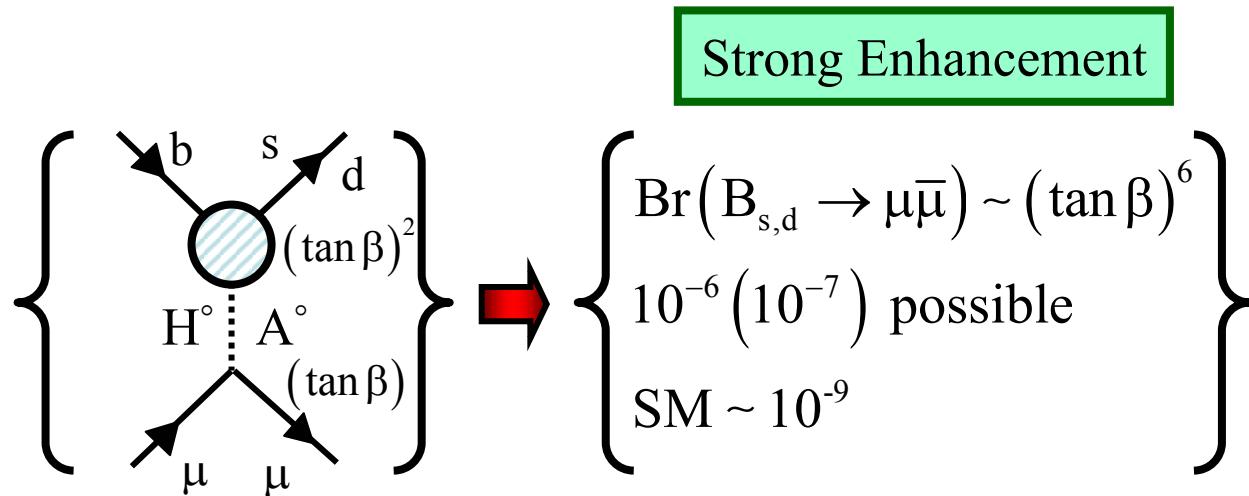
RS

LHT



$B_{s,d} \rightarrow \mu^+ \mu^-$ and MSSM with MFV at large $\tan\beta$

In MSSM at large $\tan\beta$
 (CKM still the only source of Flavour and CP Violation)



Babu, Kolda
 Chankowski, Slawianowska
 Bobeth, Ewerth, Krüger, Urban
 Huang, Liao, Yan, Zhu
 Isidori, Retico
 Dedes, Dreiner, Nierste
 Dedes, Pilaftis
 Chankowski, Rosiek
 Foster, Okumura, Roszkowski
 Carena et al.
 Isidori, Paradisi

$$\boxed{\text{Br}(B_s \rightarrow \mu\bar{\mu}) < 6 \cdot 10^{-8}}$$

95% C.L.
 (CDF, DØ)

$$\boxed{\text{Br}(B_d \rightarrow \mu\bar{\mu}) < 2 \cdot 10^{-8}}$$

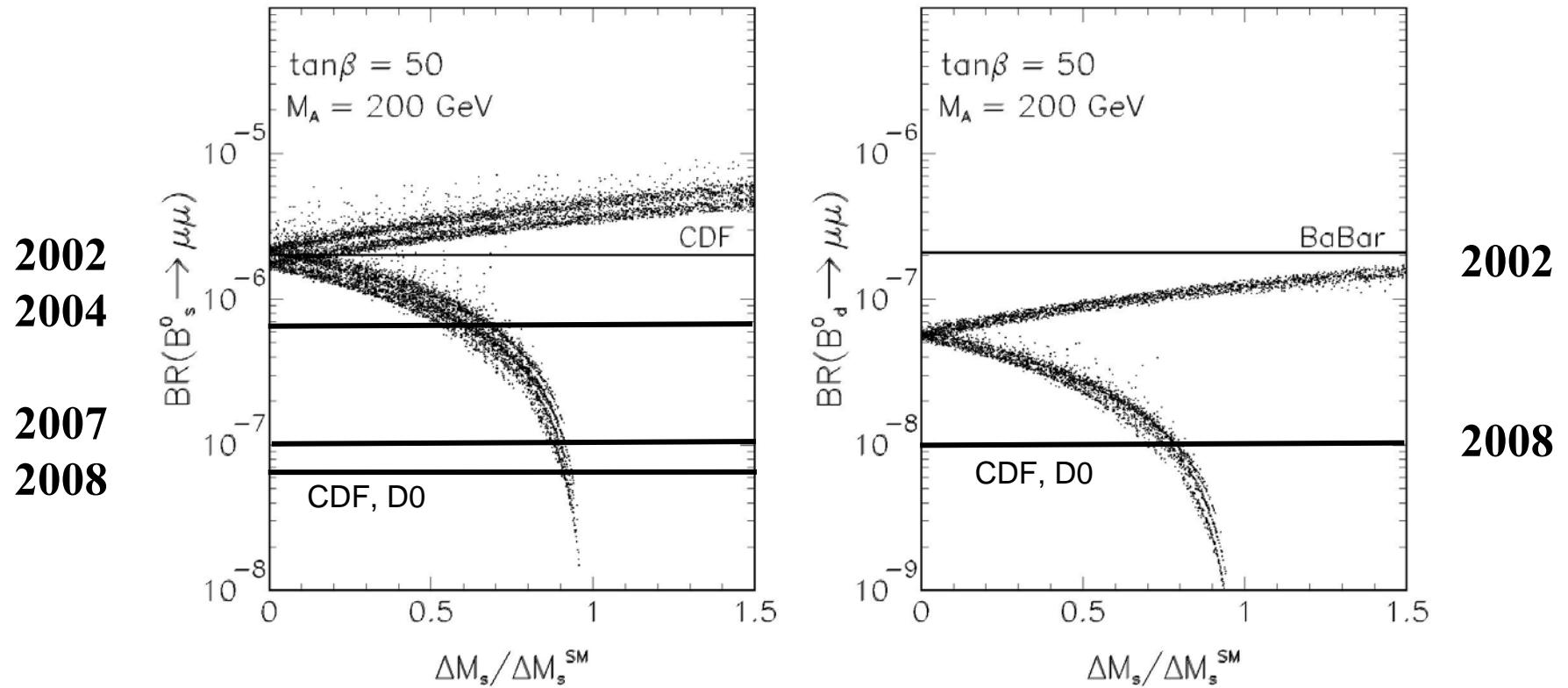
95% C.L.

$\text{Br}\left(B_{s,d} \rightarrow \mu^+ \mu^-\right)$ vs $(\Delta M_s)^{\text{exp}} / (\Delta M_s)^{\text{SM}}$ in SUSY at Large $\tan\beta$

AJB, Chankowski, Rosiek, Slawianowska (2002)

Gorbahn, Jäger, Nierste, Trine (2008)

Could be modified by Non-MFV (Chankowski; Dedes, Pilaftsis)



$$\mathbf{B}^+ \rightarrow \tau^+ \nu \quad (\mu^+ \nu)$$

$$\text{Br}\left(\mathbf{B}^+ \rightarrow \tau^+ \nu\right)_{\text{exp}} = (1.73 \pm 0.35) \cdot 10^{-4} \quad (\text{Belle, BaBar})$$

$$\text{Br}\left(\mathbf{B}^+ \rightarrow \tau \nu\right)_{\text{SM}} \approx G_F^2 F_B^2 |V_{ub}|^2 = (1.1 \pm 0.5) \cdot 10^{-4}$$

$$\frac{\text{Br}\left(\mathbf{B}^+ \rightarrow \tau \nu\right)_{\text{MSSM}}}{\text{Br}\left(\mathbf{B}^+ \rightarrow \tau \nu\right)_{\text{SM}}} = \left[1 - \left(\frac{m_B}{m_{H^\pm}} \right)^2 \frac{\tan^2 \beta}{1 + \varepsilon_0 \tan \beta} \right]^2$$

(Hou)
(Akeroyd, Recksiegel)
(Isidori, Paradisi)

This decay could be problematic for
MSSM-MFV with large $\tan \beta$

Tree-Level
 H^+ exchange

Altmannshofer, AJB, Guadagnoli, Wick (07)

$$B^+ \rightarrow \tau^+ \nu, K^+ \rightarrow l^+ \nu$$

(LFV effects in
B and K Physics)

Sensitivity
to NP

A.

$$\frac{\text{Br}(B^+ \rightarrow \mu^+ \nu)}{\text{Br}(B^+ \rightarrow \tau^+ \nu)}$$

(test of $\mu \leftrightarrow \tau$ universality)

Isidori - Paradisi (2006)

B.

$$\frac{\Gamma(K^+ \rightarrow \mu^+ \nu)}{\Gamma(K^+ \rightarrow e^+ \nu)}$$

Very accurate
precision test

Tested soon at CERN
to 0.5%

TH:
 $\pm 0.1\%$

$(g - 2)_\mu$ and EDM's

Flavour
Conserving



$(g - 2)_\mu$: Flavour and CP conserving

Resolution of the
 $(g - 2)_\mu$ problem

$$[(g - 2)_\mu]_{\text{SM}} \neq [(g - 2)_\mu]_{\text{exp}}$$

$$a_\mu^{\text{exp}} = 11659\ 2080\ (63)\ 10^{-11}$$

$$a_\mu^{\text{SM}} = 11659\ 1785\ (51)\ 10^{-11}$$

3.6 σ
discrepancy

MSSM
~~LHT~~



EDM's Flavour conserving but ~~CP~~

But e^+e^- from
BaBar $\rightarrow 0.9\ \sigma$

(?)

MSSM, ~~LHT~~, WED

Putting S0(10)-SUSY-GUT of Dermisek-Raby into difficulties

M. Albrecht, W. Altmannshofer, AJB, D. Guadagnoli, D. Straub

1.

The Model gives a nice description of quark and lepton masses, PMNS and most of CKM elements.

Also
SUSY
Spectrum

2.

But fails to describe simultaneously the data on

$$B_{s,d} \rightarrow \mu^+ \mu^-, B \rightarrow X_s \gamma, B \rightarrow X_s l^+ l^-, B_u \rightarrow \tau \nu$$

3.

Gives $|V_{ub}| \approx 3.2 \cdot 10^{-3}$

$$< \underbrace{(4.2 \pm 0.3) \cdot 10^{-3}}_{\text{Exp.}}$$



Generally
too low

Some recent
solutions:
Altmannshofer et al.

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}, K_L \rightarrow \pi^0 \nu \bar{\nu}, K_L \rightarrow \pi^0 l^+ l^-, B \rightarrow K(K^*)$$



Z⁰- Penguin dominated Decays

Decay	SM	Exp	TH
$K^+ \rightarrow \pi^+ \nu \bar{\nu}$	$(8.5 \pm 0.7) \cdot 10^{-11}$	$(17.3^{+11.5}_{-10.5}) \cdot 10^{-11}$ (BNL)	$\pm 2\text{-}3\%$
$K_L \rightarrow \pi^0 \nu \bar{\nu}$	$(2.6 \pm 0.3) \cdot 10^{-11}$	$< 6.7 \cdot 10^{-8}$ (KEK)	$\pm 1\text{-}2\%$
$K_L \rightarrow \pi^0 e^+ e^-$	$(3.5 \pm 1.0) \cdot 10^{-11}$	$< 28 \cdot 10^{-11}$ (KTeV)	$\pm 15\%$
$K_L \rightarrow \pi^0 \mu^+ \mu^-$	$(1.4 \pm 0.3) \cdot 10^{-11}$	$< 38 \cdot 10^{-11}$ (KTeV)	$\pm 15\%$
$B \rightarrow K^+ \nu \bar{\nu}$	$(4.5 \pm 0.7) \cdot 10^{-6}$	$< 14 \cdot 10^{-6}$ (Belle)	$\pm 15\%$
$B \rightarrow K^* \nu \bar{\nu}$	$(6.8 \pm 1.1) \cdot 10^{-6}$	$< 80 \cdot 10^{-6}$ (BABAR)	$\pm 15\%$
$B \rightarrow X_s \nu \bar{\nu}$	$(2.7 \pm 0.2) \cdot 10^{-5}$	$< 64 \cdot 10^{-5}$ (ALEPH)	$\pm 3\%$

Very strong Constraints on New Physics

$$\text{Br}(B \rightarrow X_s \gamma)_{\text{exp}} = (3.52 \pm 0.24) \cdot 10^{-4}$$

$$\text{Br}(B \rightarrow X_s \gamma)_{\text{SM}} = \begin{cases} (3.15 \pm 0.23) \cdot 10^{-4} & (\text{Misiak et al}) \\ (2.98 \pm 0.26) \cdot 10^{-4} & (\text{Becher, Neubert}) \end{cases}$$

$$\text{Br}(B \rightarrow X_s l^+ l^-)_{\text{exp}} = \begin{cases} (1.6 \pm 0.5) \cdot 10^{-6} & (\text{low } q^2) \\ (4.4 \pm 1.3) \cdot 10^{-7} & (\text{high } q^2) \end{cases}$$

$$\text{Br}(B \rightarrow X_s l^+ l^-)_{\text{SM}} = \begin{cases} (1.6 \pm 0.1) \cdot 10^{-6} & (\text{low } q^2) \\ (2.3 \pm 0.8) \cdot 10^{-6} & (\text{high } q^2) \end{cases}$$

$$A_{CP}(B \rightarrow X_s \gamma)_{\text{exp}} = 0.004 \pm 0.036$$

$$A_{CP}(B \rightarrow X_s \gamma)_{\text{SM}} = 0.004 \pm 0.002$$

(Still factor 10 enhancement possible !)

Isidori et al. (incl.)
Gorbahn et al. (incl.)
Feldmann et al. (excl.)

Zero in A_{FB}

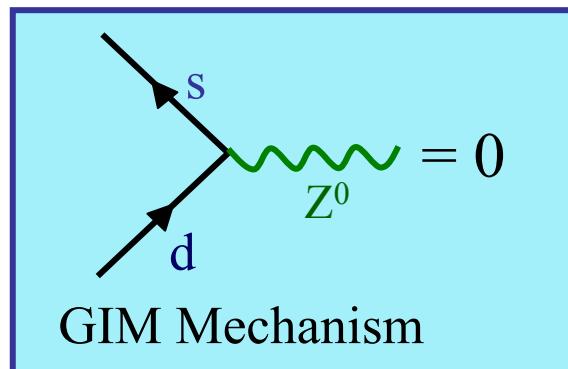
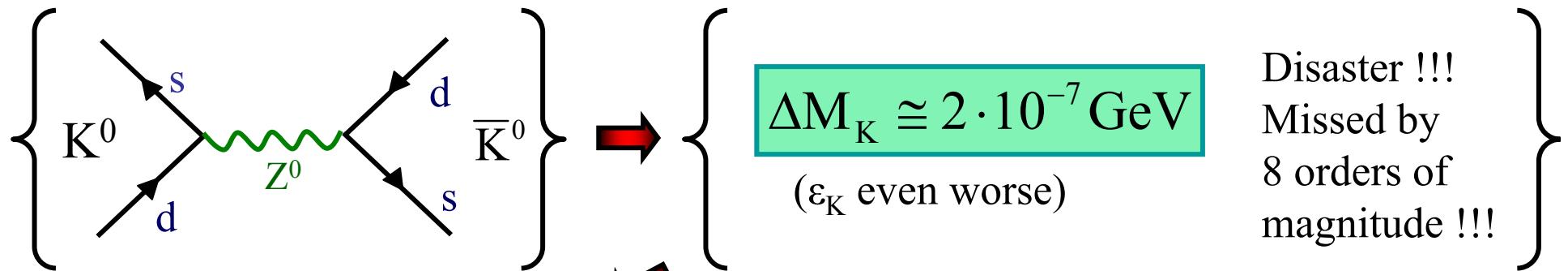
$$\hat{s}_0 = (3.50 \pm 0.12) \text{GeV}^2$$



TH
very clean

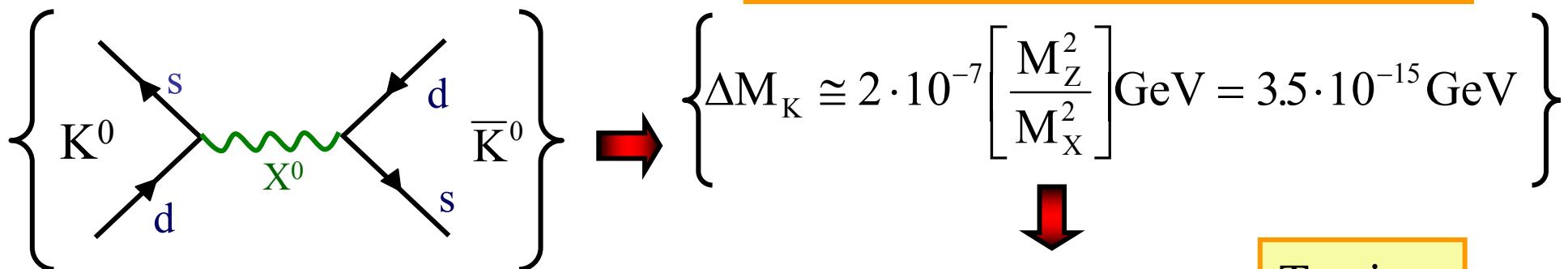
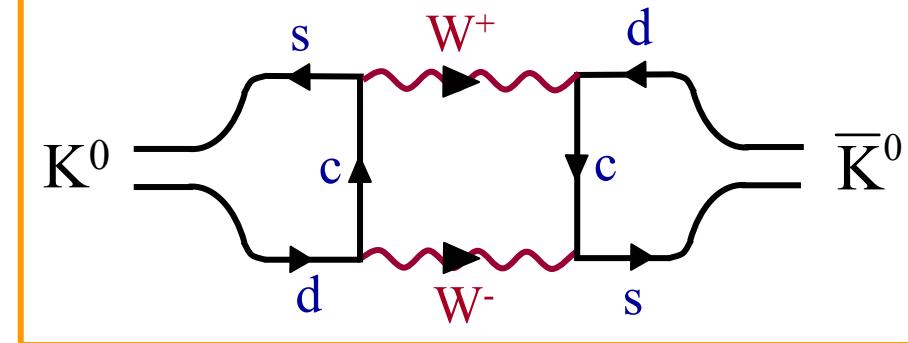
All this can be improved
at Super-B
Super-Belle

FCNCs at Tree Level and ΔM_K



(1971)

Gaillard + Lee (1974)



New very heavy neutral boson !

$$\{M_X \cong 10^6 \text{ GeV}\}$$

Testing
 10^{-22} m !

Tree Level FCNC mediated by KK gauge bosons and Z (breakdown of standard GIM mechanism)

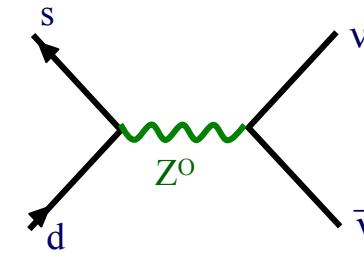
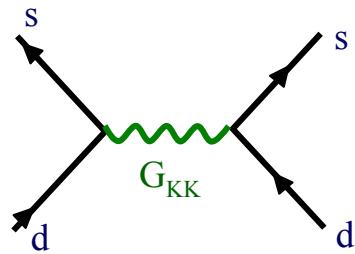
RS

$$\mathbf{d} \equiv \begin{pmatrix} \mathbf{d} \\ \mathbf{s} \\ \mathbf{b} \end{pmatrix}$$

$$\bar{\mathbf{d}} \mathbf{D}_L^+ \begin{pmatrix} \mathbf{a} & & \\ & \mathbf{b} & \\ & & \mathbf{c} \end{pmatrix} \mathbf{D}_L \gamma_\mu \mathbf{Z}^\mu \mathbf{d} \neq \bar{\mathbf{d}} \gamma_\mu \mathbf{Z}^\mu \mathbf{d}$$

(non-universality in gauge interactions)

$$0\left(\frac{\mathbf{v}^2}{M_{KK}^2}\right)$$



$$0\left(\frac{\mathbf{v}^2}{M_{KK}^2}\right)$$

But RS-GIM helps in avoiding disaster.

Gherghetta, Pomarol
Huber, Shafi
Agashe, Soni, Perez

Essential Ingredients in the Master Formula

1.

Hadronic Matrix Elements (\hat{B}_i)

(Progress still has to be made) Recent progress: \hat{B}_K

2.

QCD and QED RG-Effects for $\mu < m_t$ (η_i^{QCD})

1990's - era of NLO calculations

2000's - era of NNLO calculations

★ $B \rightarrow X_s l^+ l^-$ (Greub et al; Isidori et al, Beneke et al)

★ $B \rightarrow X_s \gamma$ (Misiak et al) Bobeth et al)

★ $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ (AJB, Gorbahn, Haisch, Nierste)

★ Non - Leptonic (Buchalla; Beneke, Jäger,...)
+ Semi - Leptonic (Gorbahn, Haisch)

3 Loop $\hat{\gamma}_{\text{anom}}$

Selected Actors for the next 15 Minutes

$|V_{ub}|, |V_{cb}|, \gamma$ from tree decays

ϵ_K

$$K^+ \rightarrow \pi^+ \nu \bar{\nu}$$

$$K_L \rightarrow \pi^0 \nu \bar{\nu}$$

$$B_{s,d} \rightarrow \mu^+ \mu^-$$

$$S_{\psi\phi}, A_{SL}^s$$

$$\mu \rightarrow e\gamma, \tau \rightarrow \mu\gamma$$

$$d_n, d_e \text{ (EDM's)}$$



$$S_{\phi K_s}, (S_{\phi\phi})$$

$$\Delta(g-2)_\mu$$

$$A_{CP} (b \rightarrow s\gamma)$$

$$B \rightarrow K^* l^+ l^-$$



4th Generation

Still a possibility !!

GIM at tree level
but strongly broken
at one loop
 $m_t, m_b, >m_t>>m_c$

New activities:

George Hou at al.

Soni, Alok, Giri, Mohanda, Nandi (08)
Bobrowski, Lenz, Riedl, Rohrwild (09)

This NP Scenario
is very different
from
SUSY, LHT, RS

Non-Decoupling Effects
of the 4th Generation
Fermions in Low Energy
Processes

:

However

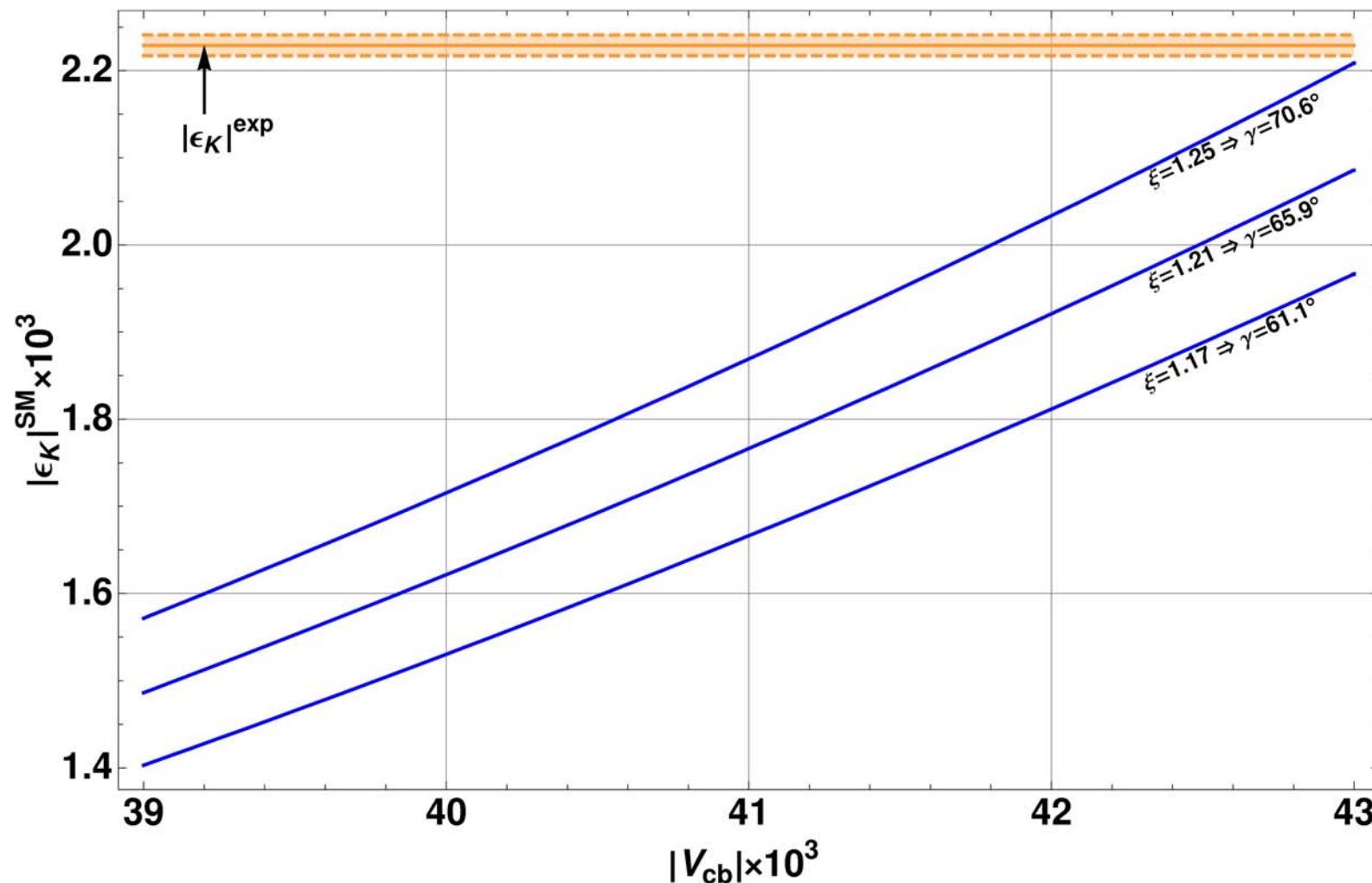
:

It does not address
the hierarchy problems

ε_K needs precise value of $|V_{cb}|$

AJB
Guadagnoli
(2009)

$$\varepsilon_K \sim |V_{cb}|^4$$



Number of new Flavour Parameters

(Quark Sector)

(physical)

Real

\mathcal{CP} Phases

	36	27	(R-parity)
SUSY			
FBMSSM	6	1	
LHT	7	3	
RS	18	9	some sensitivity to UV
SM	9	1	

Where to Expect Large NP Effects

- 1.** LFV ($\mu \rightarrow e\gamma$, $\mu \rightarrow 3e$, $\tau \rightarrow 3e$) ; EDM's
- 2.** $K_L \rightarrow \pi^0 \nu \bar{\nu}$, $K^+ \rightarrow \pi^+ \nu \bar{\nu}$, $K_L \rightarrow \pi^0 l^+ l^-$, (ε_K) , ε'/ε
- 3.** CP-Violation in B_s -Decays, in $B \rightarrow X_d \gamma$
- 4.** $B_{s,d} \rightarrow \mu^+ \mu^-$, $(B_{s,d} \rightarrow \tau^+ \nu)$
- 5.** CP-Violation in D-Decays
- 6.** $B \rightarrow X_s \nu \bar{\nu}$, $B_{s,d} \rightarrow K^* l^+ l^-$
- 7.** CP-Violation in B_d , B^\pm Decays $(S_{\phi K_s}, S_{\pi^0 K_s}, \dots)$

Other interesting Processes

- ◆ $\mu^- \rightarrow e^- e^+ e^-$: even more constrained than $\mu \rightarrow e\gamma$

$$Br(\mu^- \rightarrow e^- e^+ e^-)_{exp} < 1.0 \cdot 10^{-12}$$

[SINDRUM Collaboration]

- ◆ $\tau \rightarrow \mu\gamma$ and $\tau \rightarrow e\gamma$: similar to $\mu \rightarrow e\gamma$

$$Br(\tau \rightarrow \mu\gamma)_{exp} < 1.6 \cdot 10^{-8}$$

[Belle, BaBar]

$$Br(\tau \rightarrow e\gamma)_{exp} < 9.4 \cdot 10^{-8}$$

[BaBar, Belle]

- ◆ $\tau \rightarrow \mu\pi$: semileptonic decay

$$Br(\tau \rightarrow \mu\pi)_{exp} < 5.8 \cdot 10^{-8}$$

(Future:
Super B)

[Belle, BaBar]

- ◆ $\mu \rightarrow e$ conversion

$$R(\mu T_i \rightarrow e T_i) < 4.3 \cdot 10^{-12}$$

10⁻¹⁸ (J-Parc)

- ◆ $K_L \rightarrow \mu e$: flavour violating in both quark and lepton sectors

$$Br(K_L \rightarrow \mu e)_{exp} < 4.7 \cdot 10^{-12}$$

[BNL E871 Collaboration]

More Correlations in Flavour SUSY Models

