



# Proton Structure Function $F_L$ at HERA



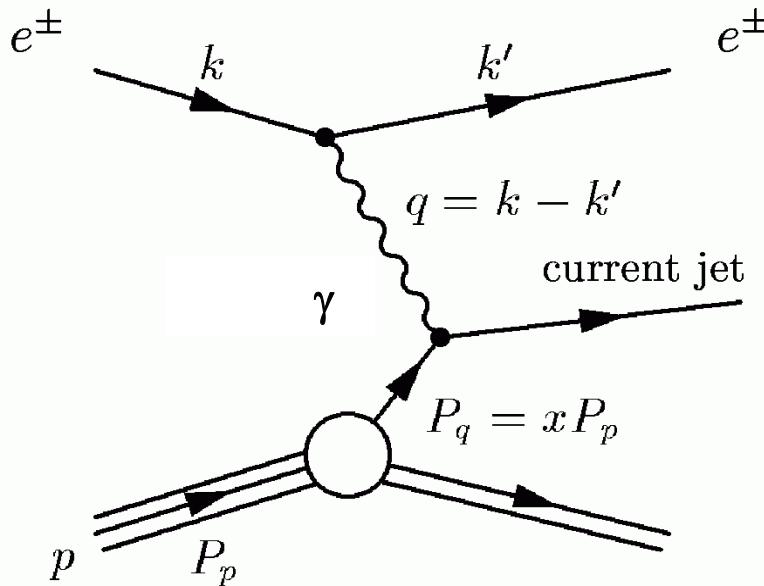
Burkard Reisert,  
Max Planck Institut für Physik,

on behalf of H1 and ZEUS



- Deep Inelastic Scattering (DIS)
- Experimental Setup
- Results on  $F_L$
- Conclusion

# Deep Inelastic Scattering



Center of mass energy  $\sqrt{s}$ :  $s = (k + p)^2$

## Kinematic Variables

- 4-momentum transfer resolving power

$$Q^2 = -q^2 = -(k - k')^2$$

- Bjørken scaling variable momentum fraction of struck parton

$$x = \frac{Q^2}{2p \cdot q}$$

- Inelasticity:  $y = \frac{p \cdot q}{p \cdot k}$

relation for fixed  $s$ :  $Q^2 = sxy$

- Neutral current DIS cross section expressed by structure functions:

$$\frac{d^2\sigma^{e^\pm p \rightarrow e^\pm X}}{dxdQ^2} = \frac{2\pi\alpha^2}{xQ^4} \underbrace{\left(1 + (1-y)^2\right)}_{Y_\pm = 1 \pm (1-y)^2} \cdot \left[ F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2) \right]$$

reduced cross section

# Deep Inelastic Scattering

Reduced ep DIS  
Cross section:

$$\frac{Q^4 x}{2\pi\alpha^2 Y_+} \frac{d^2\sigma}{dxdQ^2} = \sigma_r = F_2(x, Q^2) - \frac{y^2}{Y_+} F_L(x, Q^2)$$

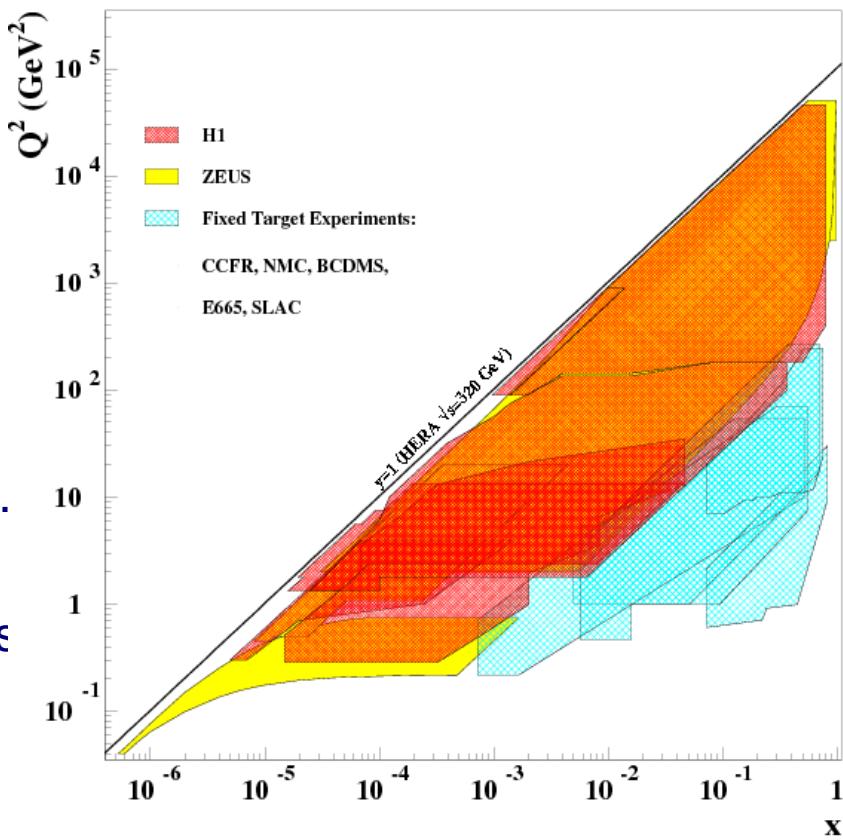
Two proton structure functions define  
inclusive DIS ep scattering cross section.

$F_2$  determines sum of quark distributions.

$F_L$ , at low  $x$ , determines gluon distribution.

The  $F_2$  term dominates the cross section,  
has been measured for 15 years at HERA.

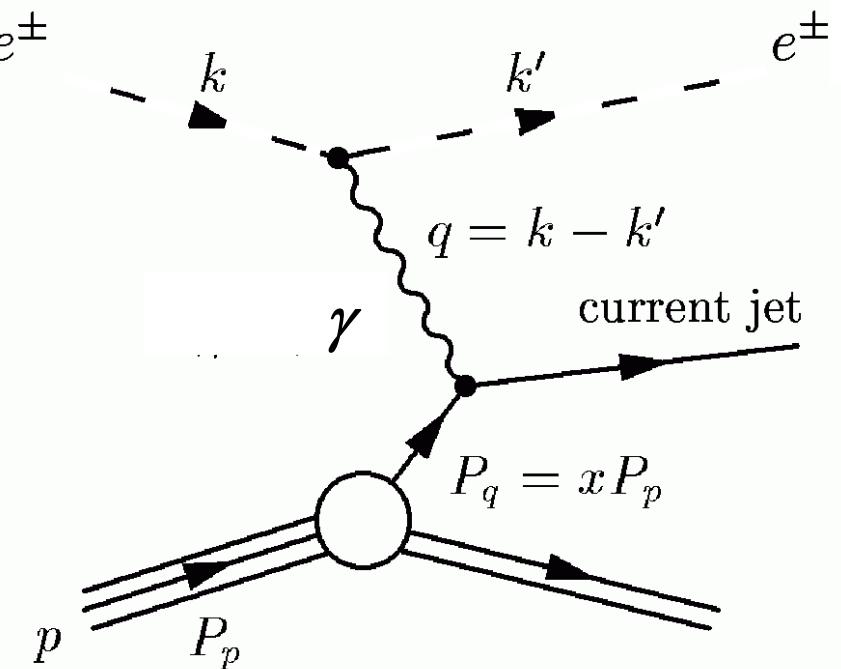
The  $F_L$  term is sizeable only at large values  
of inelasticity  $y$ . It was directly accessed  
on in the last 4 months of HERA's  
operation



MPP Munich

# Photon Proton Scattering

- The same process may be interpreted as scattering of a virtual photon off an proton
- The virtual photon may be transversely or longitudinally polarized



$\gamma p$  Cross Sections:

$$\sigma_T^{\gamma p} = \frac{4\pi\alpha}{Q^2} 2xF_1 = \frac{4\pi\alpha}{Q^2} (F_2 - F_L)$$

$$\sigma_L^{\gamma p} = \frac{4\pi\alpha}{Q^2} (F_2 - 2xF_1) = \frac{4\pi\alpha}{Q^2} F_L$$

$$\frac{\sigma_L^{\gamma p}}{\sigma_T^{\gamma p}} = R = \frac{F_L}{F_2 - F_L}$$

Quark Parton Model (QPM)

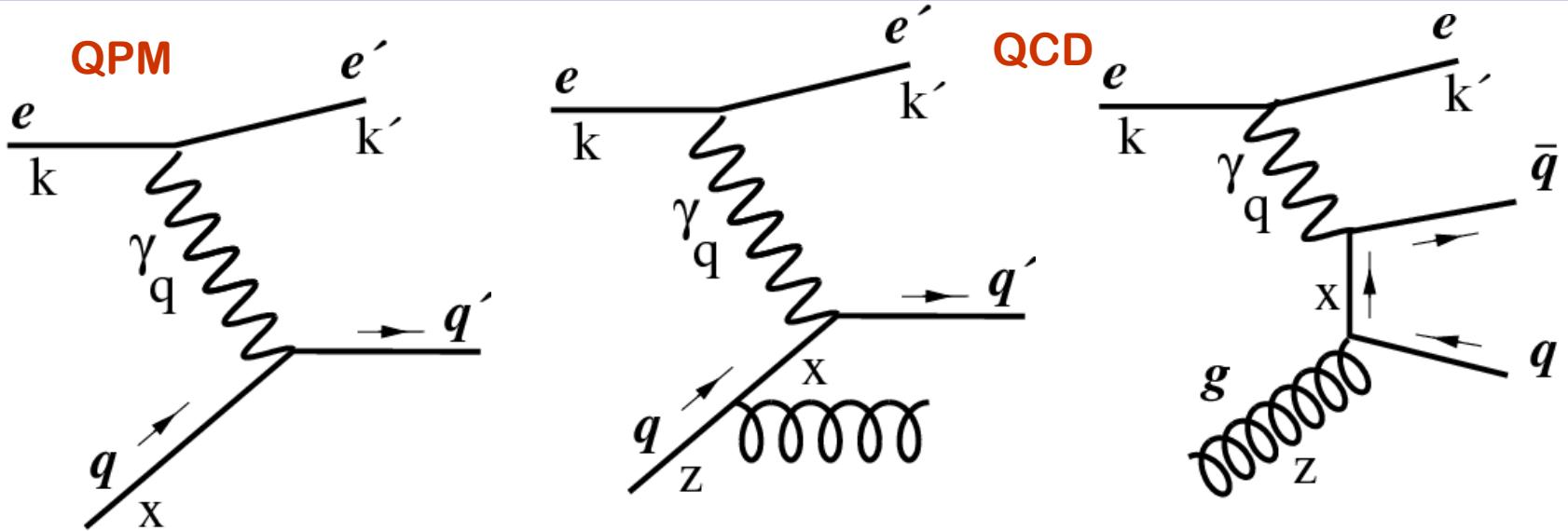
$$F_1(x) = \frac{1}{2x} \sum_q e_q^2 x q(x)$$

$$F_2(x) = \sum_q e_q^2 x q(x)$$

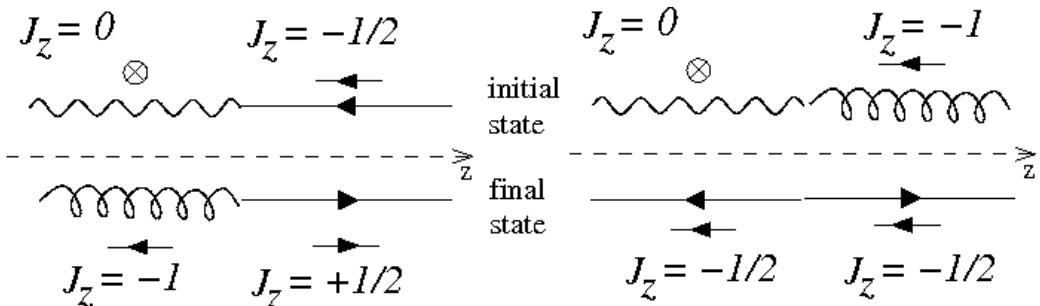
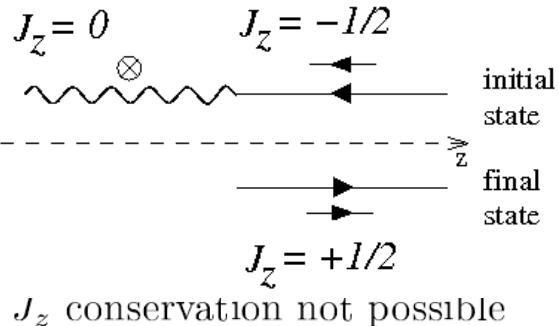
$$F_L(x) = F_2 - 2xF_1 = 0$$

Callan Gross relation

# Longitudinal Structure Function $F_L$



Scattering of longitudinally polarized photons on quarks in helicity frame



$$F_L = \frac{\alpha_s}{4\pi} x^2 \int_x^1 \frac{dz}{z^3} \left[ \frac{16}{3} \sum_q z e_q^2 (\textcolor{red}{q} + \bar{q}) + 8 \sum_q e_q^2 \left(1 - \frac{x}{z}\right) \cdot z \textcolor{red}{g} \right]$$

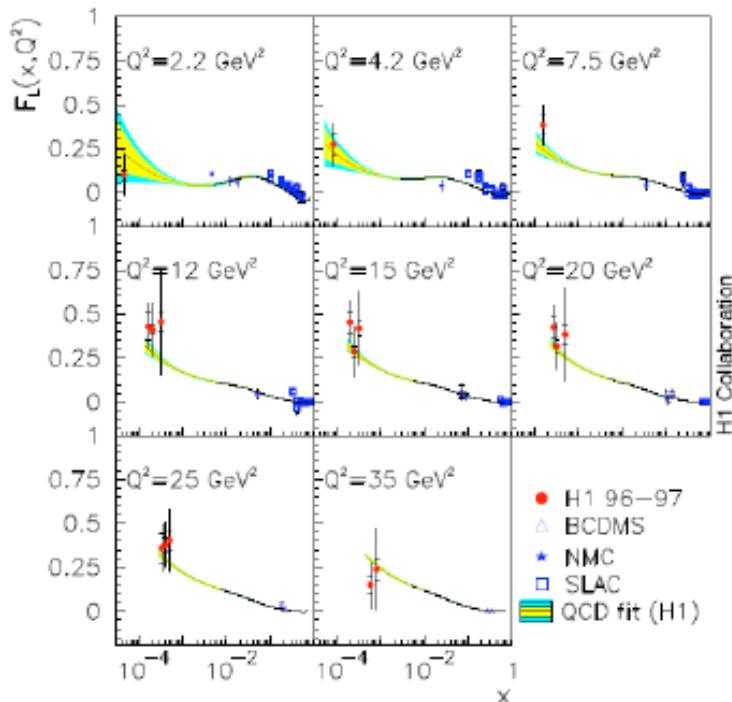
access to gluon density



MPP Munich

# Expectations on FL

## Experiment



Fixed target:  $F_L$  is small at large  $x$  (spin 1/2 quarks)  
indications for increase towards low  $x$

H1: hints to large  $F_L$  when  $F_2$  is assumed to be known

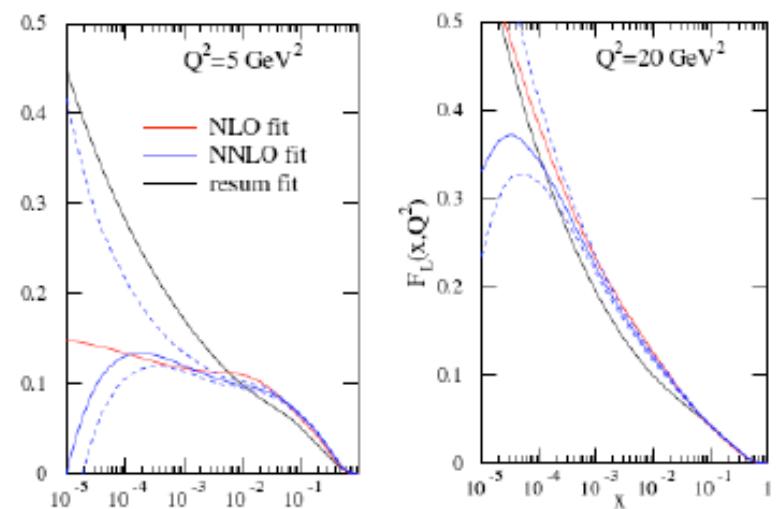
Eur.Phys.J.C21:33-61,2001

## Theory (pQCD)

$F_L$  prediction related to the gluon density,  
the size and the uncertainties on  $xg$  -  
constraints require max accuracy and range

Theory developed to NNLO  
[W.van Neerven ( $\dagger$ ), J.Vermaseren, et al.]

Global/detailed pdf analyses  
[CTEQ, MRST, Alechin, HERA, ...]



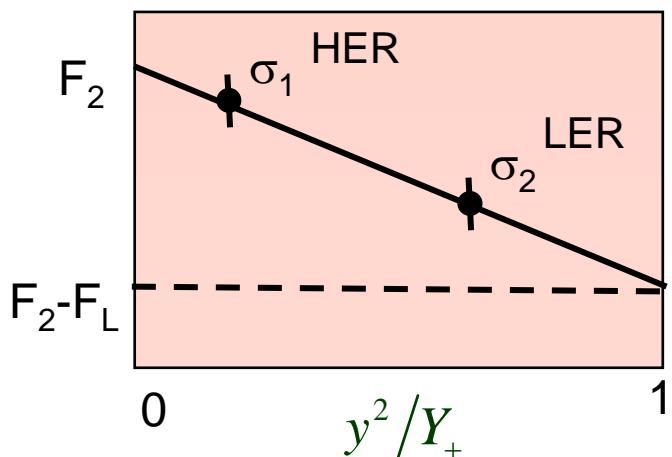
R.Thorne, DIS08



MPP Munich

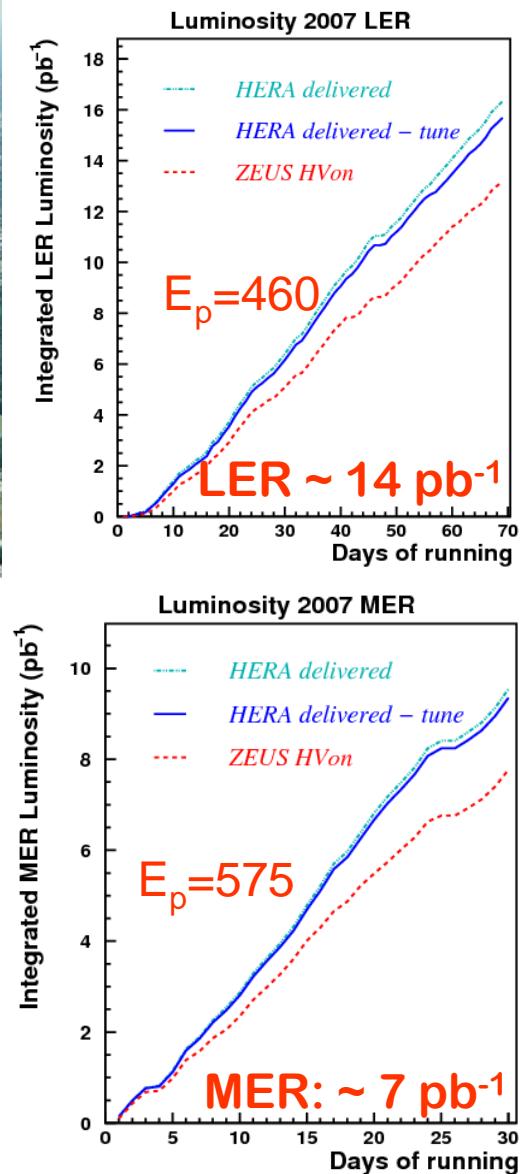
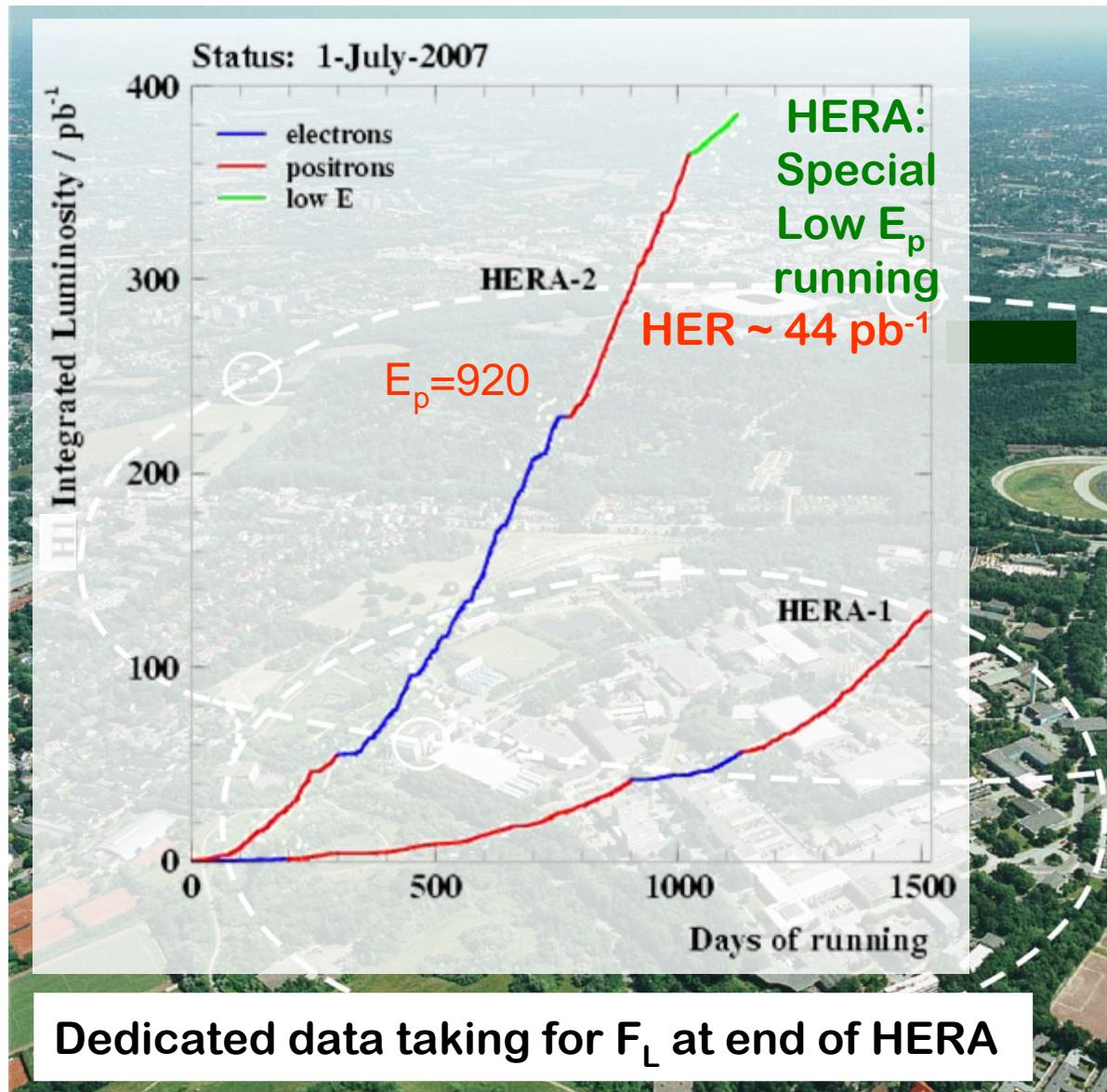
# How to Measure $F_L$ ?

- Measure cross sections at same  $x$  and  $Q^2$  but different  $y = Q^2/x \cdot s$   $\rightarrow$  vary  $s$



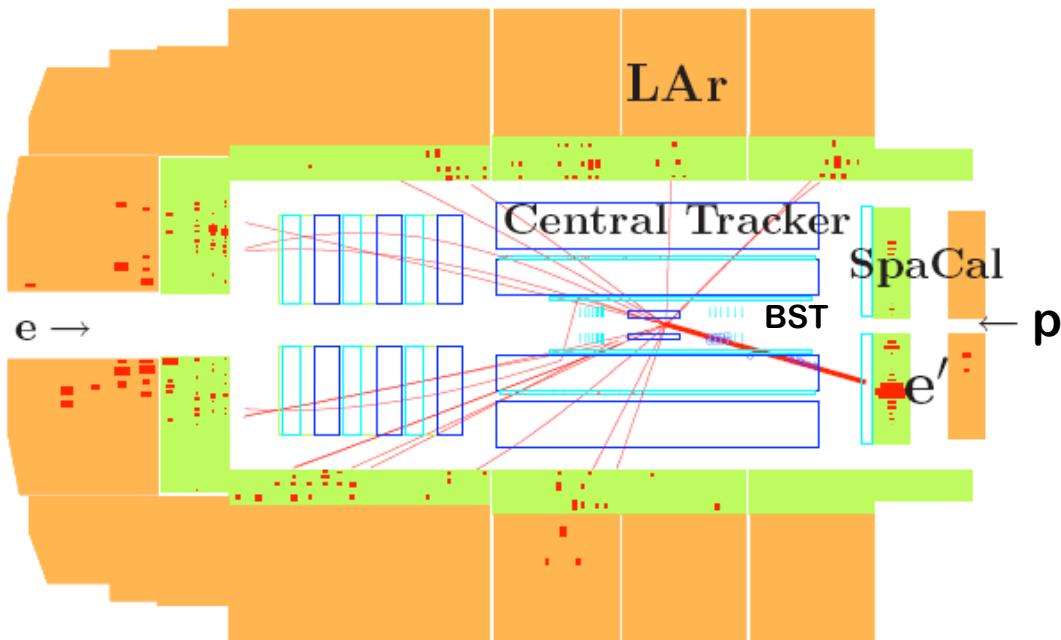
- Change proton beam energy to change cms energy
- Large level arm in  $y^2/Y_+$
- Measure at high  $y$  in LER
- Extended measurement to high  $y$  region  
 $y = 1 - E'_e/E_e(1 - \cos\theta) \rightarrow$  high  $y$  means low  $E'_e$
- Estimate: Need  $\sim 10\text{pb}^{-1}$  for measurement

# HERA Accelerator Performance



# Measuring $F_L$ with H1

DIS event of  $Q^2$  near 30 GeV $^2$



## Upgrades for FL

SpaCal (94)

BST (95+03)

## Triggers (03-07)

- Inner Chamber (CIP)
- SpaCal
- Fast Tracking (CJC)
- Jet Trigger (LAr)

## Three $Q^2$ ranges

3 to 12 GeV $^2$  SpaCal+BST  
prelim. 04/09

12 to 90 GeV $^2$  SpaCal+CT:  
published 08

35 to 800 GeV $^2$  LAr+CT:  
prelim. 03/08

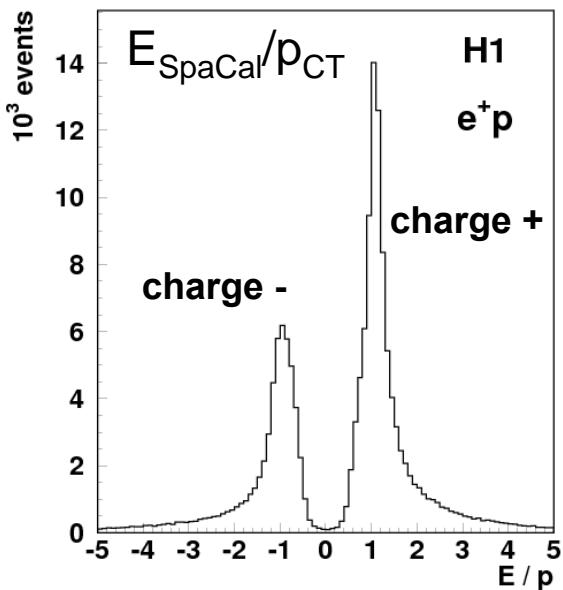
## Event selection Criteria

EI. in SpaCal or LAr (Calo & Trig)  $E'_e > 3$  GeV  
Track in CT or BST (veto neutrals, e/p)  
Interaction vertex  
 $E\text{-P}_z = \sum_i E_i (1 - \cos \theta_i) > 35$  GeV  
Reduces largely radiative corrections

# Background Subtraction – H1

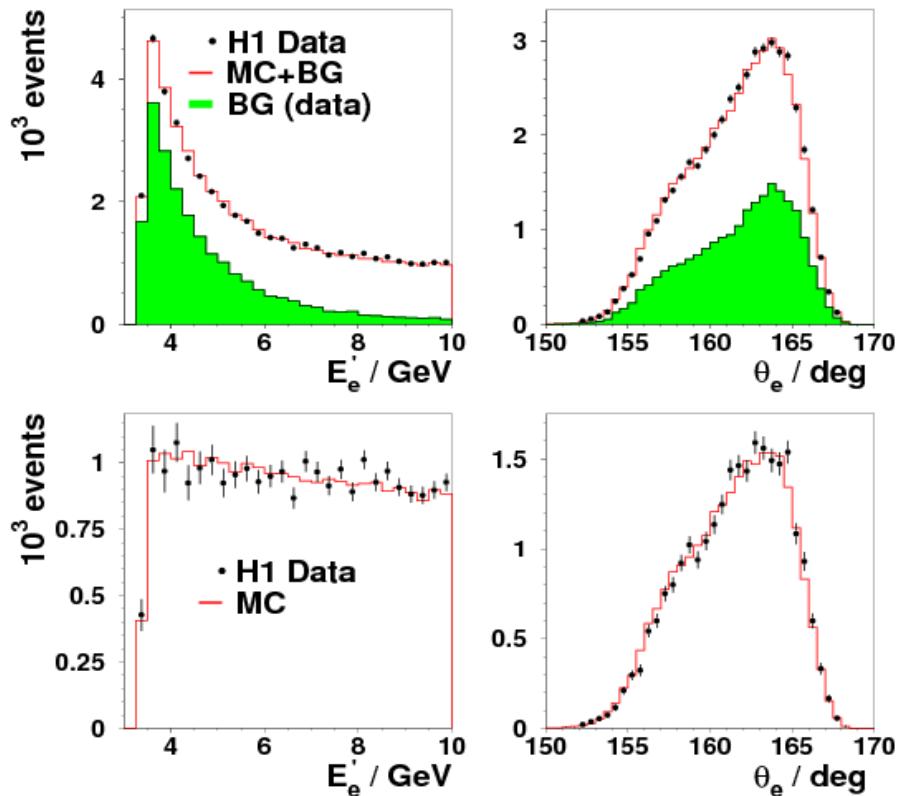
At small energies severe contamination by  $\gamma p$  events.

Those are charge symmetric, apart from small effects due to anti-proton vs protons, which is measured using  $e+p$  and  $e-p$  data, and corrected for



H1 has tracking coverage for the electron candidates for all full Q2 ranges (CT & BST)

Scattered electron distributions (SpaCal + CT)

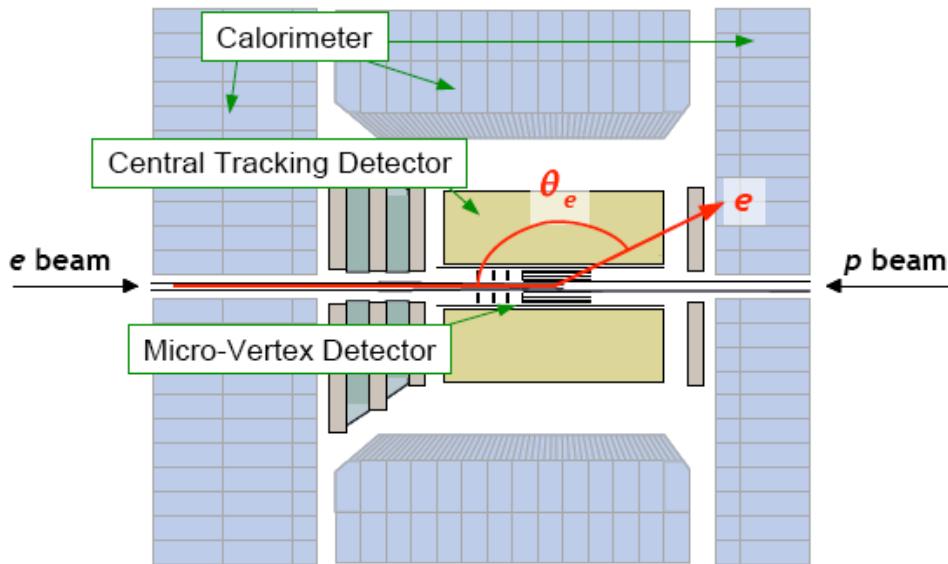


H1 background subtraction based on data.  
Trade off between background rejection and stat. unc. of background sample (wrong chrg.)



MPP Munich

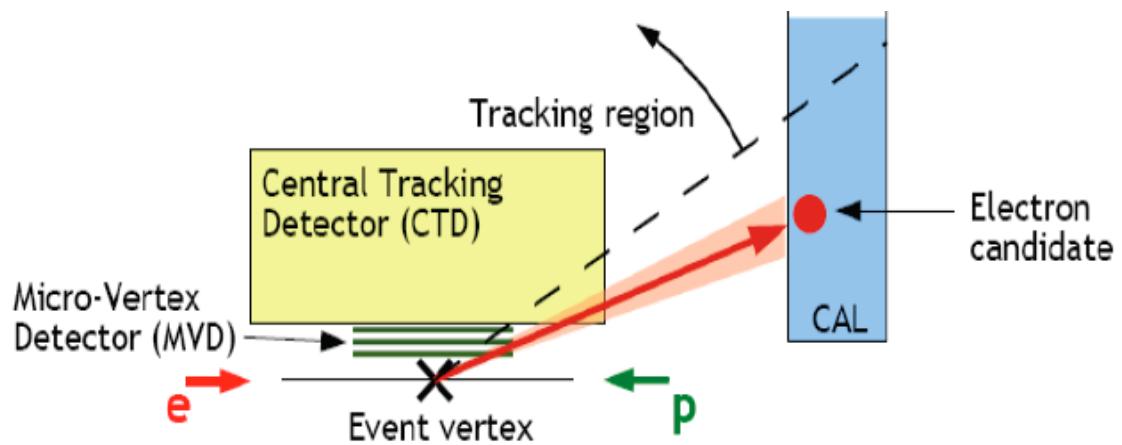
# Measuring FL with ZEUS



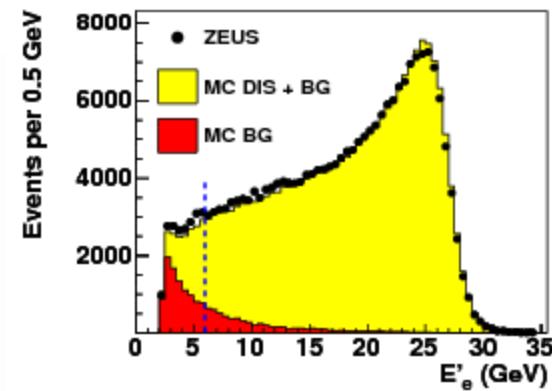
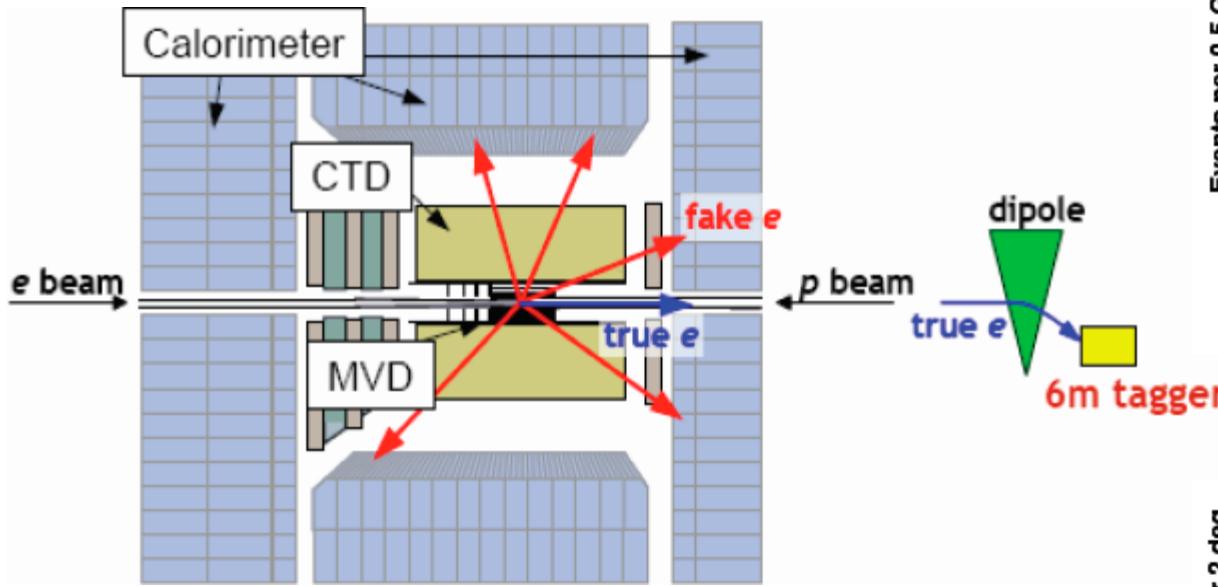
## Event Selection:

Electron in backward Calo  
 $E'_e > 6 \text{ GeV}$  (Cluster & Trigger)  
Hits in CTD & MVD (reject neutrals)  
Event vertex  
 $42 < E\text{-}p_z < 65 \text{ GeV}$

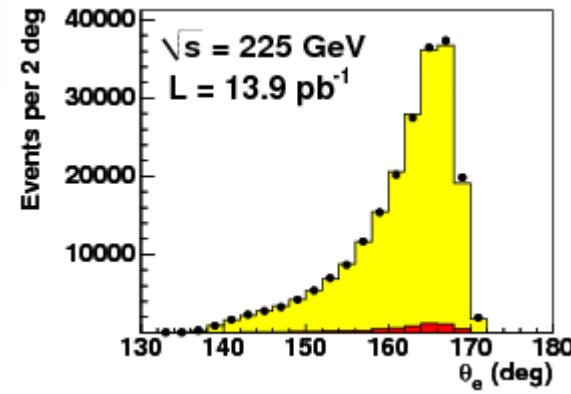
$Q^2$  range between  
24 and 110  $\text{GeV}^2$



# Background Subtraction - ZEUS



ZEUS



Photoproduction BG removed using PYTHIA MC with  
subprocesses (direct, resolved, diffractive,...) weights  
Adjusted to  $\gamma p$  cross section measurement.  
Control using 6m electron tagger. Complimentary studies  
with  $\gamma p$  enriched data sample.



MPP Munich

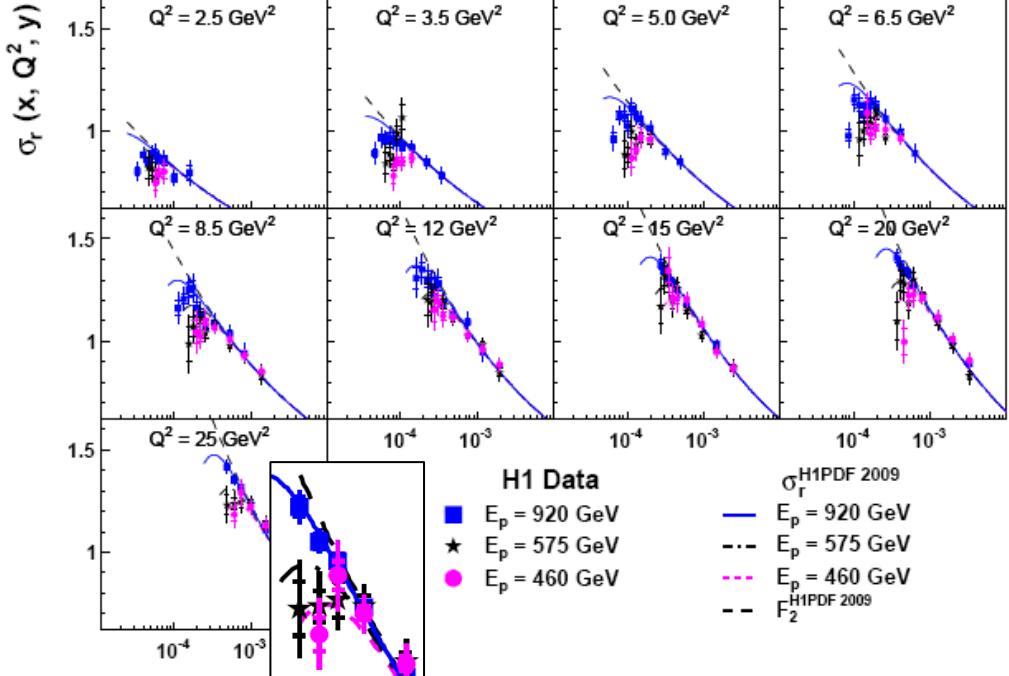
# Cross Sections for direct FL extraction

Direct  $F_L$  measurement requires measurement of the reduced cross sections at **same  $x$  and  $Q^2$  but different  $y$** :

$$\sigma_r(x, Q^2, y) = F_2(x, Q^2) - \frac{y^2}{Y_+} \cdot F_L(x, Q^2)$$

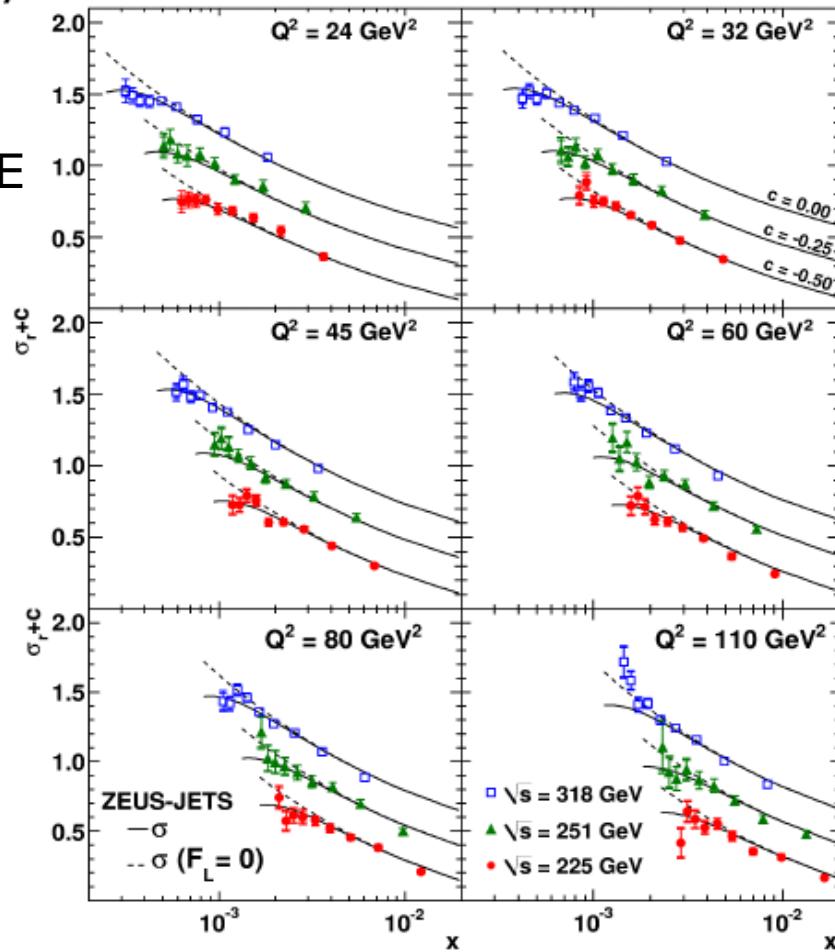
$$y = \frac{Q^2}{x \cdot s}$$

different  $y \rightarrow$  different  $s \rightarrow$  different beam  $E$



Turnover due to  $F_L$  small but visible

**ZEUS**

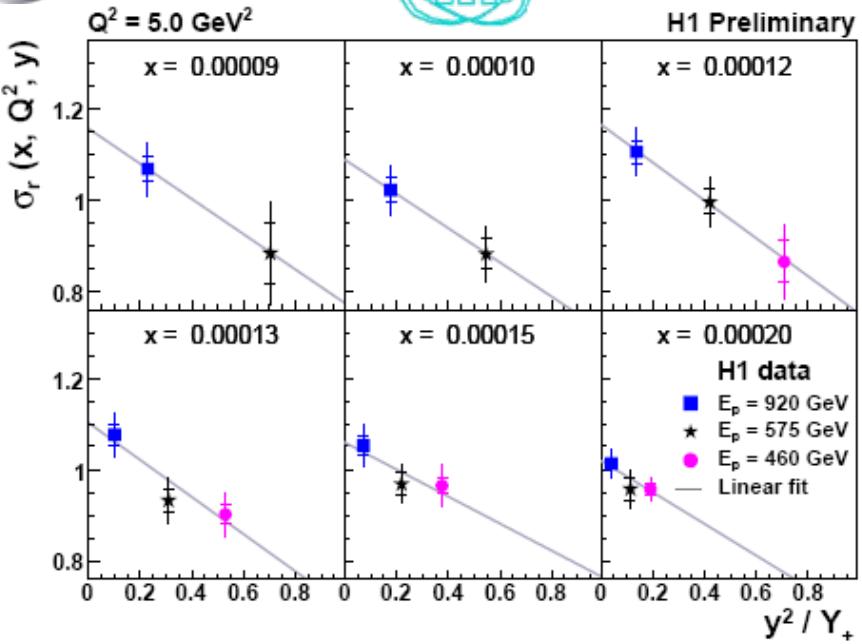


most precise  $\sigma_r$  from ZEUS

# $F_L$ Extraction: Rosenbluth plots

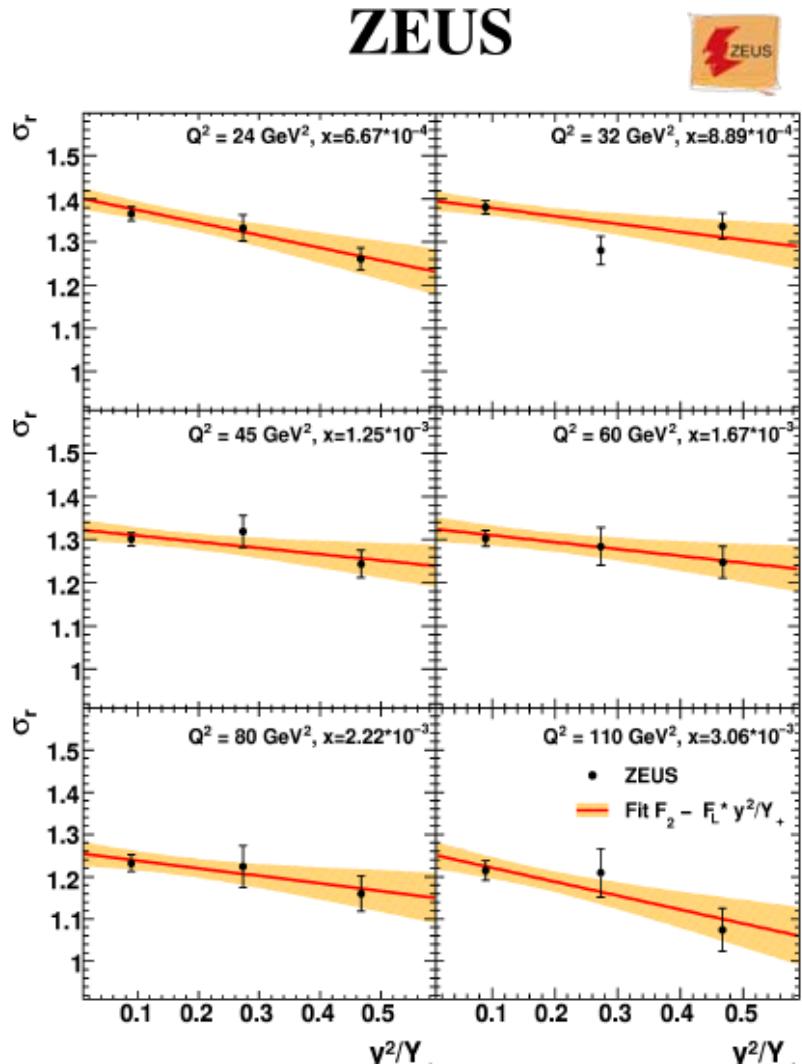
$$\sigma_r(x, Q^2, y) = F_2(x, Q^2) - \frac{y^2}{Y_+} \cdot F_L(x, Q^2)$$

Straight line fit of  $\sigma_r$  vs  $y^2/Y_+$   
 $F_L$  slope,  $F_2$  intercept

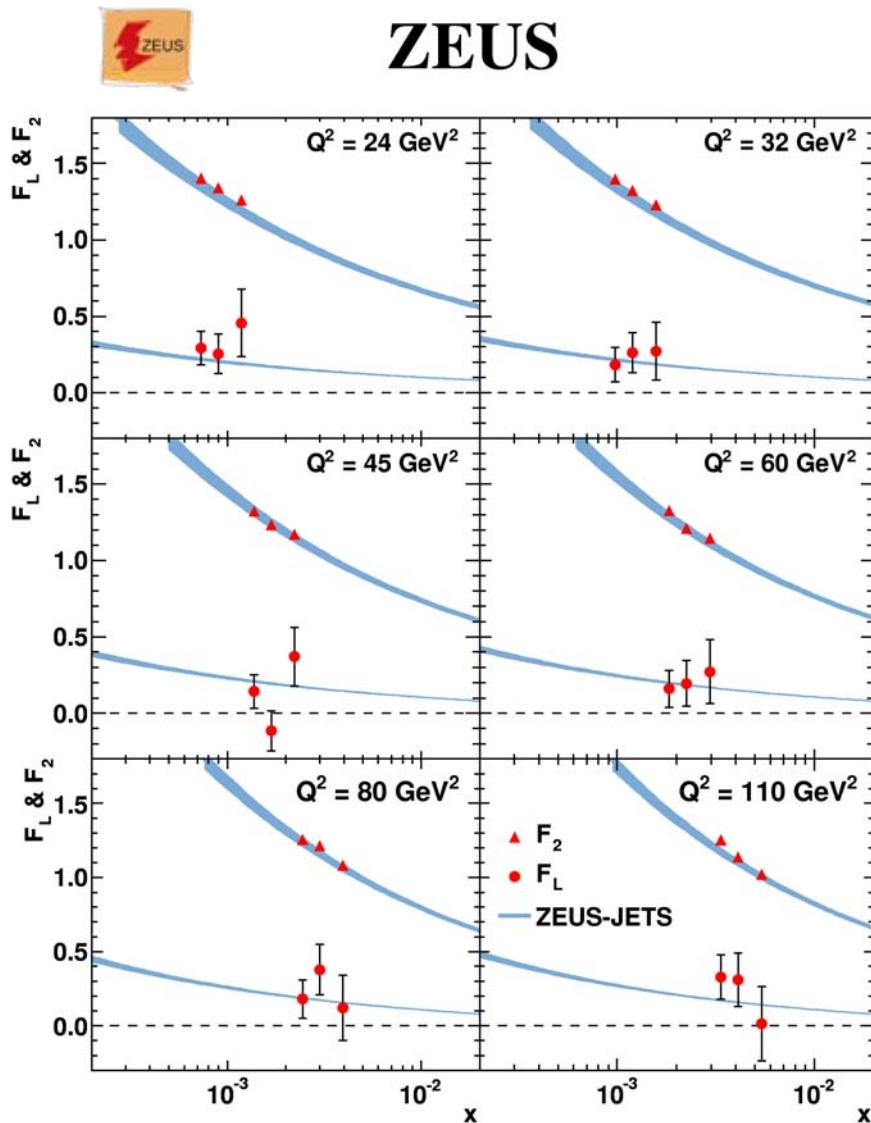


MPP Munich

**ZEUS**



# Extracted $F_L$ and $F_2$ – ZEUS

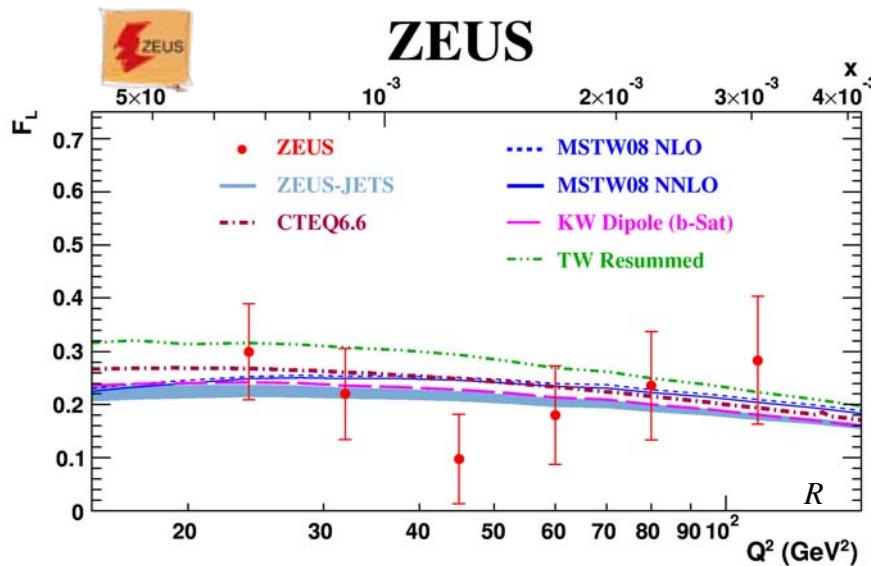


- Most precise  $F_2$  measurement from ZEUS in kinematic region studied
- First  $F_2$  measurement without assumptions on  $F_L$
- Data support a non-zero  $F_L$
- Predictions for  $F_2$  and  $F_L$  are consistent with data



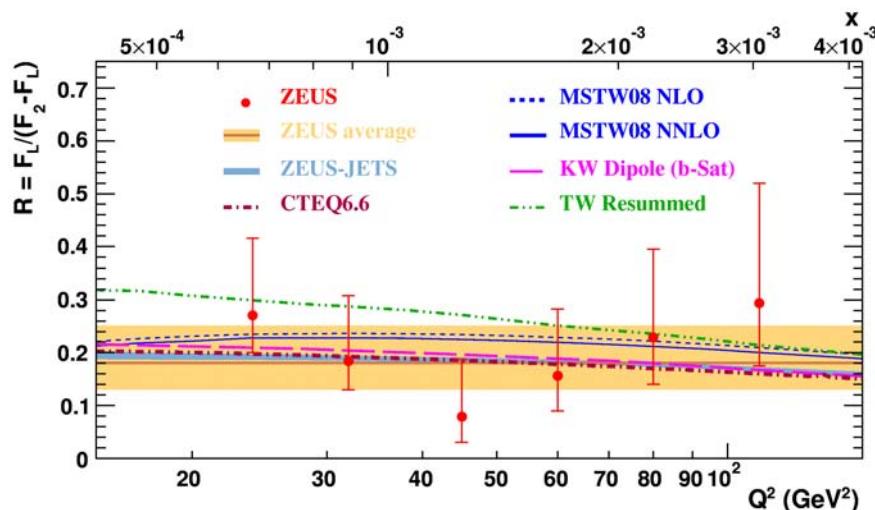
MPP Munich

# Average $F_L$ and $R$ – ZEUS



Averaged  $F_L$

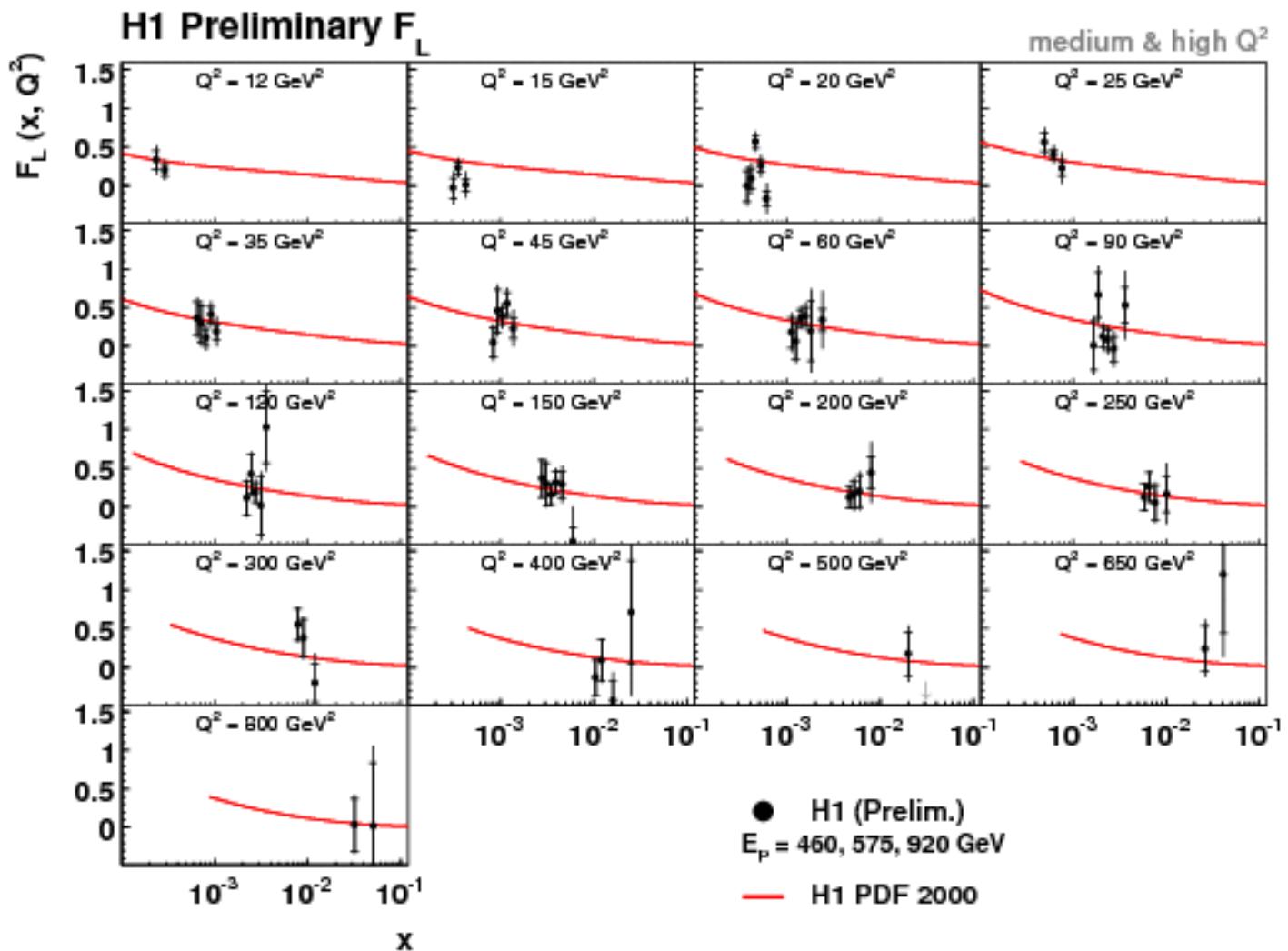
- Data support non-zero  $F_L$
- Predictions are consistent with data



Averaged  $R = F_L / (F_2 - F_L)$

■  $R = 0.18^{+0.07}_{-0.05}$

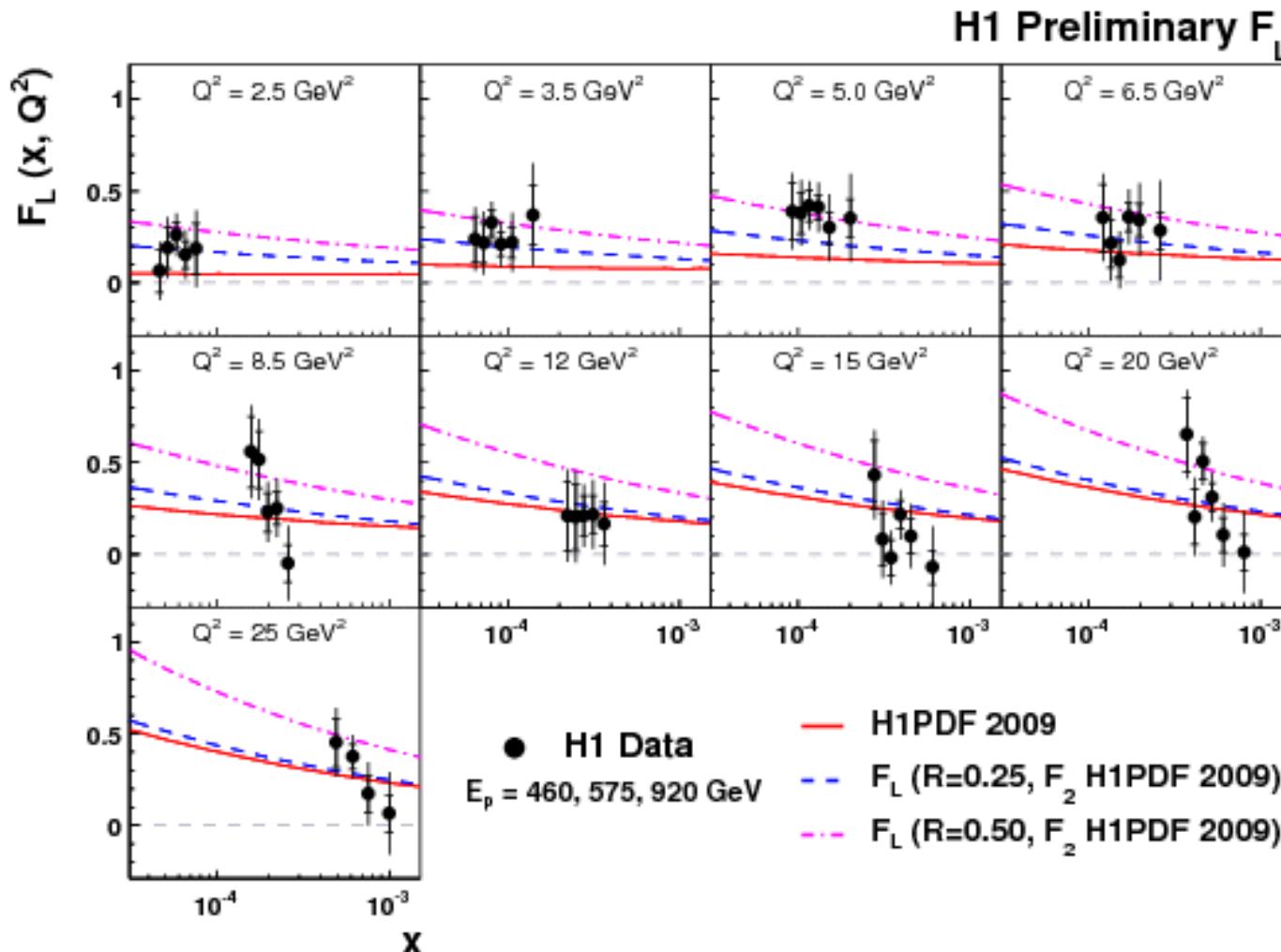
# Extracted $F_L$ – medium & high $Q^2$



Medium Q2 published in Phys. Lett. B665, p. 139



# Extracted $F_L$ – Low $Q^2$

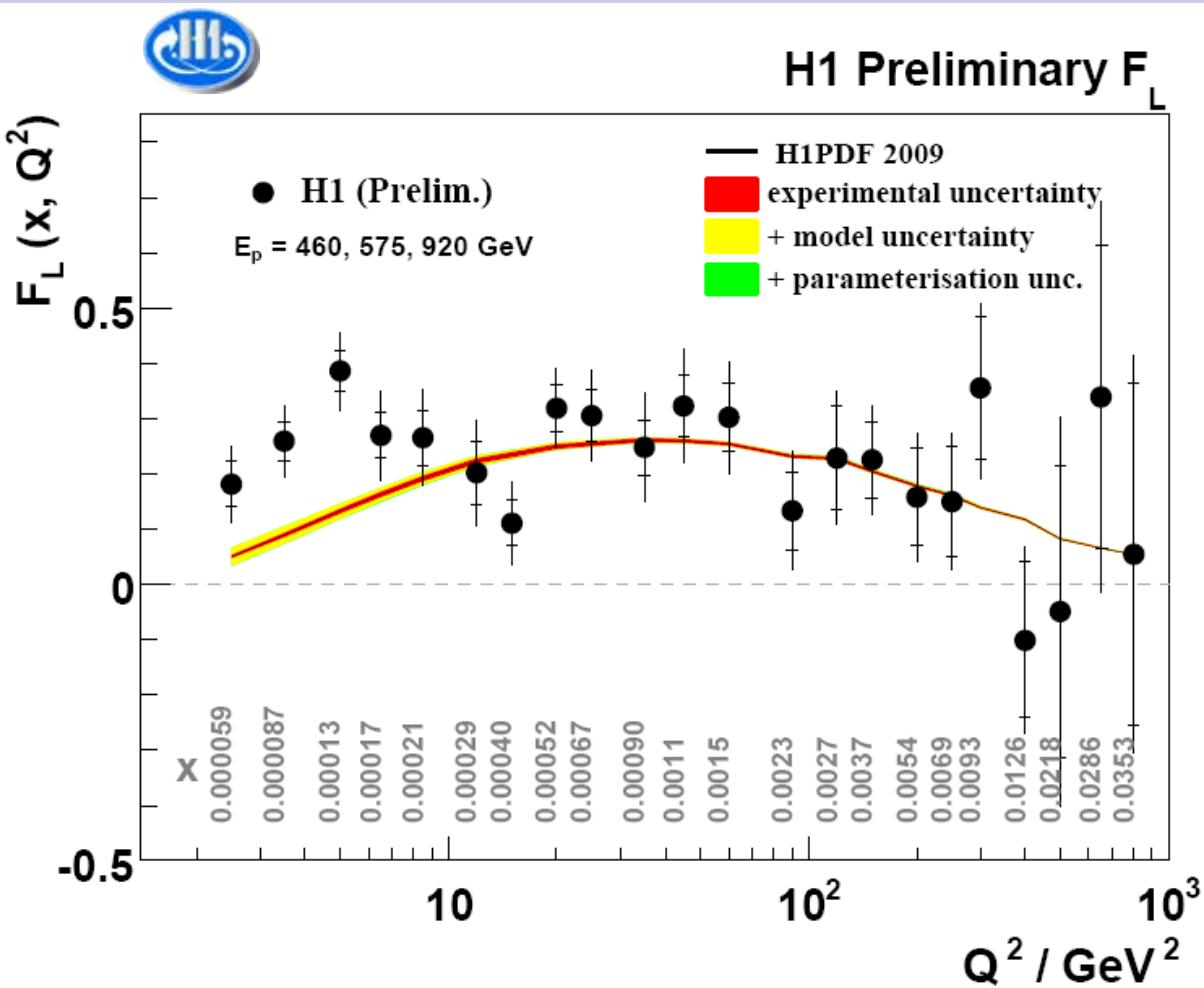


$F_L$  measured down to  $Q^2 = 2.5 \text{ GeV}^2$ !

Data are consistent with  $R \sim 0.25$  ( $F_L = 0.2 \cdot F_2$ )



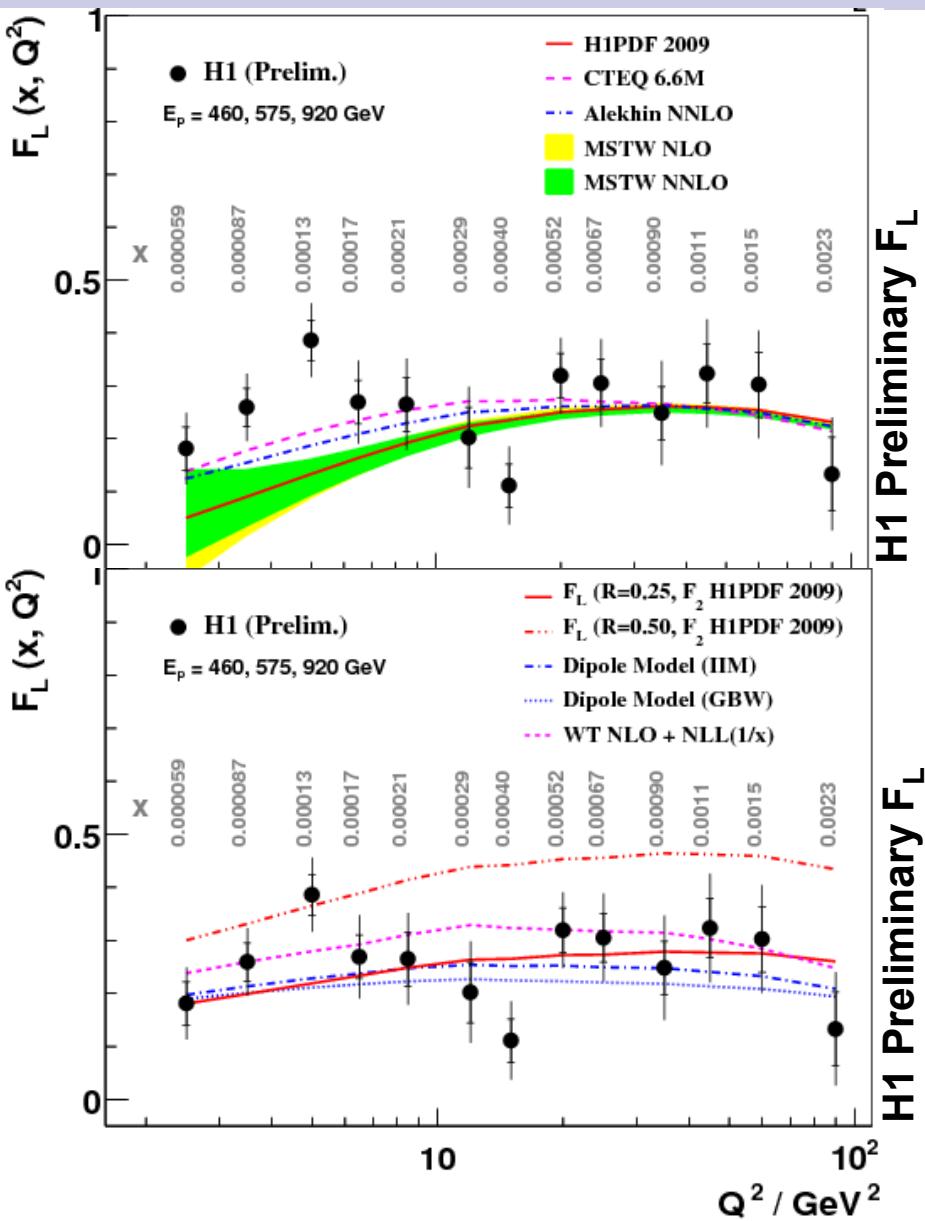
# Average $F_L - H1$



H1 measurements cover  $2.5 \leq Q^2 \leq 800 \text{ GeV}^2$  and  $0.00005 \leq x \leq 0.05$   
For  $Q^2 \geq 10 \text{ GeV}^2$ , agree well with H1PDF 2009 prediction.



# Average $F_L < 100 \text{ GeV}^2$



- MSTW and H1PDF 2009 predictions use the same heavy flavour scheme to calculate  $F_L$ .
- Data agree better with calculation of CTEQ (and Alekhin)
- Data is consistent with constant  $R \sim 0.25$ .
- Good agreement with IIM and GBW dipole models, NLL(1/x) prediction.

# Summary and Outlook

Longitudinal structure function  $F_L$  has been measured by H1 & ZEUS  
FL has thus been measured for the first time in a new kinematic range:  
 $Q^2 = 24 - 110 \text{ GeV}^2$  (ZEUS) and  $2.5 - 800 \text{ GeV}^2$  (H1),  $x = 0.00005 - 0.05$   
Data are consistent with constant  $R \sim 0.2$  (H1),  $R = 0.18^{+0.07}_{-0.05}$  (ZEUS)  
For  $Q^2 > 10 \text{ GeV}^2$ , data are in good agreement with pQCD predictions  
and thus confirm expectations on the behaviour of  $xg$  in the DIS  
kinematic region.

Measured  $F_L$  is higher than the predictions of MSTW  
at NLO and NNLO as well as H1PDF2009 for  
 $Q^2 < 10 \text{ GeV}^2$ , agree better with the CTEQ 6.6M and  
Alekhin NNLO predictions.

The FL data thus can be expected to further constrain low  $x$  theory.

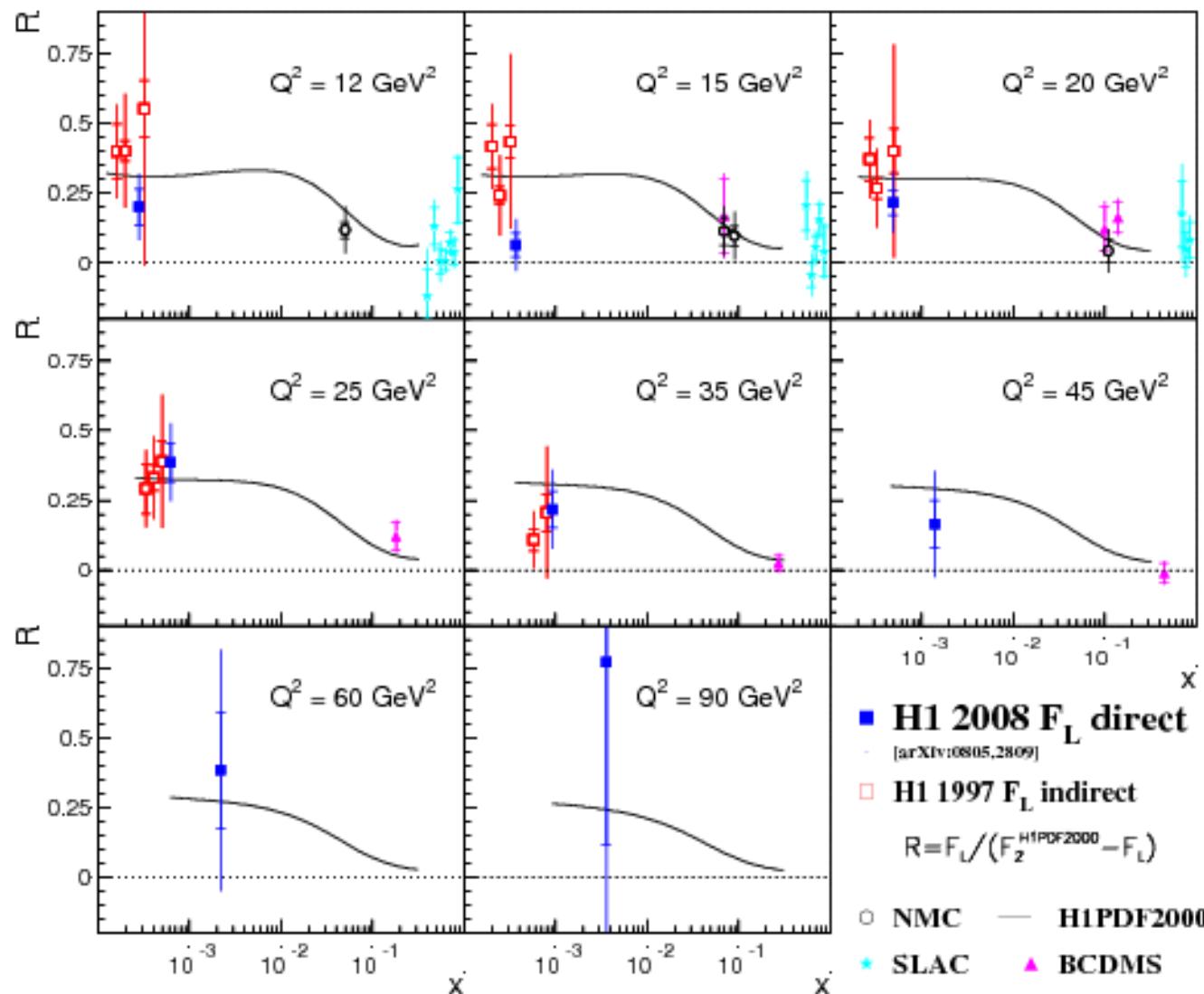
# Backupslides

- FL compare direct to indirect measurements
- ZEUS Control Plots
- H1 Control Plots
- H1 cross sections
- H1 FL ( $x, Q^2$ )
- H1 averaged FL( $Q^2$ )



MPP Munich

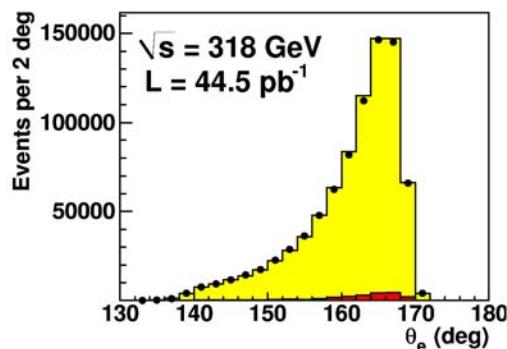
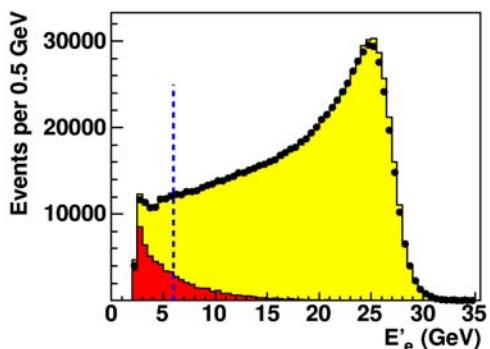
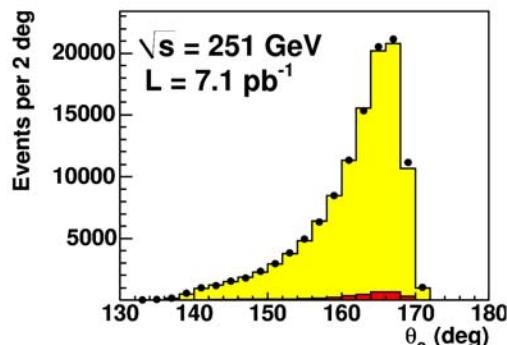
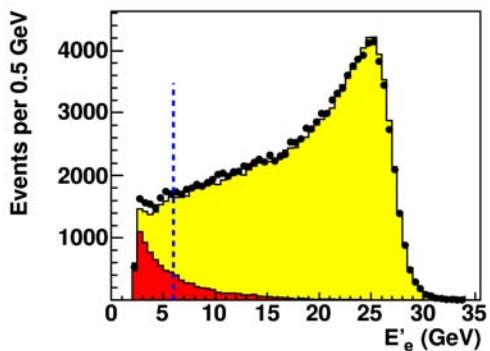
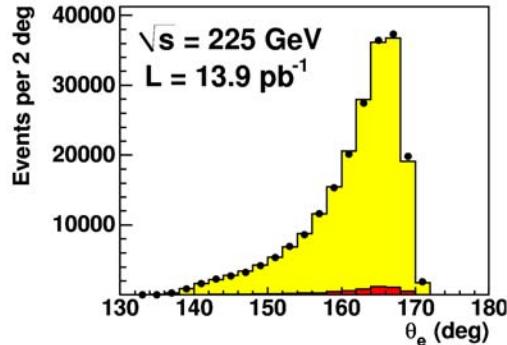
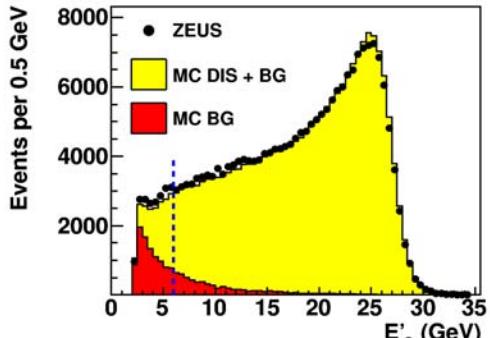
# $F_L$ direct vs. indirect Measurements



MPP Munich

# ZEUS Control Plots

ZEUS



Low Energy Run

$E_p = 460 \text{ GeV}$

Medium Energy Run

$E_p = 575 \text{ GeV}$

High Energy Run

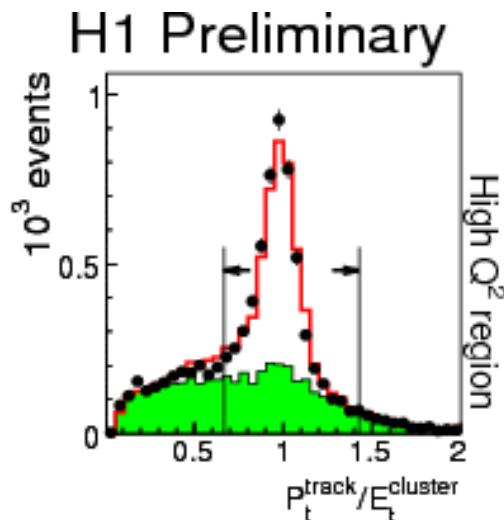
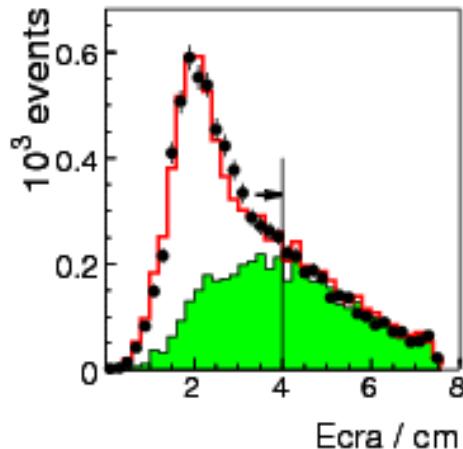
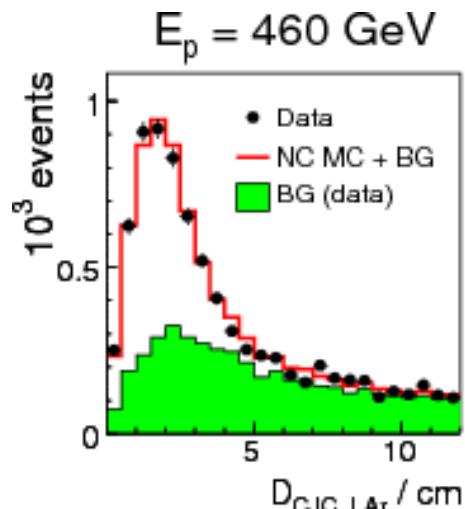
$E_p = 920 \text{ GeV}$



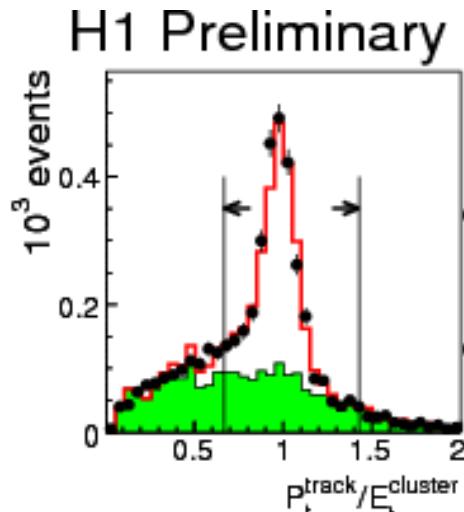
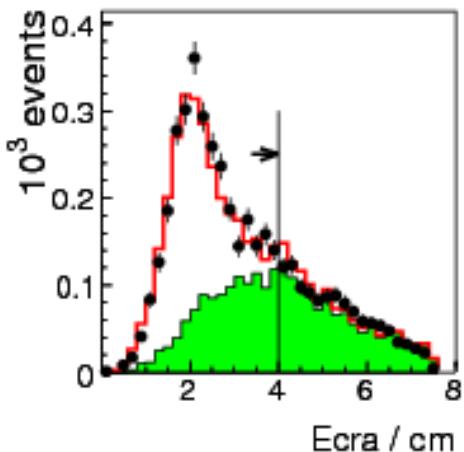
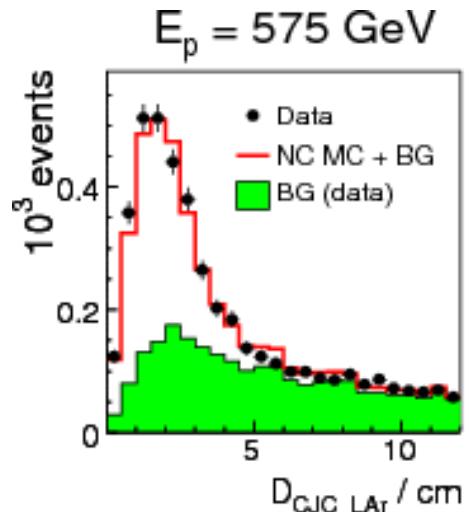
MPP Munich

Burkard  
Reisert  
EPS09

# H1 Control Plots: Electron Variables

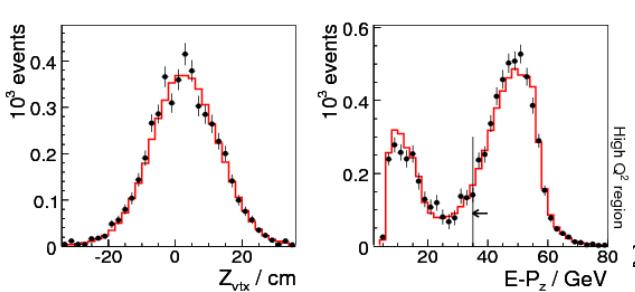
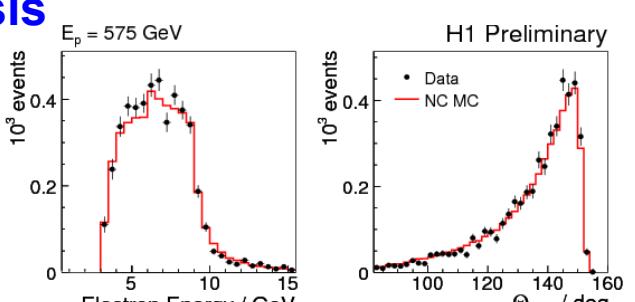
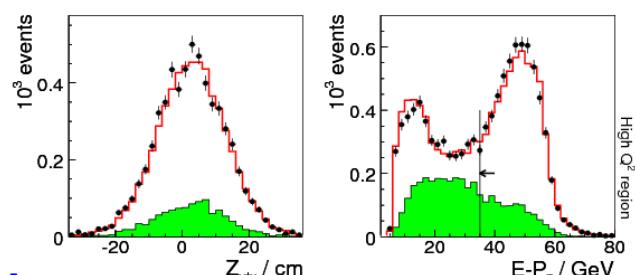
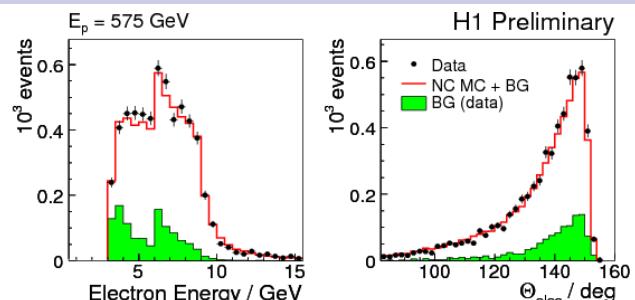
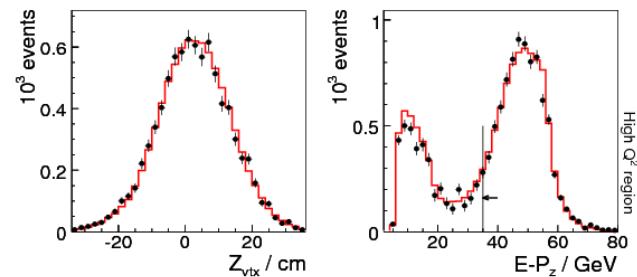
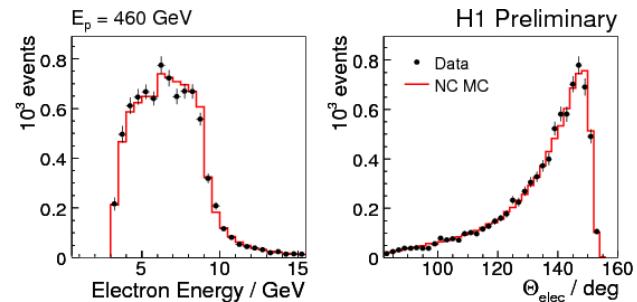
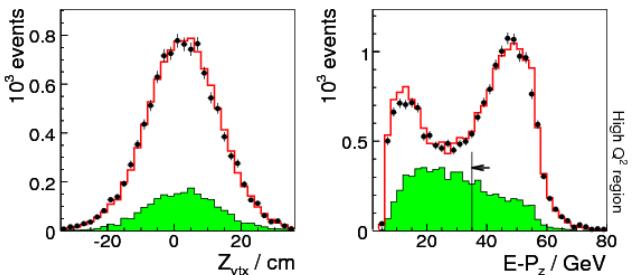
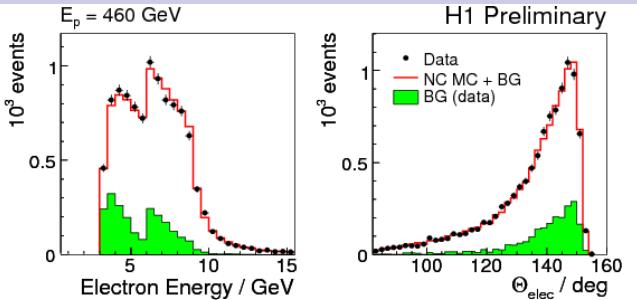


## High $Q^2$ Analysis



MPP Munich

# H1 Control Plots: BG Subtraction



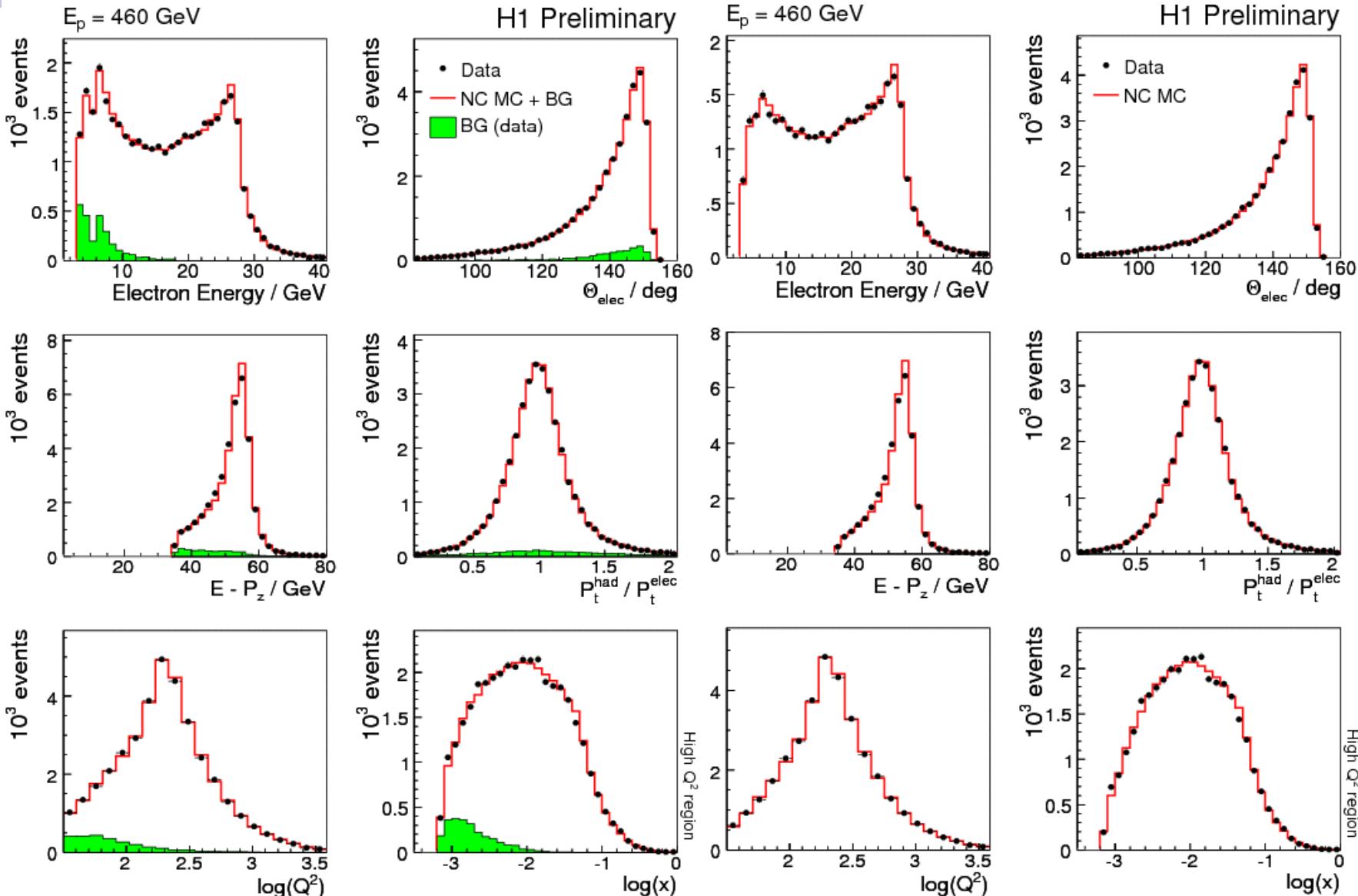
## High Q<sup>2</sup> Analysis



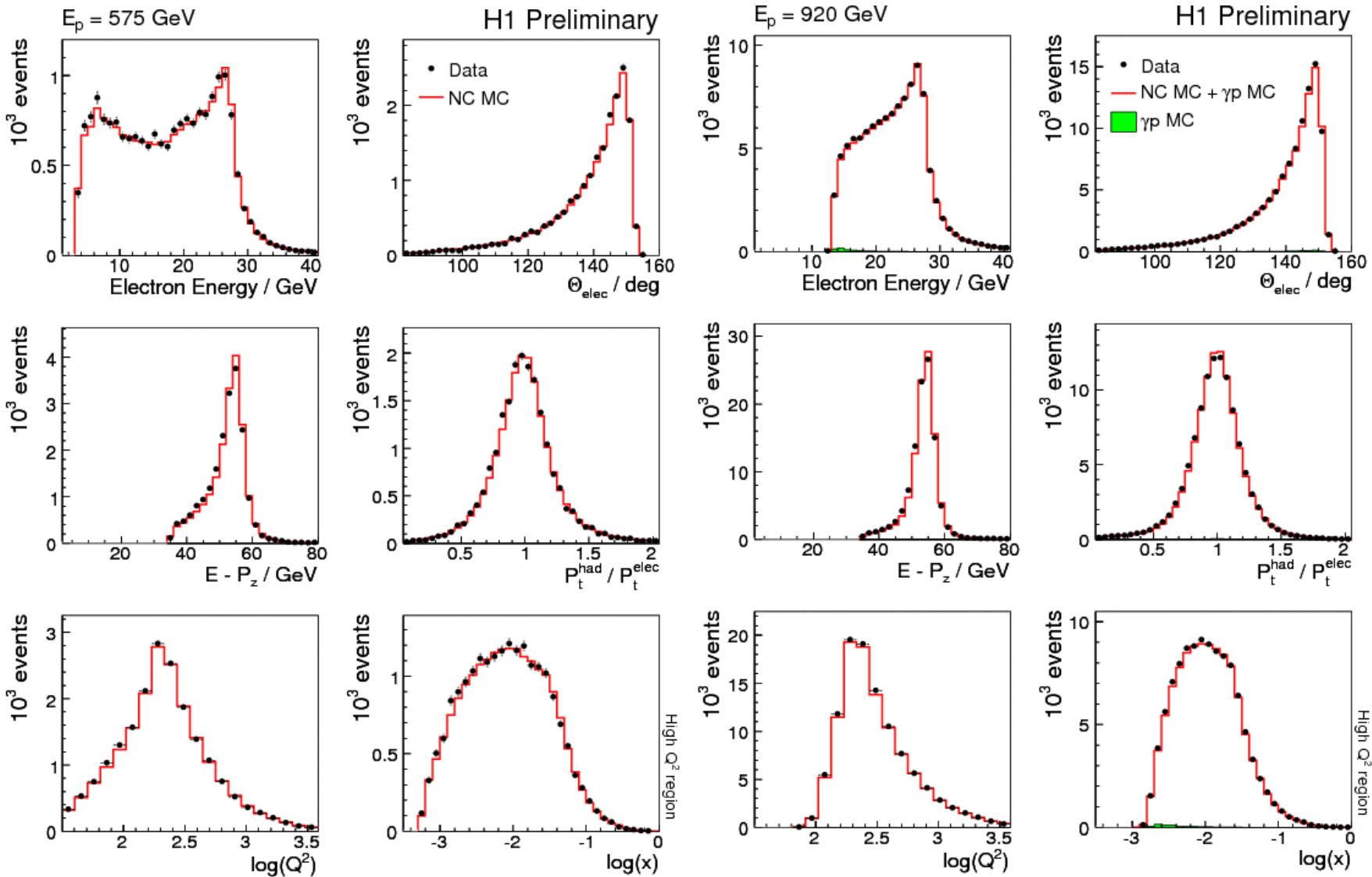
MPP Munich

Burkard  
Reisert  
EPS09

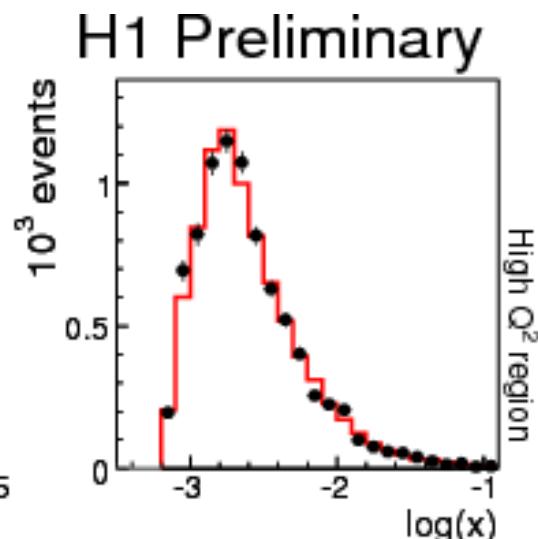
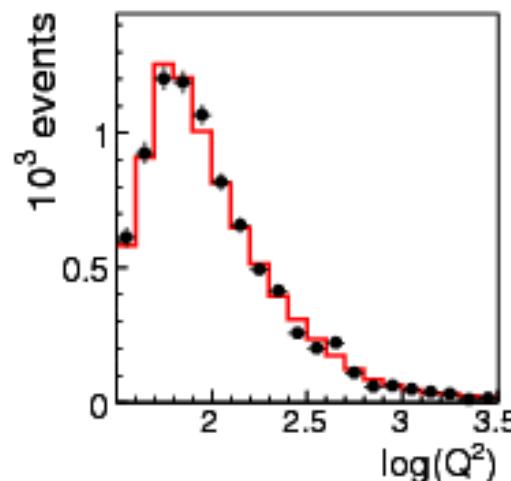
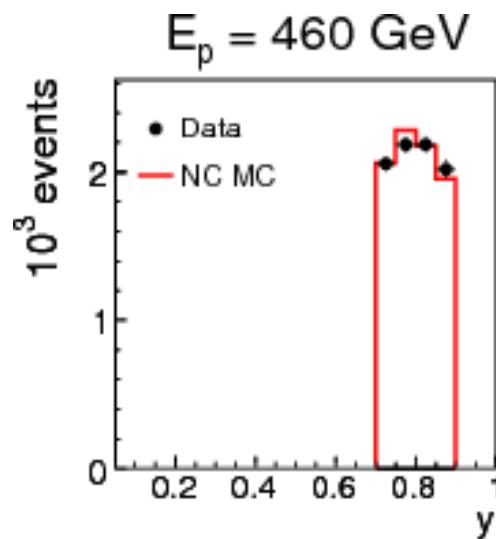
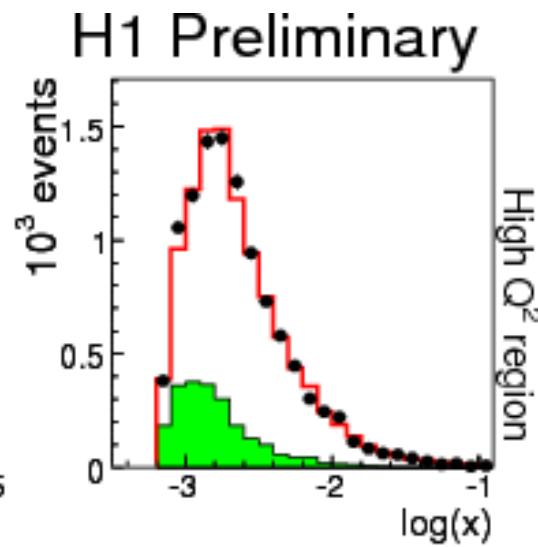
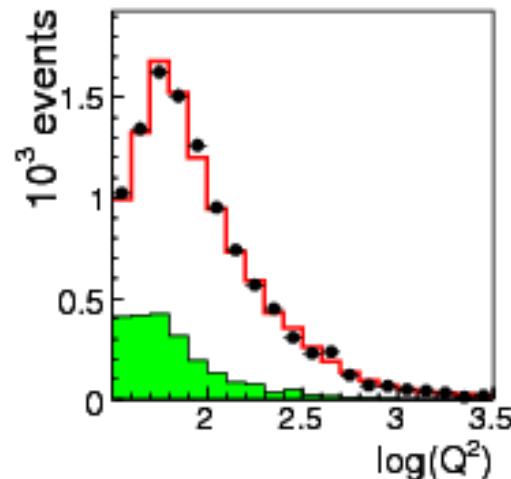
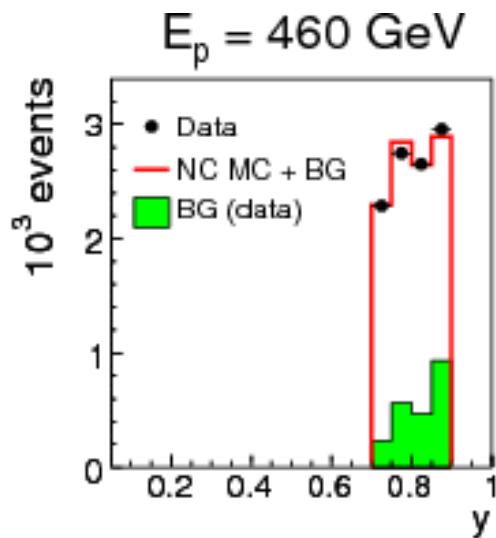
# H1 Control Plots: Event Variables



# H1 Control Plots: Event Variables

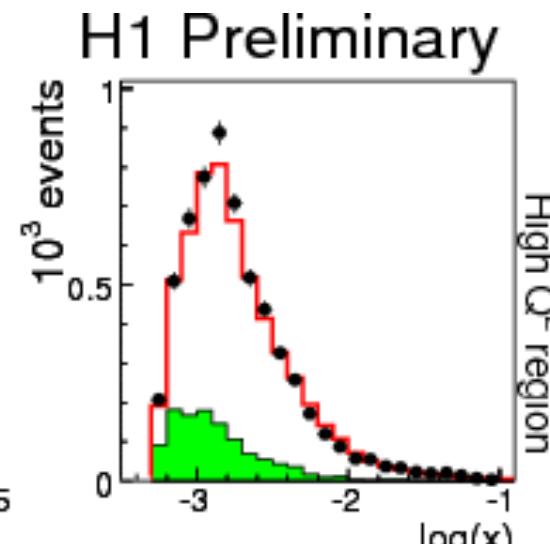
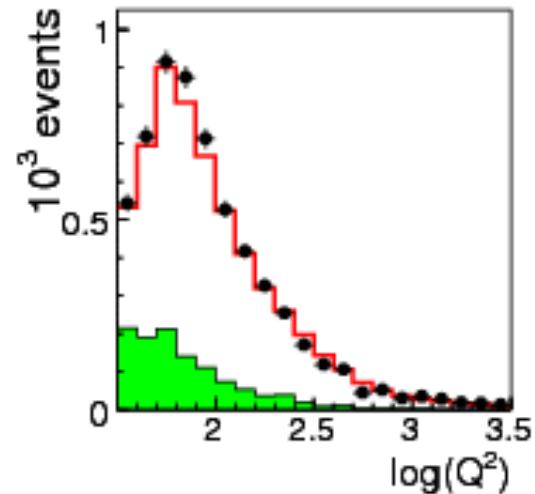
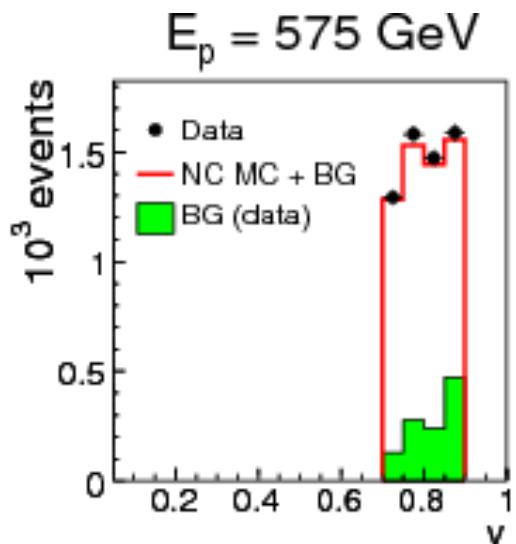
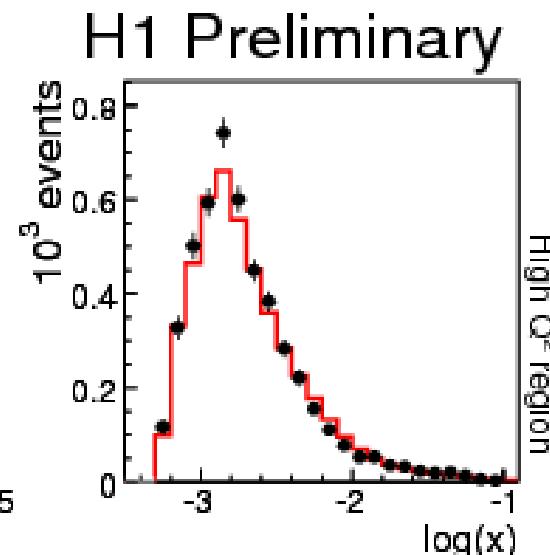
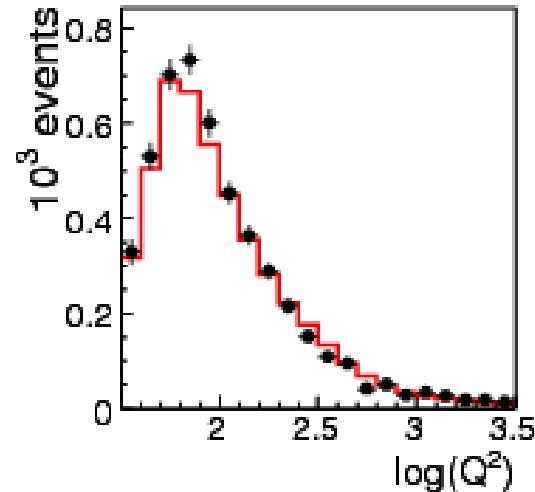
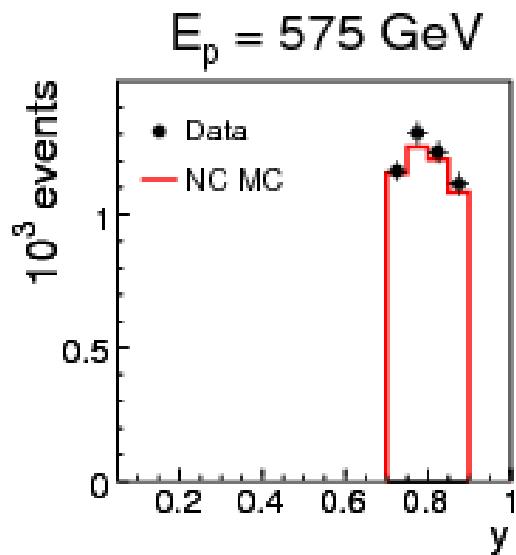


# H1: Kinematic Variables



MPP Munich

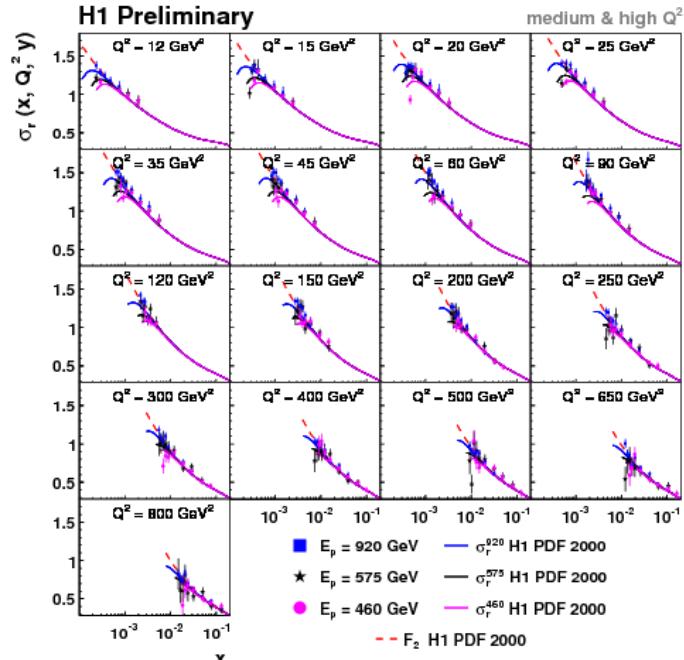
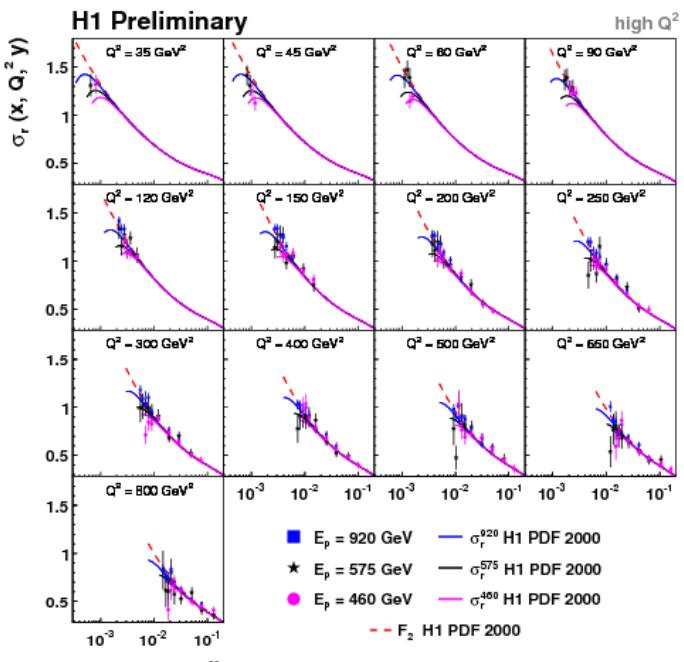
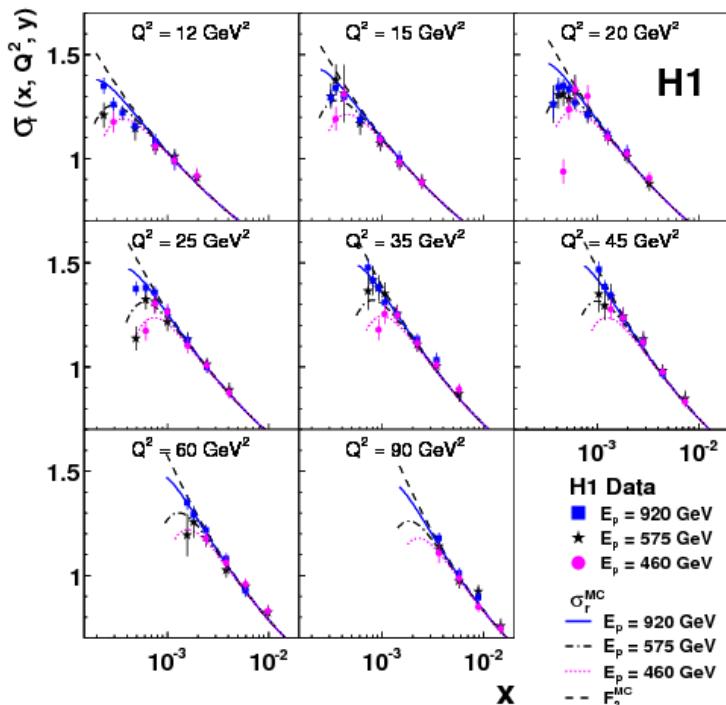
# H1: Kinematic Variables



MPP Munich

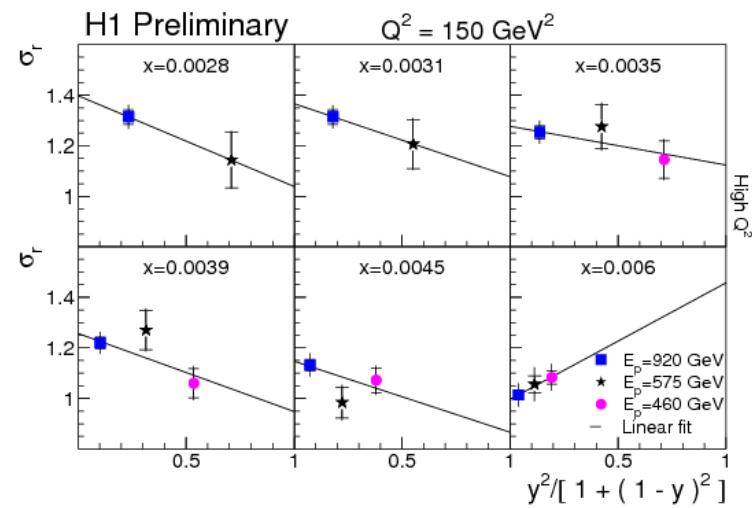
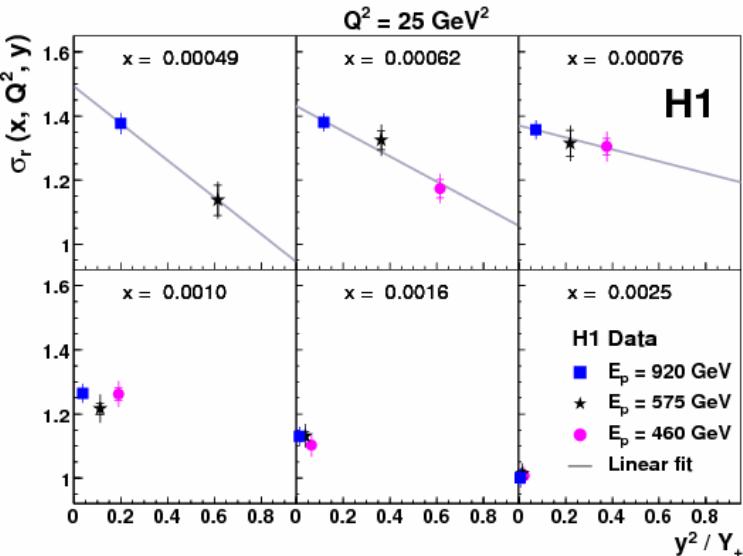
Burkard  
Reisert  
EPS09

# H1: Cross Sect.

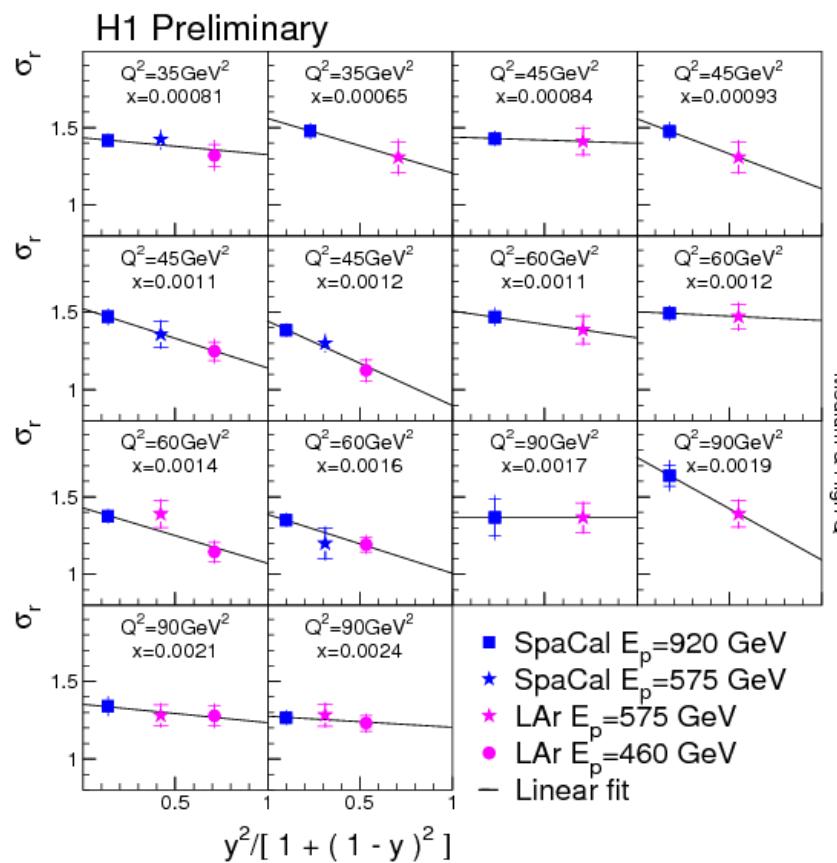


MPP Munich

Burkard  
Reisert  
EPS09

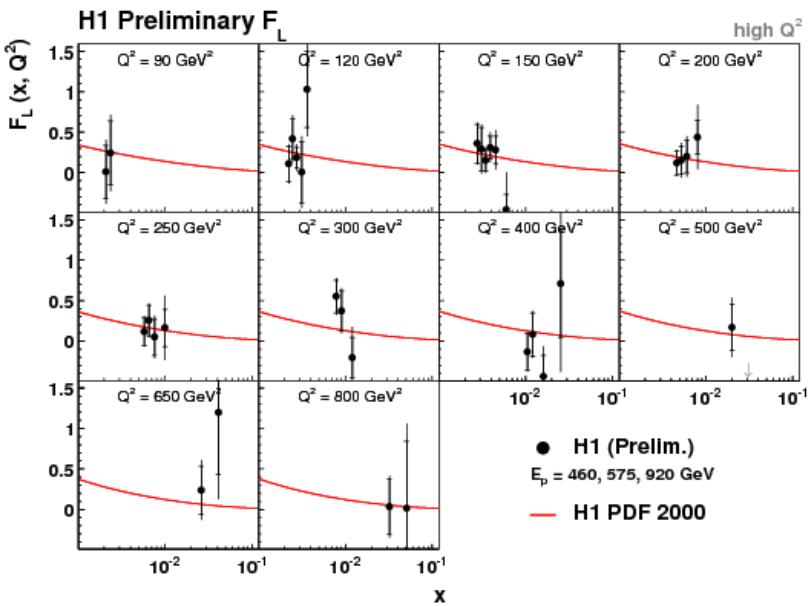
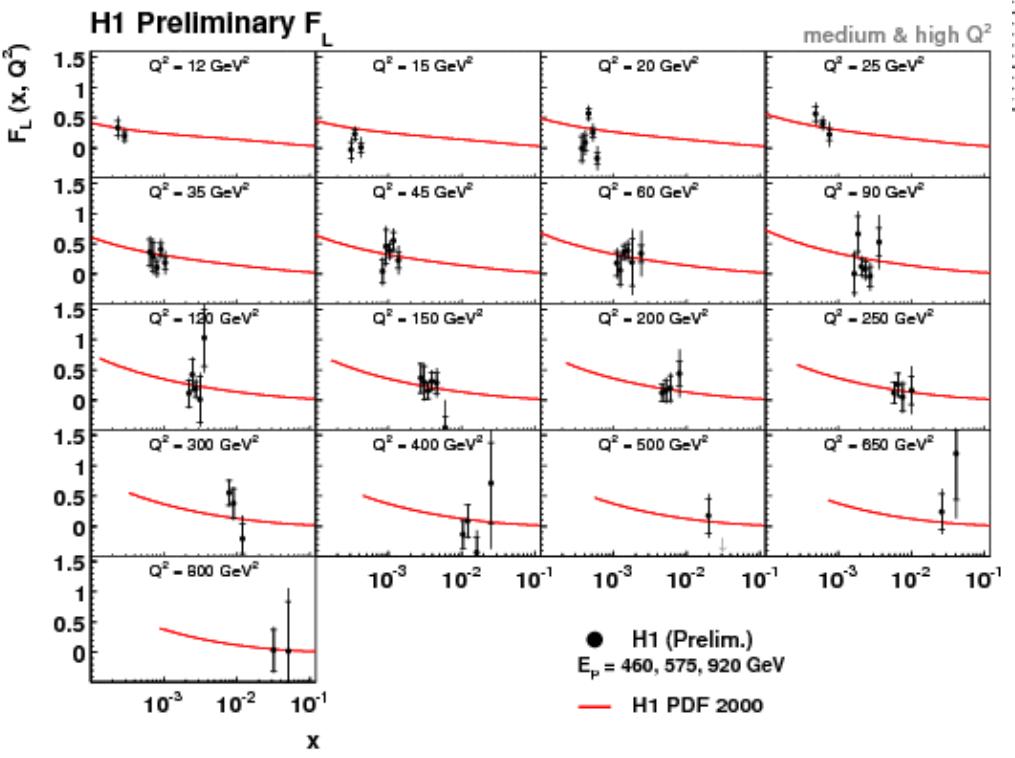
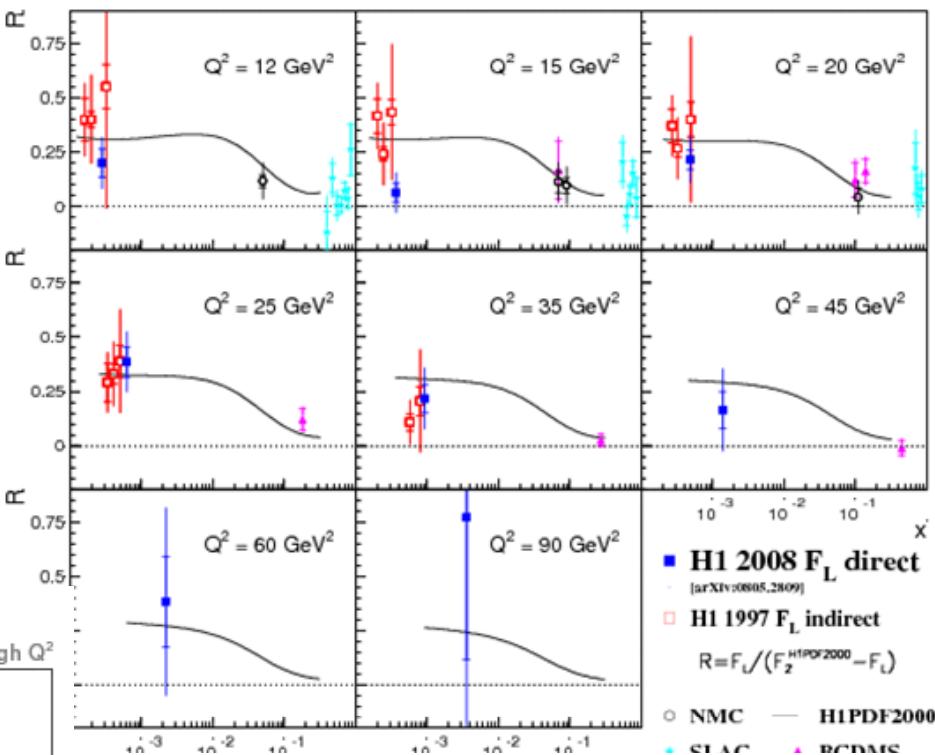
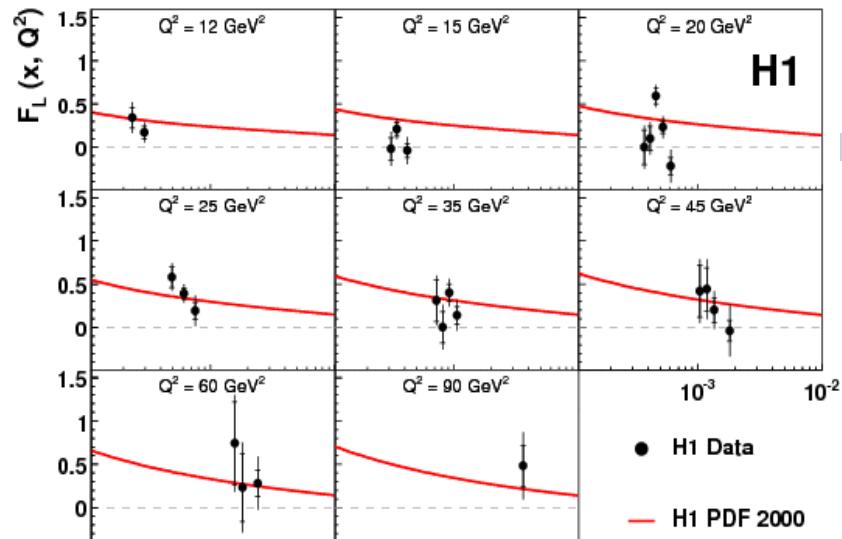


# H1 Rosenbuth Plots (Examples)

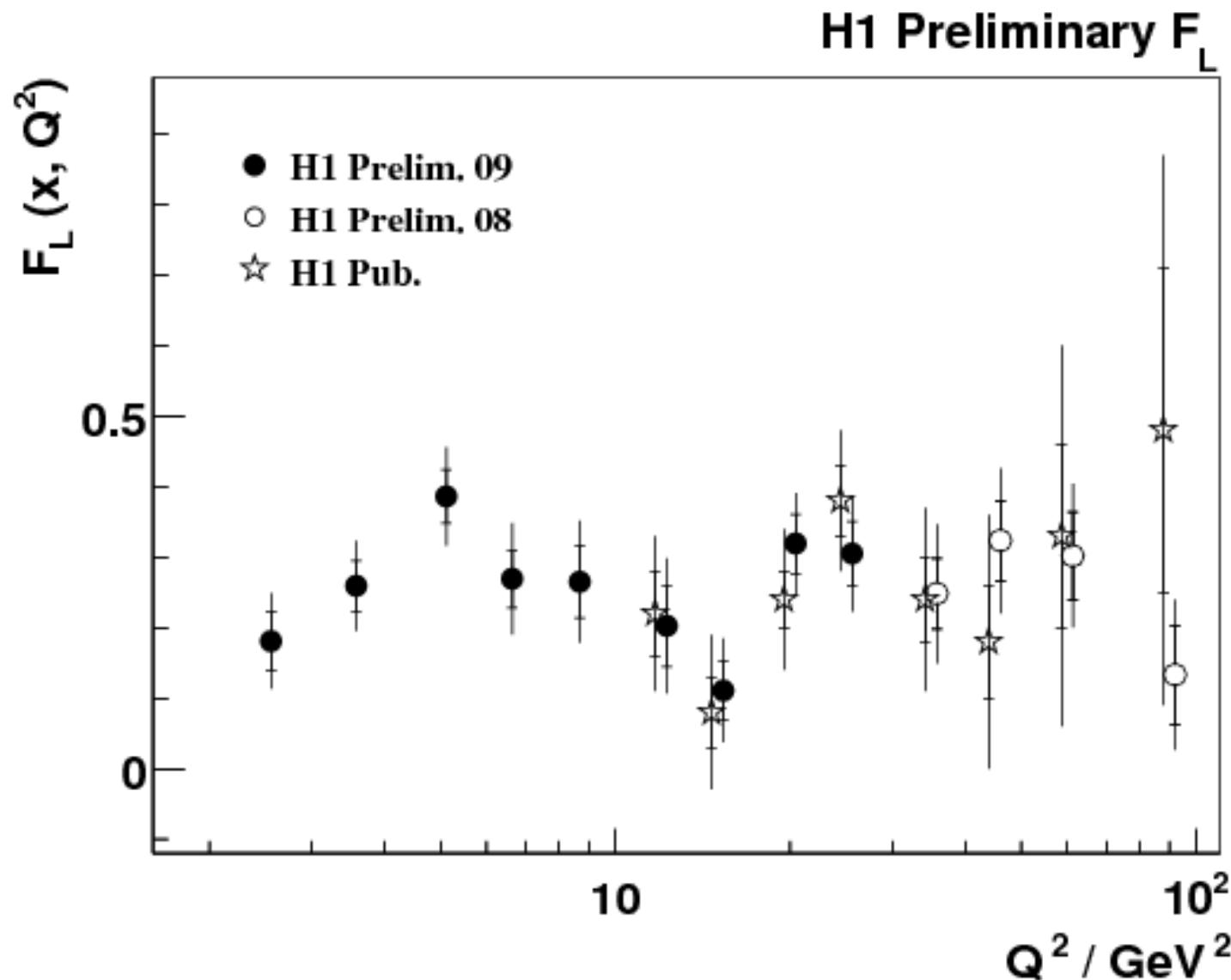


MPP Munich

Burkard  
Reisert  
EPS09



# H1 FL vs Q<sub>2</sub> (Three Analyses)



MPP Munich