

The CKM matrix : Status and sensitivity to New Physics

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On behalf of the CKMfitter group



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H. Lacker	ATLAS & BABAR	Humboldt	Berlin
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V. Niess	LHCb	LPC	Clermont-Ferrand
J. Ocariz	BABAR	LPNHE	Paris
S. T'Jampens	LHCb	LAPP	Annecy-le-Vieux
V. Tisserand	BABAR	LAPP	Annecy-le-Vieux
K. Trabelsi	Belle	KEK	Tsukuba

This talk

- Introduction
- The CKM Global Fit as of Summer 2009
 - Experimental, theoretical inputs, results
- Selected topics from the CKM global fit
 - α , ε_K , V_{ub} , β and $B \rightarrow \tau\nu$
 - will skip NP in $B_{(s)}$ mixing
- A hint on the future : CKM from rare kaon decays
- Conclusions

The CKM Matrix

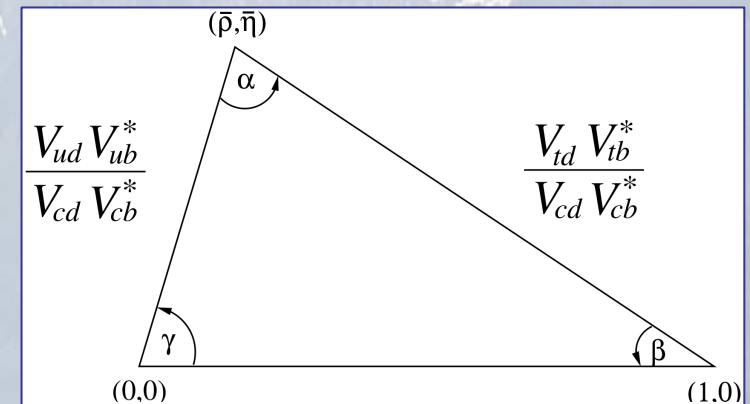
$$\lambda^2 = \frac{|V_{us}|^2}{|V_{ud}|^2 + |V_{us}|^2}$$

$$A^2 \lambda^4 = \frac{|V_{cb}|^2}{|V_{ud}|^2 + |V_{us}|^2}$$

$$\bar{\rho} + i\bar{\eta} = -\frac{V_{ud} V_{ub}^*}{V_{cd} V_{cb}^*}$$

The CKM Matrix:

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix}_J = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}_M$$



Unitary-exact, phase independent Wolfenstein parametrisation :

V_{ud} , V_{us} and V_{cb} determine A and λ

$\bar{\rho} + i\bar{\eta}$ are determined from the angles and sides of the UT

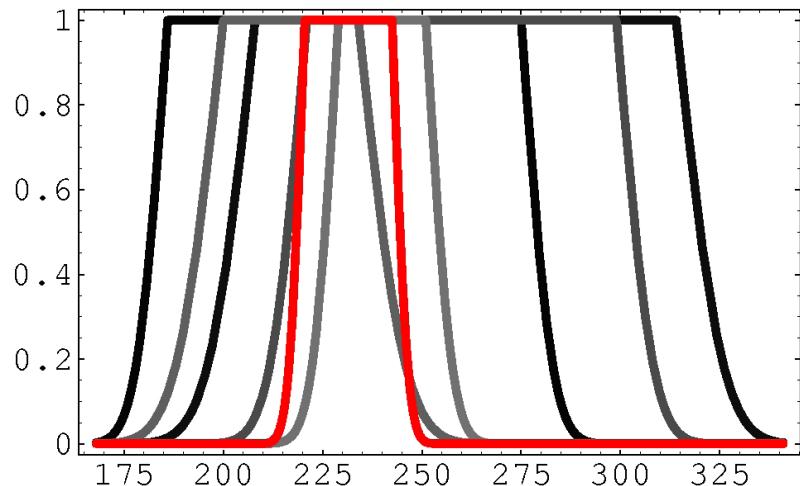
Inputs to the global CKM fit

<i>Parameter</i>	<i>Experimental source</i>	<i>Method, theoretical parameters, references</i>
$ V_{ud} $	Superallowed b decays	Towner & Hardy, PRC 77, 025501 (2008)
$ V_{us} $	K _{I3} (WA Flavianet)	$f_+^{K\pi}(0)=0.964(5)$
$ V_{cb} $	HFAG incl.+excl. $B \rightarrow X_c \bar{L} n$	
$ V_{ub} $	HFAG incl.+excl. $B \rightarrow X_d \bar{L} n$	OOA : $3.87(9)(46) \times 10^{-3}$
Δm_d	WA HFAG B_d - \bar{B}_d mixing	OOA : $B_{Bs}/B_{Bd} = 1.05(2)(5) + f_{Bs} + f_{Bd}$
Δm_s	CDF B_s - \bar{B}_s mixing	OOA : $B_{Bs} = 1.23(3)(5) + f_{Bs} + f_{Bd}$
$B^- \rightarrow \tau^- \nu$	WA: BaBar/Belle	OOA : $f_{Bs}/f_{Bd} = 1.196(8)(23)$ & $f_{Bs} = 228(3)(17)$
$ \varepsilon_K $	$K^0 - \bar{K}^0$ (KLOE, KTeV)	OOA : $B_K = 0.721(5)(40)$
β	WA HFAG	
α	WA $\pi\pi/\rho\pi/\rho\rho$	isospin SU(2)
γ	WA HFAG $B^- \rightarrow D^{(*)} K^{(*)-}$	GLW/ADS/GGSZ

Frequentist hypothesis-testing approach :
confidence intervals obtained through $\Delta\chi^2$
dedicated RFit scheme for theoretical uncertainties

The RFit statistical scheme, OOA

- theoretical uncertainties are bounded over a range without any preference
- minimisation explores uniformly the theoretical parameter space



OOA for B_s decay constant

Reference	N_f	Mean	Stat	Syst
CP-PACS01	2	242	9	+53 -34
MILC02	2	217	6	+58 -31
JLQCD03	2	215	9	+19 -15
HPQCD03	2+1	260	7	39
FNAL-MILC07*	2+1	240	5	26
Our average		228	3	17

In presence of multiple, different estimations of theoretical parameters,
we use the ``educated RFit'' approach to obtain Our Own Averages (OOA) :

- central values : weighted average from statistical errors only
- statistical errors : combination of statistical errors
- theoretical errors : use the RFit range for the most precise input

The Global CKM fit : result

INPUTS :

$|V_{ud}|, |V_{us}|, |V_{cb}|,$
 $|V_{ub}|, BR(B^- \rightarrow \tau^- \nu),$
 $\Delta m_d, \Delta m_s,$
 $|\varepsilon_K|,$
 α, β, γ

RESULTS :

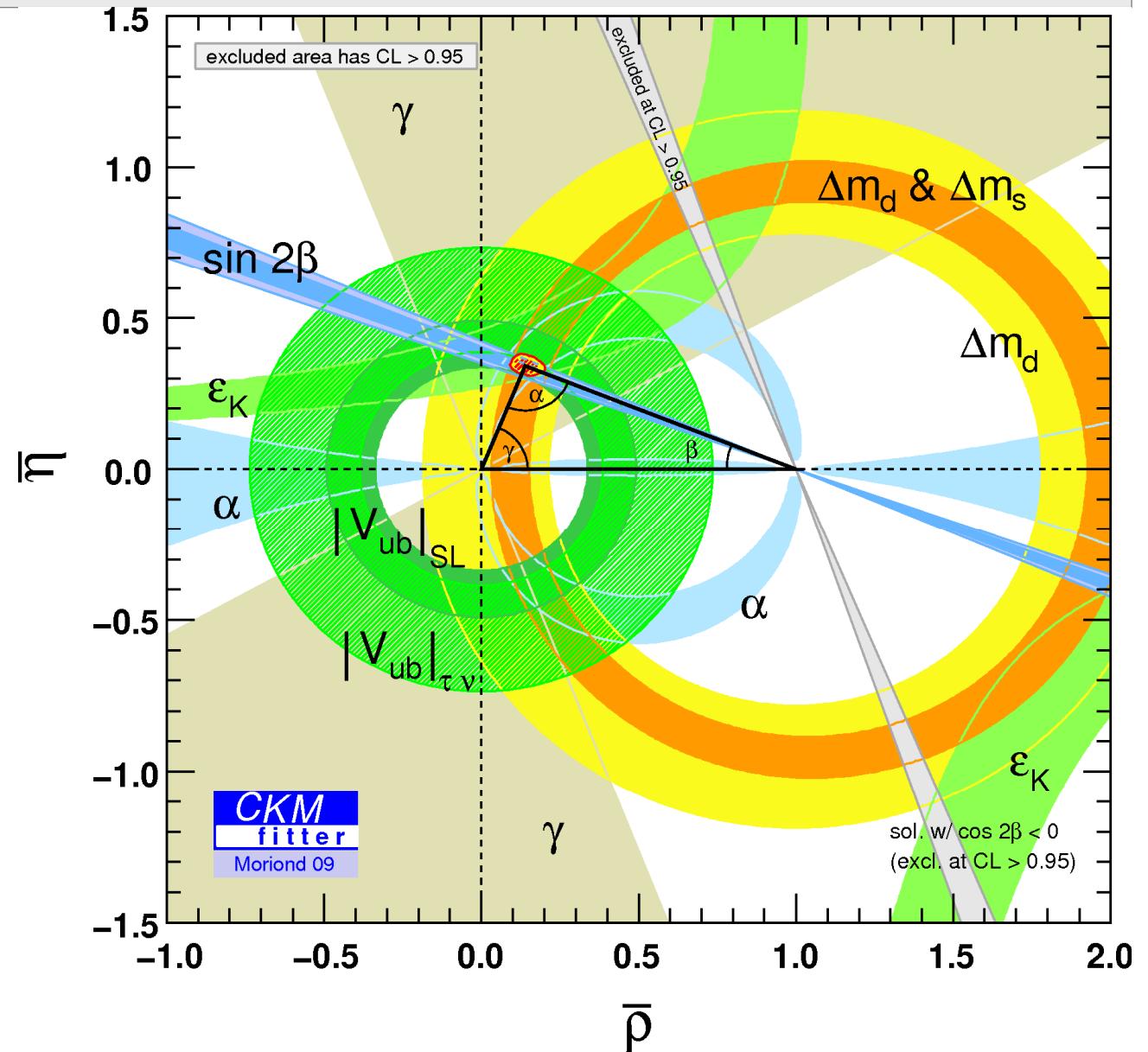
$$A = 0.812^{+0.010}_{-0.024}$$

$$\lambda = 0.2252 \pm 0.0008$$

$$\bar{\rho} = 0.139^{+0.025}_{-0.027}$$

$$\bar{\eta} = 0.341^{+0.016}_{-0.015}$$

(68% C.L.)



The Global CKM fit : result

Overall consistency at 95% C.L.

Global fit p-value : 45% (0.8σ)

Fit dominated by :

$\sin 2\beta$, $\Delta m_d/\Delta m_s$, α

RESULTS :

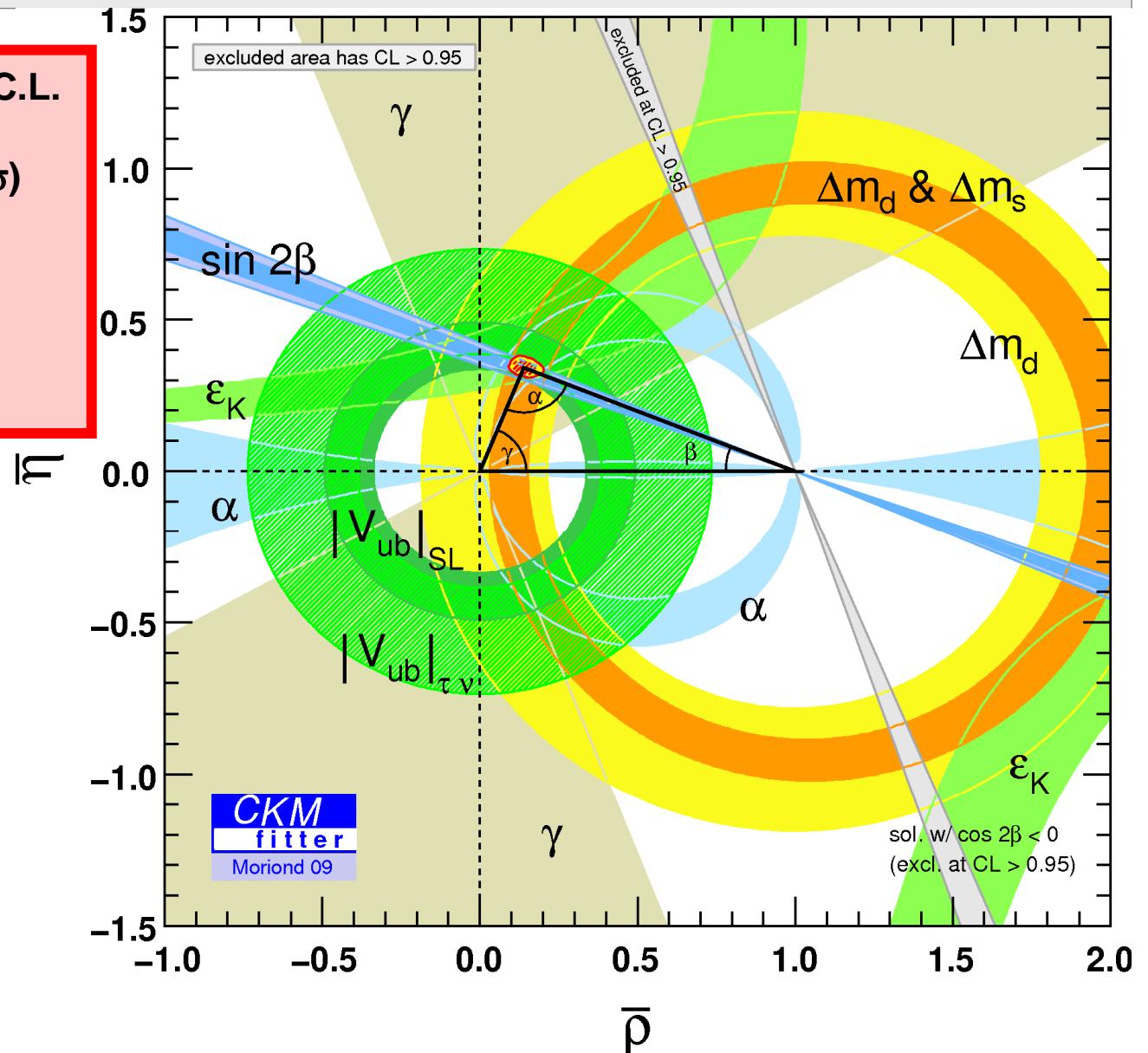
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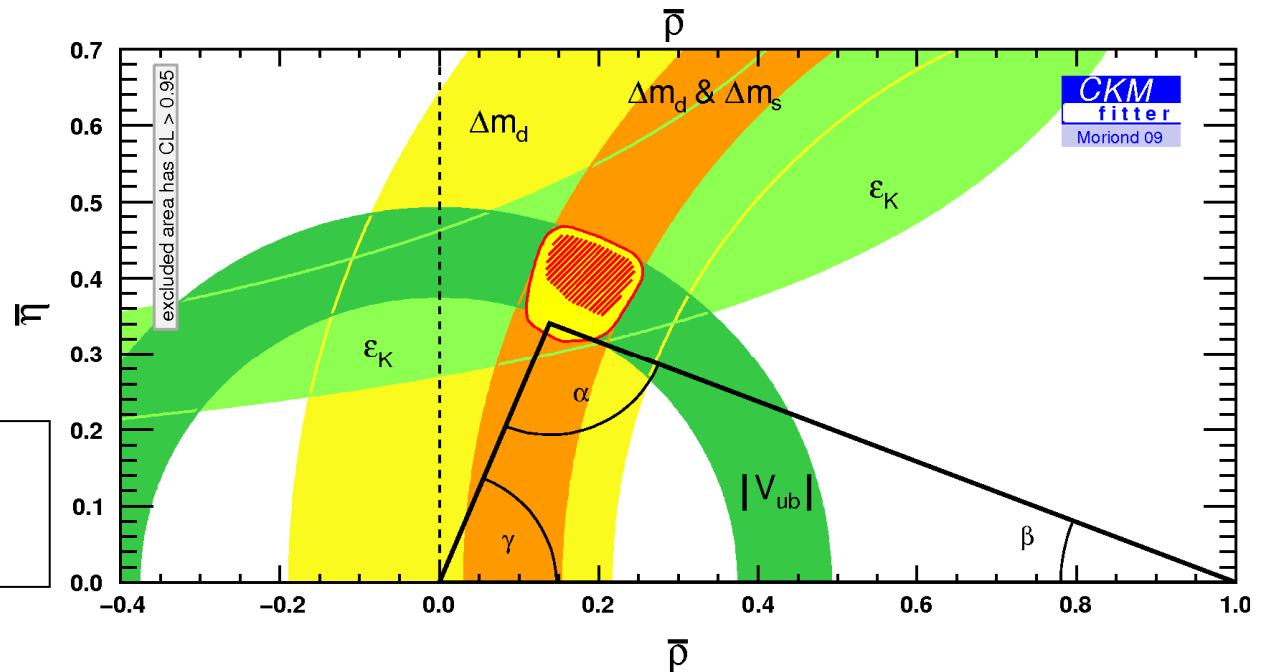
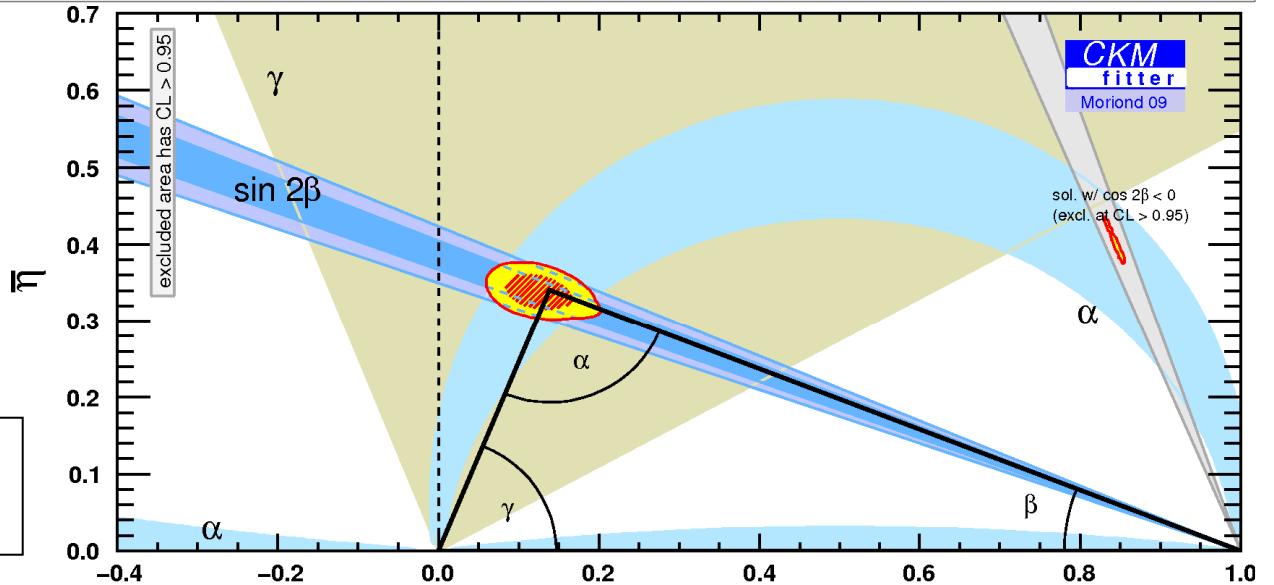
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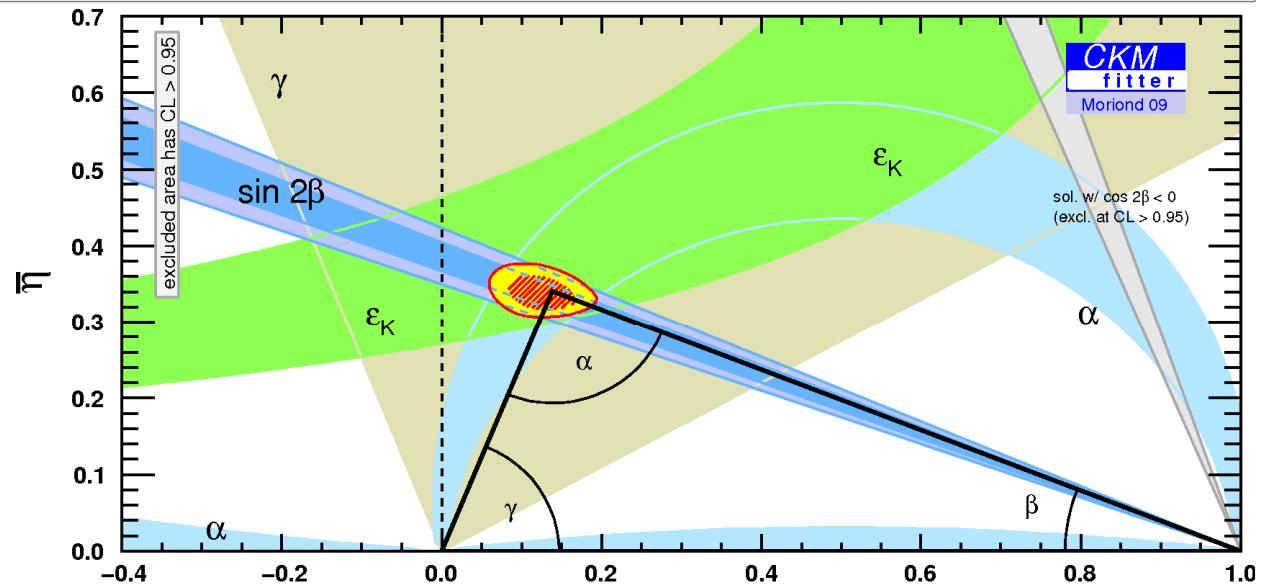


The Global CKM fit : result

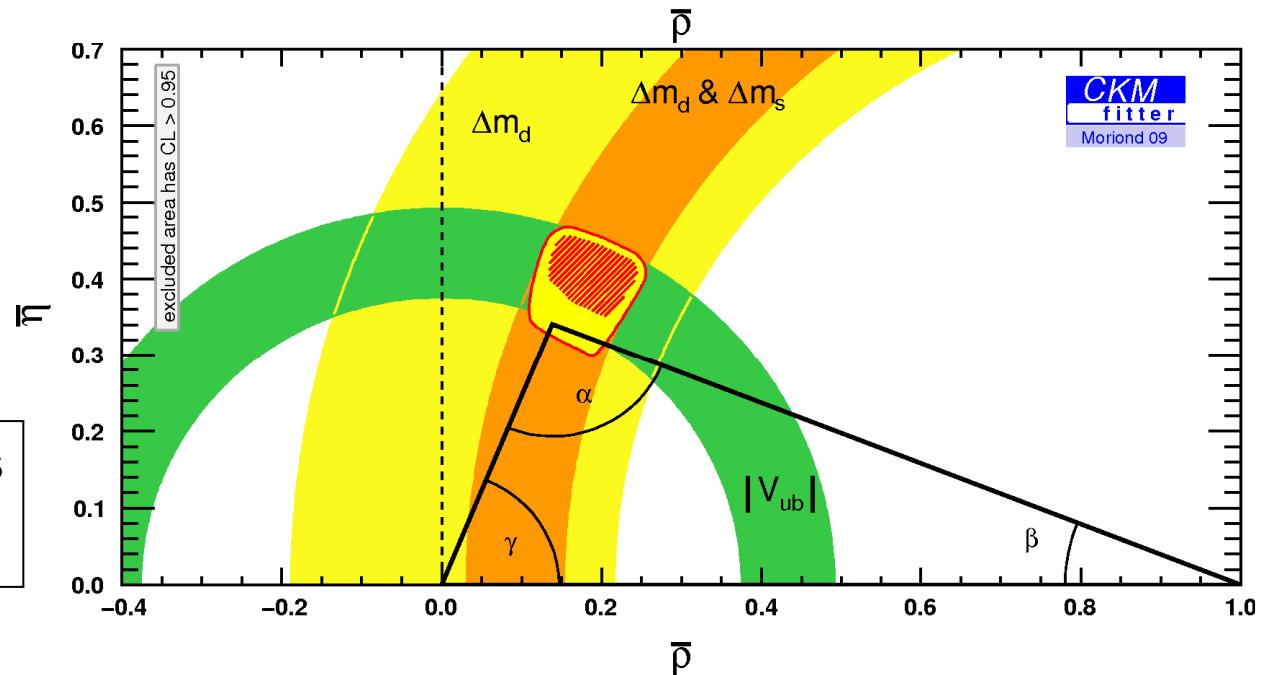


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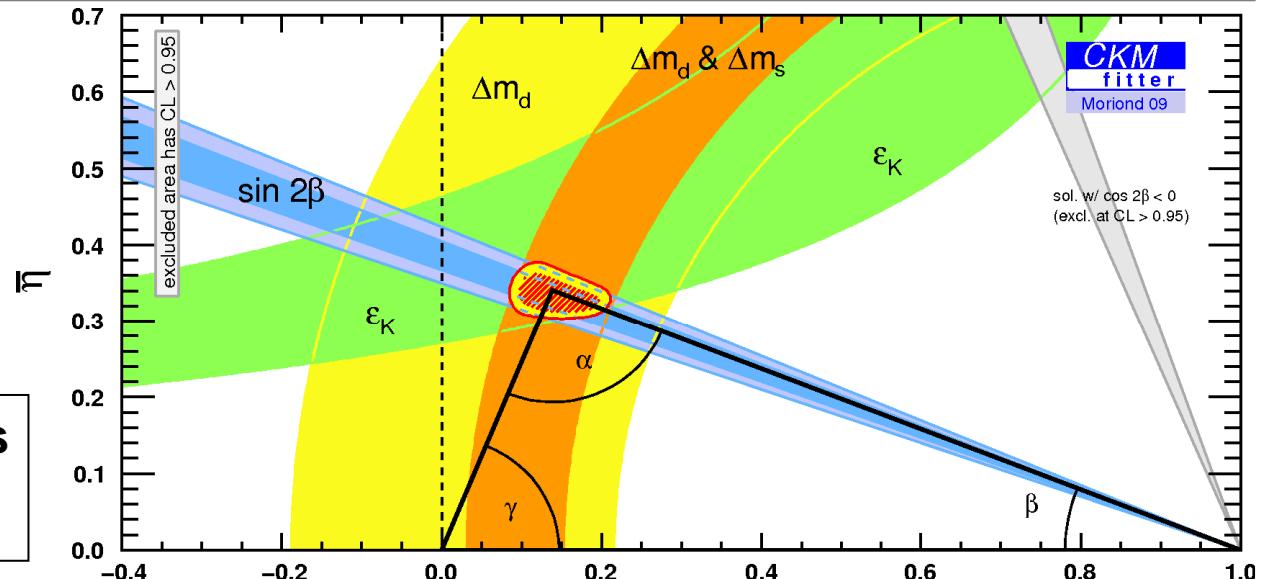
**CP-violating observables
as only inputs...**



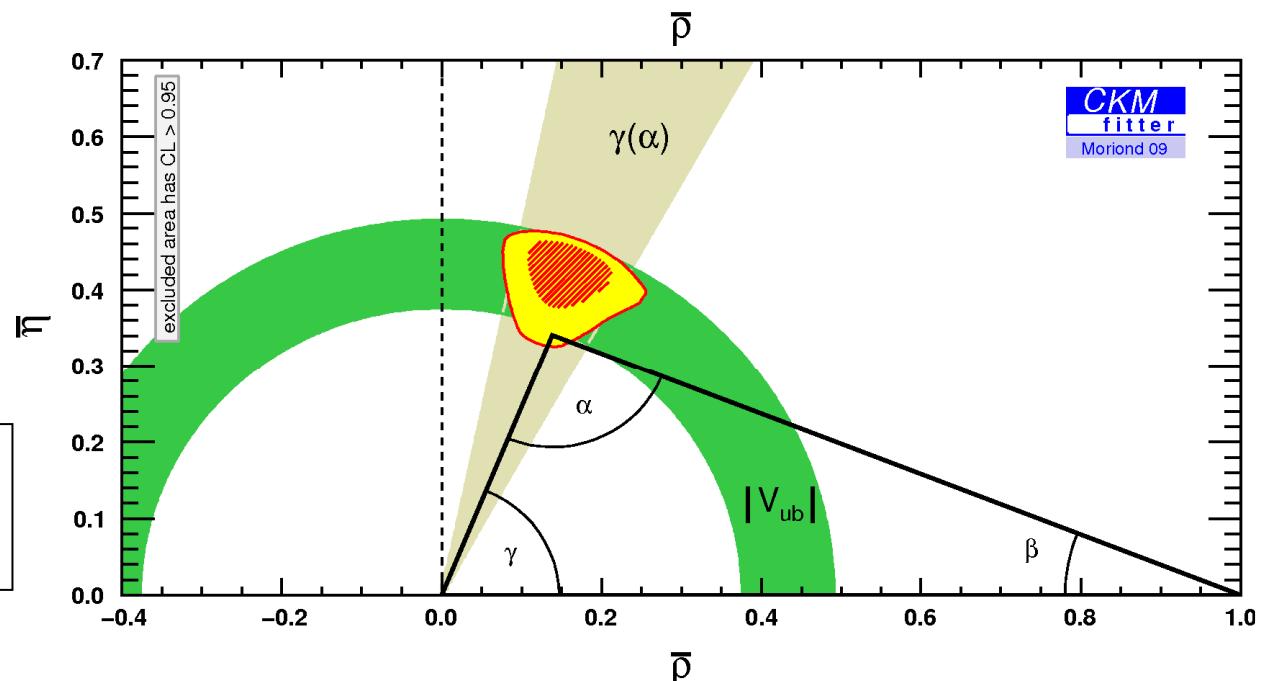
**CP-conserving observables
as only inputs ...**



The Global CKM fit : result



Using Loop-level processes
as only inputs...



Using Tree-level processes
as only inputs ...

The Global CKM fit : results

file:///C:/Documents%20a... http://ckmfitter.in2p3.fr/plots_Moriond09/ckmEval_results.html

CKMfitter global fit results:

The inputs for the global fit ([pdf](#)).

- [Wolfenstein parameters](#)
- [UT angles and sides](#)
- [UT_s angle and apex](#)
- [CKM elements](#)
- [Theory parameters](#)
- [Rare branching fractions \(\$B \rightarrow l\nu\$, \$B \rightarrow ll\$ \)](#)

Wolfenstein parameters and Jarlskog invariant:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
A	0.8116 [+0.0097 -0.0241]	0.812 [+0.019 -0.036]	0.812 [+0.029 -0.045]
λ	0.22521 [+0.00082 -0.00082]	0.2252 [+0.0016 -0.0016]	0.2252 [+0.0025 -0.0025]
pbar	0.139 [+0.025 -0.027]	0.139 [+0.053 -0.040]	0.139 [+0.073 -0.052]
$\eta_{\bar{b}b}$	0.341 [+0.016 -0.015]	0.341 [+0.032 -0.025]	0.341 [+0.048 -0.034]
J [10^{-5}]	2.92 [+0.15 -0.15]	2.92 [+0.30 -0.19]	2.92 [+0.45 -0.23]

UT angles and sides:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$\sin 2\alpha$	-0.02 [+0.15 -0.13]	-0.02 [+0.22 -0.26]	-0.02 [+0.28 -0.35]
$\sin 2\alpha$ (meas. not in the fit)	-0.20 [+0.30 -0.11]	-0.20 [+0.41 -0.17]	-0.20 [+0.48 -0.23]
$\sin 2\beta$	0.684 [+0.023 -0.021]	0.684 [+0.046 -0.035]	0.684 [+0.068 -0.049]
$\sin 2\beta$ (meas. not in the fit)	0.817 [+0.026 -0.040]	0.817 [+0.039 -0.114]	0.817 [+0.052 -0.171]
$ \sin(2\beta + \gamma) $	0.934 [+0.023 -0.030]	0.934 [+0.039 -0.051]	0.934 [+0.049 -0.071]
α [deg]	90.6 [+3.8 -4.2]	90.6 [+7.5 -6.3]	90.6 [+10.2 -8.2]
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α [deg] (dir. meas.)	89.0 [+4.4 -4.2]	89.0 [+9.1 -8.3] 178.3 [+1.7 -5.6] 0 [+5 -0]	89 [+21 -13] 178.3 [+1.7 -13.8] 0 [+12 -0]
β [deg]	21.58 [+0.91 -0.81]	21.6 [+1.8 -1.4]	21.6 [+2.8 -1.9]
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γ [deg]	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
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γ [deg] (dir. meas.)	70 [+27 -30]	70 [+44 -41]	70 [+60 -52] 131.14 [+0.18 -0.25]
R _u	0.368 [+0.015 -0.013]	0.368 [+0.030 -0.022]	0.368 [+0.045 -0.030]
R _t	0.926 [+0.027 -0.025]	0.926 [+0.040 -0.053]	0.926 [+0.052 -0.072]

UT_s apex and angle:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
p _b bar	-0.0074 [+0.0014 -0.0013]	-0.0074 [+0.0022 -0.0029]	-0.0074 [+0.0028 -0.0040]
$\eta_{\bar{b}b}$	-0.01821 [+0.00081 -0.00085]	-0.0182 [+0.0013 -0.0017]	-0.0182 [+0.0018 -0.0026]
$\beta_s = -\arg(-V_{cs} V_{cb}^* / V_{ts} V_{tb}^*)$ [rad]	0.01807 [+0.00086 -0.00081]	0.0181 [+0.0017 -0.0014]	0.0181 [+0.0026 -0.0018]

The Global CKM fit : discussion on β

CKMfitter global fit results:

The inputs for the global fit (pdf).

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CKM angle β measured with a $\sim 1^\circ$ accuracy

Indirect constraint has similar precision

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CKM angle β measured with a $\sim 1^\circ$ accuracy

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...but prefers a larger value (more on this later)

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α [deg] (meas. not in the fit)	95.6 [+3.3 -8.8]	95.6 [+5.2 -11.8]	95.6 [+6.8 -13.9]
α [deg] (dir. meas.)	89.0 [+4.4 -4.2]	89.0 [+9.1 -8.3] 178.3 [+1.7 -5.6] 0 [+5 -0]	89 [+21 -13] 178.3 [+1.7 -13.8] 0 [+12 -0]
β [deg]	21.58 [+0.91 -0.81]	21.6 [+1.8 -1.4]	21.6 [+2.8 -1.9]
β [deg] (meas. not in the fit)	27.4 [+1.3 -1.9]	27.4 [+2.0 -5.0]	27.4 [+2.8 -7.3]
β [deg] (dir. meas.)	21.07 [+0.90 -0.88]	21.1 [+1.8 -1.7]	21.1 [+2.8 -2.6]
γ [deg]	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (meas. not in the fit)	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (dir. meas.)	70 [+27 -30]	70 [+44 -41]	70 [+60 -52] 131.14 [+0.18 -0.25]
R_u	0.368 [+0.015 -0.013]	0.368 [+0.030 -0.022]	0.368 [+0.045 -0.030]
R_t	0.926 [+0.027 -0.025]	0.926 [+0.040 -0.053]	0.926 [+0.052 -0.072]

UT_s apex and angle:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$p_s \bar{b}$	-0.0074 [+0.0014 -0.0013]	-0.0074 [+0.0022 -0.0029]	-0.0074 [+0.0028 -0.0040]
$\eta_s \bar{b}$	-0.01821 [+0.00081 -0.00085]	-0.0182 [+0.0013 -0.0017]	-0.0182 [+0.0018 -0.0026]
$\beta_s \equiv -\arg(-V_{cs} V_{cb}^* V_{ts} V_{tb}^*)$ [rad]	0.01807 [+0.00086 -0.00081]	0.0181 [+0.0017 -0.0014]	0.0181 [+0.0026 -0.0018]

The Global CKM fit : discussion on α

CKMfitter global fit results:

The inputs for the global fit (pdf).

- Wolfenstein parameters
- UT angles and sides
- UT_s angle and apex
- CKM elements
- Theory parameters
- Rare branching fractions ($B \rightarrow l\nu$, $B \rightarrow ll$)

Wolfenstein parameters and Jarlskog invariant:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
A	0.8116 [+0.0097 -0.0241]	0.812 [+0.019 -0.036]	0.812 [+0.029 -0.045]
λ	0.22521 [+0.00082 -0.00082]	0.2252 [+0.0016 -0.0016]	0.2252 [+0.0025 -0.0025]
$p_{\bar{b}b}$	0.139 [+0.025 -0.027]	0.139 [+0.053 -0.040]	0.139 [+0.073 -0.052]
$\eta_{\bar{b}b}$	0.341 [+0.016 -0.015]	0.341 [+0.032 -0.025]	0.341 [+0.048 -0.034]
J [10^{-5}]	2.92 [+0.15 -0.15]	2.92 [+0.30 -0.19]	2.92 [+0.45 -0.23]

UT angles and sides:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$\sin 2\alpha$	-0.02 [+0.15 -0.13]	-0.02 [+0.22 -0.26]	-0.02 [+0.28 -0.35]
$\sin 2\alpha$ (meas. not in the fit)	-0.20 [+0.30 -0.11]	-0.20 [+0.41 -0.17]	-0.20 [+0.48 -0.23]
$\sin 2\beta$	0.684 [+0.023 -0.021]	0.684 [+0.046 -0.035]	0.684 [+0.068 -0.049]
$\sin 2\beta$ (meas. not in the fit)	0.817 [+0.026 -0.040]	0.817 [+0.039 -0.114]	0.817 [+0.052 -0.171]
$ \sin(2\beta + \gamma) $	0.934 [+0.023 -0.030]	0.934 [+0.039 -0.051]	0.934 [+0.049 -0.071]
α [deg]	90.6 [+3.8 -4.2]	90.6 [+7.5 -6.3]	90.6 [+10.2 -8.2]
α [deg] (meas. not in the fit)	95.6 [+3.3 -8.8]	95.6 [+5.2 -11.8]	95.6 [+6.8 -13.9]
α [deg] (dir. meas.)	89.0 [+4.4 -4.2]	89.0 [+9.1 -8.3] 178.3 [+1.7 -5.6] 0 [+5 -0]	89 [+21 -13] 178.3 [+1.7 -13.8] 0 [+12 -0]
β [deg]	21.58 [+0.91 -0.81]	21.6 [+1.8 -1.4]	21.6 [+2.8 -1.9]
β [deg] (meas. not in the fit)	27.4 [+1.3 -1.9]	27.4 [+2.0 -5.0]	27.4 [+2.8 -7.3]
β [deg] (dir. meas.)	21.07 [+0.90 -0.88]	21.1 [+1.8 -1.7]	21.1 [+2.8 -2.6]
γ [deg]	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (meas. not in the fit)	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (dir. meas.)	70 [+27 -30]	70 [+44 -41]	70 [+60 -52] 131.14 [+0.18 -0.25]
R_u	0.368 [+0.015 -0.013]	0.368 [+0.030 -0.022]	0.368 [+0.045 -0.030]
R_t	0.926 [+0.027 -0.025]	0.926 [+0.040 -0.053]	0.926 [+0.052 -0.072]

UT_s apex and angle:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$p_{\bar{s}s}$	-0.0074 [+0.0014 -0.0013]	-0.0074 [+0.0022 -0.0029]	-0.0074 [+0.0028 -0.0040]
$\eta_{\bar{s}s}$	-0.01821 [+0.00081 -0.00085]	-0.0182 [+0.0013 -0.0017]	-0.0182 [+0.0018 -0.0026]
$\beta_s = -\arg(-V_{cs} V_{cb}^* / V_{ts} V_{tb}^*)$ [rad]	0.01807 [+0.00086 -0.00081]	0.0181 [+0.0017 -0.0014]	0.0181 [+0.0026 -0.0018]

The Global CKM fit : discussion on α

CKMfitter global fit results:

The inputs for the global fit (pdf).

- Wolfenstein parameters
- UT angles and sides
- UT_s angle and apex
- CKM elements
- Theory parameters
- Rare branching fractions ($B \rightarrow l\nu$, $B \rightarrow ll$)

CKM angle α now measured with a $\sim 4^\circ$ accuracy !

Wolfenstein parameters and Jarlskog invariant:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
A	0.8116 [+0.0097 -0.0241]	0.812 [+0.019 -0.036]	0.812 [+0.029 -0.045]
λ	0.22521 [+0.00082 -0.00082]	0.2252 [+0.0016 -0.0016]	0.2252 [+0.0025 -0.0025]
pbar	0.139 [+0.025 -0.027]	0.139 [+0.053 -0.040]	0.139 [+0.073 -0.052]
η bar	0.341 [+0.016 -0.015]	0.341 [+0.032 -0.025]	0.341 [+0.048 -0.034]
J [10^{-5}]	2.92 [+0.15 -0.15]	2.92 [+0.30 -0.19]	2.92 [+0.45 -0.23]

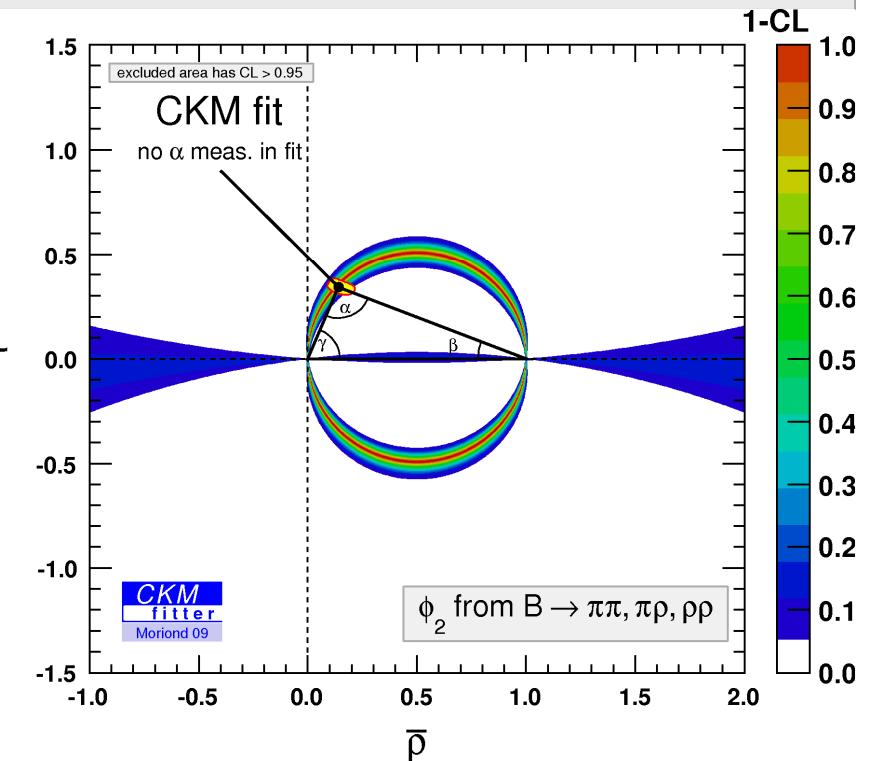
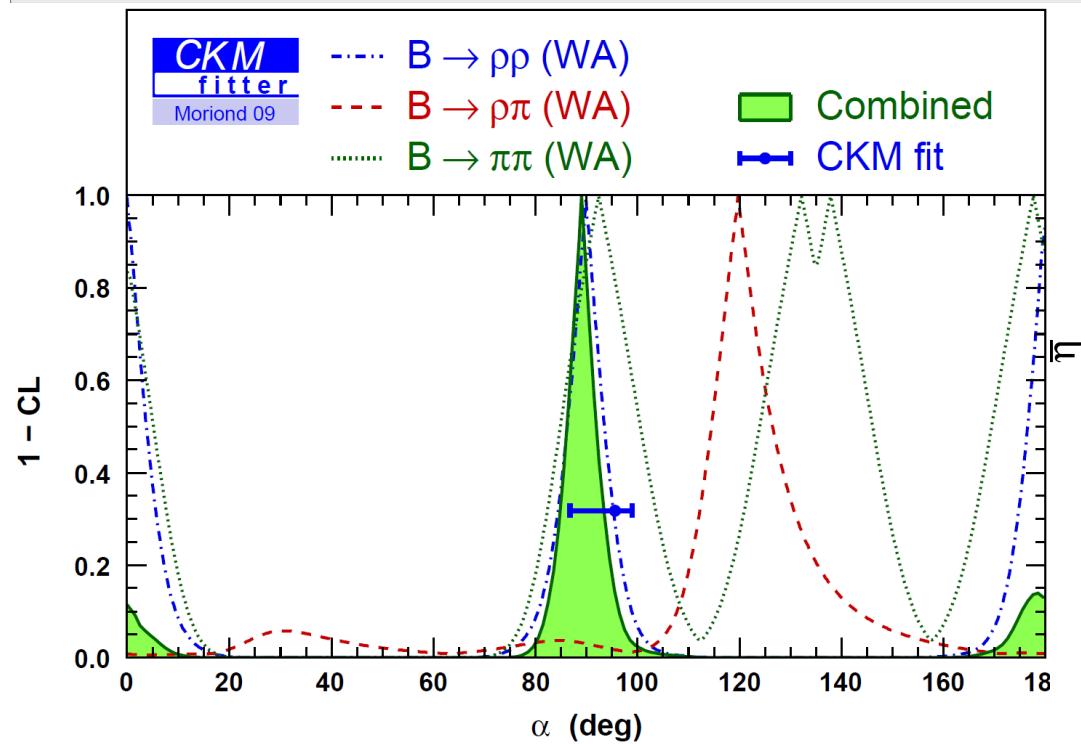
UT angles and sides:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$\sin 2\alpha$	-0.02 [+0.15 -0.13]	-0.02 [+0.22 -0.26]	-0.02 [+0.28 -0.35]
$\sin 2\alpha$ (meas. not in the fit)	-0.20 [+0.30 -0.11]	-0.20 [+0.41 -0.17]	-0.20 [+0.48 -0.23]
$\sin 2\beta$	0.684 [+0.023 -0.021]	0.684 [+0.046 -0.035]	0.684 [+0.068 -0.049]
$\sin 2\beta$ (meas. not in the fit)	0.817 [+0.026 -0.040]	0.817 [+0.039 -0.114]	0.817 [+0.052 -0.171]
$ \sin(2\beta + \gamma) $	0.934 [+0.023 -0.030]	0.934 [+0.039 -0.051]	0.934 [+0.049 -0.071]
α [deg]	90.6 [+3.8 -4.2]	90.6 [+7.5 -6.3]	90.6 [+10.2 -8.2]
α [deg] (meas. not in the fit)	95.6 [+3.3 -8.8]	95.6 [+5.2 -11.8]	95.6 [+6.8 -13.9]
α [deg] (dir. meas.)	89.0 [+4.4 -4.2]	89.0 [+9.1 -8.3] 178.3 [+1.7 -5.6] 0 [+5 -0]	89 [+21 -13] 178.3 [+1.7 -13.8] 0 [+12 -0]
β [deg]	21.58 [+0.91 -0.81]	21.6 [+1.8 -1.4]	21.6 [+2.8 -1.9]
β [deg] (meas. not in the fit)	27.4 [+1.3 -1.9]	27.4 [+2.0 -5.0]	27.4 [+2.8 -7.3]
β [deg] (dir. meas.)	21.07 [+0.90 -0.88]	21.1 [+1.8 -1.7]	21.1 [+2.8 -2.6]
γ [deg]	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (meas. not in the fit)	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (dir. meas.)	70 [+27 -30]	70 [+44 -41]	70 [+60 -52] 131.14 [+0.18 -0.25]
R_u	0.368 [+0.015 -0.013]	0.368 [+0.030 -0.022]	0.368 [+0.045 -0.030]
R_t	0.926 [+0.027 -0.025]	0.926 [+0.040 -0.053]	0.926 [+0.052 -0.072]

UT_s apex and angle:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
p_s bar	-0.0074 [+0.0014 -0.0013]	-0.0074 [+0.0022 -0.0029]	-0.0074 [+0.0028 -0.0040]
η_s bar	-0.01821 [+0.00081 -0.00085]	-0.0182 [+0.0013 -0.0017]	-0.0182 [+0.0018 -0.0026]
$\beta_s = -\arg(-V_{cs} V_{cb}^* / V_{ts} V_{tb}^*)$ [rad]	0.01807 [+0.00086 -0.00081]	0.0181 [+0.0017 -0.0014]	0.0181 [+0.0026 -0.0018]

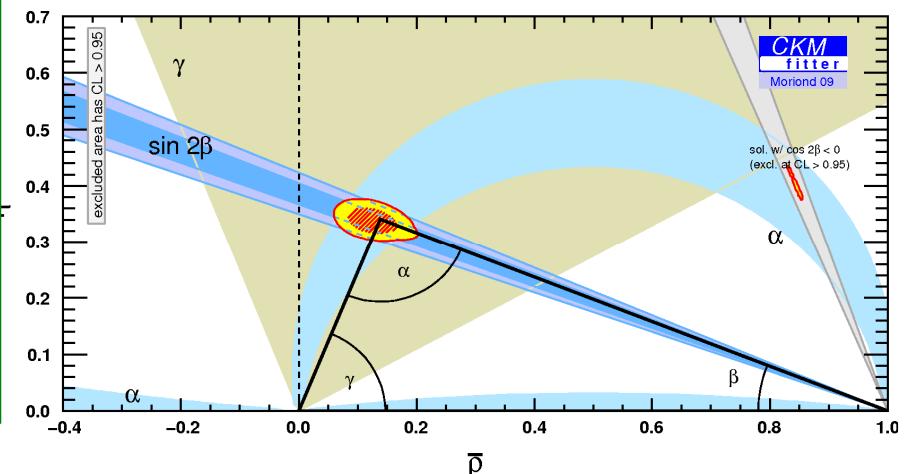
The Global CKM fit : discussion on α



3 contributions to α :

- Isospin analysis of $B \rightarrow \pi\pi$, $B \rightarrow \rho\rho$
- Time-dependent Dalitz analysis of $B \rightarrow \rho\pi$

The dominant contribution is $B \rightarrow \rho\rho$



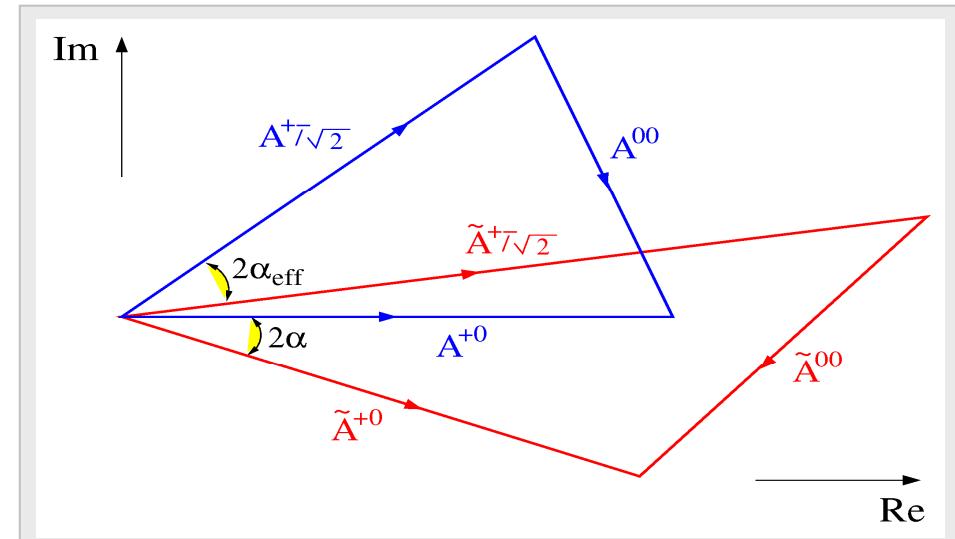
α from isospin analyses

Triangular relation on amplitudes :

$$A^{+-} - \sqrt{2}A^{+0} + \sqrt{2}A^{00} = 0$$

(plus a similar relation for the CP-conjugated amplitudes)

- neglect EW penguins
 - shifts α by $\sim 2^\circ$
- $A+0$ pure tree : no DCPV
- testable against data
- neglect isospin-breaking effects

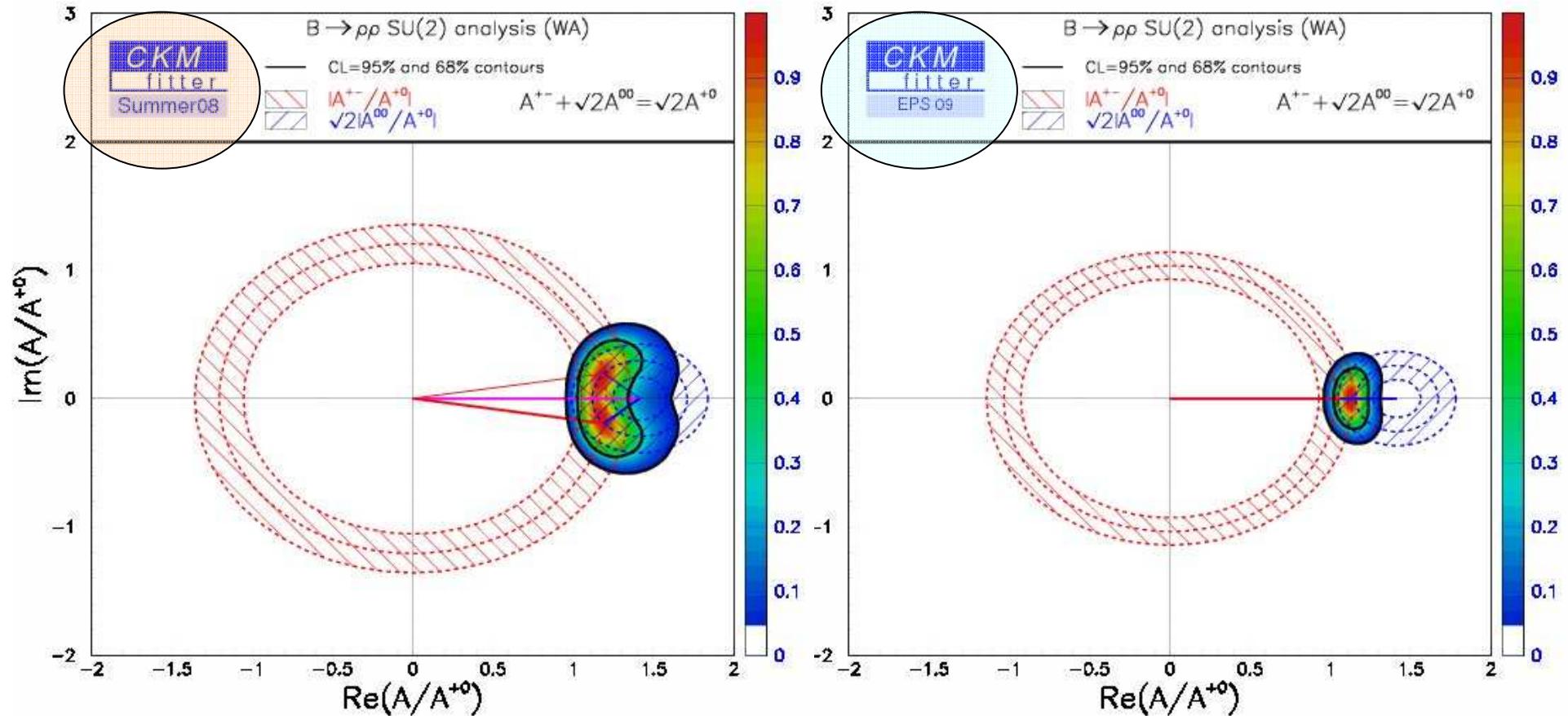


α can be resolved up to an 8-fold ambiguity within $[0, \pi]$

Unknowns	Observables	Constraints	Account
$\alpha,$ $T^+, P^+,$ $T^{+0}, P^{+0},$ T^{00}, P^{00}	$B^{+-}, S_{\pi\pi}, C_{\pi\pi}$ B^{+0}, A_{CP} $B^{00}, (S_{00}), C_{00}$	2 isospin triangles and one common side	13 unknowns – 7 observables – 5 constraints – 1 global phase = 0 ☺

Isospin analysis of $B \rightarrow pp$: the triangles

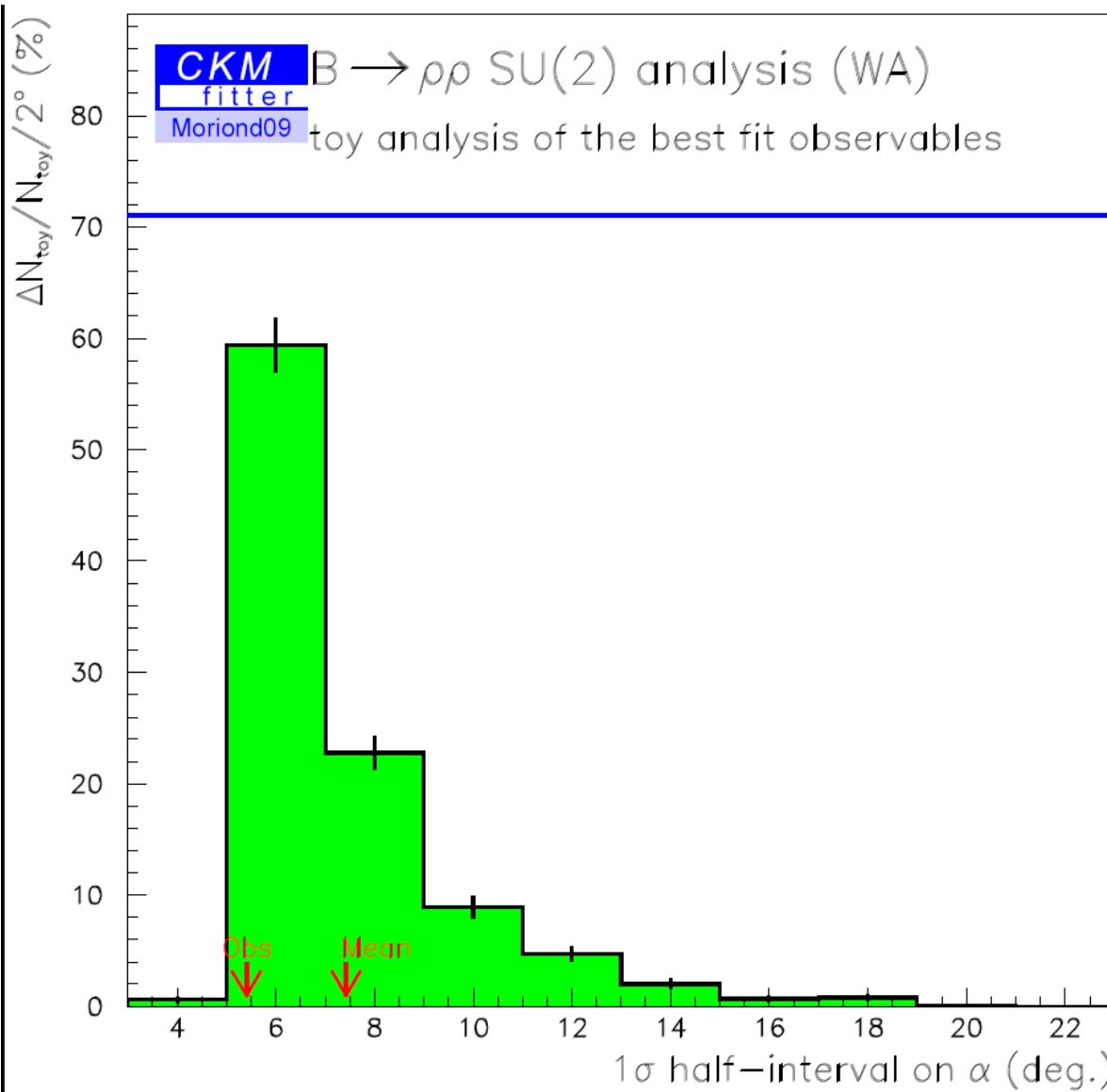
Both B and B̄ isospin triangles do not close (consistent within errors)
 mirror solutions are degenerated in a single peak



$$\delta\alpha = (0.5^{+12.6}_{-5.5})^\circ \rightarrow (1.4 \pm 3.7)^\circ$$

$$\alpha = (90.9^{+6.7}_{-14.9})^\circ \rightarrow (89.9 \pm 5.4)^\circ$$

Isospin analysis of $B \rightarrow \rho\rho$: the lucky shot



34% of the triangles close
Long asymmetric tail (20°) where pseudo-mirror solutions kick in
Average toy error is 7.5° (observed: 5.4°)
68% of the toys have a larger error than the data

Isospin analysis of $B \rightarrow \rho\rho$: breaking effects

At this level of accuracy, consider potential isospin-breaking effects :

- ρ/ω mixing
- finite ρ width
- EPWs
- ...

Test 4%, 10% and 15% violation of the triangular relation with arbitrary additional amplitude:

$$\Rightarrow A^{+0} \rightarrow A^{+0} + \Delta A^{+0}$$

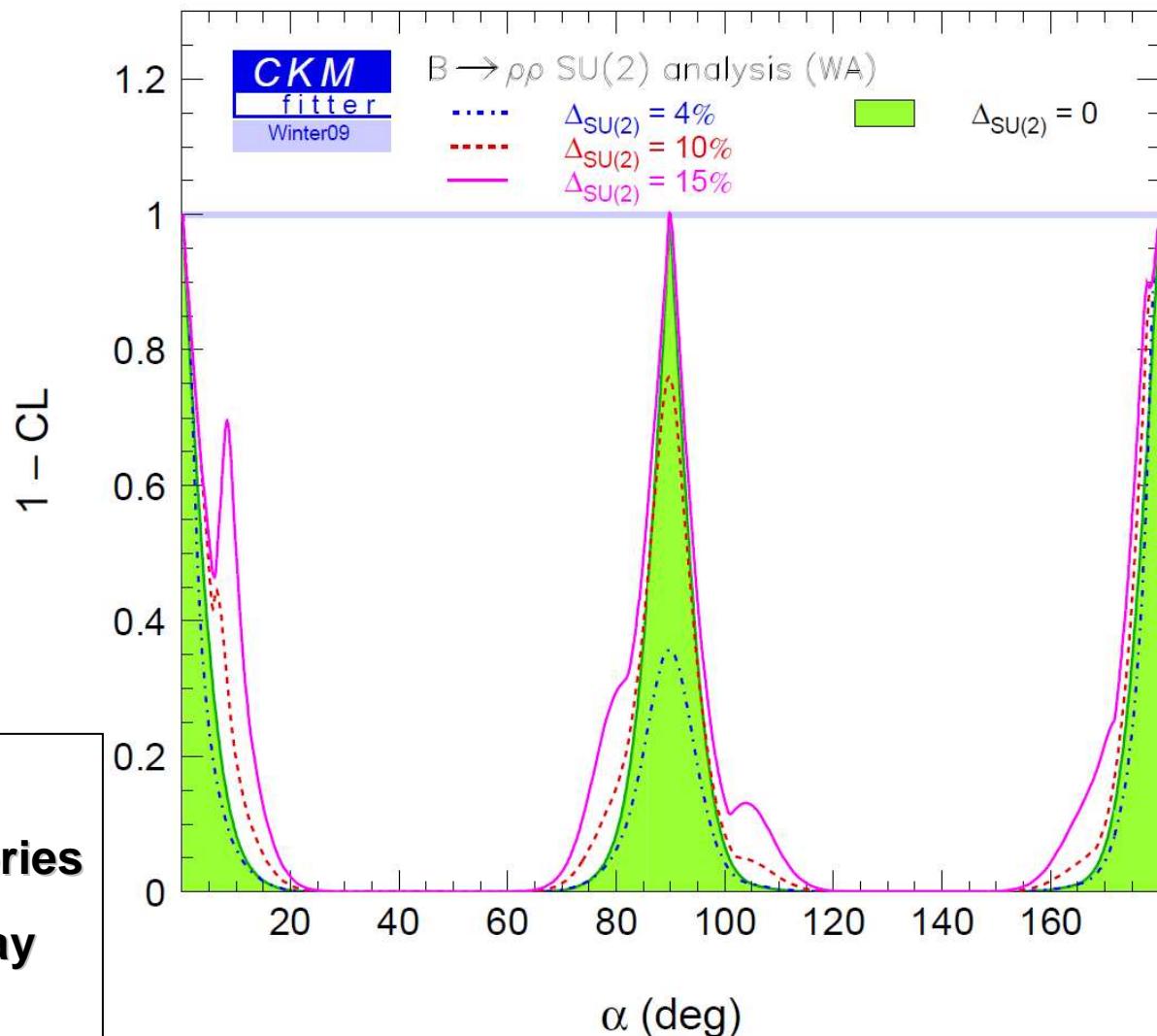
Small values of isospin breaking do not change the pattern.

Similar issue :

f^+/f^{00} normalisation at B factories

A 6.5% (2.4σ) effect as of today

... similar conclusion



The Global CKM fit : discussion on Vub

UT _s apex and angle:			
Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
p_s [deg] (our meas.)	[21.07 [+0.90 -0.88]	[21.1 [+1.0 -1.1]	[21.1 [+2.0 -2.0]
γ [deg]	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (meas. not in the fit)	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (dir. meas.)	70 [+27 -30]	70 [+44 -41]	70 [+60 -52] 131.14 [+0.18 -0.25]
R_u	0.368 [+0.015 -0.013]	0.368 [+0.030 -0.022]	0.368 [+0.045 -0.030]
R_t	0.926 [+0.027 -0.025]	0.926 [+0.040 -0.053]	0.926 [+0.052 -0.072]

CKM elements:			
Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$ V_{ud} $	0.97430 [+0.00019 -0.00019]	0.97430 [+0.00038 -0.00038]	0.97430 [+0.00057 -0.00057]
$ V_{us} $	0.22521 [+0.00082 -0.00082]	0.2252 [+0.0016 -0.0016]	0.2252 [+0.0025 -0.0025]
$ V_{ub} $	0.00350 [+0.00015 -0.00014]	0.00350 [+0.00029 -0.00022]	0.00350 [+0.00044 -0.00029]
$ V_{cb} $	0.04117 [+0.00038 -0.00115]	0.04117 [+0.00077 -0.00161]	0.0412 [+0.0011 -0.0019]
$ V_{ud} $ (meas. not in the fit)	0.97444 [+0.00028 -0.00028]	0.97444 [+0.00055 -0.00056]	0.97444 [+0.00082 -0.00084]
$ V_{us} $ (meas. not in the fit)	0.2257 [+0.0011 -0.0011]	0.2257 [+0.0022 -0.0023]	0.2257 [+0.0033 -0.0034]
$ V_{ub} $ (meas. not in the fit)	0.00350 [+0.00015 -0.00016]	0.00350 [+0.00029 -0.00029]	0.00350 [+0.00045 -0.00040]
$ V_{cb} $ (meas. not in the fit)	0.04399 [+0.00069 -0.00397]	0.0440 [+0.0014 -0.0047]	0.0440 [+0.0024 -0.0052]
$ V_{cd} $	0.22508 [+0.00082 -0.00082]	0.2251 [+0.0016 -0.0016]	0.2251 [+0.0025 -0.0025]
$ V_{cs} $	0.97347 [+0.00019 -0.00019]	0.97347 [+0.00039 -0.00038]	0.97347 [+0.00058 -0.00057]
$ V_{td} $	0.00859 [+0.00027 -0.00029]	0.00859 [+0.00042 -0.00049]	0.00859 [+0.00056 -0.00064]
$ V_{ts} $	0.04041 [+0.00038 -0.00115]	0.04041 [+0.00076 -0.00162]	0.0404 [+0.0011 -0.0019]
$ V_{tb} $	0.999146 [+0.000047 -0.000016]	0.999146 [+0.000065 -0.000032]	0.999146 [+0.000078 -0.000048]

Theory parameters:			
Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
Δm_d [ps ⁻¹] (meas. not in the fit)	0.563 [+0.068 -0.076]	0.56 [+0.11 -0.13]	0.56 [+0.16 -0.16]
Δm_s [ps ⁻¹] (meas. not in the fit)	17.6 [+1.7 -1.8]	17.6 [+3.2 -3.5]	17.6 [+4.2 -4.5]
ϵ_K [10 ⁻³] (meas. not in the fit)	2.06 [+0.47 -0.53]	2.06 [+0.62 -0.64]	2.06 [+0.77 -0.75]
m_c [GeV/c ²] (meas. not in the fit)	1.44 [+0.43 -0.40]	1.44 [+0.52 -0.56]	1.44 [+0.62 -0.73]
m_t [GeV/c ²] (meas. not in the fit)	160 [+13 -10]	160 [+44 -14]	160 [+60 -17]
B_K (lattice value not in the fit)	0.79 [+0.20 -0.12]	0.79 [+0.28 -0.16]	0.79 [+0.37 -0.19]
$\xi_{SU(3)}$ (lattice value not in the fit)	1.188 [+0.059 -0.044]	1.188 [+0.131 -0.085]	1.19 [+0.18 -0.13]

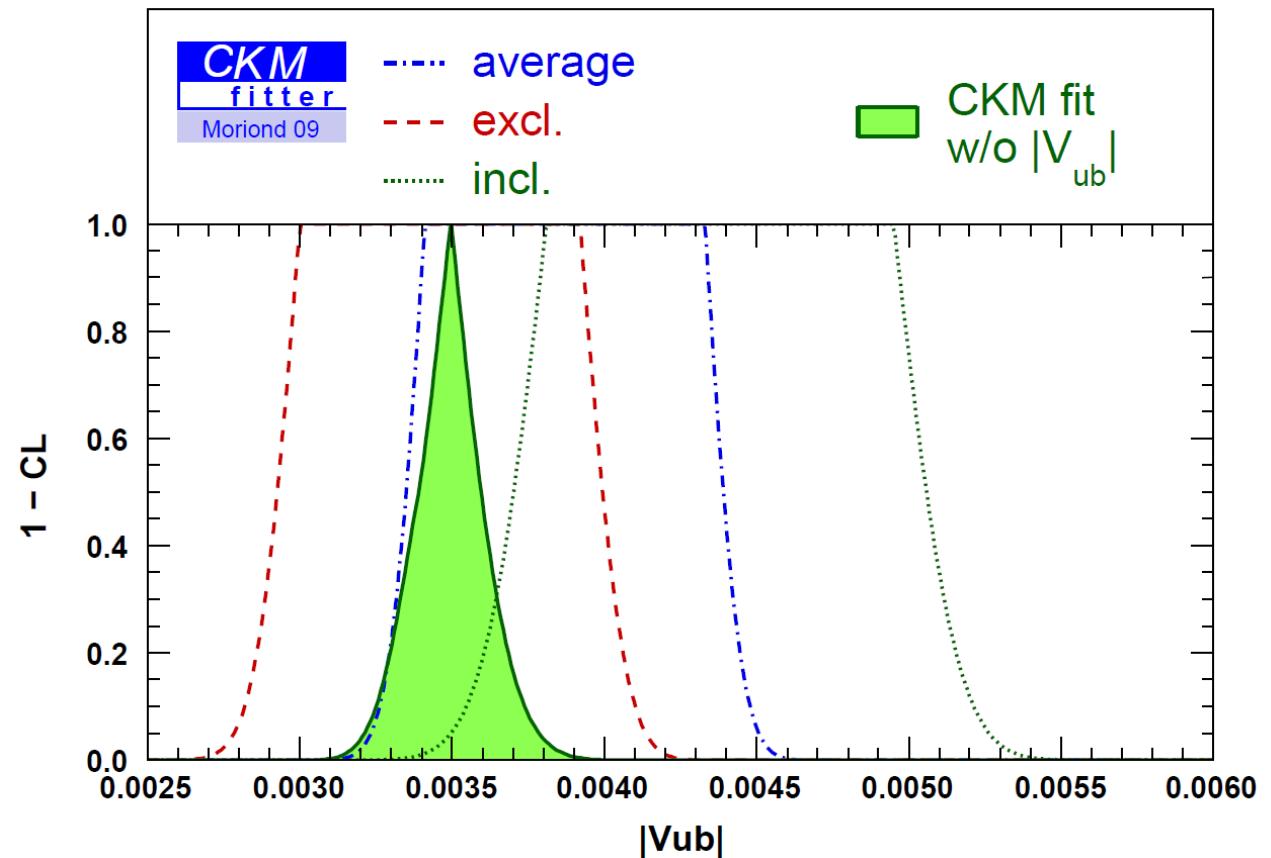
The Global CKM fit : discussion on $|V_{ub}|$

- The *significant* difference between $|V_{ub}|$ derived from inclusive and exclusive $B \rightarrow X_u l \nu$ semileptonic measurements drops when treating systematics within the *Educated RFit* scheme

OOA adapted from HFAG summer 08

$ V_{ub} _{\text{incl.}} = 4.38(16)(57) 10^{-3}$
$ V_{ub} _{\text{excl.}} = 3.46(11)(46) 10^{-3}$
<hr/>
$ V_{ub} = 3.87(9)(46) 10^{-3}$

$\Delta|V_{ub}| = 0.92$, consistent with **OOA** error budget



The Global CKM fit : discussion on ε_K

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$ V_{ud} $	0.97430 [+0.00019 -0.00019]	0.97430 [+0.00038 -0.00038]	0.97430 [+0.00057 -0.00057]
$ V_{us} $	0.22521 [+0.00082 -0.00082]	0.2252 [+0.0016 -0.0016]	0.2252 [+0.0025 -0.0025]
$ V_{ub} $	0.00350 [+0.00015 -0.00014]	0.00350 [+0.00029 -0.00022]	0.00350 [+0.00044 -0.00029]
$ V_{cb} $	0.04117 [+0.00038 -0.00115]	0.04117 [+0.00077 -0.00161]	0.0412 [+0.0011 -0.0019]
$ V_{ud} $ (meas. not in the fit)	0.97444 [+0.00028 -0.00028]	0.97444 [+0.00055 -0.00056]	0.97444 [+0.00082 -0.00084]
$ V_{us} $ (meas. not in the fit)	0.2257 [+0.0011 -0.0011]	0.2257 [+0.0022 -0.0023]	0.2257 [+0.0033 -0.0034]
$ V_{ub} $ (meas. not in the fit)	0.00350 [+0.00015 -0.00016]	0.00350 [+0.00029 -0.00029]	0.00350 [+0.00045 -0.00040]
$ V_{cb} $ (meas. not in the fit)	0.04399 [+0.00069 -0.00397]	0.0440 [+0.0014 -0.0047]	0.0440 [+0.0024 -0.0052]
$ V_{cd} $	0.22508 [+0.00082 -0.00082]	0.2251 [+0.0016 -0.0016]	0.2251 [+0.0025 -0.0025]
$ V_{cs} $	0.97347 [+0.00019 -0.00019]	0.97347 [+0.00039 -0.00038]	0.97347 [+0.00058 -0.00057]
$ V_{td} $	0.00859 [+0.00027 -0.00029]	0.00859 [+0.00042 -0.00049]	0.00859 [+0.00056 -0.00064]
$ V_{ts} $	0.04041 [+0.00038 -0.00115]	0.04041 [+0.00076 -0.00162]	0.0404 [+0.0011 -0.0019]
$ V_{tb} $	0.999146 [+0.000047 -0.000016]	0.999146 [+0.000065 -0.000032]	0.999146 [+0.000078 -0.000048]

Theory parameters:			
Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
Δm_d [ps^{-1}] (meas. not in the fit)	0.563 [+0.068 -0.076]	0.56 [+0.11 -0.13]	0.56 [+0.16 -0.16]
Δm_s [ps^{-1}] (meas. not in the fit)	17.6 [+1.7 -1.8]	17.6 [+3.2 -3.5]	17.6 [+4.2 -4.5]
ε_K [10^{-3}] (meas. not in the fit)	2.06 [+0.47 -0.53]	2.06 [+0.62 -0.64]	2.06 [+0.77 -0.75]
m_c [GeV/c^2] (meas. not in the fit)	1.44 [+0.43 -0.40]	1.44 [+0.52 -0.56]	1.44 [+0.62 -0.73]
m_t [GeV/c^2] (meas. not in the fit)	160 [+13 -10]	160 [+44 -14]	160 [+60 -17]
B_K (lattice value not in the fit)	0.79 [+0.20 -0.12]	0.79 [+0.28 -0.16]	0.79 [+0.37 -0.19]
$\xi_{SU(3)}$ (lattice value not in the fit)	1.188 [+0.059 -0.044]	1.188 [+0.131 -0.085]	1.19 [+0.18 -0.13]
f_B (lattice value not in the fit)	0.2448 [+0.0099 -0.0103]	0.245 [+0.015 -0.019]	0.245 [+0.019 -0.023]

Rare branching fractions ($B \rightarrow l\nu$, $B \rightarrow ll$):			
Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$B(B^+ \rightarrow e\nu) [10^{-4}]$	0.92 [+0.10 -0.11]	0.92 [+0.19 -0.22]	0.92 [+0.28 -0.26]
$B(B^+ \rightarrow e\nu) [10^{-4}]$ (meas. not in the fit)	0.796 [+0.154 -0.093]	0.80 [+0.26 -0.13]	0.80 [+0.35 -0.17]
$B(B^+ \rightarrow e\nu) [10^{-4}]$ (dir. meas.)	1.73 [+0.35 -0.35]	1.73 [+0.70 -0.70]	1.75 [+1.05 -1.05]
$B(B^+ \rightarrow \mu\nu) [10^{-6}]$	0.412 [+0.047 -0.048]	0.412 [+0.086 -0.098]	0.41 [+0.13 -0.12]
$B(B^+ \rightarrow e\nu) [10^{-11}]$	0.96 [+0.11 -0.11]	0.96 [+0.20 -0.23]	0.96 [+0.30 -0.28]
$B(B \rightarrow e^+ e^-) [10^{-5}]$	2.523 [+0.090 -0.207]	2.52 [+0.18 -0.53]	2.52 [+0.26 -0.62]
$B(B \rightarrow \mu^+ \mu^-) [10^{-11}]$	10.78 [+0.38 -0.88]	10.78 [+0.75 -2.26]	10.8 [+1.1 -2.6]
$B(B_s \rightarrow e^+ e^-) [10^{-14}]$	7.70 [+0.22 -0.62]	7.70 [+0.43 -1.08]	7.70 [+0.64 -1.27]
$B(B_s \rightarrow \mu^+ \mu^-) [10^{-9}]$	3.291 [+0.094 -0.267]	3.29 [+0.18 -0.46]	3.29 [+0.27 -0.54]

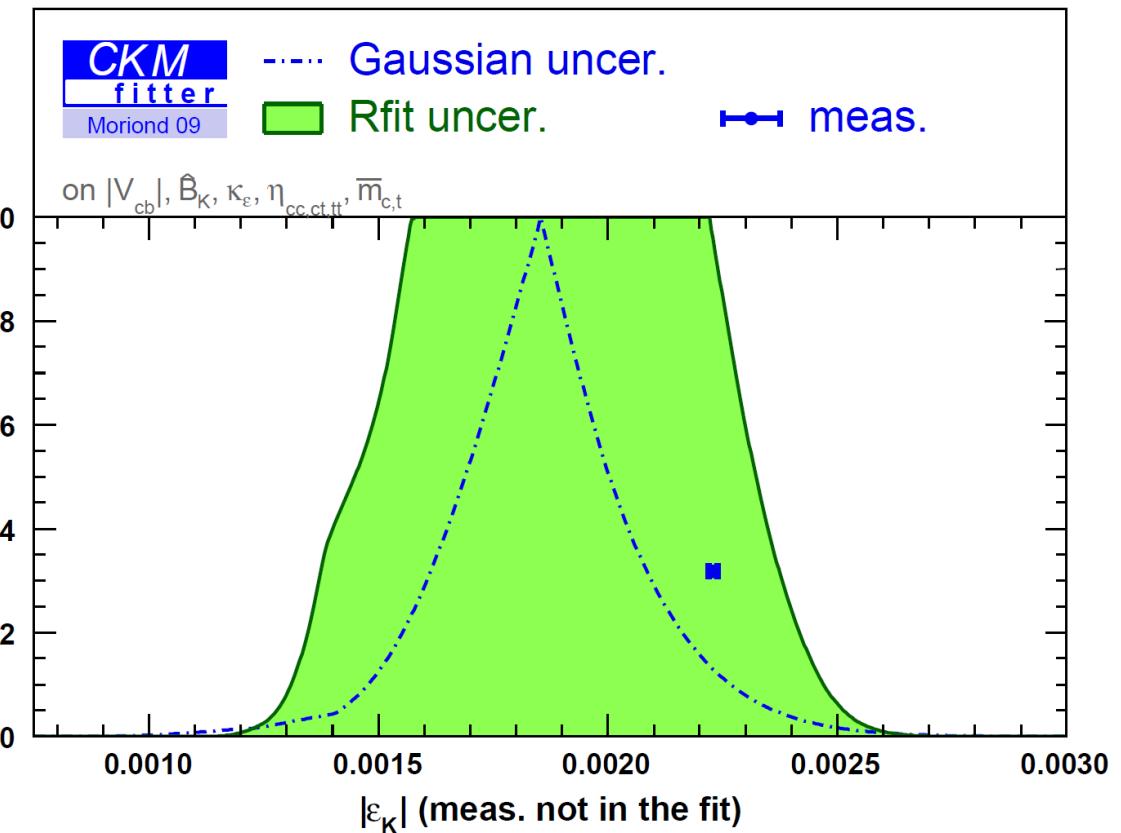
The Global CKM fit : discussion on ε_K

- Reminder from Buras & Guadagnoli (Phys. Rev. D78, 033005 (2008)): there is an additional suppression factor, κ_ε , to $|\varepsilon_K|$, estimated to be $\kappa_\varepsilon = 0.92(2)$.
⇒ Note that this factor has not yet been accounted for in the Global Fit. Its in the line for next update

- Any tension between direct measurement of $|\varepsilon_K|$ and indirect measurement from the global fit (through $\sin(2\beta_{cc})$)?

⇒ Using Gaussian distributions for systematic uncertainties and including the factor $\kappa_\varepsilon = 0.92(2)$ we get 1.5σ deviation

⇒ With our *Educated RFit* treatment of systematics **no deviation is seen**. The measurement is compatible with our fit best guess considering **uncertainties** on CKM parameters (through $|V_{cb}|^4 \sim 7\%$) mainly and hadronic uncertainties from B_K ($\sim 5\%$).



The Global CKM fit : back to β

CKMfitter global fit results:

The inputs for the global fit (pdf).

- Wolfenstein parameters
- UT angles and sides
- UT_s angle and apex
- CKM elements
- Theory parameters
- Rare branching fractions ($B \rightarrow l\nu$, $B \rightarrow ll$)

CKM angle β measured with a $\sim 1^\circ$ accuracy

Indirect constraint has similar precision ...

...but prefers a larger value ...

Wolfenstein parameters and Jarlskog invariant:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
A	0.8116 [+0.0097 -0.0241]	0.812 [+0.019 -0.036]	0.812 [+0.029 -0.045]
λ	0.22521 [+0.00082 -0.00082]	0.2252 [+0.0016 -0.0016]	0.2252 [+0.0025 -0.0025]
$p_{\bar{b}b}$	0.139 [+0.025 -0.027]	0.139 [+0.053 -0.040]	0.139 [+0.073 -0.052]
$\eta_{\bar{b}b}$	0.341 [+0.016 -0.015]	0.341 [+0.032 -0.025]	0.341 [+0.048 -0.034]
$J [10^{-5}]$	2.92 [+0.15 -0.15]	2.92 [+0.30 -0.19]	2.92 [+0.45 -0.23]

UT angles and sides:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$\sin 2\alpha$	-0.02 [+0.15 -0.13]	-0.02 [+0.22 -0.26]	-0.02 [+0.28 -0.35]
$\sin 2\alpha$ (meas. not in the fit)	-0.20 [+0.30 -0.11]	-0.20 [+0.41 -0.17]	-0.20 [+0.48 -0.23]
$\sin 2\beta$	0.684 [+0.023 -0.021]	0.684 [+0.046 -0.035]	0.684 [+0.068 -0.049]
$\sin 2\beta$ (meas. not in the fit)	0.817 [+0.026 -0.040]	0.817 [+0.039 -0.114]	0.817 [+0.052 -0.171]
$ \sin(2\beta + \gamma) $	0.934 [+0.023 -0.030]	0.934 [+0.039 -0.051]	0.934 [+0.049 -0.071]
α [deg]	90.6 [+3.8 -4.2]	90.6 [+7.5 -6.3]	90.6 [+10.2 -8.2]
α [deg] (meas. not in the fit)	95.6 [+3.3 -8.8]	95.6 [+5.2 -11.8]	95.6 [+6.8 -13.9]
α [deg] (dir. meas.)	89.0 [+4.4 -4.2]	89.0 [+9.1 -8.3] 178.3 [+1.7 -5.6] 0 [+5 -0]	89 [+21 -13] 178.3 [+1.7 -13.8] 0 [+12 -0]
β [deg]	21.58 [+0.91 -0.81]	21.6 [+1.8 -1.4]	21.6 [+2.8 -1.9]
β [deg] (meas. not in the fit)	27.4 [+1.3 -1.9]	27.4 [+2.0 -5.0]	27.4 [+2.8 -7.3]
β [deg] (dir. meas.)	21.07 [+0.90 -0.88]	21.1 [+1.8 -1.7]	21.1 [+2.8 -2.6]
γ [deg]	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (meas. not in the fit)	67.8 [+4.2 -3.9]	67.8 [+6.3 -8.0]	67.8 [+8.2 -10.6]
γ [deg] (dir. meas.)	70 [+27 -30]	70 [+44 -41]	70 [+60 -52] 131.14 [+0.18 -0.25]
R_u	0.368 [+0.015 -0.013]	0.368 [+0.030 -0.022]	0.368 [+0.045 -0.030]
R_t	0.926 [+0.027 -0.025]	0.926 [+0.040 -0.053]	0.926 [+0.052 -0.072]

UT_s apex and angle:

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$p_s \bar{b}$	-0.0074 [+0.0014 -0.0013]	-0.0074 [+0.0022 -0.0029]	-0.0074 [+0.0028 -0.0040]
$\eta_s \bar{b}$	-0.01821 [+0.00081 -0.00085]	-0.0182 [+0.0013 -0.0017]	-0.0182 [+0.0018 -0.0026]
$\beta_s \equiv -\arg(-V_{cs} V_{cb}^* V_{ts} V_{tb}^*)$ [rad]	0.01807 [+0.00086 -0.00081]	0.0181 [+0.0017 -0.0014]	0.0181 [+0.0026 -0.0018]

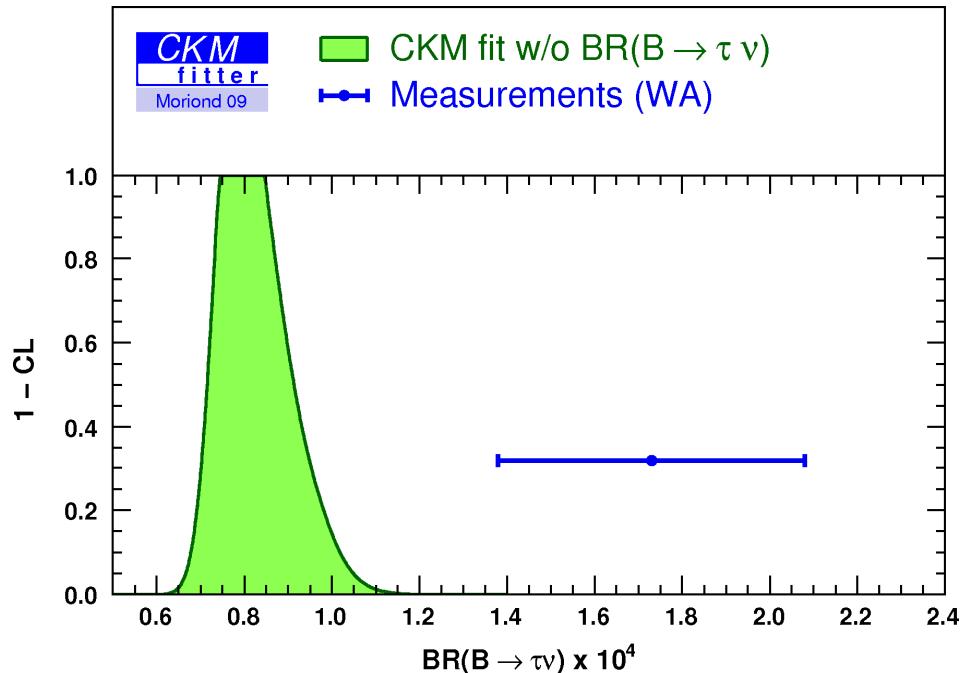
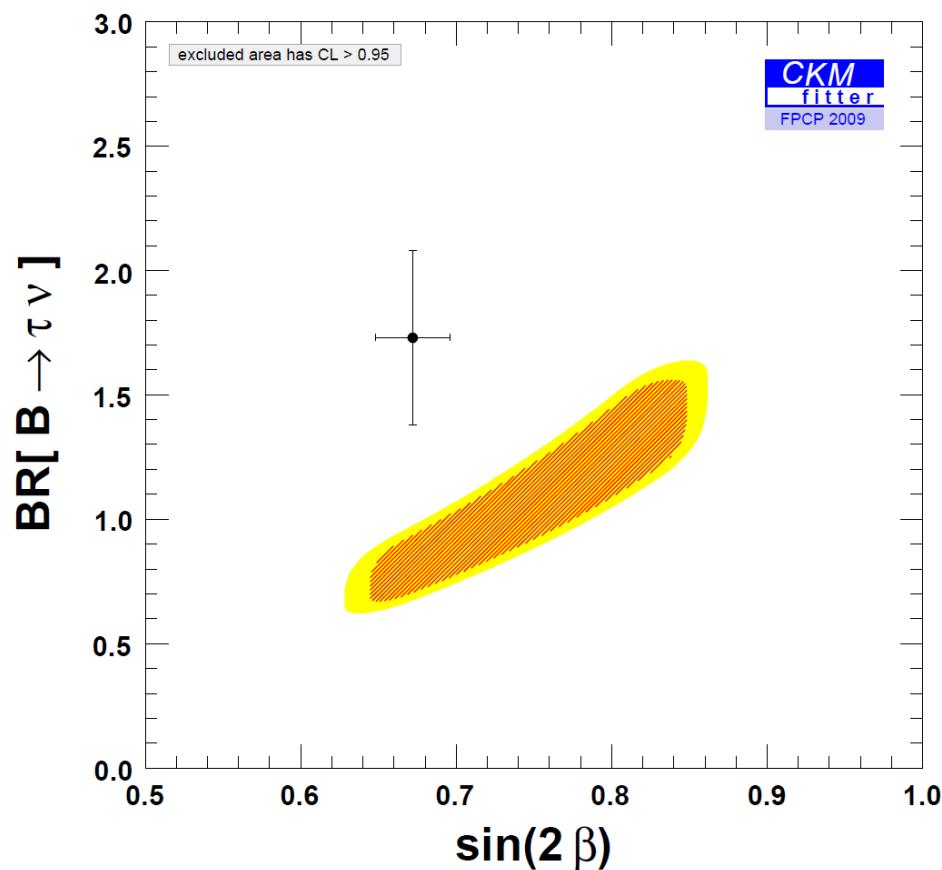
The Global CKM fit : discussion on $B \rightarrow TV$

Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
$ V_{ud} $	0.97430 [+0.00019 -0.00019]	0.97430 [+0.00038 -0.00038]	0.97430 [+0.00057 -0.00057]
$ V_{us} $	0.22521 [+0.00082 -0.00082]	0.2252 [+0.0016 -0.0016]	0.2252 [+0.0025 -0.0025]
$ V_{ub} $	0.00350 [+0.00015 -0.00014]	0.00350 [+0.00029 -0.00022]	0.00350 [+0.00044 -0.00029]
$ V_{cb} $	0.04117 [+0.00038 -0.00115]	0.04117 [+0.00077 -0.00161]	0.0412 [+0.0011 -0.0019]
$ V_{ud} $ (meas. not in the fit)	0.97444 [+0.00028 -0.00028]	0.97444 [+0.00055 -0.00056]	0.97444 [+0.00082 -0.00084]
$ V_{us} $ (meas. not in the fit)	0.2257 [+0.0011 -0.0011]	0.2257 [+0.0022 -0.0023]	0.2257 [+0.0033 -0.0034]
$ V_{ub} $ (meas. not in the fit)	0.00350 [+0.00015 -0.00016]	0.00350 [+0.00029 -0.00029]	0.00350 [+0.00045 -0.00040]
$ V_{cb} $ (meas. not in the fit)	0.04399 [+0.00069 -0.00397]	0.0440 [+0.0014 -0.0047]	0.0440 [+0.0024 -0.0052]
$ V_{cd} $	0.22508 [+0.00082 -0.00082]	0.2251 [+0.0016 -0.0016]	0.2251 [+0.0025 -0.0025]
$ V_{cs} $	0.97347 [+0.00019 -0.00019]	0.97347 [+0.00039 -0.00038]	0.97347 [+0.00058 -0.00057]
$ V_{td} $	0.00859 [+0.00027 -0.00029]	0.00859 [+0.00042 -0.00049]	0.00859 [+0.00056 -0.00064]
$ V_{ts} $	0.04041 [+0.00038 -0.00115]	0.04041 [+0.00076 -0.00162]	0.0404 [+0.0011 -0.0019]
$ V_{tb} $	0.999146 [+0.000047 -0.000016]	0.999146 [+0.000065 -0.000032]	0.999146 [+0.000078 -0.000048]

Theory parameters:			
Observable	Central $\pm 1\sigma$	$\pm 2\sigma$	$\pm 3\sigma$
Δm_d [ps^{-1}] (meas. not in the fit)	0.563 [+0.068 -0.076]	0.56 [+0.11 -0.13]	0.56 [+0.16 -0.16]
Δm_s [ps^{-1}] (meas. not in the fit)	17.6 [+1.7 -1.8]	17.6 [+3.2 -3.5]	17.6 [+4.2 -4.5]
ϵ_K [10^{-3}] (meas. not in the fit)	2.06 [+0.47 -0.53]	2.06 [+0.62 -0.64]	2.06 [+0.77 -0.75]
m_c [GeV/c^2] (meas. not in the fit)	1.44 [+0.43 -0.40]	1.44 [+0.52 -0.56]	1.44 [+0.62 -0.73]
m_t [GeV/c^2] (meas. not in the fit)	160 [+13 -10]	160 [+44 -14]	160 [+60 -17]
B_K (lattice value not in the fit)	0.79 [+0.20 -0.12]	0.79 [+0.28 -0.16]	0.79 [+0.37 -0.19]
$\xi_{SU(3)}$ (lattice value not in the fit)	1.188 [+0.059 -0.044]	1.188 [+0.131 -0.085]	1.19 [+0.18 -0.13]
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$B(B_s \rightarrow \mu^+ \mu^-) [10^{-9}]$	3.291 [+0.094 -0.267]	3.29 [+0.18 -0.46]	3.29 [+0.27 -0.54]

The Global CKM fit : β and $B \rightarrow \tau v$



The Global fit χ^2_{\min} drops by $\sim 2.4 \sigma$ if taking out $\sin(2\beta_{cc})$ or $B \rightarrow \tau v$.

$$BR(B^+ \rightarrow \tau^+ \nu) = G_F^2 \frac{m_B m_\tau^2 \tau_{B^+}}{8\pi} \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 |V_{ub}|^2 f_{B_d}^2$$

Non-trivial correlation of indirect constraints on β and $B \rightarrow \tau v$...

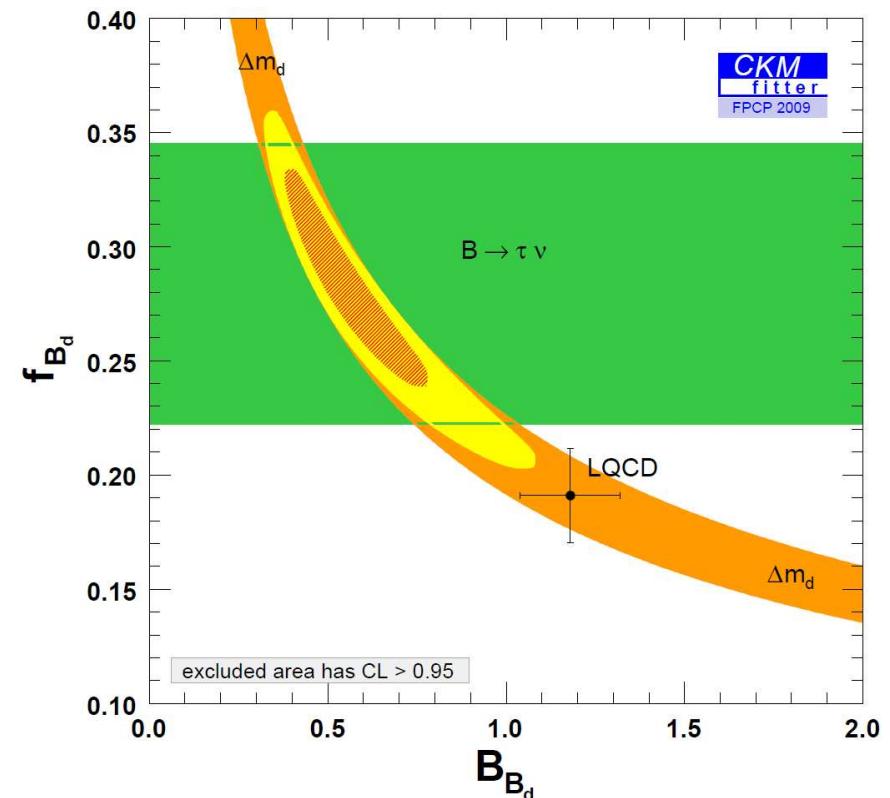
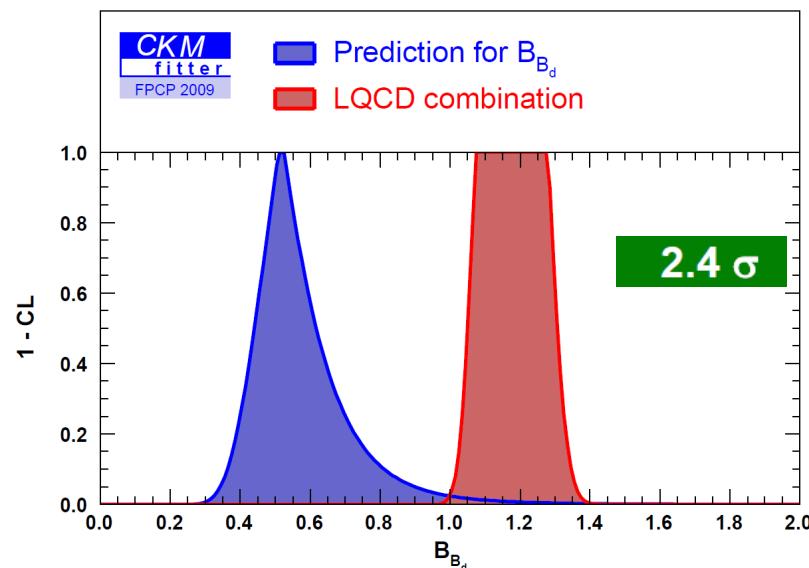
Can be shown that V_{ub} and f_{B_d} are unrelated to this correlation (next slide)

The Global CKM fit : β and $B \rightarrow \tau v$

$$\frac{BR(B^+ \rightarrow \tau^+ v)}{\Delta m_d} = \frac{3\pi}{4} \frac{m_\tau^2 \tau_{B^+}}{m_W^2 S(x_t)} \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 \frac{\sin^2(\beta)}{\sin^2(\gamma)} \frac{1}{|V_{ud}|^2 B_{B_d}}$$

Simultaneous constraint on B_{B_d} and f_{B_d}

Theory-free estimation of B_{B_d} and f_{B_d}

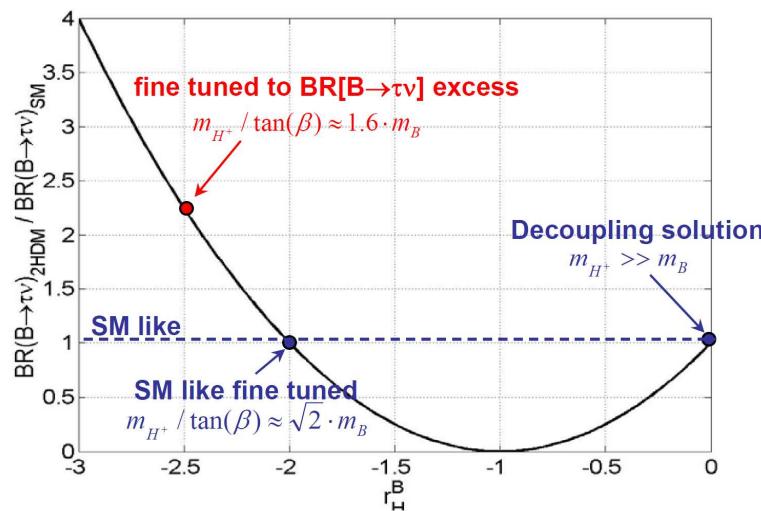


⇒ The global fit is accommodated keeping $f_{B_d}^{-2} \times B_{B_d} \approx \text{const}$ to fit Δm_d while increasing f_{B_d} to fit $B \rightarrow \tau v$

Beyond the global CKM fit : $B \rightarrow \tau\nu$

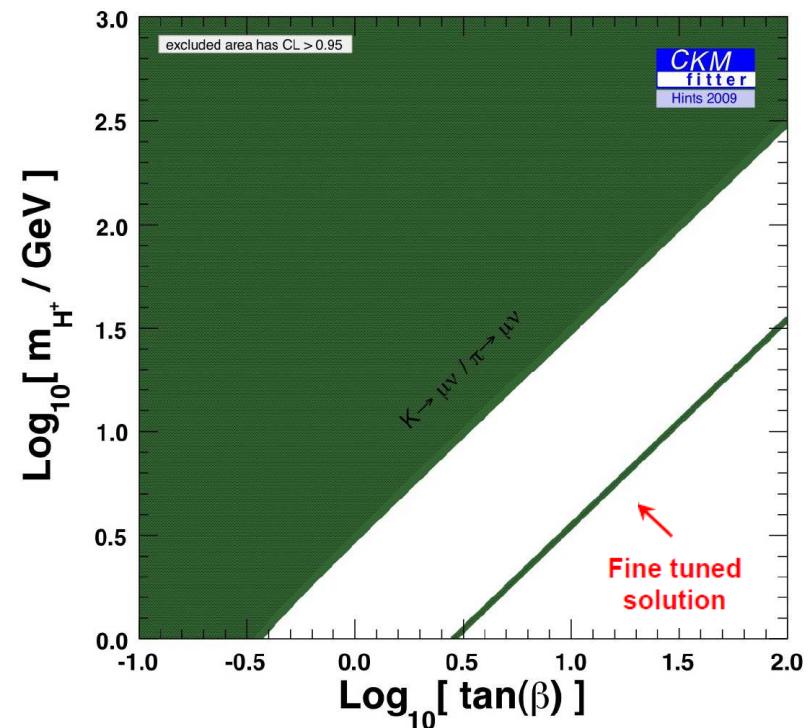
$$BR(B^+ \rightarrow \tau^+\nu)(NP) = BR(B^+ \rightarrow \tau^+\nu)(SM) \times \left(1 - \frac{m_B^2}{m_{H^+}^2} \tan \beta\right)$$

- Charged higgs contribution can modify $B[B \rightarrow \tau\nu]$ as a multiplicative term: $r_H^B \approx -\tan^2(\beta)m_B^2 / m_{H^+}^2$ in 2HDM Type II model. Note that one would need $r_H^B \approx -2.5$ to fit $B[B \rightarrow \tau\nu]$ (fine tuned solution).



Agreement with the SM can be recovered 2 ways:

- $r_H^B \rightarrow 0 \Rightarrow m_{H^+}/m_B \rightarrow \infty$ irrespective $\tan(\beta)$. This is the **decoupling solution**
- $r_H^B = -2 \Rightarrow m_{H^+}/\tan(\beta) \approx \sqrt{2} \cdot m_B$; requires a **fine tuning of $m_{H^+}/\tan(\beta)$ to the meson mass**.



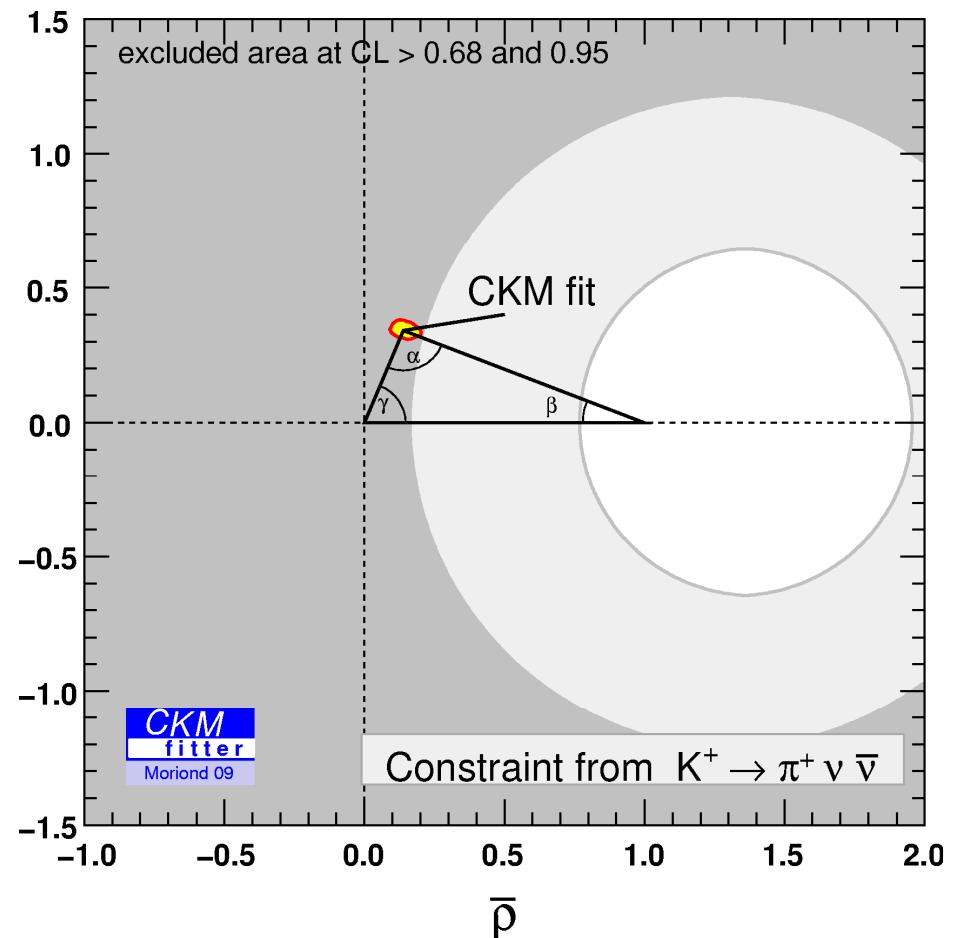
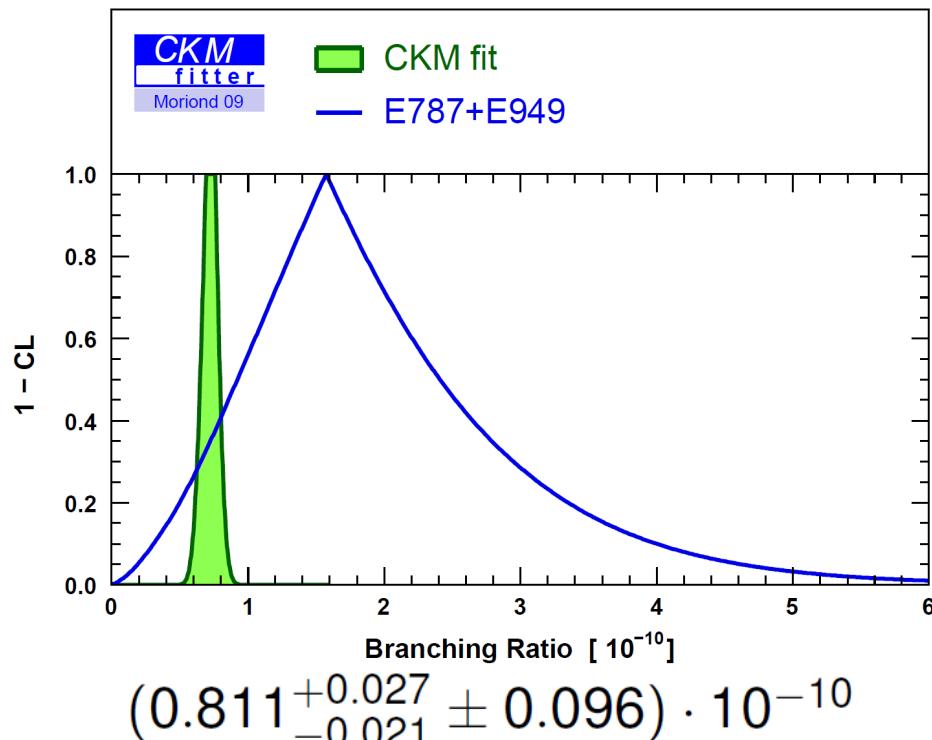
Fine-tuned solution can be ruled out
By using other semileptonic information

A word on the rare kaon decay $K^+ \rightarrow \pi^+ \nu \bar{\nu}$

with contributions from R. Camacho

- Recent E949 update (arXiv:0903.0030 with 5 events (& incl. E787)): $(1.73^{+1.15}_{-1.05}) \cdot 10^{-10}$
- BR parameterization as Brod & Gorbahn '08 (PRD 78, 034006)
NLO QED-QCD & EW corr. to the charm quark contribution
 $\alpha_s(m_Z)=0.1176(20)$ & $m_c(m_c)=1.286(13)(40)$

Charm term $P_c(X)$ controlled at ~few %

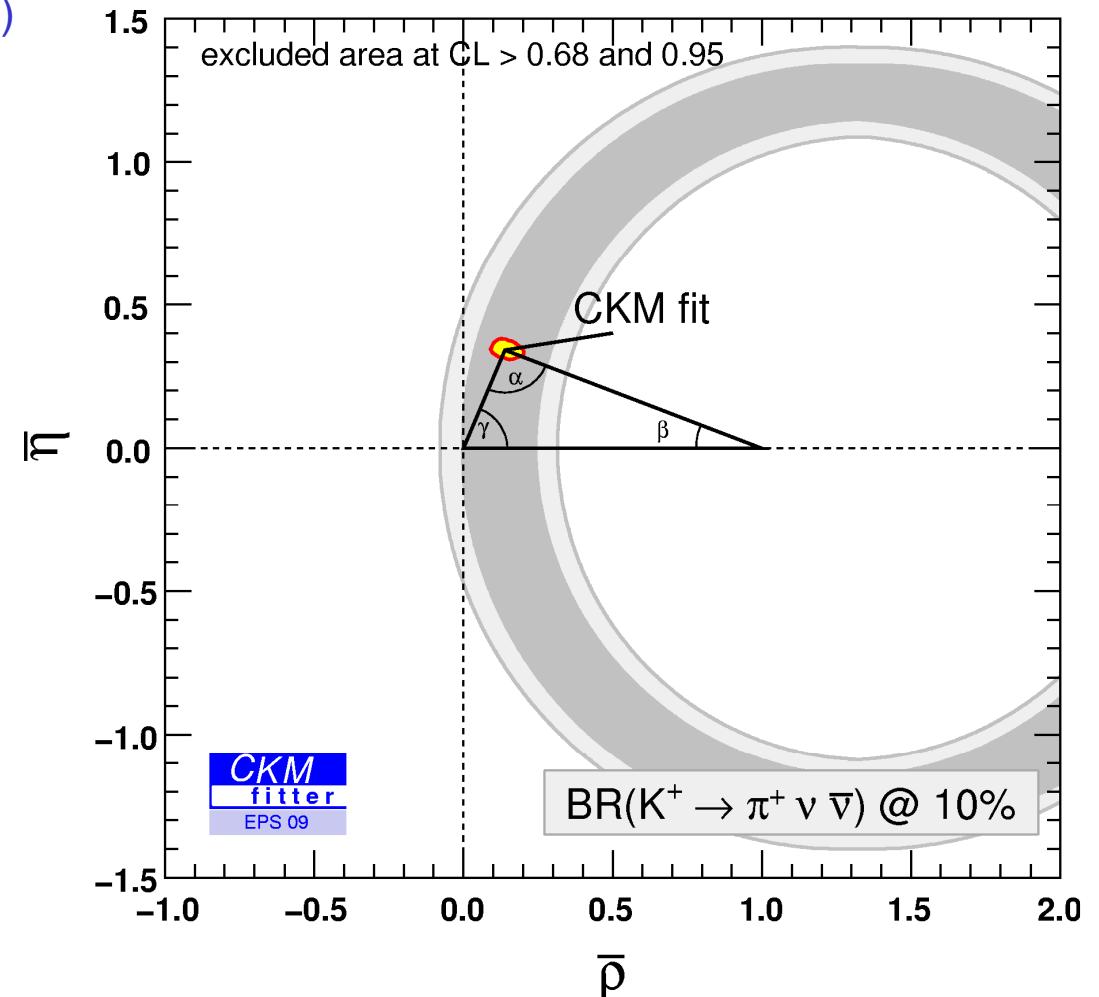


A word on the rare kaon decays $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ and $K_L \rightarrow \pi^0 \nu \bar{\nu}$

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Prospective study : assume

- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ measured by NA62 (~10%)

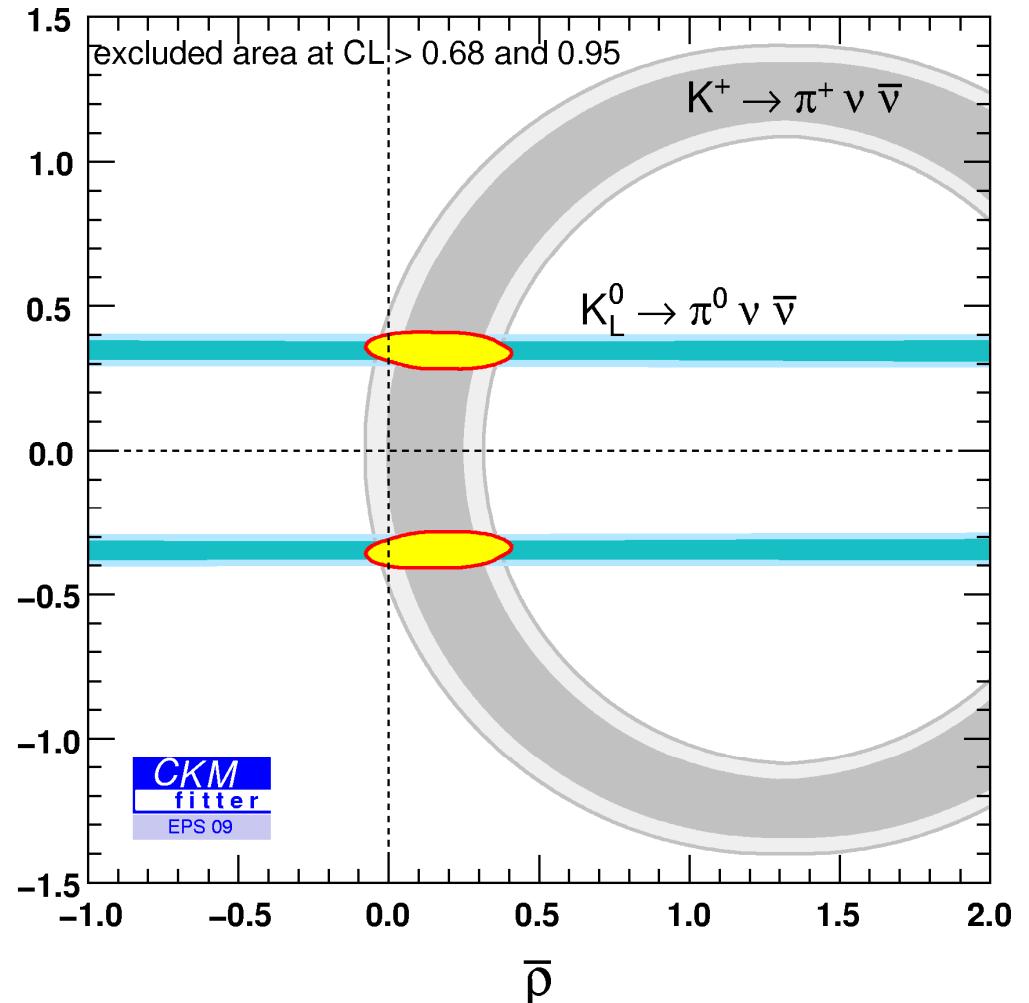


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A word on the rare kaon decays $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ and $K_L \rightarrow \pi^0 \nu \bar{\nu}$

- Recent E949 update (arXiv:0903.0030 with 5 events (& incl. E787)):

$$\text{BR } [10^{-10}] = 1.73^{+1.15}_{-1.05}$$

- BR parameterization as Brod & Gorbahn '08 (PRD 78, 034006)

NLO QED-QCD & EW corr. to the charm quark contribution

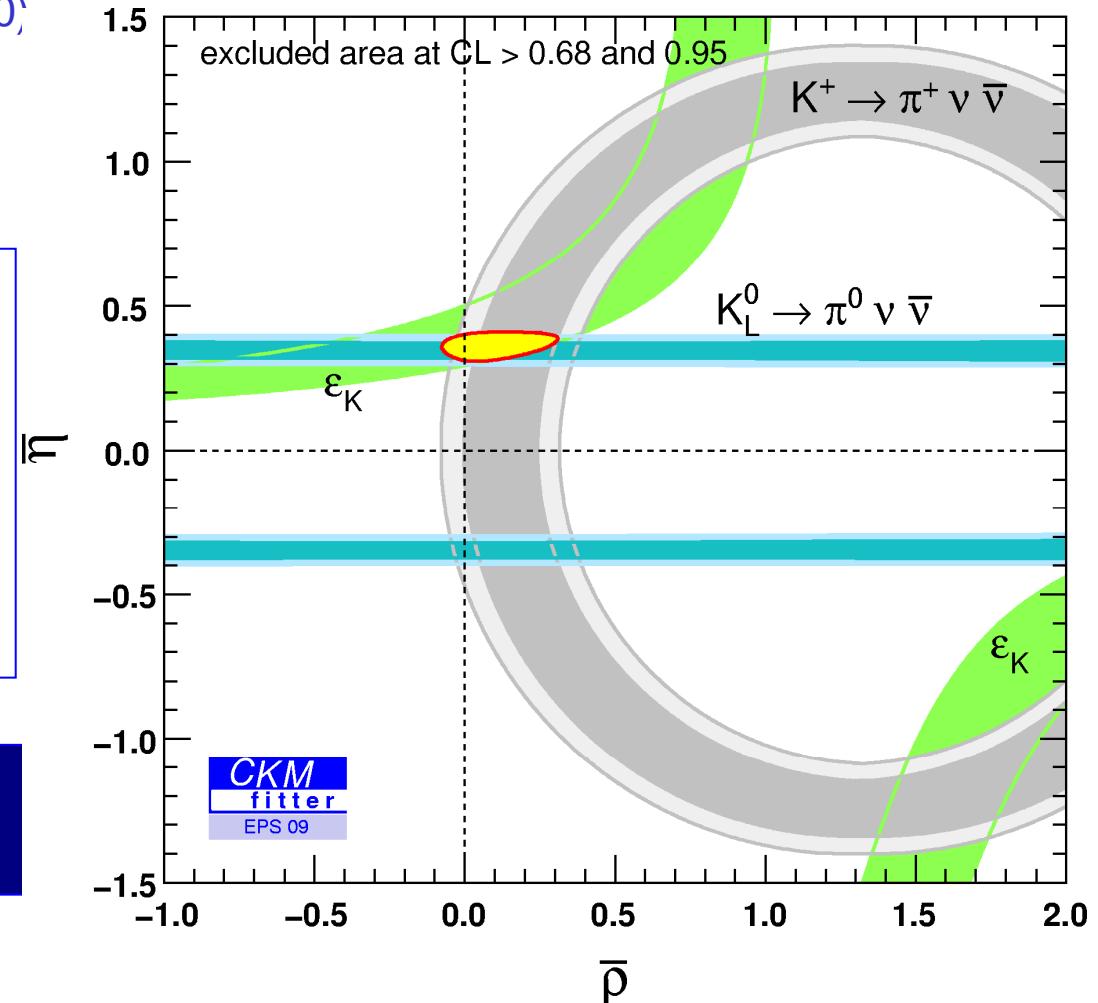
$$\alpha_s(m_Z) = 0.1176(20) \text{ and } m_c(m_c) = 1.286(13)(40)$$

Prospective study : assume

- $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ measured by NA62 (~10%)
- $K_L \rightarrow \pi^0 \nu \bar{\nu}$ measured by J-PARC (~15%)
- Use ε_K (and ε'/ε ?) to lift ambiguities

(pessimistic scenario: no improvement of theoretical errors)

A strong constrain on the CKM matrix
only using Kaon inputs



Summary

- KM mechanism at work, main source of CP violation
- Increased precision on α
 - keep an eye on possible non-SU(2) effects
- $\sin 2\beta$ vs $B \rightarrow \tau v$ (and/or V_{ub} and/or ε_K)
 - issue of hadronic/lattice inputs
- eagerly waiting for updates from B factories
 - γ !
 - new news on $B \rightarrow \tau v$?
- Results from TeVatron and soon LHC, to test for NP scenarios
- Support Kaon physics !