

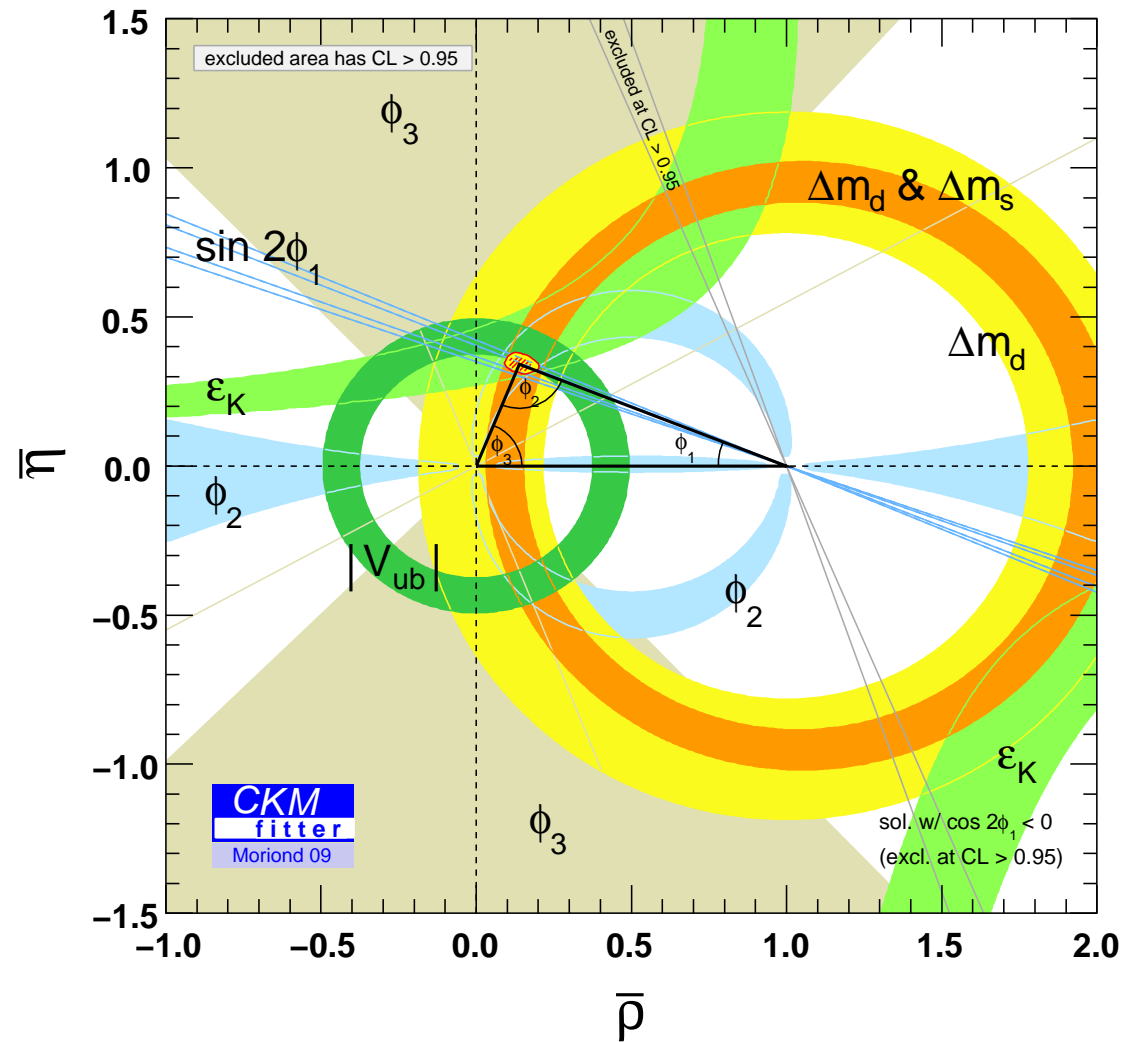
# Inclusive $b \rightarrow u$ Decays and Determination of $V_{ub}$ at Belle

The 2009 Europhysics Conference on High Energy Physics

Krakow, Poland, 16–22.July.2009

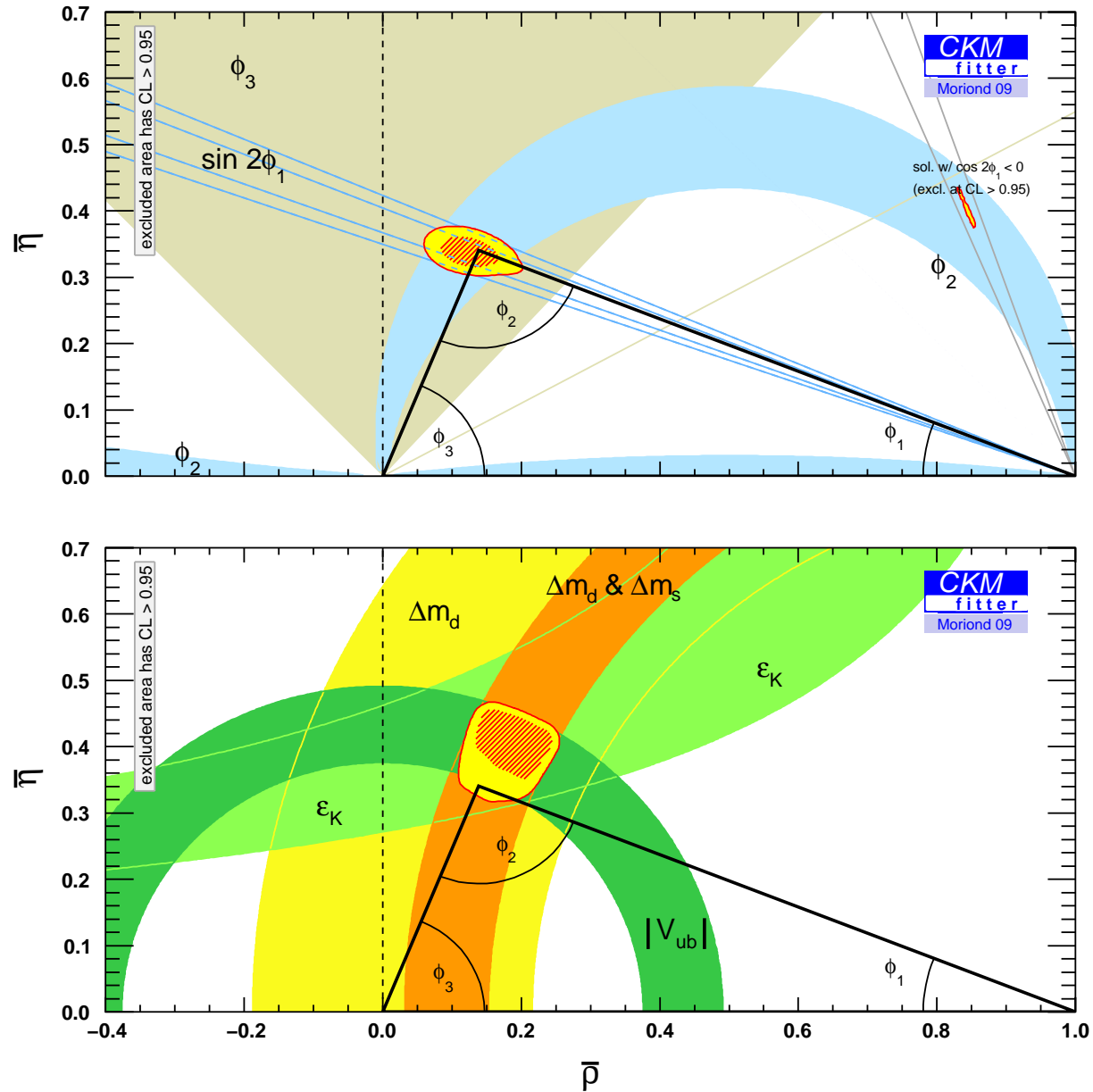
中村 勇 / KEK

# Introduction



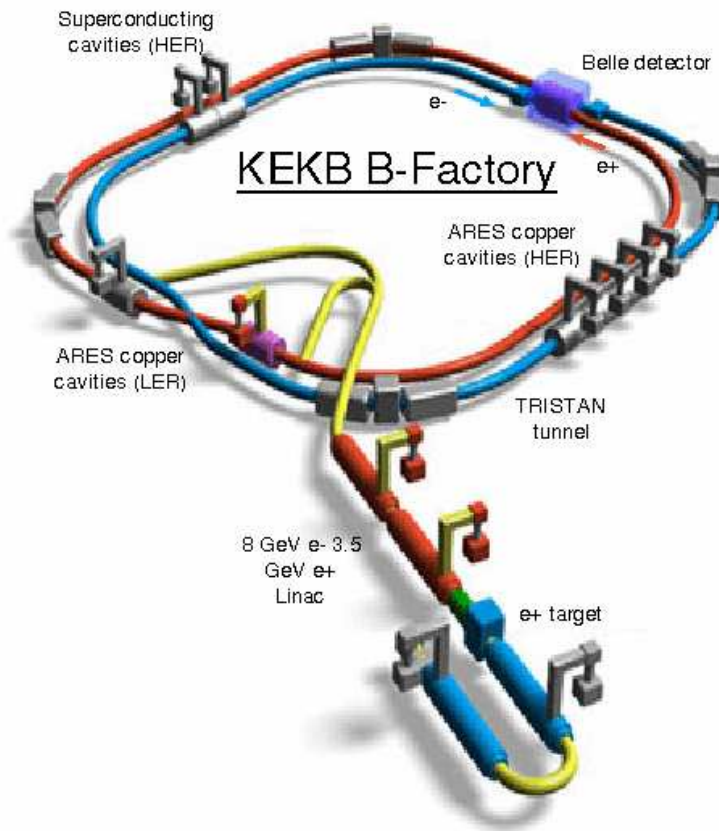
- Precise Determination of  $|V_{ub}|$  is important for the test of CKM mechanism

# Introduction

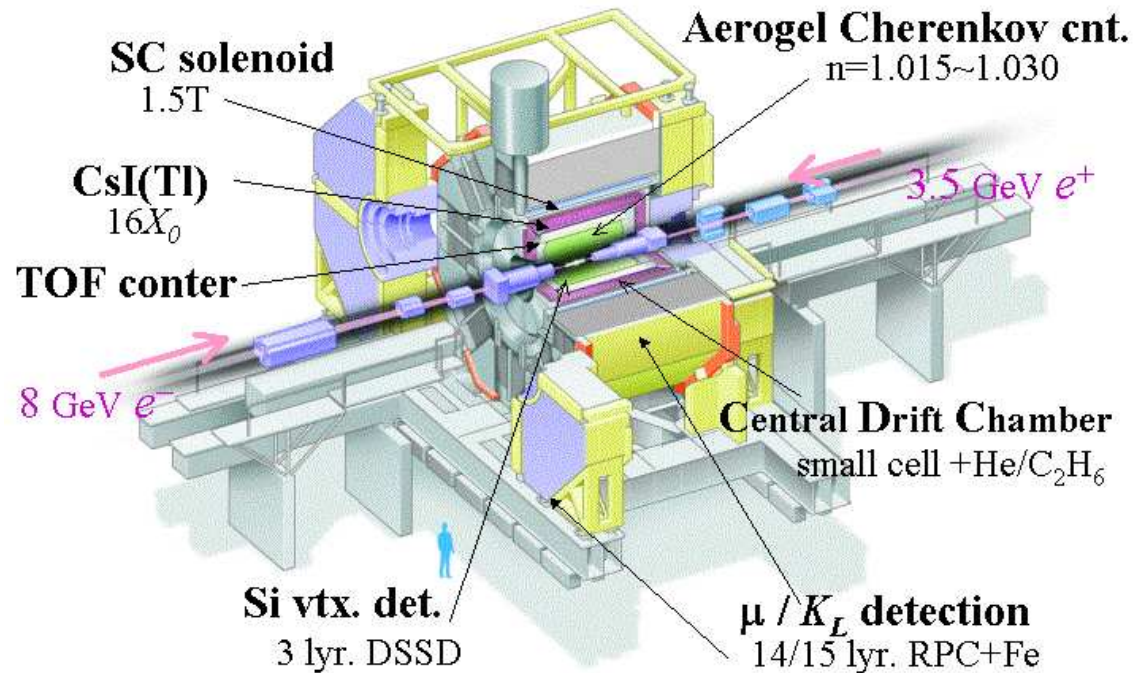


- Sides measurement not as accurate as angles

# KEKB and Belle

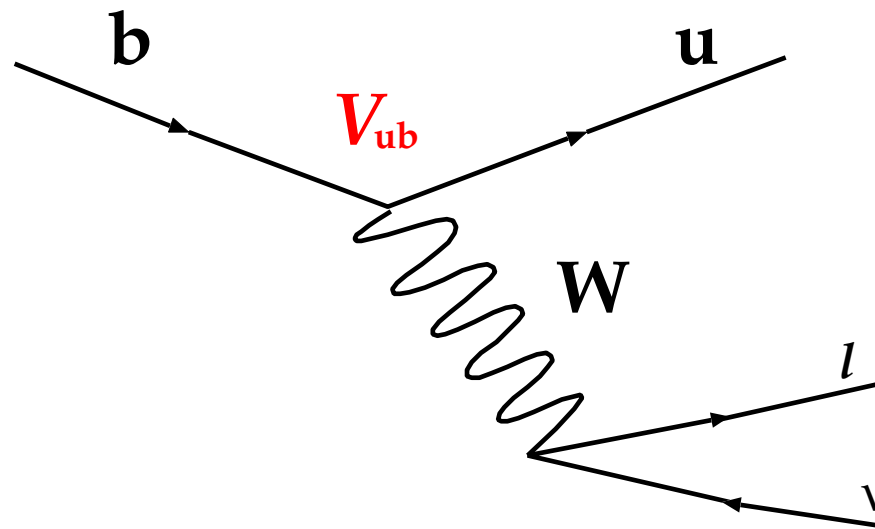


## Belle Detector



- Belle Detector, KEKB collider at KEK, Tsukuba, Japan
- World brightest collider  $\mathcal{L} = 21 \text{ nb}^{-1}/\text{s}$
- Accumulated  $\sim 950 \text{ fb}^{-1}$

## Measurement of $V_{ub}$



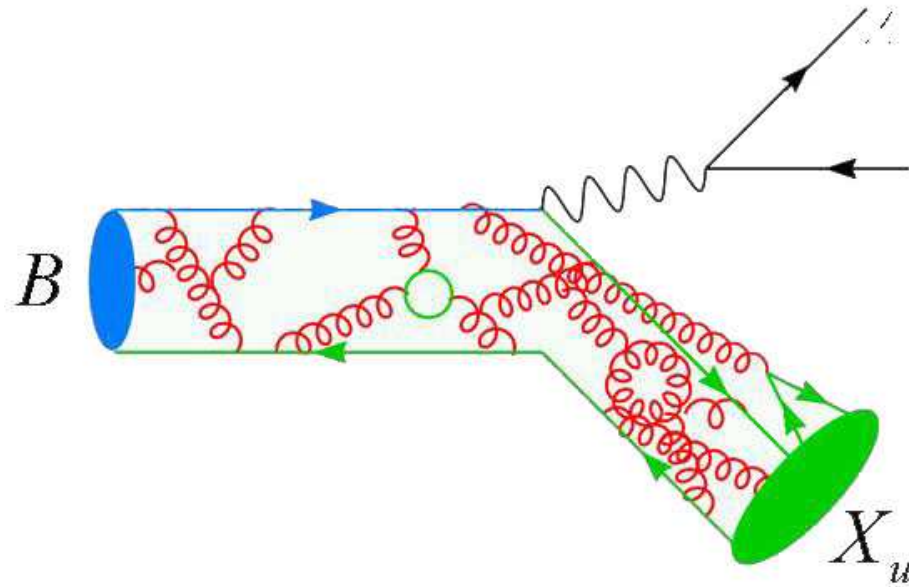
- Measurement is very straightforward, use a relation

$$\Gamma(b \rightarrow u \ell^- \bar{\nu}) = \frac{G_F^2}{192\pi^2} |V_{ub}|^2 m_b^5 (1 + \text{補正項})$$

- Only need to count the number of  $b \rightarrow u \ell^- \bar{\nu}$  events, however in reality

# Measurement of $V_{ub}$

- In reality,



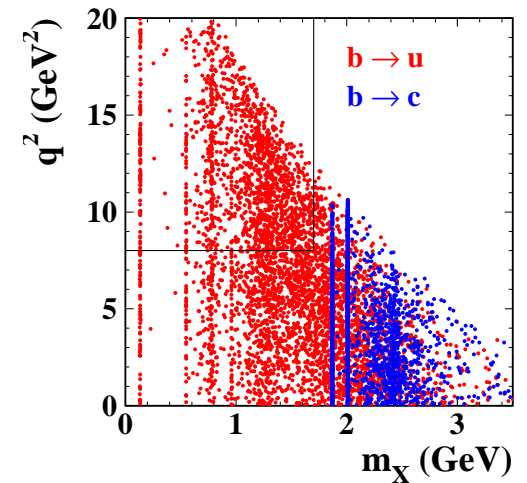
- To get 補正項, we have to know structure of B meson
  - ◇ In inclusive case
    - ⇒ HQET parameters, b and c quark masses
  - ◇ in exclusive case
    - ⇒ form factors

# $|V_{ub}|$ from Inclusive Semileptonic

- must deal with 50 times bigger background with identical topology.

$$\frac{\Gamma(\mathbf{b} \rightarrow \mathbf{u}\ell^{-}\bar{\nu})}{\Gamma(\mathbf{b} \rightarrow \mathbf{c}\ell^{-}\bar{\nu})} \approx \frac{|V_{ub}|^2}{|V_{cb}|^2} \approx \frac{1}{50}$$

- enhance  $\mathbf{b} \rightarrow \mathbf{u}\ell^{-}\bar{\nu}$  using kinematic variables,
  - ◇  $E_\ell$ : Lepton energy distribution around endpoint
  - ◇  $m_X, q^2$  or  $P_+ \equiv E_X - |\mathbf{p}_X|$



hence We actually measure,

$$\Delta\mathcal{B}(\mathbf{B} \rightarrow \mathbf{X}_u\ell^{-}\bar{\nu}) = f_u \cdot \mathcal{B}(\mathbf{B} \rightarrow \mathbf{X}_u\ell^{-}\bar{\nu})$$

- ◇  $f_u$  is the fraction of phase space

# Belle Endpoint Measurement

- Phys.Lett.B621:28-40,2005
- $27 \text{ fb}^{-1}$
- Measure  $\Delta\mathcal{B}$  for  $p_e^* > p_{\text{cut}}$   
( $p_e^*$ : electron momentum in  $\Upsilon(4S)$  frame)
- Lowest  $p_{\text{cut}} = 1.9 \text{ GeV}$
- Systematic error dominant because of large background

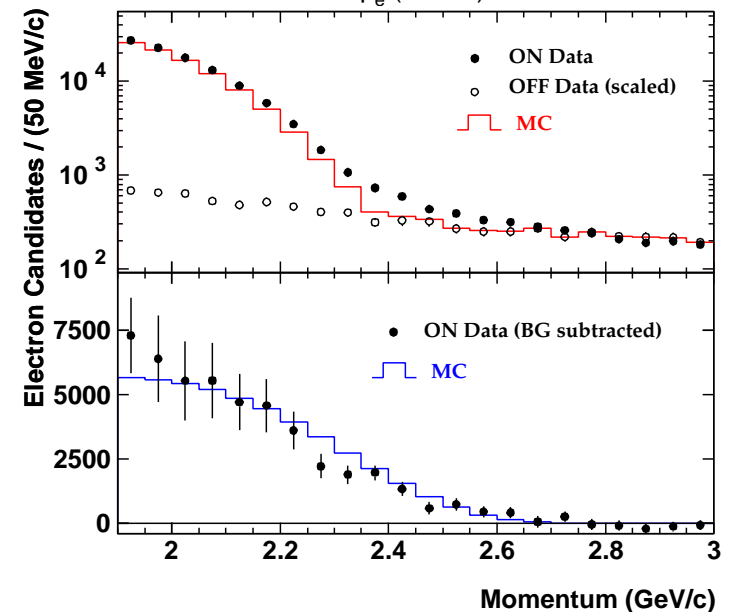
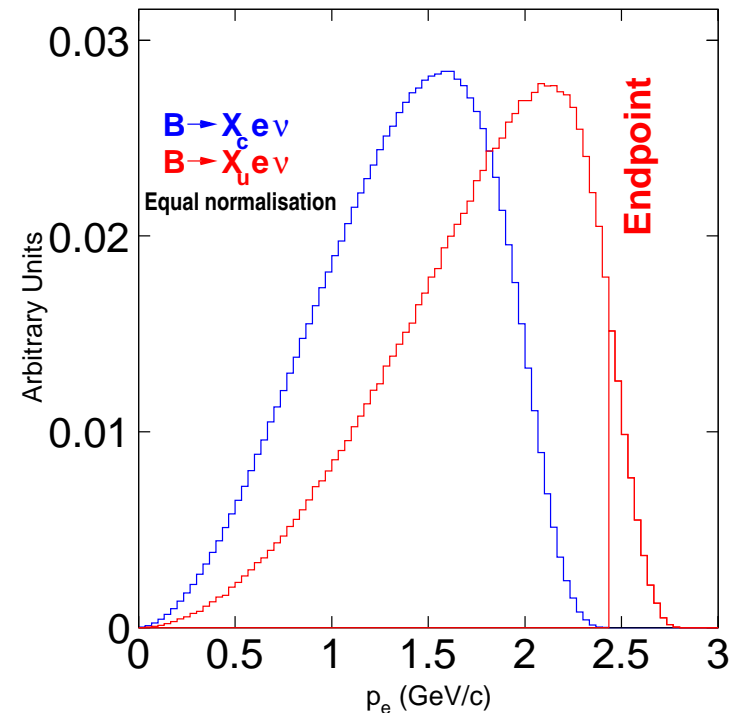
$$\Delta\mathcal{B} = (8.47 \pm 0.37(\text{stat.}) \pm 1.53(\text{syst.})) \times 10^{-4}$$

for  $p^* > 1.9 \text{ GeV}$

with BLNP, Phys. Rev. D 72, 073006 (2005)

$$V_{\text{ub}} = (4.64 \pm 0.43^{+0.29}_{-0.31}) \times 10^{-3}$$

HFAG Winter 2009 combination



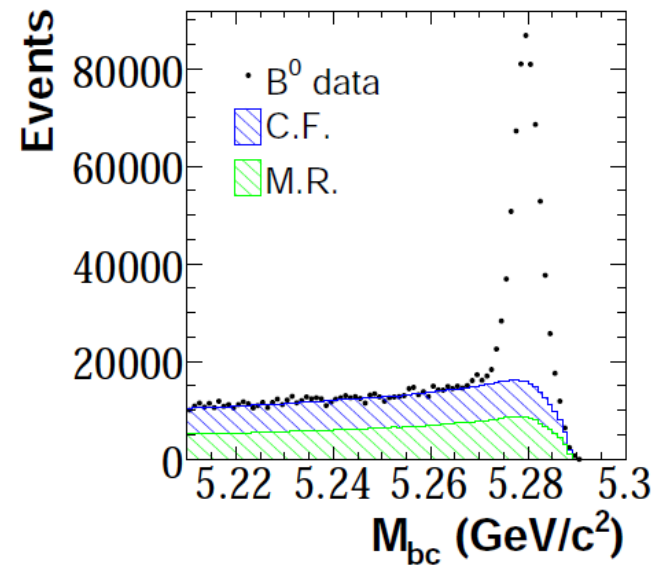
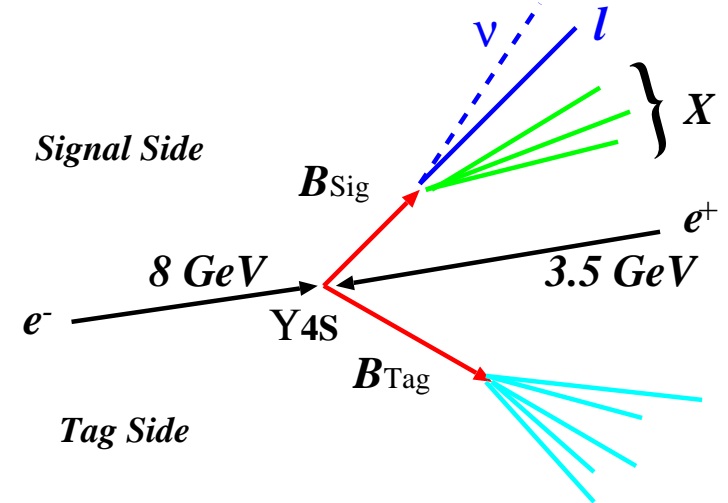


# Belle Hadronic Tag Measurement

- arXiv:0907.0379 (July 2009)
- “Fully” reconstruct one B ( $B_{\text{tag}}$ ), exclusively
  - ◇ Total of  $\sim 180$  exclusive modes
  - ◇ Known  $B_{\text{sig}}$  4-momentum
  - ◇ High purity, low efficiency
  - ◇ need many events
- $605 \text{ fb}^{-1}$  Belle Data ( $\sim 2005$ )

	eff. (%)	purity	$N_{\text{tag}} (\times 10^3)$
charged	0.29	0.25	689
neutral	0.28	0.30	479

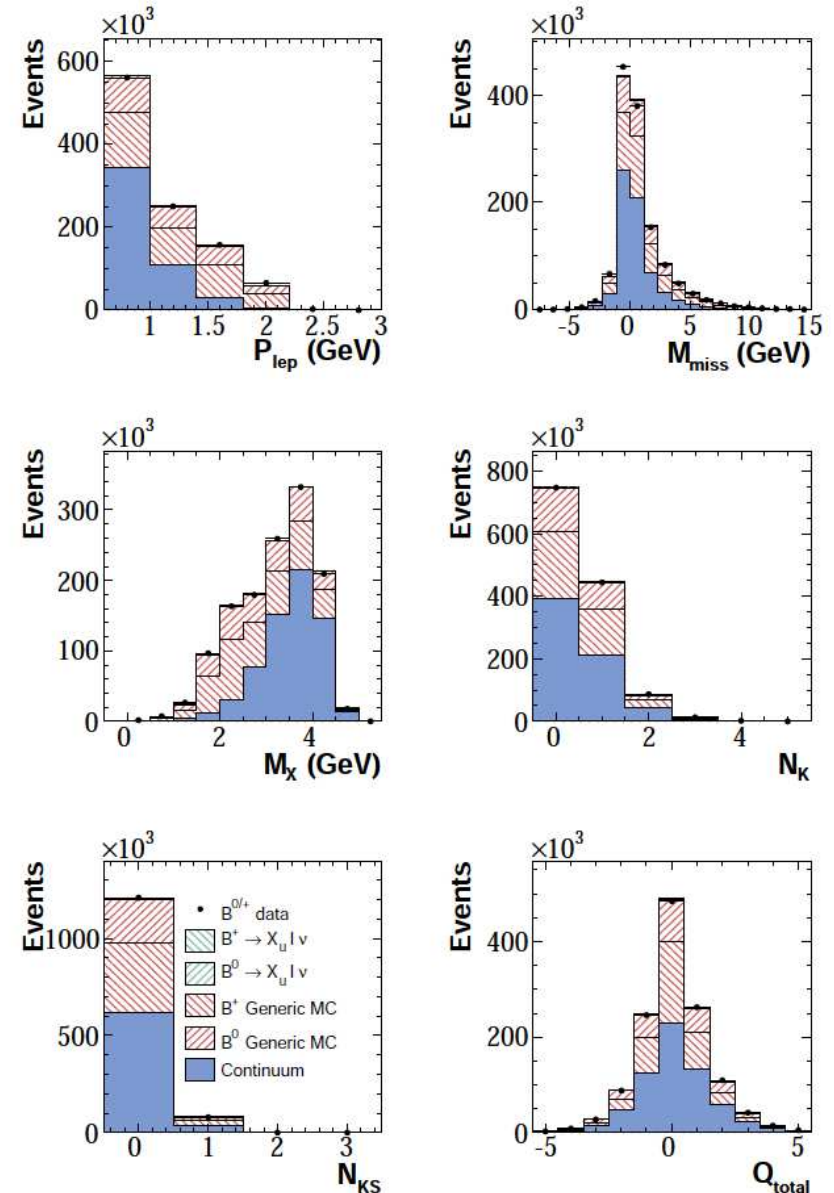
- ◇  $m_{bc} > 5.27 \text{ GeV}, |\Delta E| < 0.05 \text{ GeV}$
- ◇ more than million reconstructed B



# Event Selection with BDT

- One Lepton with  $p^B > 1$  GeV
- Further suppression of  $b \rightarrow c$  events with Boosted Decision Tree method
- 17 variables with correlations
  - ◇ Number of Kaons (charged and  $K_S^0$ )
  - ◇  $m_X$
  - ◇  $q^2$
  - ◇  $m_{\text{mis}}^2$
  - ◇  $P_+ \equiv E_X - |p_X|$
  - ◇  $m_{bc}, \Delta E$
  - ◇ Impact parameters
  - ◇ Total charge of the Event
  - ◇ ...
- single optimised cut in BDT classifier
- efficiency  $\sim 22\%$

## Variables in BDT

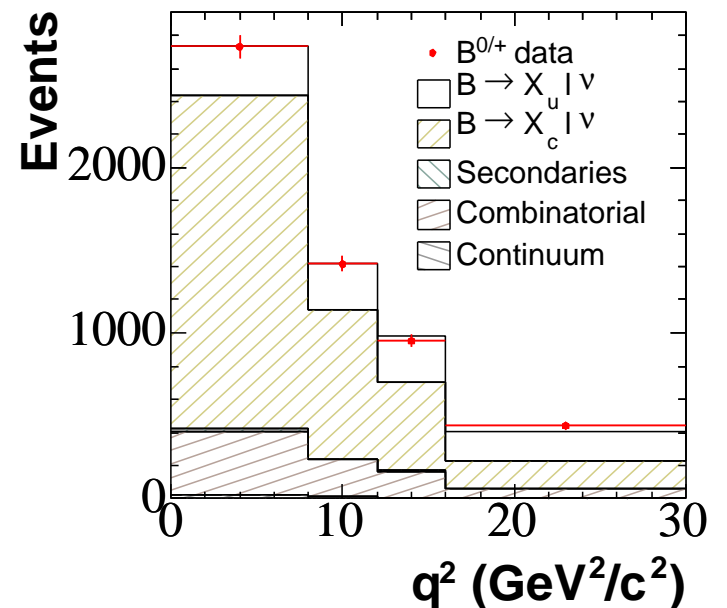
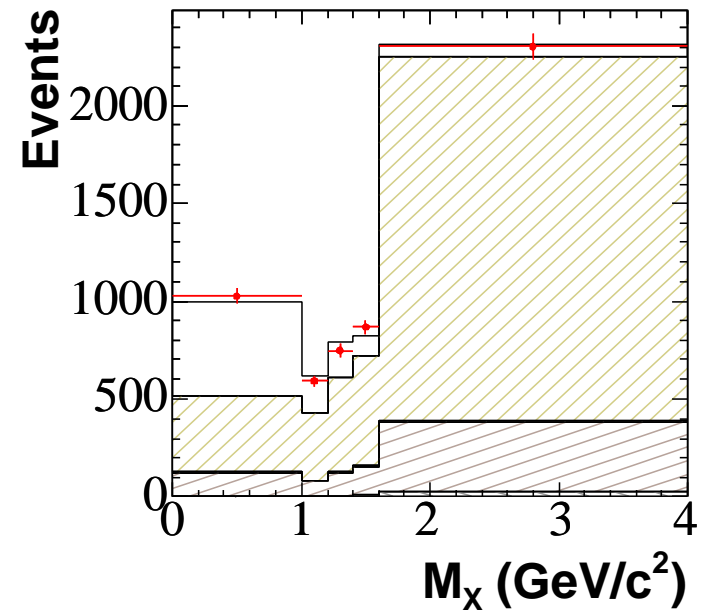


# Signal Extraction

- Background subtracted prior to fit
  - ◇ not from B decay (scaled off resonance)
  - ◇ not correctly reconstructed  $B_{\text{tag}}$  (MC shape scaled to  $m_{bc}$  sideband)
- Fit in 2D  $m_X - q^2$  distribution (5×4 bins)
- 3 components (MC driven)
  - ◇  $X_u l \nu$  contribution
  - ◇  $X_c l \nu$  contribution
  - ◇ Secondary and fakes

Source	# Events
BDT selected	$5544 \pm 54$
scaled off-resonance	$35 \pm 18$
wrong $B_{\text{tag}}$	$825 \pm 38$
$X_u l \nu$	$1032 \pm 91$
$X_c l \nu$	$3615 \pm 32$
Secondary and fakes	$38 \pm 2$

## Projected Distributions



# Result

- Partial branching fraction expressed by

$$\Delta\mathcal{B}(\mathbf{B} \rightarrow \mathbf{X}_u \ell^- \bar{\nu}, \Delta) = \frac{N_{\mathbf{b} \rightarrow \mathbf{u}}^\Delta}{\varepsilon_{\mathbf{b} \rightarrow \mathbf{u}}^\Delta N_{\text{tag}}} (1 - \delta_{\text{rad}})$$

- $\delta_{\text{rad}}$ : correction from QED radiation
- $\varepsilon_{\mathbf{b} \rightarrow \mathbf{u}}^\Delta$ : selection efficiency  $\sim 22\%$

$$\Delta\mathcal{B} = 1.963(1 \pm 0.088 \pm 0.081) \times 10^{-3}$$

for  $p_\ell^{\mathbf{B}} > 1 \text{ GeV}$

## Systematic Errors

$p_\ell^{\mathbf{B}} > 1.0 \text{ GeV}$	$\Delta\mathcal{B}/\mathcal{B} (\%)$
$\mathcal{B}(\mathbf{D}^{(*)} \ell \nu)$	1.2
$(\mathbf{D}^{(*)} \ell \nu)$ form factors	1.2
$\mathcal{B}(\mathbf{D}^{**} e \nu)$ & form factors	0.2
$\mathbf{B} \rightarrow \mathbf{X}_u \ell \nu$ (SF)	3.6
$\mathbf{B} \rightarrow \mathbf{X}_u \ell \nu$ ( $g \rightarrow s\bar{s}$ )	1.5
$\mathcal{B}(\mathbf{B} \rightarrow \pi/\rho/\omega \ell \nu)$	2.3
$\mathcal{B}(\mathbf{B} \rightarrow \eta, \eta' \ell \nu)$	3.2
$\mathcal{B}(\mathbf{B} \rightarrow \mathbf{X}_u \ell \nu)$ un-meas.	2.9
Cont./Comb.	1.8
Sec./Fakes/Fit.	1.0
PID/Reconstruction	3.1
BDT	3.1
Systematics	8.1
Statistics	8.8

# $\Delta\mathcal{B}$ to $V_{ub}$

$V_{ub}$  is obtained by relation,

$$|V_{ub}|^2 = \frac{\Delta\mathcal{B}(B \rightarrow X_u \ell^- \bar{\nu}, \Delta)}{\tau_B \Delta\mathcal{R}}$$

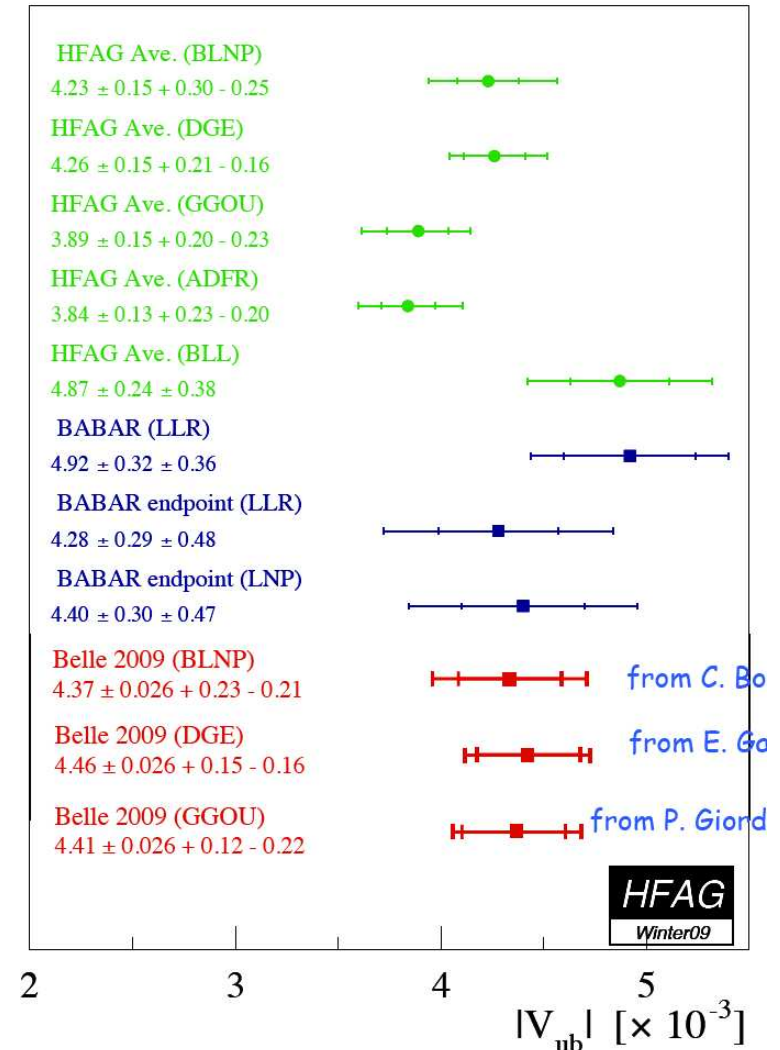
- $\tau_B$  average B lifetime
- $\Delta\mathcal{R}$ : partial rate from theory
  - ◊ BLNP, Phys. Rev. D 72, 073006 (2005)
  - ◊ DGE, arXiv:0806.4524 [hep-ph] (2008)
  - ◊ GGOU, JHEP 0710, 058 (2007)

Theory	$ V_{ub}  \times 10^3$	stat.	sys.	$m_b$	th.
BLNP	4.37	4.3	4.0	+3.1 -2.7	+4.3 -4.0
DGE	4.46	4.3	4.0	+3.2 -3.3	+1.0 -1.5
GGOU	4.41	4.3	4.0	1.9	+2.1 -4.5

relative errors in %

- New combination will come later

## Summary of $V_{ub}$



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