

Measurements of Charmless B Decays related to α @ BaBar



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On behalf of the BaBar Collaboration

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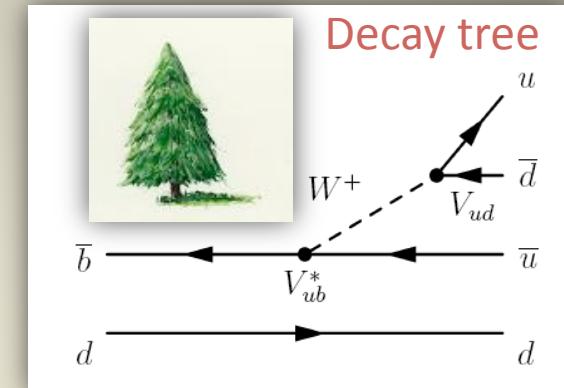
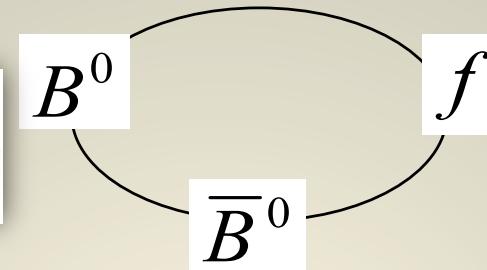
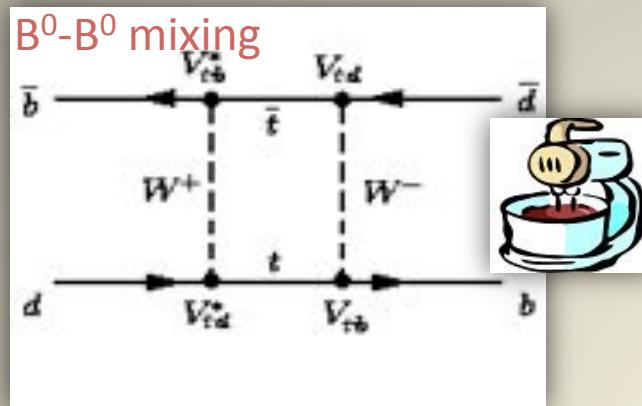
Outline

- Improved Measurements of $B^+ \rightarrow \rho^+\rho^0$
Determination of the Quark-Mixing Phase α in $B \rightarrow \rho\rho$

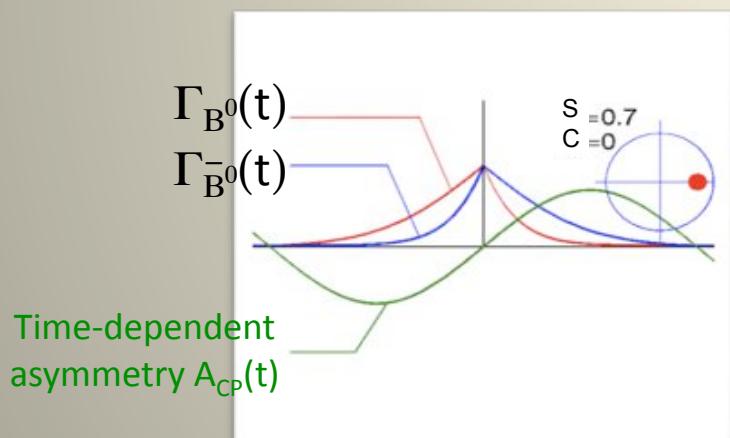
- Measurement of B decays to $K_1(1270) \pi$ and $K_1(1400) \pi$
Observation of the neutral modes
Extraction of CKM angle α from the measurement B^0 to $a_1(1260) \pi$ 

- Measurement of Branching Fraction of B^0 to $a_1(1260)^+ a_1(1260)^-$
First Observation of this decay mode
First polarization measurement of $B \rightarrow AA$
In principle this mode can be used to measure α 

Measuring α_{eff}



If f is a CP eigenstate ($\pi^+\pi^-$ for instance) and if only one CKM amplitude contributes to the decay:

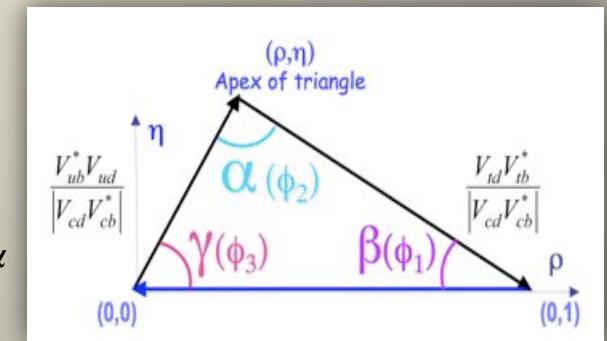


$$a_{CP}(t) \equiv \frac{\Gamma(\bar{B}^0(t) \rightarrow \pi^+ \pi^-) - \Gamma(B^0(t) \rightarrow \pi^+ \pi^-)}{\Gamma(\bar{B}^0(t) \rightarrow \pi^+ \pi^-) + \Gamma(B^0(t) \rightarrow \pi^+ \pi^-)}$$

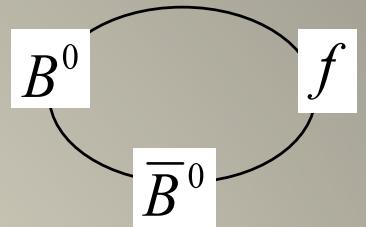
$$= S \sin(\Delta m_d t) - C \cos(\Delta m_d t)$$

$S = \sin(2\alpha), C = 0$

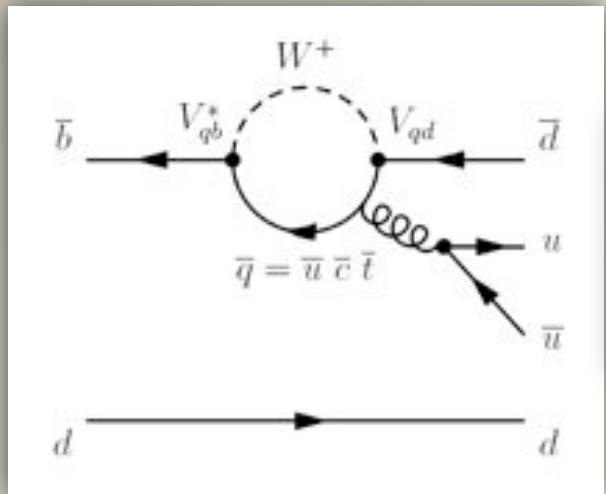
$$S = \frac{2 \operatorname{Im} \lambda}{1 + |\lambda|^2} \quad C = \frac{1 - |\lambda|^2}{1 + |\lambda|^2} \quad \lambda = \frac{q}{p} \frac{\bar{A}}{A} = e^{-i2\beta} e^{-i2\gamma} = e^{i2\alpha}$$



Measuring α_{eff}



In fact there are additional diagrams with a different CKM phase information...



Penguin pollution?

$$\lambda = \frac{q}{p} \frac{\bar{A}}{A} = e^{i2\alpha} \rightarrow$$

$$S = \frac{P}{T} \frac{e^{+iy} e^{i\delta}}{1 + \frac{P}{T} e^{-iy} e^{i\delta}}$$

(P) Penguin amplitude

(δ) strong phase

(T) Tree amplitude

$$S = \sqrt{1 - C^2} \sin(2\alpha_{eff})$$

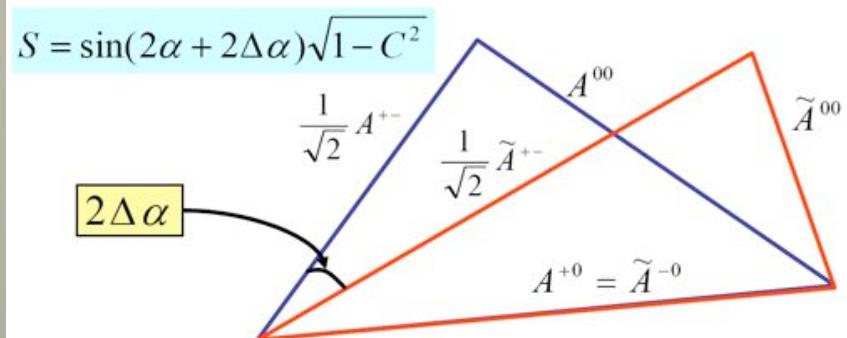
$$C \propto \sin \delta$$

α_{eff} is an effective value of α

Extraction of the angle α of the UT

- The difficulty in extracting α is the presence of subleading penguin amplitudes with a different weak phase than that of the dominant tree amplitudes.
- This difficulty can be overcome by using symmetries:
 - **isospin SU(2)** *Gronau, London PRL 65, 3381 (1990), Gronau, Zupan PRD 71, 074017 (2005)*
 - **approx. flavour SU(3)** *Dighe, Gronau, Rosner PRD 57, 1783 (1998), Beneke et al., PLB 638, 68 (2006)*

$SU(2)$



Neglecting EW penguins, ± 0 is a pure tree mode, and so the two triangles share a common side:

$$A(B^+ \rightarrow h^+ h^0) = \tilde{A}(B^- \rightarrow h^- h^0)$$

$h = \pi, \rho, a_1$

$$\begin{aligned} A_{hh} &= e^{+i\gamma} T + e^{-i\beta} P \\ \tilde{A}_{hh} &= e^{-i\gamma} T + e^{+i\beta} P \end{aligned}$$

$SU(3)$

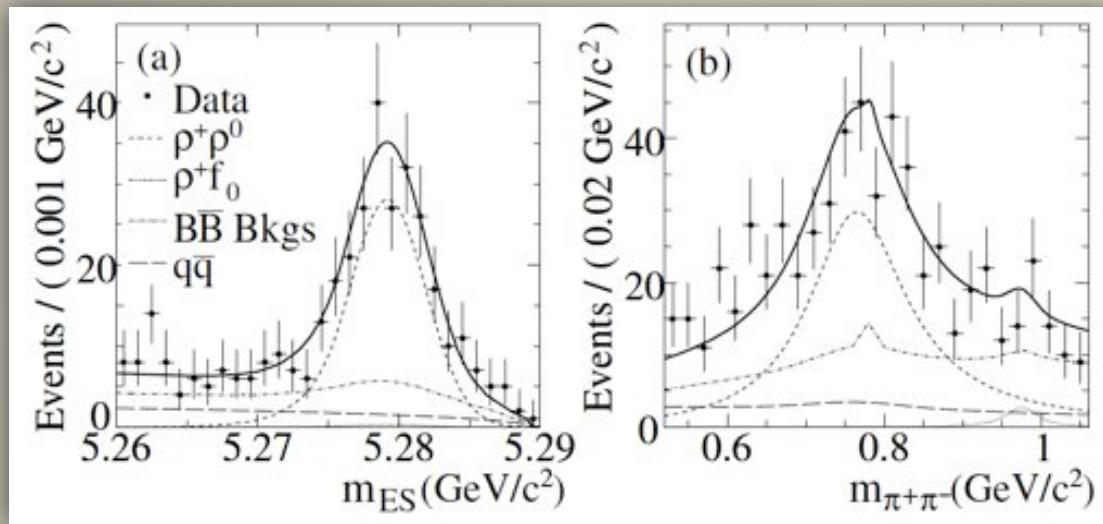
In $\Delta S=0$ decays: $T \sim V_{ub} V_{ud}^*$ and $P \sim V_{cb} V_{cd}^*$
 In $\Delta S=1$ decays: $T' \sim V_{ub} V_{us}^*$ and $P' \sim V_{cb} V_{cs}^*$

thus P'/T' is $1/\lambda^2$ enhanced over P/T
 \Rightarrow can be used to bound P/T

Improved Measurements of $B^+ \rightarrow \rho^+\rho^0$

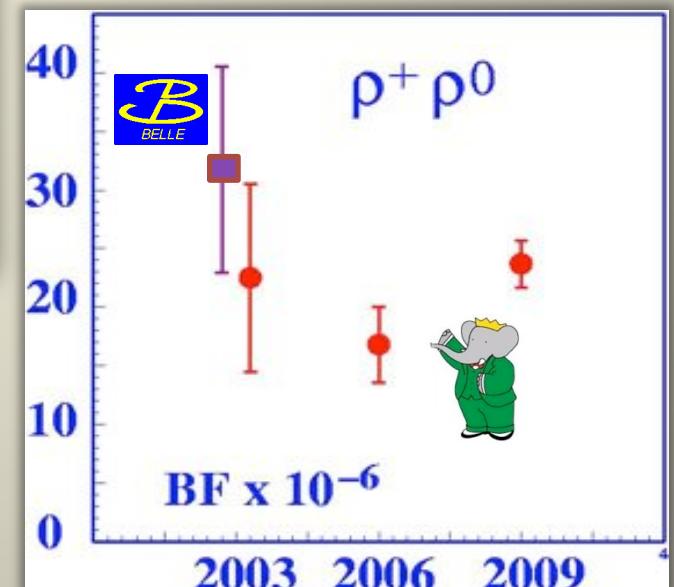
465 \pm 5 M $B\bar{B}$ pairs

- Improved methods (3D PDFs) to account for correlations in the main (continuum & combinatoric BB) backgrounds

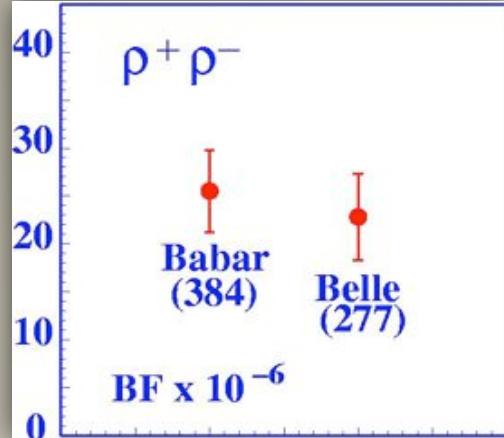


$$\mathcal{B}(B^+ \rightarrow \rho^+\rho^0) = (23.7 \pm 1.4 \pm 1.4) \times 10^{-6}$$
$$f_L = 0.950 \pm 0.015 \pm 0.006$$

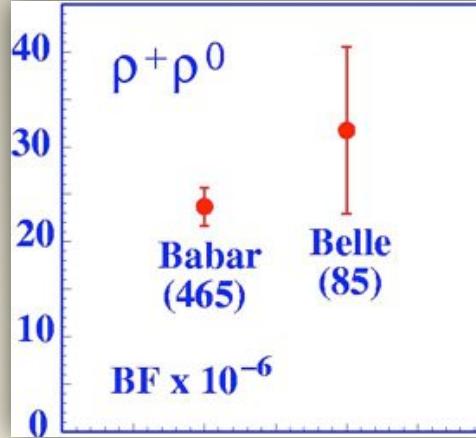
BaBar PRL102, 141802 (2009)



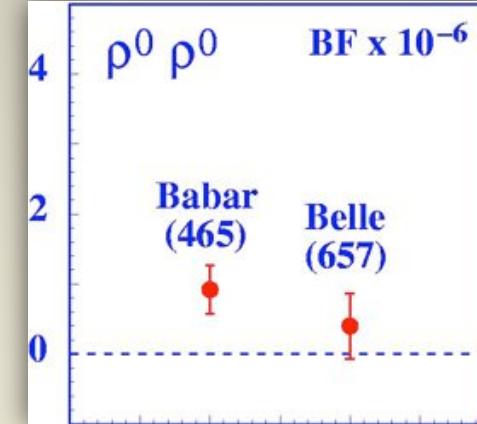
$B \rightarrow \rho\rho$: Branching fractions and A_{CP} 's



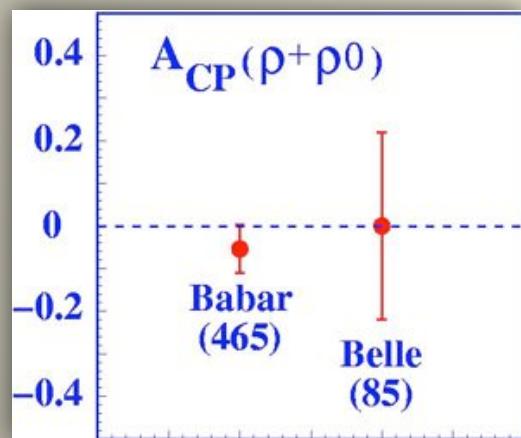
Babar PRD76 (2007) 052007
Belle PRL96 (2006) 171801



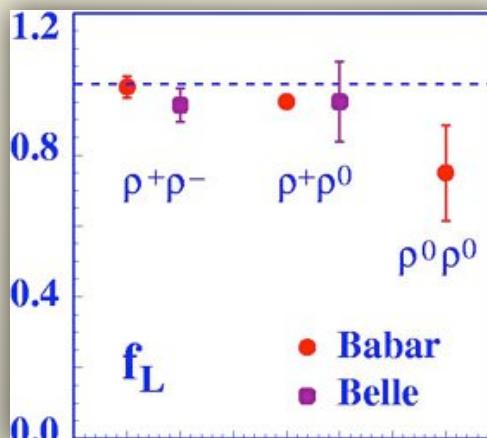
Babar PRL102 (2009) 141802
Belle PRL91 (2003) 221801



Babar PRD78 (2008) 071104
Belle PRD78 (2008) 111102



Babar PRL102 (2009) 141802
Belle PRL91 (2003) 221801



Vincenzo Lombardo

- $BF(\rho^0 \rho^0)/BF(\rho^+ \rho^-) \approx (3.6 \pm 1.5)\%$
small penguin contribution
- $A_{CP}(\rho^+ \rho^0) \approx 0$
small EW penguin contribution

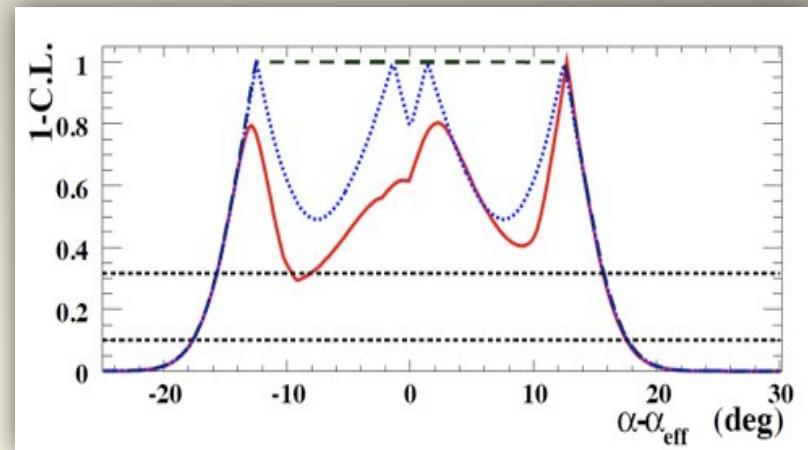
Isospin analysis $B \rightarrow (\rho\rho)_{Long}$

- 10 inputs: 3 BF's, 3 f_L 's, 2 S's & 2 C's
- Perform α scan, minimize χ^2

□ Impact of S^{00} and C^{00} :

BaBar PRD78, 071104 (2008)

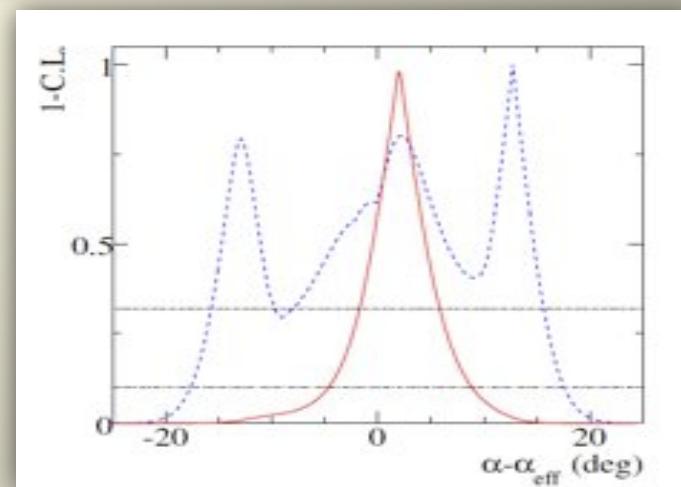
- without S^{00} or C^{00}
- with only C^{00}
- with S^{00} and C^{00}



□ Impact of BF ($B^+ \rightarrow \rho^+\rho^0$):

BaBar PRL102, 141802 (2009)

- with 2006 result
- with 2009 result



$$\alpha_{\rho\rho} = (92.4_{-6.5}^{+6.0})^\circ \text{ and } -1.8^\circ < \Delta\alpha < 6.7^\circ @ 68\% \text{ CL}$$

Measurement of B decays to $K_1(1270)\pi$ and $K_1(1400)\pi$



Theoretical predictions for BF's $0(10^{-6})$

- *Laporta et al., PRD 74, 054035 (2006)*
- *Calderon et al., PRD 76, 094019 (2007)*
- *Cheng et al., PRD 76, 114020 (2007)*

From ARGUS Coll., *PLB 254, 288 (1991)*:

$$\mathcal{B}(B^0 \rightarrow K_1(1400)^+ \pi^-) < 1.1 \times 10^{-3} \text{ @ 90% C.L.}$$

$$\mathcal{B}(B^+ \rightarrow K_1(1400)^0 \pi^+) < 2.6 \times 10^{-3} \text{ @ 90% C.L.}$$

BaBar Preliminary result (ICHEP 2008)

$$\mathcal{B}(B^0 \rightarrow K_1(1400)^+ \pi^- + K_1(1270)^+ \pi^-) \sim 0(10^{-5})$$

Measurement of B decays to $K_1(1270)\pi$ and $K_1(1400)\pi$

□ $K_1(1270) + K_1(1400)$ treated as a whole

- SU(3) octet states K_{1A}, K_{1B} :

$$|K_1(1400)\rangle = |K_{1A}\rangle \cos\theta + |K_{1B}\rangle \sin\theta \quad \theta=58^\circ$$

$$|K_1(1270)\rangle = -|K_{1A}\rangle \sin\theta + |K_{1B}\rangle \cos\theta \quad \text{Cheng, Yang PRD76, 114020 (2007)}$$

- nearly equal masses

- same quantum numbers and final state ($K\pi\pi$)

interference effects

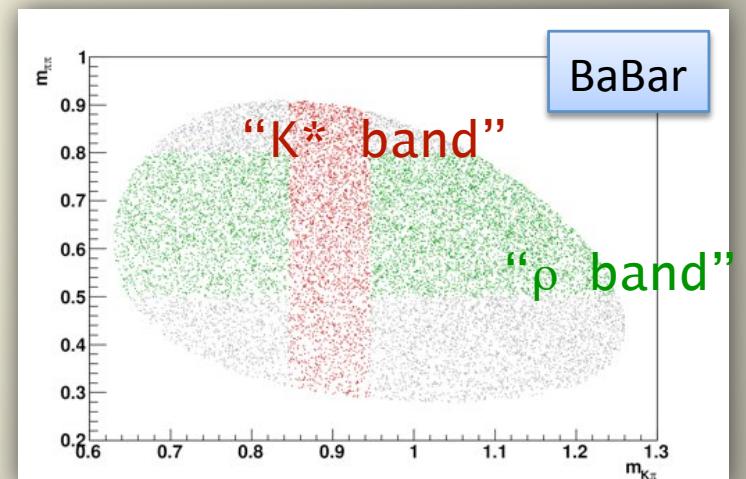
□ Most high-statistics data from WA3 exp. ($K^- p \rightarrow K^-\pi^+\pi^- p$)

- ACCMOR Coll., NPB 187, 1 (1981)

- $K\pi\pi$ analyzed using a two-resonance, six channel K-matrix model

Measurement of B decays to $K_1(1270)\pi$ and $K_1(1400)\pi$

- Decay parameters fixed to the values extracted from a fit to WA3 data
- Extended ML fit for BF
- Fit variables: m_{ES} , ΔE , Fisher, $m_{K\pi\pi}$, $|H|$
- Neutral modes ($B^0 \rightarrow K_1^+ \pi^-$)
 - simultaneous fit to “ K^* ” and “ ρ ” band
 - signal, qq, $K^*(1410)\pi$, $K^*\pi\pi + \rho K\pi$,
- Charged modes ($B^+ \rightarrow K_1^0 \pi^+$)
 - fit to “ K^* ” band only
 - signal, qq, $K^*(1410)\pi$, $K^*\pi\pi + \rho K^0\pi$, $K^*\rho$



Fit results - $K_1\pi$

454 ± 5 M $B\bar{B}$ pairs

$$\text{BF}(B^0 \rightarrow K_1(1400)^+ \pi^- + K_1(1270)^+ \pi^-) = (3.1^{+0.8}_{-0.7}) \times 10^{-5}$$

$$\text{BF}(B^+ \rightarrow K_1(1400)^0 \pi^+ + K_1(1270)^0 \pi^+) = (2.9^{+3.0}_{-1.7}) \times 10^{-5}$$

$S=7.5\sigma$
 $S=3.2\sigma$

Neutral modes

$$\mathcal{B}(B^0 \rightarrow K_1(1400)^+ \pi^-) = (1.6^{+0.8}_{-0.9}) \times 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow K_1(1270)^+ \pi^-) = (1.6^{+0.9}_{-1.0}) \times 10^{-5}$$

$$\mathcal{B}(B^0 \rightarrow K_{1A}^+ \pi^-) = (1.4^{+0.9}_{-1.0}) \times 10^{-5}$$

Charged modes

$$\mathcal{B}(B^+ \rightarrow K_1(1400)^0 \pi^+) < 3.9 \times 10^{-5}$$

$$\mathcal{B}(B^+ \rightarrow K_1(1270)^0 \pi^+) < 4.0 \times 10^{-5}$$

$$\mathcal{B}(B^+ \rightarrow K_{1A}^0 \pi^+) < 3.6 \times 10^{-5}$$

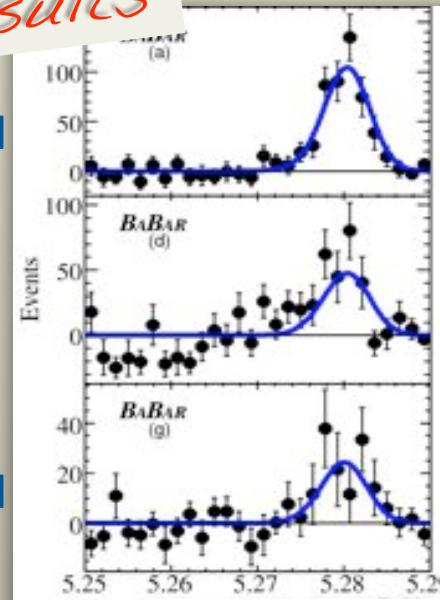
Preliminary BaBar Results

Neutral modes

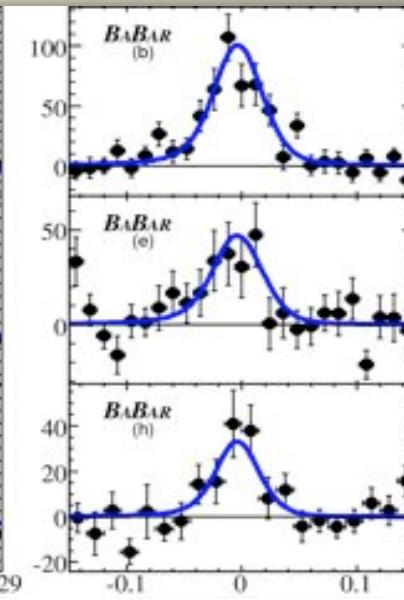
“K*” band
“ρ” band

Charged modes

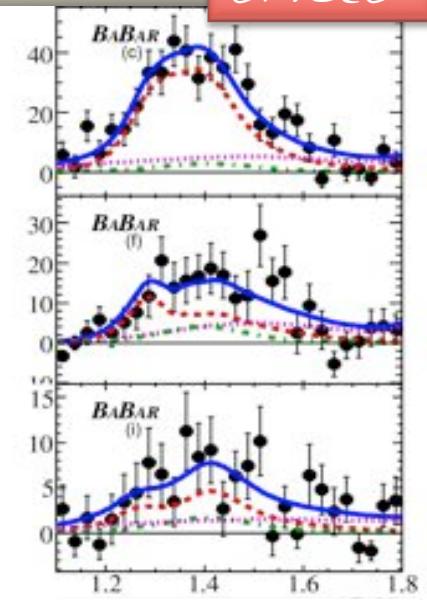
“K*” band



$m_{ES}(\text{GeV})$



$\Delta E(\text{GeV})$



$M_{K\pi\pi}(\text{GeV}/c^2)$

Bounds on α from CP-violation asymmetries in $B^0 \rightarrow a_1\pi$

The BF's and the CP asymmetries needed to extract α from $B^0 \rightarrow a_1\pi$ using flavor SU(3) are:

Gronau and Zupan, PRD 73, 057502 (2006)

$B \rightarrow a_1\pi$ branching fraction *PRL 97, 051802 (2006), BaBar Coll.*

$B \rightarrow a_1\pi$ TD CPV asymmetries ($S = \sin 2\alpha_{\text{eff}}$) *PRL 98, 181803 (2007), BaBar Coll.*

$B \rightarrow a_1 K$ branching fractions *PRL 100, 051803 (2008), BaBar Coll.*

$B \rightarrow K_1\pi$ branching fractions (*to be submitted to PRD*)

We obtain $|\alpha_{\text{eff}} - \alpha| < 11^\circ$ (13°) at 68% (90%) probability

The determination of α presents an eightfold ambiguity in the range $[0^\circ, 180^\circ]$. Assuming that the relative strong phase between the relevant tree amplitudes is negligible \rightarrow **two-fold ambiguity** ($\alpha_{\text{eff}} = 11^\circ \pm 7^\circ$ and $\alpha_{\text{eff}} = 79^\circ \pm 7^\circ$).

We combine the solution near 90° with the bounds on $|\alpha_{\text{eff}} - \alpha|$ and estimate the weak phase:

$$\alpha_{a_1\pi} = 79^\circ \pm 7^\circ \pm 11^\circ$$



Polarization Puzzle

- ❑ Considerable theoretical attention on charmless B decays to final states involving Vector mesons in the last few years

- ❑ Significant progress in experimental constraints on $B \rightarrow VV, VT, AV$

- ❑ $B \rightarrow \rho\rho$ decays fit the pattern $f_L = 1 - \frac{m_V^2}{m_B^2}$

- ❑ f_L large also for $K^{*0}K^{*0}$, $\omega\rho^+$, ϕK_2^{*0} , ρK^{*+}

- ❑ $f_L \sim 0.5$ for some penguin dominated modes: notably ϕK^* and $K^{*0}\rho^+$

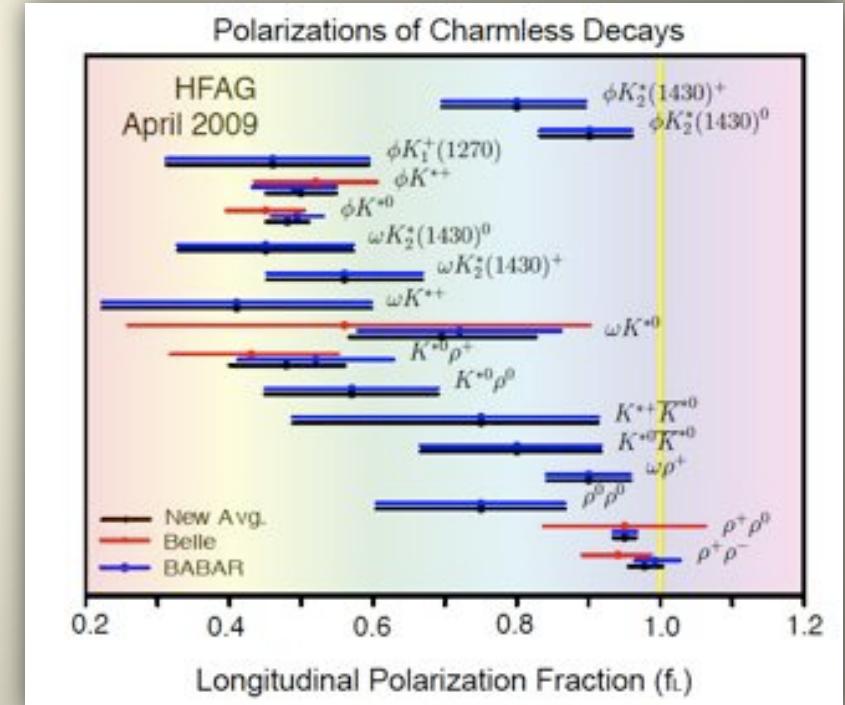
- ❑ Still puzzled by polarization: several non-trivial polarization have been measured

- ❑ Important to study polarization in new decays

We define the fraction of longitudinally polarised events as:

$$\begin{aligned} \frac{\Gamma_L}{\Gamma} &= \frac{|H_0|^2}{|H_0|^2 + |H_{+1}|^2 + |H_{-1}|^2}, \\ &= f_L. \end{aligned}$$

where the H_m are helicity amplitudes.



Observation and Polarization measurement of B^0 to $a_1(1260)^+ a_1(1260)^-$ decay



Theoretical expectations for $B^0 \rightarrow a_1(1260)^+ a_1(1260)^-$

QCD Factorization framework

$$BF = 37.4_{-13.7-1.4}^{+16.1+9.7} \times 10^{-6}$$
$$f_{LN} = 0.64_{-0.17}^{+0.07}$$

Branching Ratios and Polarization in $B \rightarrow VV$, VA and AA decays

H.Y.Cheng and K.C.Yang Phys. Rev. D 78, 094001 (2008)

Assume naive factorization + improved nonrelativistic ISGW quark model for form factors $B \rightarrow A$ transitions

$$BF = 6.4 \times 10^{-6}$$

Nonleptonic two-body B -decays including axial-vector mesons in the final state

G. Calderon, J.H.Munoz and C.E.Vera Phys. Rev. D76, 094019 (2007)

BF upper limit of 2.8×10^{-3} @ 90% CL measured by CLEO (1989)

Observation and Polarization measurement of B^0 to $a_1(1260)^+ a_1(1260)^-$ decay

- First measurement of longitudinal polarization in this mode
- Don't separate the dominant P-wave $(\pi\pi)_P$ and S-wave $(\pi\pi)_S$ in $a_1 \rightarrow 3\pi$ (accounted for in systematics)
- Limited number of signal to perform a full angular analysis
- Using helicity formalism (after integrating over azimuthal angle between decay planes of the two a_1 mesons) we get:

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta} \propto f_L (1 - \cos^2 \theta) + \frac{1}{2} f_T (1 + \cos^2 \theta)$$

$$f_T = 1 - f_L$$

longitudinal polarization fraction

where θ is the angle between the normal to the decay plane of the three pions of one a_1 and the flight direction of the other a_1 , both calculated in the rest frame of the a_1

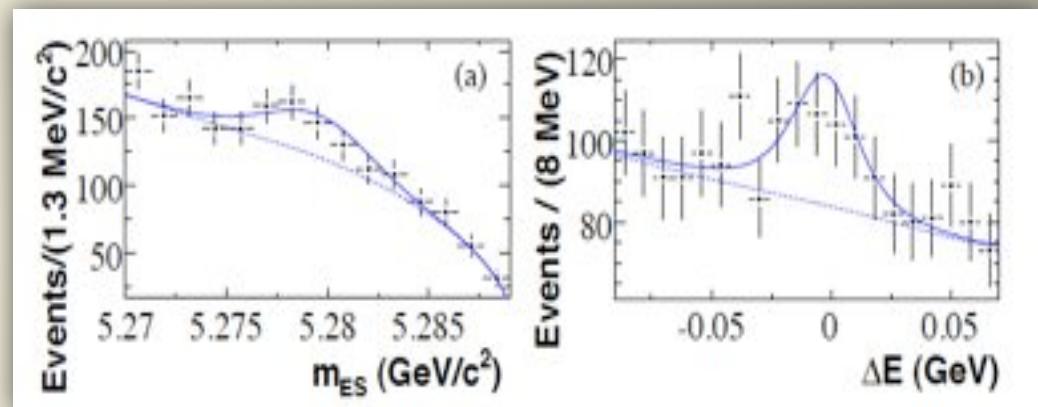
Observation and Polarization measurement of B^0 to $a_1(1260)^+ a_1(1260)^-$ decay

ML fit results

465 ± 5 M $B\bar{B}$ pairs

Projections

Signal yield	545 ± 118
Signal yield bias	+14
f_L bias	-0.06
ϵ_L (%)	9.0
ϵ_T (%)	10.0
S (σ)	5.0
\mathcal{B} ($\times 10^{-6}$)	$11.8 \pm 2.6 \pm 1.6$
f_L	$0.31 \pm 0.22 \pm 0.10$



- Specific component for charmless non-resonant backgrounds to 6 pions
- 5 sigma observation (f_L not defined in the zero signal hypothesis, taken into account)
- Assuming $\text{BF}(a_1^+ \rightarrow \pi^- \pi^+ \pi^+) = \text{BF}(a_1^- \rightarrow \pi^+ \pi^0 \pi^0)$ and $\text{BF}(a_1^+ \rightarrow (3\pi)^+) = 100\%$
- $\mathcal{B}(B^+ \rightarrow a_1^+ a_1^-) = (47.3 \pm 10.5 \pm 6.3) \cdot 10^{-6}$
- BF and f_L in general agreement with QCD Factorization

arXiv: 0907.1776



Conclusions

□ Improved Measurements of $B^+ \rightarrow \rho^+\rho^0$

Determination of the Quark-Mixing Phase α in $B \rightarrow \rho\rho$

$\alpha = (92.4_{-6.5}^{+6.0})^\circ$ and $-1.8^\circ < \Delta\alpha < 6.7^\circ$ @ 68% CL (substantial improvement)

CP asymmetries in $B \rightarrow \rho^+\rho^-$ using full dataset will improve further this measurement!

□ Measurement of B decays to $K_1(1270)\pi$ and $K_1(1400)\pi$

Observation of the neutral modes (7.5σ)

First time extraction of CKM angle α from the measurement B^0 to $a_1(1260)\pi$:

$\alpha = 79^\circ \pm 7^\circ \pm 11^\circ$

A new and independent measurement of α is now available!

$a_1\pi$ join the “ $\pi\pi/\rho\rho/\rho\pi$ ” club for measuring α !

□ Measurement of Branching Fraction of B^0 to $a_1(1260)^+ a_1(1260)^-$

First Observation of this decay mode (5.0σ)

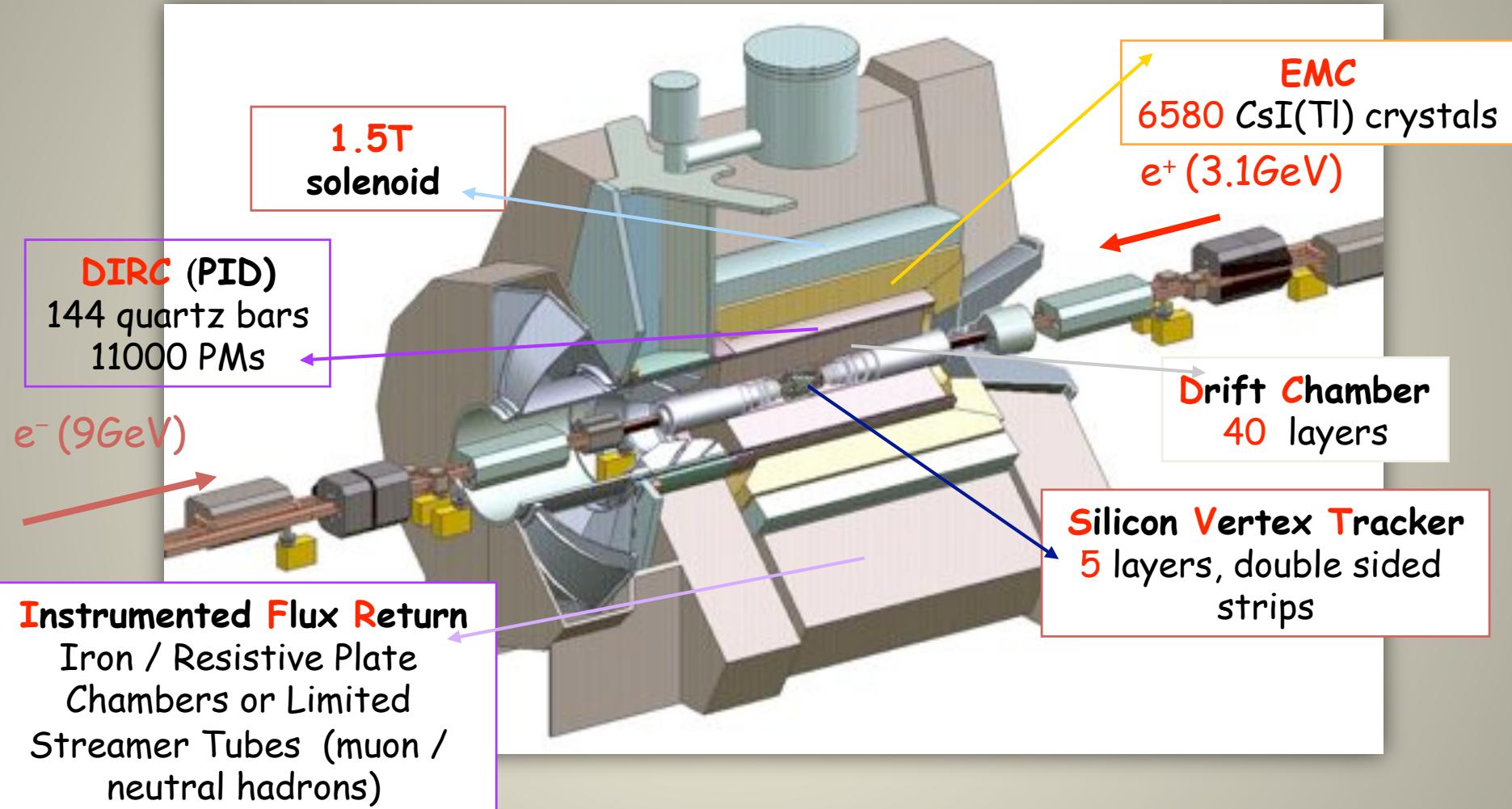
First polarization measurement of $B \rightarrow AA$

BF and longitudinal polarization in general agreement with QCD factorization

Errors are too large to extract α with the available statistics

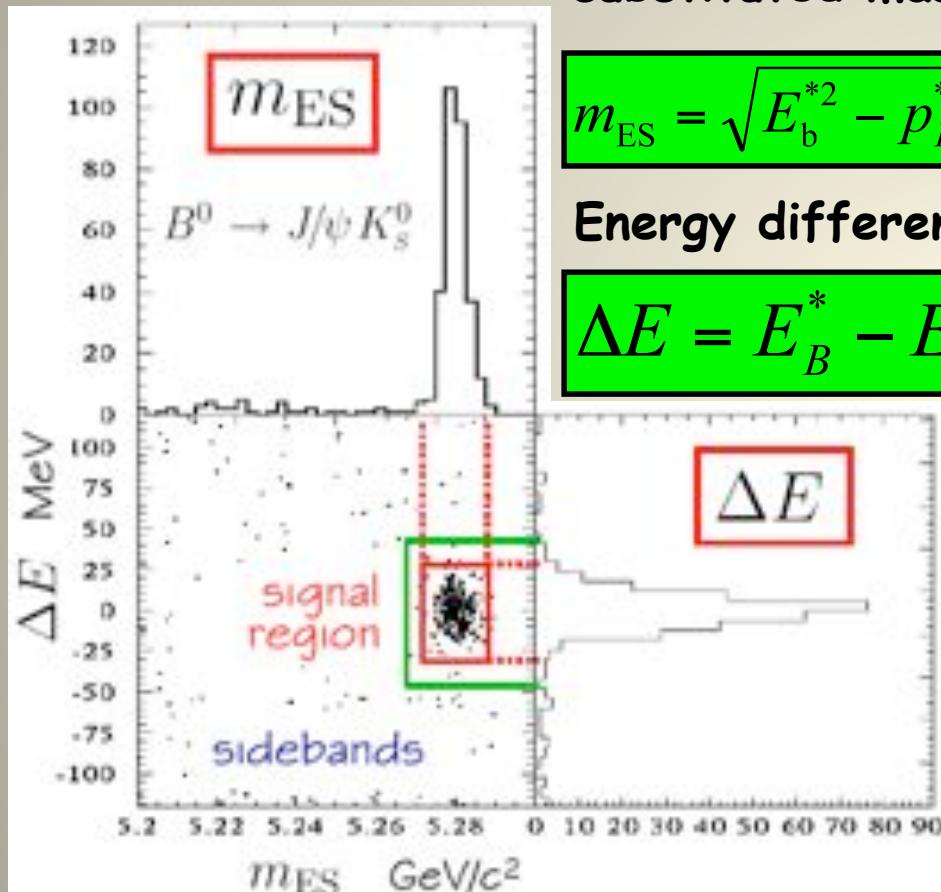
Backup Slides

Babar Detector



Physics Analysis with a Boosted $\Upsilon(4S)$

- Kinematics:



Beam energy substituted mass

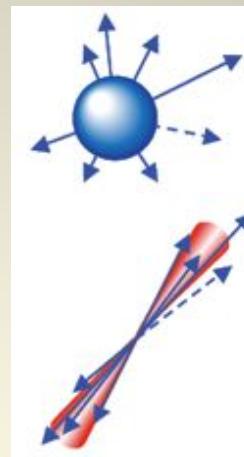
$$m_{ES} = \sqrt{E_b^{*2} - p_B^{*2}}$$

Energy difference

$$\Delta E = E_B^* - E_b^*$$

- Hadron ID \Rightarrow separation π/K

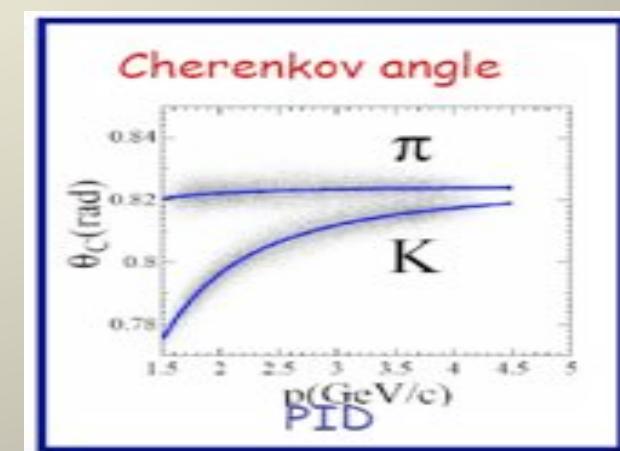
- Topology:



spherical BB events

"jetty" qq events

Event-shape variables combined in a neural network or Fisher discriminant to suppress jet-like continuum events.



SU(3) : $\rho\rho$

- Can relate the penguin contribution in $K^{*0}\rho^+$ to that in $\rho^+\rho^-$

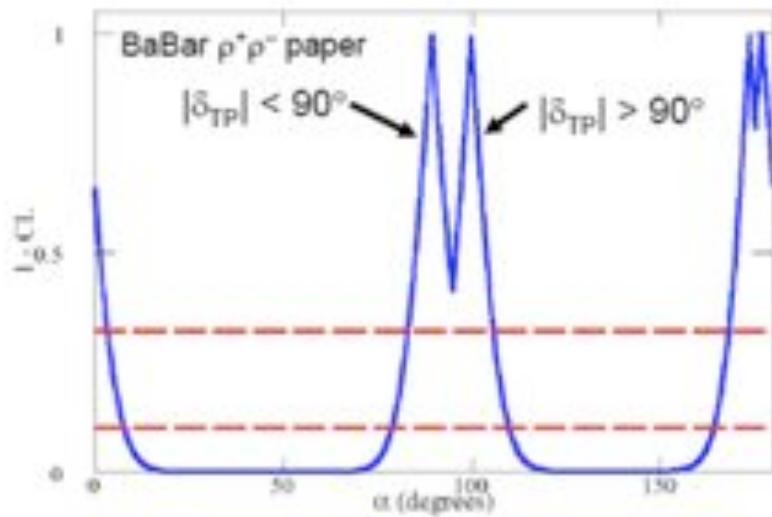
$$C_{\text{long}} = \frac{2r \sin \delta_{\text{TP}} \sin(\beta + \alpha)}{1 - 2r \cos \delta_{\text{TP}} \cos(\beta + \alpha) + r^2},$$

$$S_{\text{long}} = \frac{\sin 2\alpha + 2r \cos \delta_{\text{TP}} \sin(\beta - \alpha) - r^2 \sin 2\beta}{1 - 2r \cos \delta_{\text{TP}} \cos(\beta + \alpha) + r^2}$$

$$\left(\frac{|V_{cd}| f_\rho}{|V_{cs}| f_{K^*}} \right)^2 \frac{\Gamma_L(B^\pm \rightarrow K^{*0} \rho^\pm)}{\Gamma_L(B^0 \rightarrow \rho^+ \rho^-)} = \frac{Fr^2}{1 - 2r \cos \delta_{\text{TP}} \cos(\beta + \alpha) + r^2}$$

The dominant $SU(3)$ breaking correction accounted for by F is the neglect of annihilation diagrams in the $B^+ \rightarrow K^{*0} \rho^+$ decay.

$$F = 0.9 \pm 0.6$$



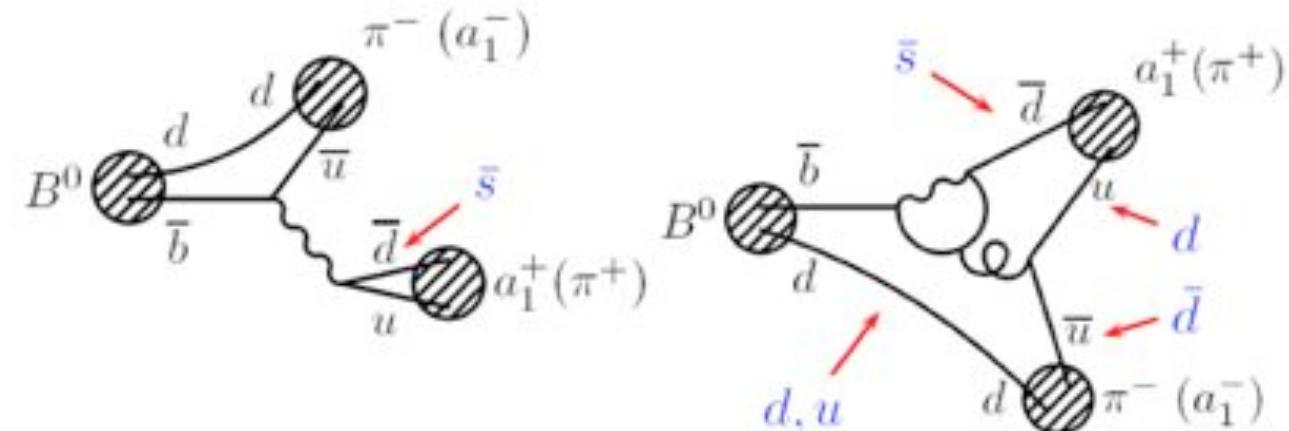
- If we assume that $|\delta_{\text{TP}}| < 90^\circ$:
 $\alpha = (89.8^{+7.0}_{-6.4})^\circ$
- Relaxing this assumption:
 $\alpha = [83.3, 105.8]^\circ$
- Common inputs with SU(2) result,
do not average the two!

M. Beneke, M. Gronau, J. Rohrer, and M. Spranger
Phys. Lett. B 638, 68 (2006).

Systematics: B^0 to $K_1\pi$

Quantity	$B^0 \rightarrow K_1^+ \pi^-$			$B^+ \rightarrow K_1^0 \pi^+$	
	\mathcal{B}	ϑ	ϕ	\mathcal{B}	ϑ
PDF parameters (A)	0.8	0.01	0.15	1.4	0.07
MC/data correction (A)	0.8	0.00	0.01	1.0	0.02
ML fit bias (A)	0.6	0.03	0.02	2.0	0.08
Fixed phase (A)	—	—	—	0.6	0.06
Scan (A)	0.9	0.04	0.16	0.0	0.04
K_1 K -matrix parameters (A)	2.2	0.01	0.36	0.5	0.05
K_1 offset phases (A)	0.2	0.01	0.02	0.0	0.00
K_1 intermediate resonances (A)	0.5	0.00	0.06	0.2	0.02
K^*/ρ bands (A)	0.2	0.05	0.00	1.2	0.05
Peaking $B\bar{B}$ bkg (A)	0.8	0.01	0.13	1.0	0.01
Fixed background yields (A)	0.0	0.00	0.00	0.4	0.02
Interference (A)	6.0	0.25	0.52	10.6	0.43
MC statistics (M)	1.0	—	—	1.0	—
Particle identification (M)	2.9	—	—	3.1	—
Track finding (M)	1.0	—	—	0.8	—
K_S reconstruction (M)	—	—	—	1.6	—
$\cos\theta_T$ (M)	1.0	—	—	1.0	—
Track multiplicity (M)	1.0	—	—	1.0	—
Number $B\bar{B}$ (M)	1.1	—	—	1.1	—

Approx SU(3) flavour symmetry: $a_1\pi$



$$t'_+ = \frac{f_{K_1}}{f_{a_1}} \frac{V_{ub}^* V_{us}}{V_{ub}^* V_{ud}} t_+ = \frac{f_{K_1}}{f_{a_1}} \bar{\lambda} t_+$$

$$p'_+ = \frac{f_{K_1}}{f_{a_1}} \frac{V_{cb}^* V_{cs}}{V_{cb}^* V_{cd}} p_+ = -\frac{f_{K_1}}{f_{a_1}} \bar{\lambda}^{-1} p_+$$

$$t'_- = \frac{f_K}{f_\pi} \frac{V_{ub}^* V_{us}}{V_{ub}^* V_{ud}} t_- = \frac{f_K}{f_\pi} \bar{\lambda} t_-$$

$$p'_+ = \frac{f_K}{f_\pi} \frac{V_{cb}^* V_{cs}}{V_{cb}^* V_{cd}} p_+ = -\frac{f_K}{f_\pi} \bar{\lambda}^{-1} p_+$$

penguins enhanced, tree suppressed, $\bar{\lambda} = 0.23$
 factorized SU(3) breaking accounted for
 annihilation like topologies neglected

Bounds on α from CP-violation asymmetries in $B^0 \rightarrow a_1 \pi$

$$\begin{aligned} A_+ &\equiv A(B^0 \rightarrow a_1^+ \pi^-), & A_- &\equiv A(B^0 \rightarrow a_1^- \pi^+), \\ \bar{A}_+ &\equiv A(\bar{B} \rightarrow a_1^- \pi^+), & \bar{A}_- &\equiv A(\bar{B} \rightarrow a_1^+ \pi^-). \end{aligned}$$

$$C \pm \Delta C \equiv \frac{|A_{\pm}|^2 - |\bar{A}_{\mp}|^2}{|A_{\pm}|^2 + |\bar{A}_{\mp}|^2}$$

$$\begin{aligned} \mathcal{A}_{CP}^+ &= -\frac{\mathcal{A}_{CP}^{a_1\pi}(1 + \Delta C) + C}{1 + \mathcal{A}_{CP}^{a_1\pi}C + \Delta C}, \\ \mathcal{A}_{CP}^- &= \frac{\mathcal{A}_{CP}^{a_1\pi}(1 - \Delta C) - C}{1 - \mathcal{A}_{CP}^{a_1\pi}C - \Delta C}, \end{aligned}$$

\mathcal{A}_{CP} are time- and flavor- integrated charge asymmetry in $B^0 \rightarrow a_1 \pi$

- SU(3) relations result in: *Gronau and Zupan, PRD 73, 057502 (2006)*

$$\cos 2(\alpha_{\text{eff}}^{\pm} - \alpha) \geq \frac{1 - R_{\pm}^0}{\sqrt{1 - \mathcal{A}_{CP}^{\pm 2}}}$$

$$\cos 2(\alpha_{\text{eff}}^{\pm} - \alpha) \geq \frac{1 - R_{\pm}^+}{\sqrt{1 - \mathcal{A}_{CP}^{\pm 2}}}$$

where

$$\begin{aligned} R_+^0 &\equiv \frac{\bar{\lambda}^2 f_{a_1}^2 \bar{\mathcal{B}}(K_{1A}^+ \pi^-)}{f_{K_{1A}}^2 \bar{\mathcal{B}}(a_1^+ \pi^-)} \\ R_-^0 &\equiv \frac{\bar{\lambda}^2 f_\pi^2 \bar{\mathcal{B}}(a_1^- K^+)}{f_K^2 \bar{\mathcal{B}}(a_1^- \pi^+)} \\ R_+^+ &\equiv \frac{\bar{\lambda}^2 f_{a_1}^2 \bar{\mathcal{B}}(K_{1A}^0 \pi^+)}{f_{K_{1A}}^2 \bar{\mathcal{B}}(a_1^+ \pi^-)} \\ R_-^+ &\equiv \frac{\bar{\lambda}^2 f_\pi^2 \bar{\mathcal{B}}(a_1^+ K^0)}{f_K^2 \bar{\mathcal{B}}(a_1^- \pi^+)}. \end{aligned}$$

- $|\Delta\alpha| = (|\alpha_{\text{eff}}^+ - \alpha| + |\alpha_{\text{eff}}^- - \alpha|)/2$
- get $|\alpha_{\text{eff}}^+, - - \alpha|$ by solving the system
- Metod works much better if smaller penguin/tree

BF and Polarization measurement of B^0 to $a_1(1260)^+ a_1(1260)^-$ decay

Selection - ML fit

- ❑ Reconstruct $a_1^+ \rightarrow \pi^+ \pi^- \pi^+$ with 2π to form a ρ^0 candidate
- ❑ $0.87 < a_1$ mass < 1.75 GeV/c²
- ❑ PID for pions
- ❑ Veto to suppress charm bkg
- ❑ Best candidate from highest B vertex χ^2 probability
- ❑ 5 hypotheses in the likelihood model:
signal, continuum bkg, charmless, generic charm and peaking charm bkg
- ❑ charmless non-resonant decays (6 pions in the final state) taken into account

Projections: B^0 to $a_1(1260)^+ a_1(1260)^-$ decay

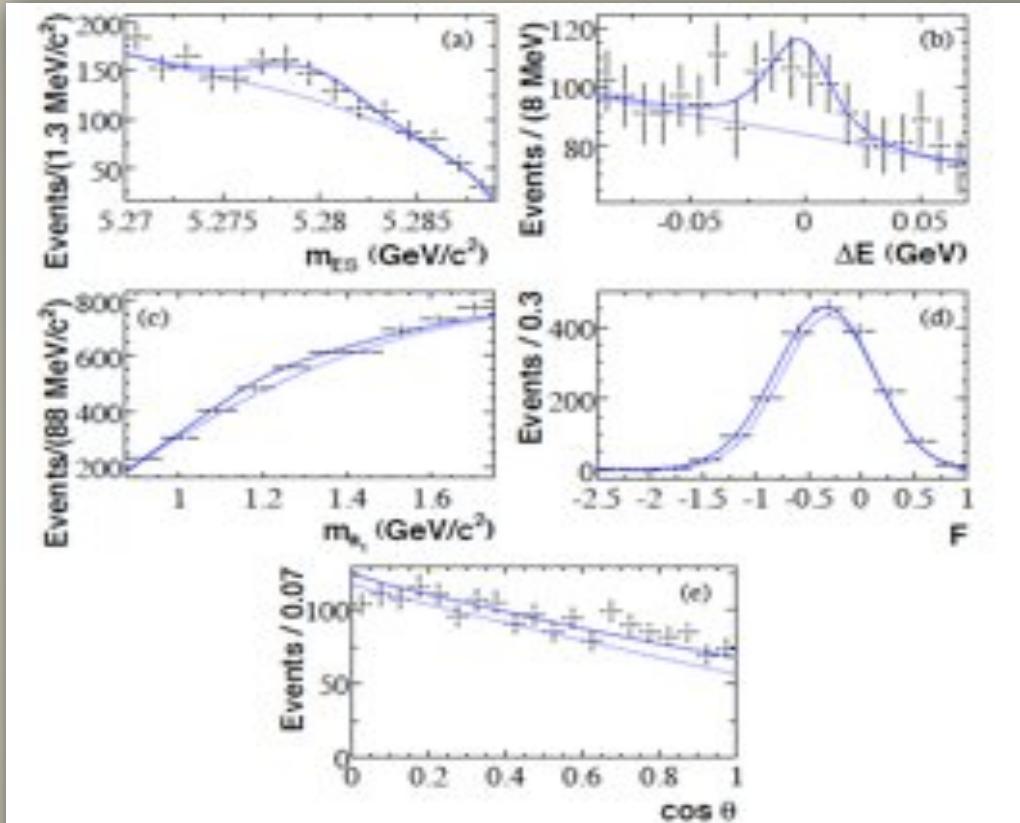
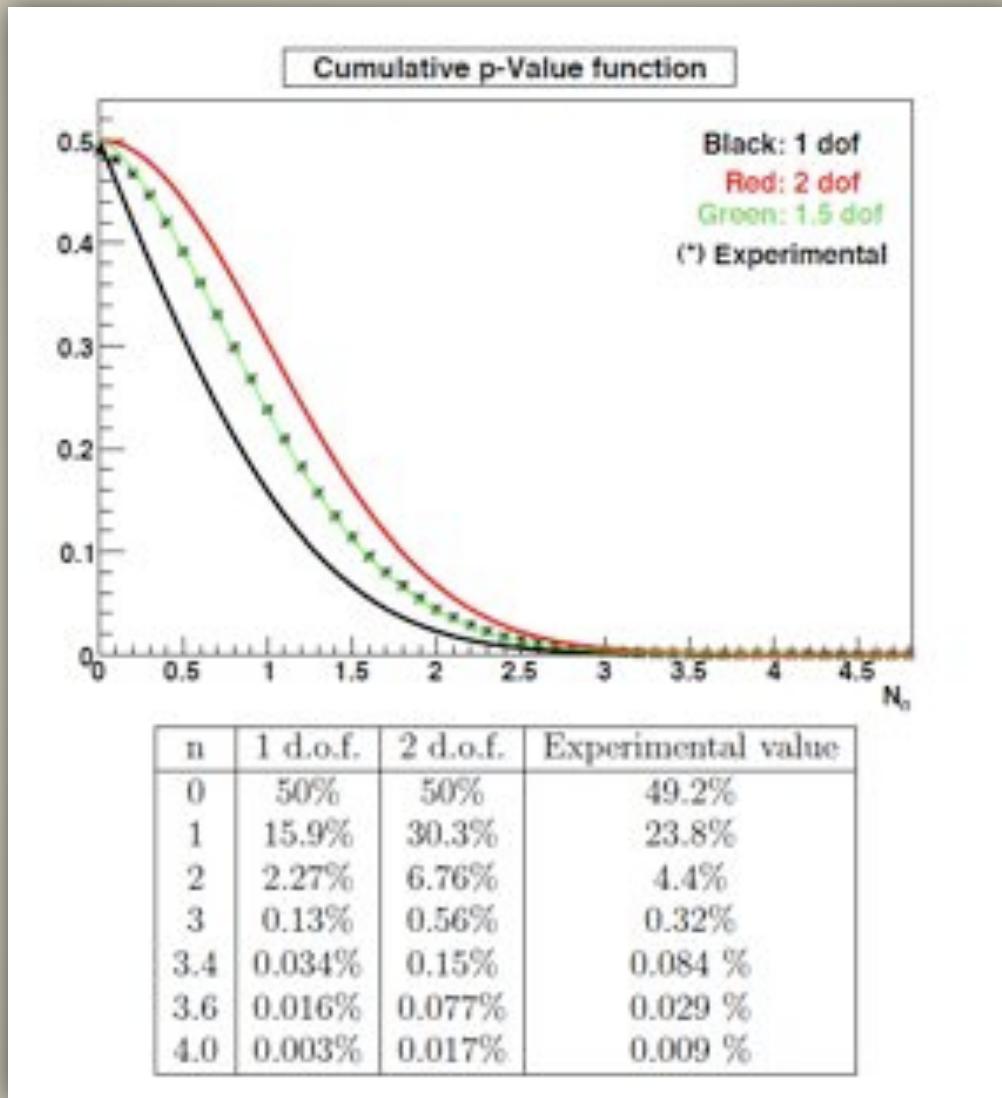


FIG. 1: Projections of (a) m_{ES} , (b) ΔE , (c) a_1 invariant mass (average of $m_{a_1^+}$ and $m_{a_1^-}$ is shown), (d) \mathcal{F} and (e) $\mathcal{H} = |\cos \theta|$ (average of $|\cos \theta_{a_1^+}|$ and $|\cos \theta_{a_1^-}|$ is shown). Points with error bars (statistical only) represent the data, the solid line the full fit function, and the dashed line the background component. These plots are made with a requirement on the signal likelihood that selects 25%-40% of the signal and 2%-5% of the background.

Significance: B^0 to $a_1(1260)^+ a_1(1260)^-$ decay



Systematics: B^0 to $a_1(1260)^+ a_1(1260)^-$ decay

Quantity	Sig. yield	f_{LN}
Additive errors (events)		
Fit yield	37.7	0.084
Fit bias	7.0	0.030
a_1 paramet.	30.8	0.043
SXF	12.1	0.009
NON-Res	10	0.015
$B^0 \rightarrow a_1^+ a_2^-$	19	0.01
Total additive (events)	55.0	0.101
Multiplicative errors (%)		
MC statistics	0.1	-
Track multiplicity	1.0	-
Tracking find eff.	1.4	-
PID	3.6	-
Number $B\bar{B}$	1.1	-
Evt shape	2.5	-
σ corr.	6.8	1.5
Total multiplicative (%)	8.3	1.5
Total (events)	70.7	0.101